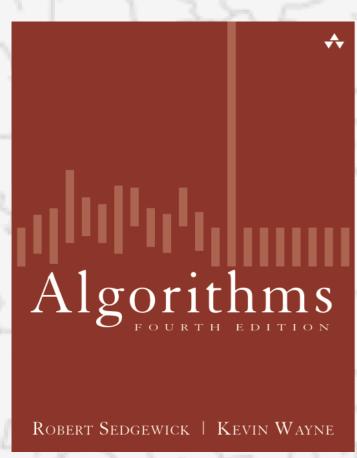
Algorithms



http://algs4.cs.princeton.edu

PRIM'S ALGORITHM DEMO

- Prim's algorithm
- lazy implementation
- eager implementation



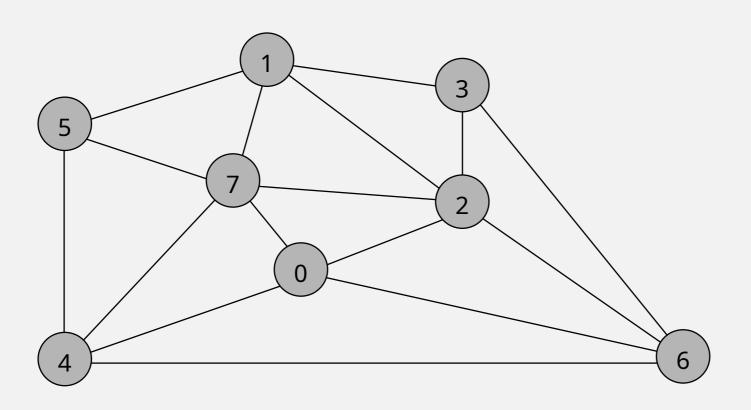
ROBERT SEDGEWICK | KEVIN WAYNE

http://algs4.cs.princeton.edu

PRIM'S ALGORITHM DEMO

- Prim's algorithm
- lazy implementation
- eager implementation

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



an edge-weighted graph

0-7 0.16

2-3 0.17

1-7 0.19

0-2 0.26

