

#### Assignment Project Exam Help

# Arithmeticufor Computers 1

CS 154: Computer Architecture
WeChat:Lecster#80TCS
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#### Administrative

Lab 4 underway...

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Syllabus (Schedule Section) shas been updated

# Midterm Exam (Wed. 2/12)

#### What's on It?

Everything we've covered in lecture from start to Monday, 2/10

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#### What Else?

- Closed book son We Chat destit ords llow)
- Random seat assignments come to class EARLY!

#### Lecture Outline

MIPS Instructions: Arrays vs. Pointers

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- Arithmetic https://tutorcs.comAddition / Subtraction

  - Multiplication Weivistincstutores

#### Arrays vs. Pointers

- Array indexing involves
  - Multiplying index by element size Assignment Project Exam Help
  - Adding to array base address

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- Pointers correspondiatirestly tromemory addresses
  - Can avoid indexing complexity

# Example: Clearing an Array (the classic way)

```
clear1(int array[], int size) {
  int i;
  for (i = 0; i < size; i += 1)
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       https://tutorcs.com
      move t0,\zero # i = 0
loop1: sMeCthattocatuto#cst1 = i * 4
      add t2,a0,t1 # t2 =
                          &array[i]
      sw zero, 0(t2) # array[i] = 0
      addi t0,t0,1 # i = i + 1
      s1t $t3,$t0,$a1 # $t3 =
                       # (i < size)
      bne $t3,$zero,loop1 # if (...)
                          # goto loop1
```

#### Example: Clearing an Array (using a pointer)

```
clear2(int *array, int size) {
  int *p:
  for (p = &array[0]; p < &array[size];</pre>
  Assignment)Project Exam Help
       https://tutorcs.com
      move t0,a0 # p = & array[0]
      sWeschaticstutpiscs = size * 4
      add t2,a0,t1 # t2 =
                      # &array[size]
loop2: sw zero,0(t0) # Memory[p] = 0
      addi t0,t0,4 \# p = p + 4
      s1t $t3,$t0,$t2 # $t3 =
                      #(p<&array[size])
      bne $t3,$zero,loop2 # if (...)
                          # goto loop2
```

#### Comparison of the Two...

```
t0,szero # i = 0
                                                   $t0.$a0 # p = & array[0]
     move
                                              move
          t1,t0,2 # t1 = i * 4
                                                   $t1,$a1,2 # $t1 = size * 4
loop1:sll
                                              s11
         t2,a0,t1 # t2 = array[i]
     add
                                              add
                                                   $t2.$a0.$t1
                                                               \# $t2 = &array[size]
          $zero, 0($tAs$igninent Project Exam Help
                                                               \# Memory[p] = 0
     SW
     addi $t0.$t0.1
                                                               \# p = p + 4
                                              slt
                                                   $t3,$t0,$t2 # $t3=(p<&array[size])
     slt
          $t3.$t0.$a1
                       # $t3 = (i < size)
          $t3.$zero.loop1# https://tutorcs.com $t3,$zero,loop2# if () go to loop2
     bne
```

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- Version on the left must water that the loop
- Memory pointer version on the right increments the pointer p directly.
- Moves the scaling shift and the array bound addition <u>outside</u> the loop
- It reduces instructions executed per iteration from 6 to 4.
- This is how a lot of compilers optimize code like this.

#### Arithmetic Overview 1

- Addition / subtraction
  - Carry outass gyerflow premember the pifference!

# Examples in 8-bit adders: https://tutorcs.com

• 
$$0x24 + 0xB0$$
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• 
$$0x7F + 0x66$$
  $0xE5$ ,  $C = 0$ ,  $V = 1$ 

• 
$$0x15 + 0xFB$$
  $0x10$ ,  $C = 1$ ,  $V = 0$ 

• 
$$0x87 + 0xAA$$
  $0x31$ ,  $C = 1$ ,  $V = 1$ 

# Dealing with Overflow in C/C++

- Some languages (e.g., C/C++, Java) ignore overflow
- What happens when you do:

```
0x87000000 + 0xAA0000000 in C++?

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(i.e. -2,030,043,136 + -1,442,840,576?)
```

- You get 822,083,5 https://tutorcs.com
- In MIPS, you'd use WeChat: cstutorcs
   addu, addui, subu instructions to not trigger overflow
   (this is what a C/C++ compiler would issue)
- Why?
  - Checking for overflow for every calculation can be demanding on CPU run time