5-7 0.28

1-3 0.29

1-5 0.32

2-7 0.34

4-5 0.35

1-2 0.36

4-7 0.37

0-4 0.38

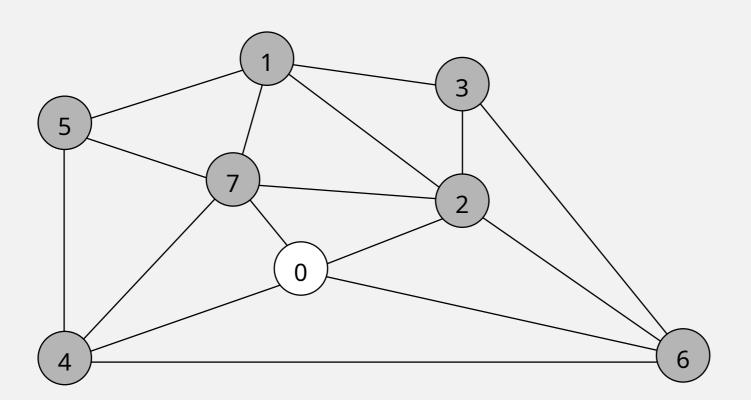
6-2 0.40

3-6 0.52

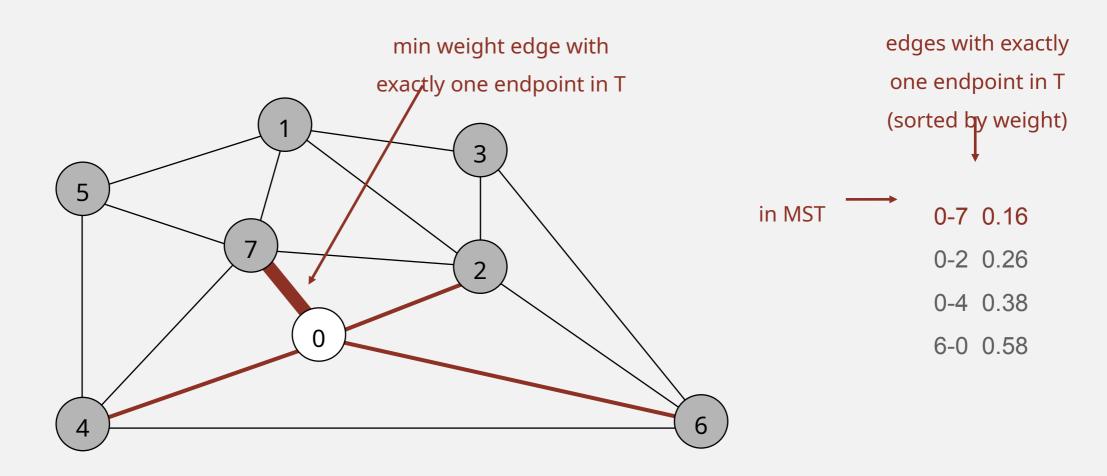
6-0 0.58

0 4 0 00

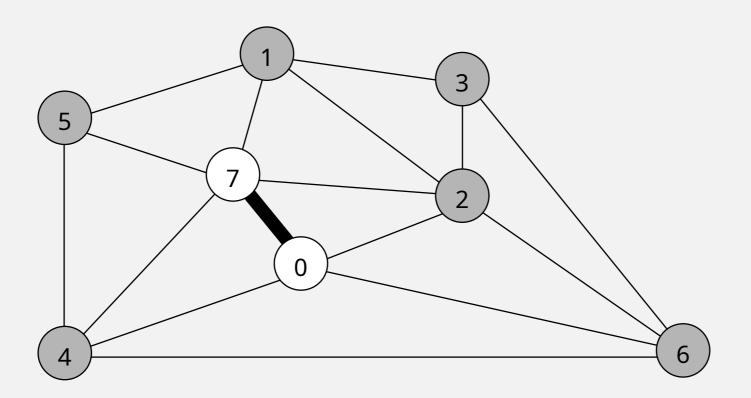
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



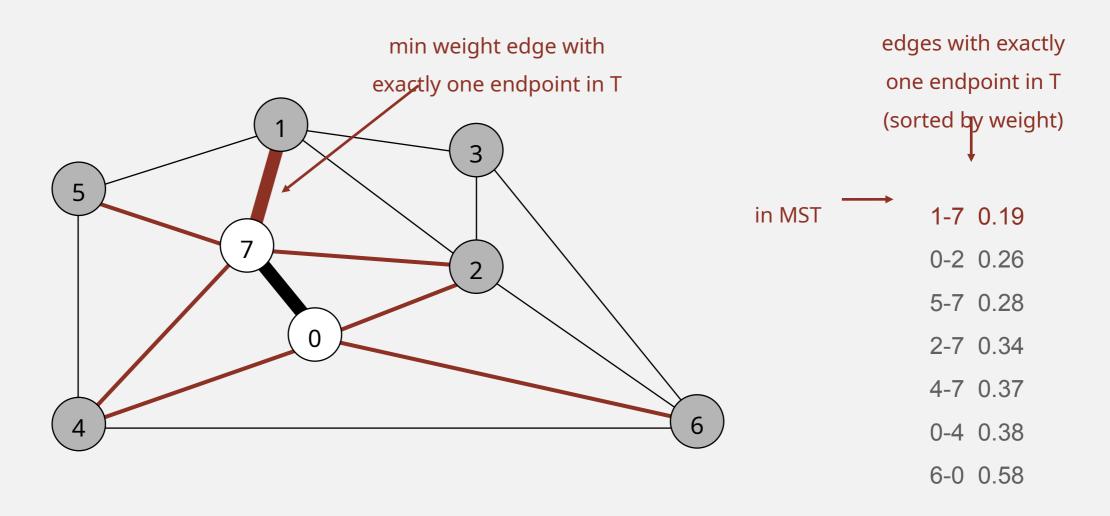
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



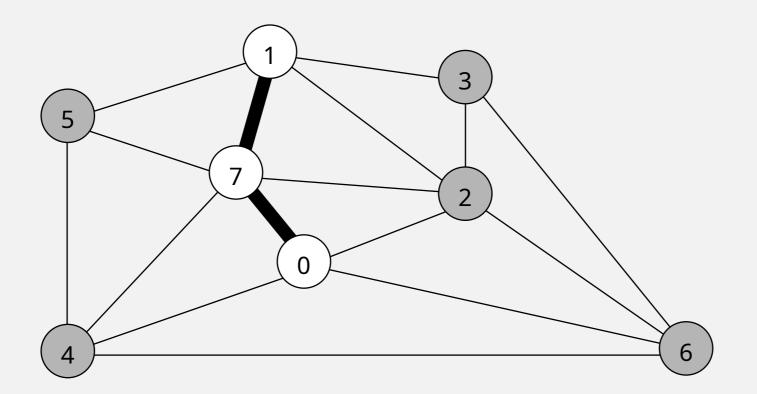
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



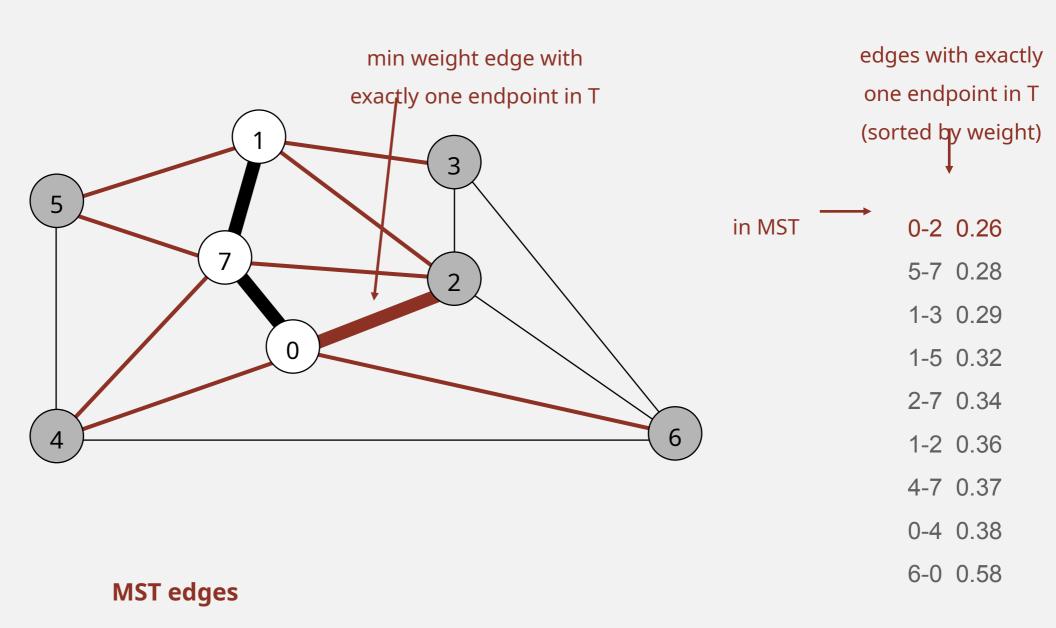
- Start with vertex 0 and greedily grow tree T.
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- Repeat until V 1 edges.



- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

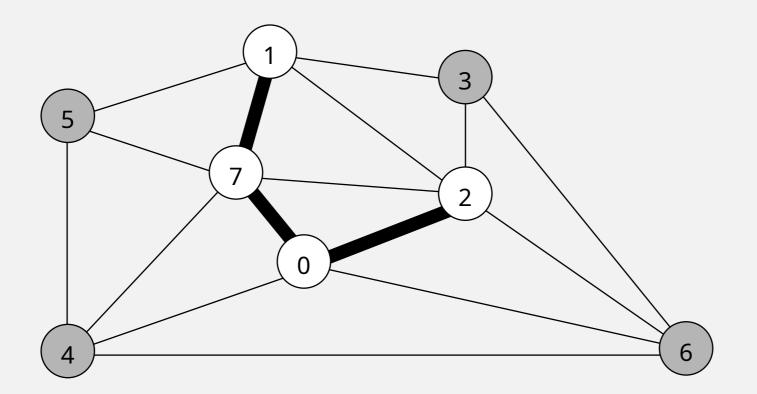


- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



0-7 1-7

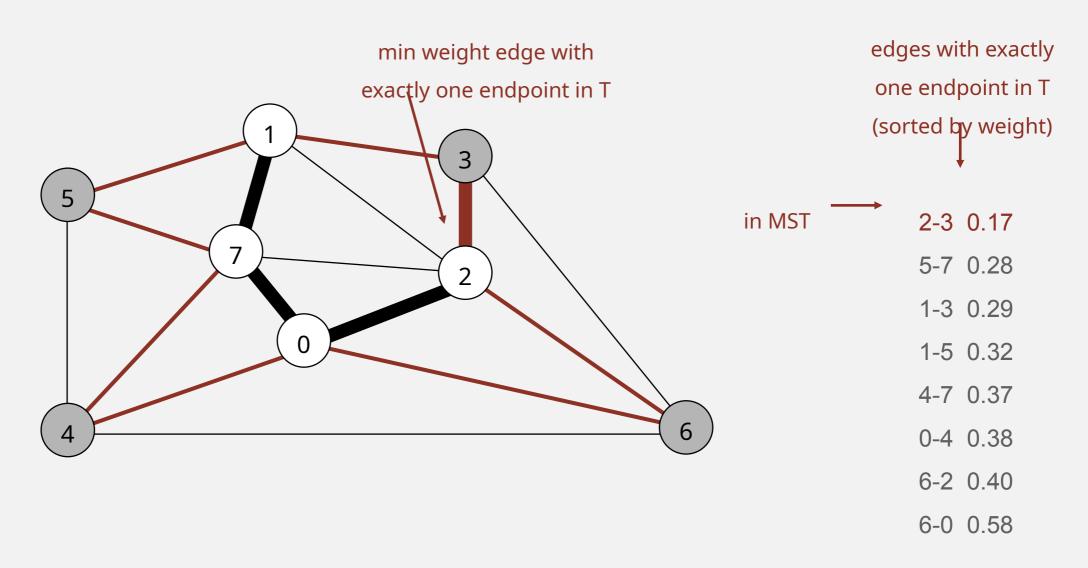
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2

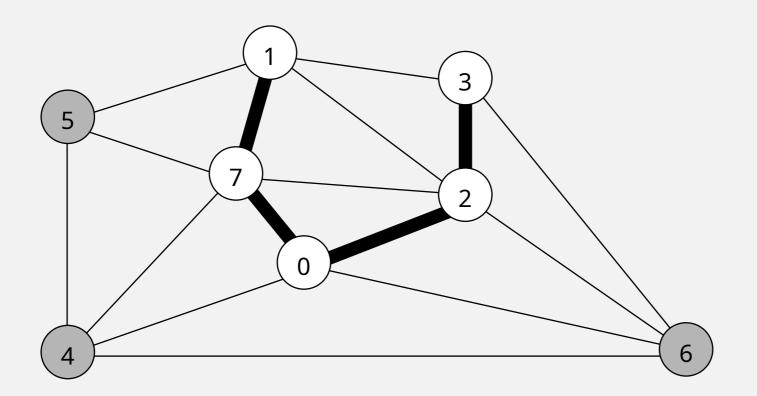
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2

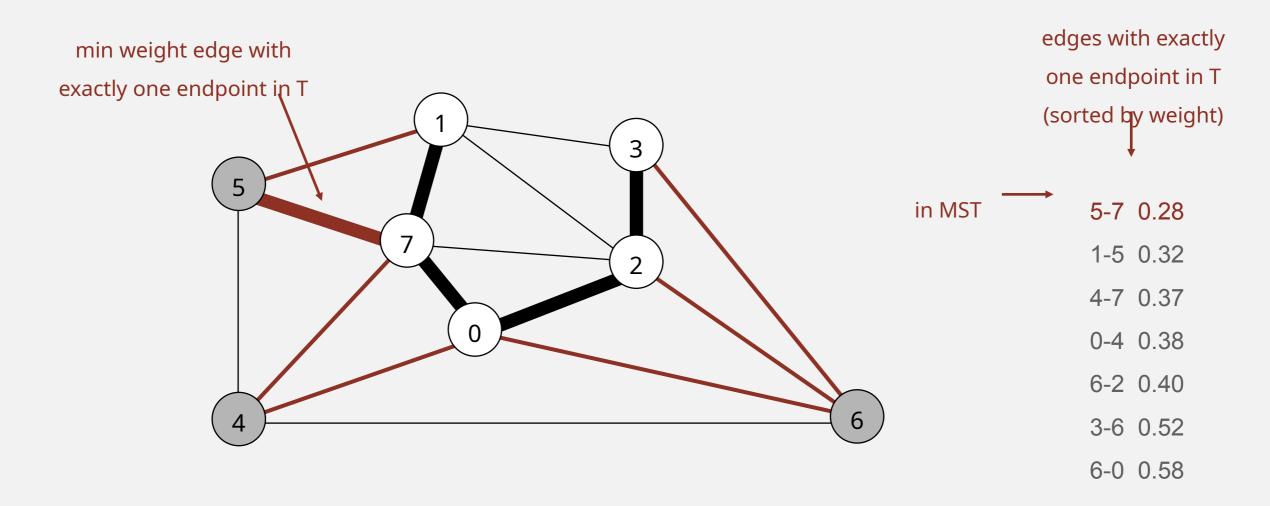
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3