## Dealing with Overflow in Other Languages

 Other languages (e.g., Ada, Fortran – older ones) require raising an exception

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- In MIPS, you'd use MIPS add, addi, sub instructions <a href="https://tutorcs.com">https://tutorcs.com</a>
- What actually happene: Chat: cstutorcs
  - On overflow, an "exception handler" is invoked
  - PC is saved in exception program counter (EPC) register
  - Jump executed to predefined handler address
  - mfc0 (move from coprocessor reg) instruction can retrieve EPC value, to return after corrective action

#### Arithmetic Overview 2

#### Multiplication

- Left bit shifting by N bits ←→ Multiplying by 2<sup>N</sup>

https://tutorcs.com

- Division
  - Right bit shifting the lite state of the lite of the
  - Using div / divu (again, with mflo or mfhi)
    - No checking for overflow or divide-by-zero
  - Raises questions about floating point...
    - Will be coming up...

# Multiplication in Computers: The Algorithm using a Decimal Example

```
Initially, P is 0
Loop:

If N is 0, then P = the result, exit Loop
Else, P += (the rightmost digit of N) times M
Shift N right once, and M left once
Repeat Loop
```

# Example with Decimals 803 \* 151 (which we expect to be 121,253)

P	M	N	
0			1. N is not 0 t Project Exam Help
		https://	2. P += (rightmost digit of N[1]) * M[803] tutores common once, M left once
		WeCh	at: Cstutorcs 3. P += (rightmost digit of N[5]) * M[8030] Shift N right once, M left once
			N is not 0
			4. P += (rightmost digit of N[1]) * M[80300]
			Shift N right once, M left once
			NISO; END

# Example with Decimals 803 \* 151 (which we expect to be 121,253)

P	M	N	
0			1. N is not 0 t Project Exam Help
803			2. P += (rightmost digit of N[1]) * M[80 tutores Chant once, M left once
40953	80300	WeCh 1	Chat: Cstutorcs 3. P += (rightmost digit of N <sub>[5]</sub> ) * M <sub>[8030]</sub> Shift N right once, M left once N is not 0 4. P += (rightmost digit of N <sub>[1]</sub> ) * M <sub>[80300]</sub> Shift N right once, M left once
121253	803000	0	
			N IS 0; END

# Multiplication in Computers: The Algorithm using a **Binary** Example

 ...Even easier than the decimal example:
 Shown here for 32 bits Assignment Project Exam Help

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Initially, P is 0 We Chat: cstutorcs Loop 32 times: If  $N_{bit0} = 1$ , then P += M

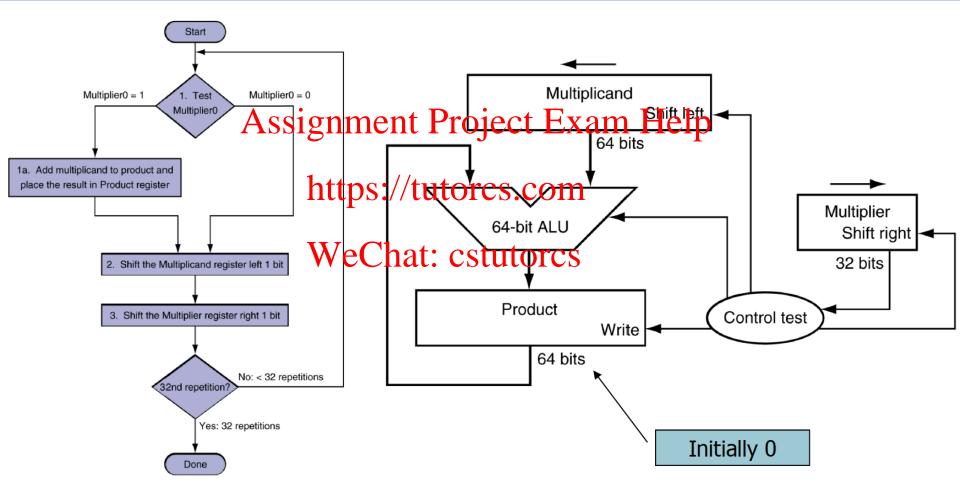
Shift N right once, and M left once

#### Simple Example using 8 bits

```
M = 0x04 = 0000 0100 \quad \text{(multiplicand)}
N = 0x05 = 0000 0101 \quad \text{(multiplier)}
Assignment Project Exam Help
\bullet P = 0 \quad \text{https://tutorcs.com}
\bullet N_0 = 1 \Rightarrow P += 0x0 \text{ We Oxoat: cst of exo 0 0010, M = 0000 1000}
\bullet N_0 = 0 \Rightarrow P = 0x04 \text{ (unchanged), N = 0000 0001, M = 0001 0000}
\bullet N_0 = 1 \Rightarrow P += 0x10 = 0x14, \qquad N = 0000 0000, M = 0010 0000
```