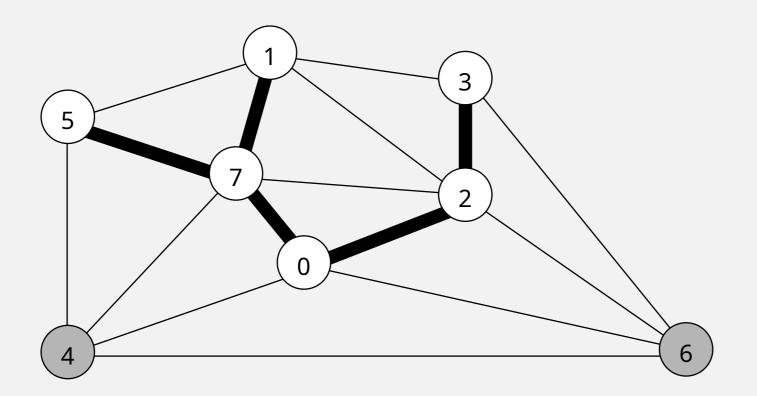
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3

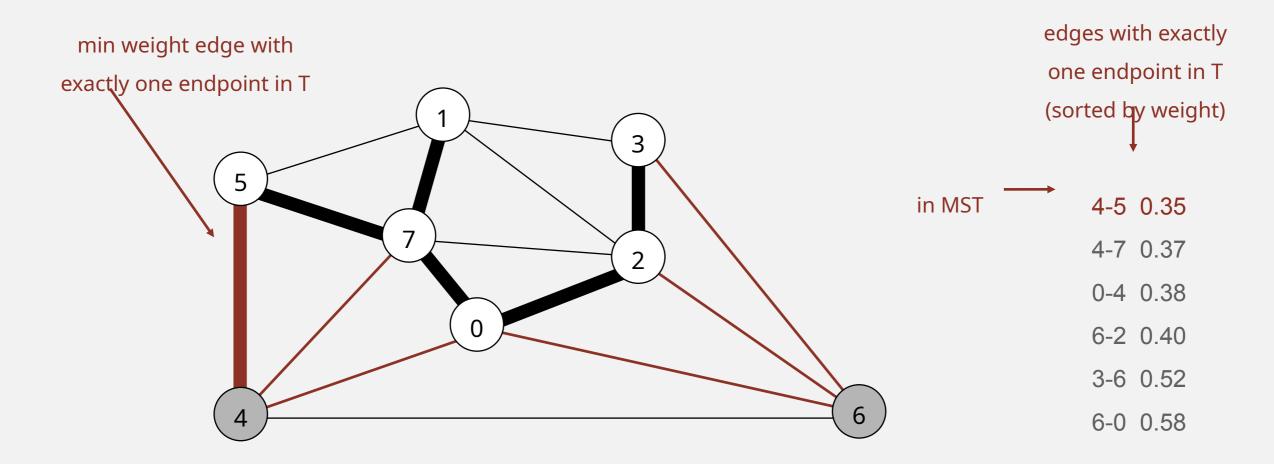
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3 5-7

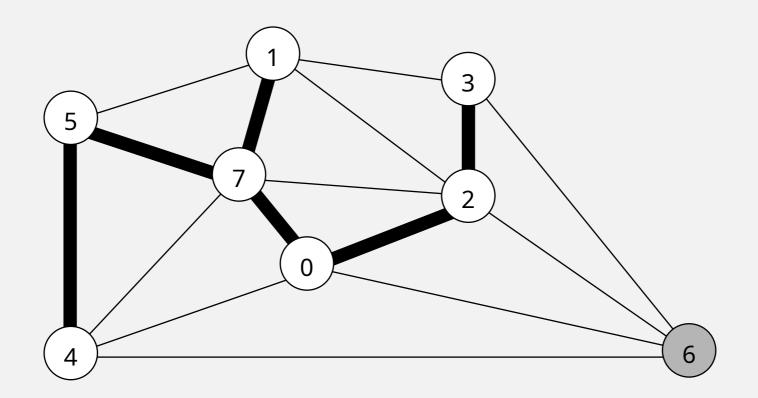
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3 5-7

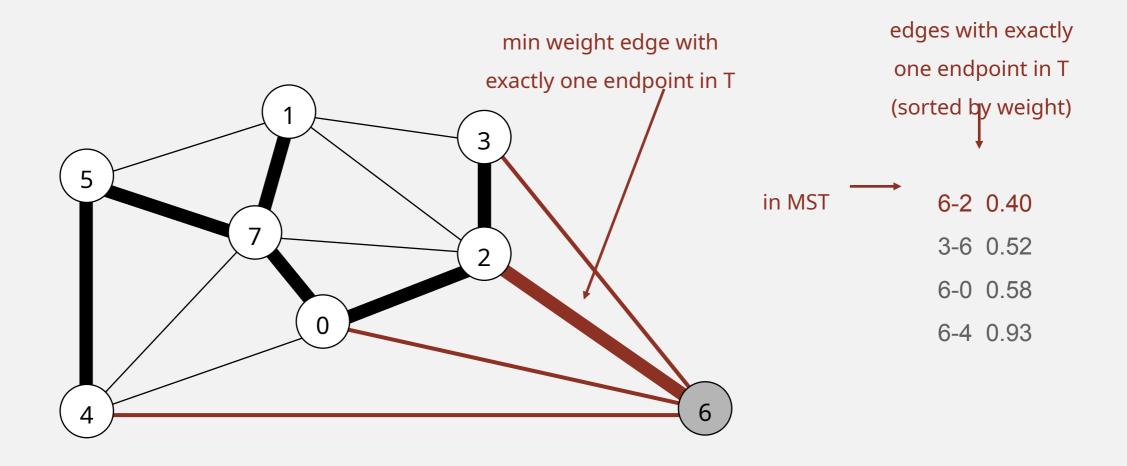
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3 5-7 4-5

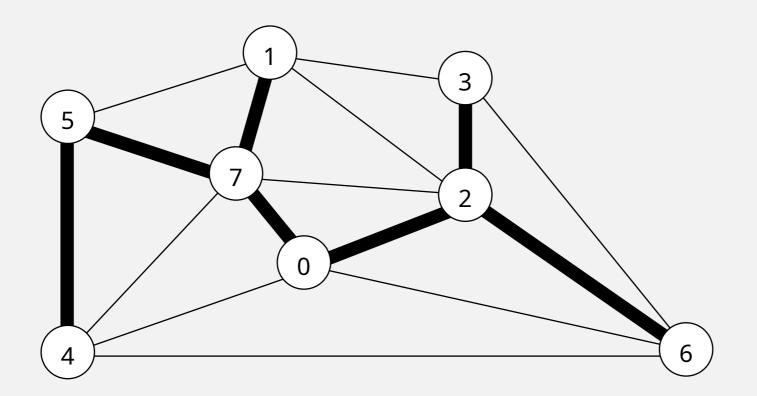
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3 5-7 4-5