• Exit with P = 0x14 (correct answer, since 0x14 = 20)

## Multiplication Hardware



Can be further optimized with added HW

#### Optimization of HW for Multiplication

Multiplicand You can perform some steps 32 bits in parallel: add/shift Assignment partial-product addition is https://tutorcs.com One cycle per Shift right Control **Product** ok to do, if frequency echat: cstutor¢ Write test 64 bits multiplications in program is low

# quotient $\begin{array}{c|c} \hline & 1001 \\ \hline & 1000 \\ \hline & 100101010 \\ \hline & -1000 \\ \hline & 101 \\ \hline & 1010 \\ \hline & -1000 \\ \hline & remainder \end{array}$

#### Division in Computers: The Algorithm

• Dividend (N) ÷ Divisor (D)= Quotient, Remainder

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```
Initially, R = Nttps://tutorcs.com
Loop 32 times:

R = R - V
Loop 32 times:

R = R - V
Loop 32 times:

S = R - V
Loop 44 times:

S = R + D
Loop 45 times:

S = R + D
Loop 47 times:

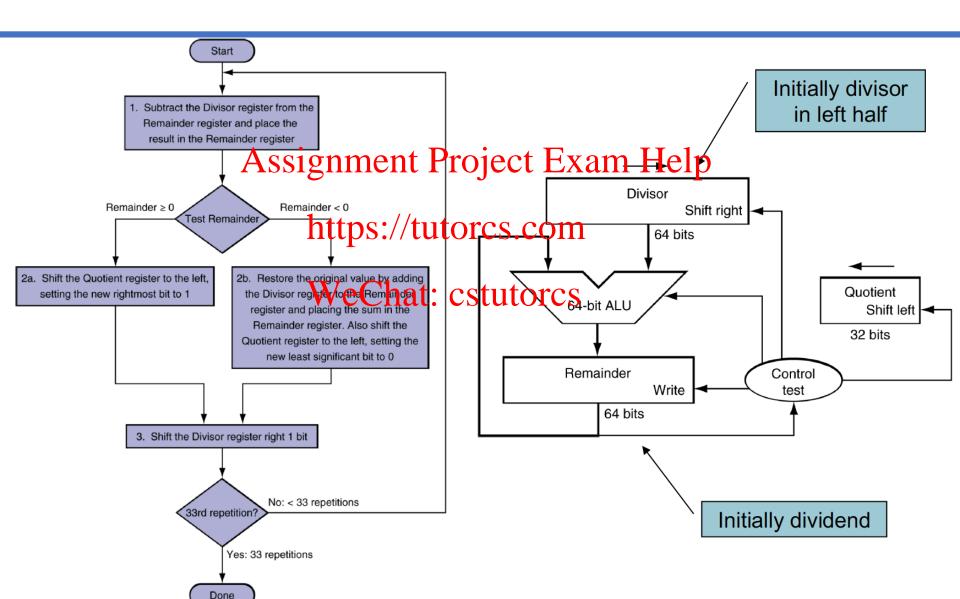
S = R + D
Loop 48 times:

S = R + D
Loop 49 times:

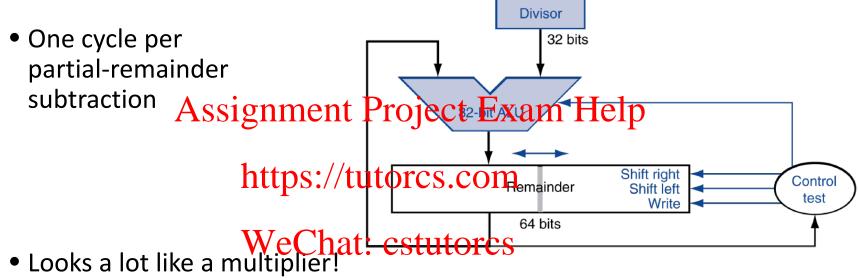
S = R + D
Loop 40 times:

S =
```

#### **Division Hardware**



#### Optimization of HW for Division



• In fact, we can use the same hardware for both...

## Floating Point

- Representation for non-integral numbers
- Including very small and very large numbers
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- Usually follows spmes". normalized form of scientific notation
- Example:  $-2.34 \times 10^6$  (ok) vs.  $-234 \times 10^4$  (not ok) WeChat: cstutorcs
- In binary, the form is: ± 1.xxxxxxx<sub>(base 2)</sub> x 2<sup>yyyy</sup>
- Types float and double in C/C++
- More in next lecture...

#### YOUR TO-DOs for the Week

•Readings!

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•Work on Lab 4! https://tutorcs.com

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