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3 5-7 4-5 6-2

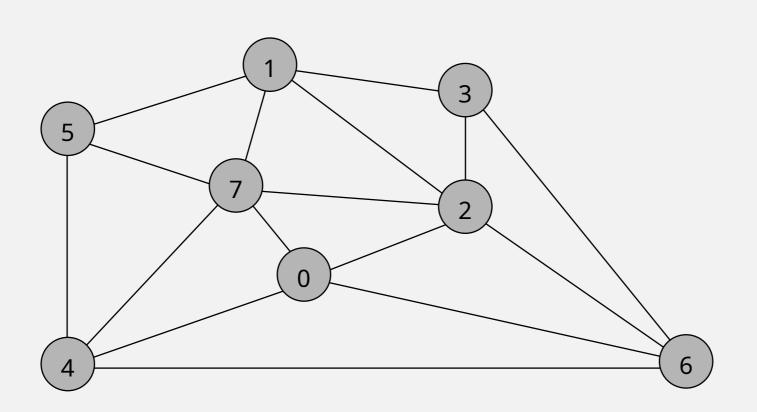


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PRIM'S ALGORITHM DEMO

- Prim's algorithm
- lazy implementation
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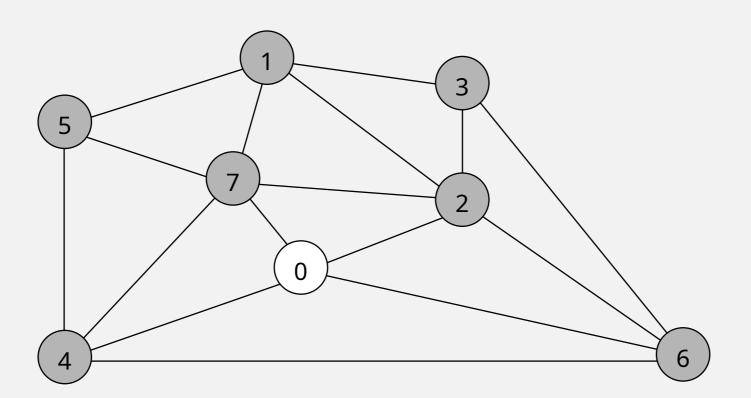
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



an edge-weighted graph

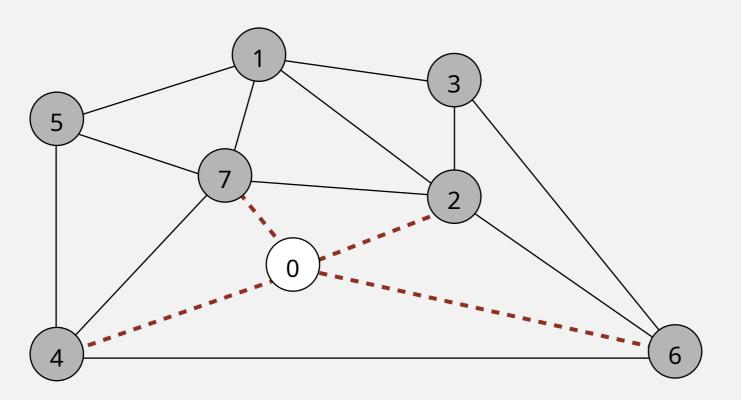
- 0-7 0.16
- 2-3 0.17
- 1-7 0.19
- 0-2 0.26
- 5-7 0.28
- 1-3 0.29
- 1-5 0.32
- 2-7 0.34
- 4-5 0.35
- 1-2 0.36
- 4-7 0.37
- 0-4 0.38
- 6-2 0.40
- 36 052

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

add to PQ all edges incident to 0

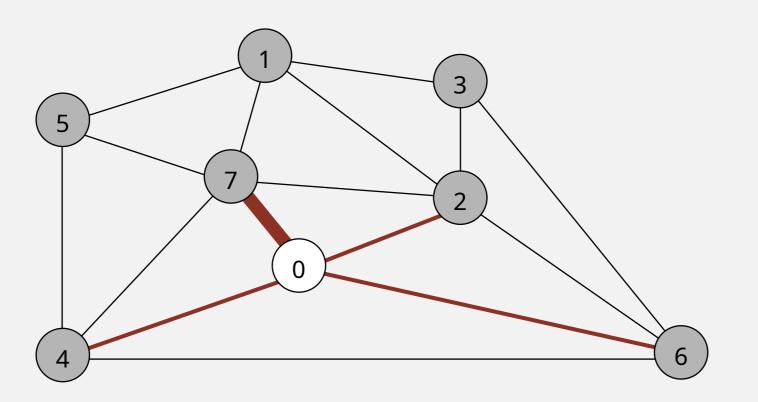


edges on PQ (sorted by weight)

- * 0-7 0.16
- * 0-2 0.26
- * 0-4 0.38
- * 6-0 0.58

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 0-7 and add to MST



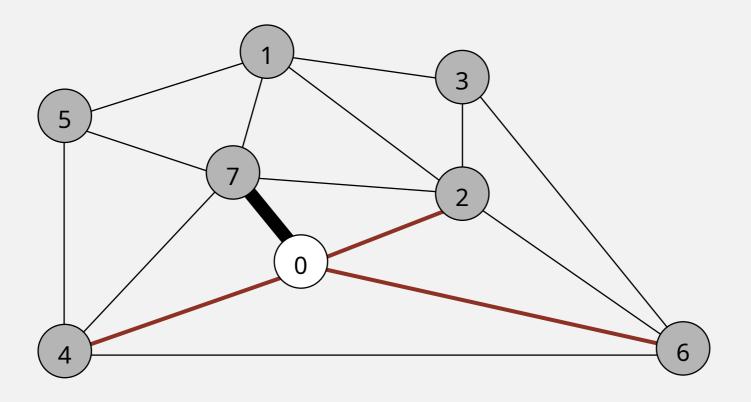
edges on PQ
(sorted by weight)

0-7 0.16

0-2 0.26

0-4 0.38

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



edges on PQ
(sorted by weight)

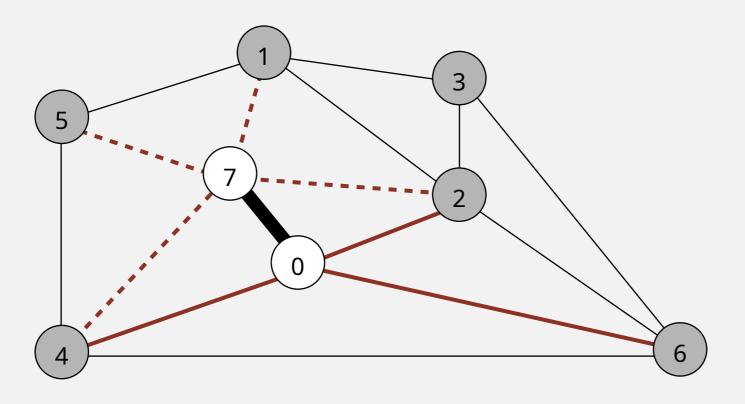
0-2 0.26

0-4 0.38

6-0 0.58

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

add to PQ all edges incident to 7



edges on PQ
(sorted by weight)

* 1-7 0.19

0-2 0.26

* 5-7 0.28

* 2-7 0.34

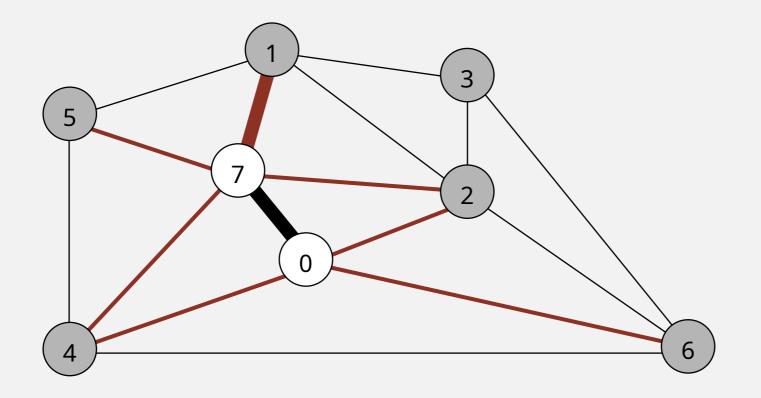
* 4-7 0.37

0-4 0.38

6-0 0.58

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 1-7 and add to MST



edges on PQ (sorted by weight)

1-7 0.19

0-2 0.26

5-7 0.28

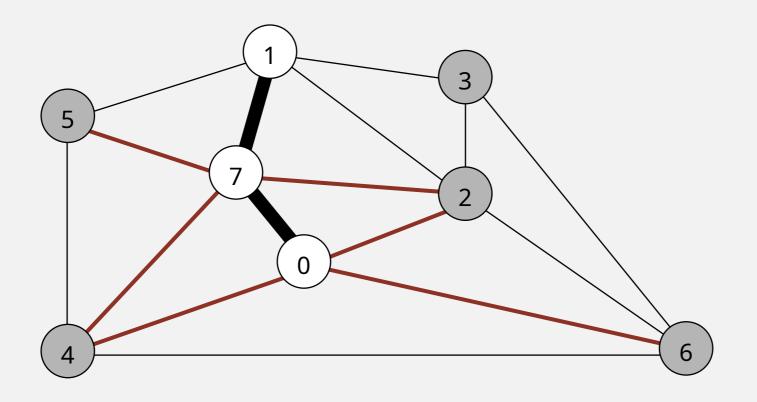
2-7 0.34

4-7 0.37

0-4 0.38

6-0 0.58

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



edges on PQ (sorted by weight)

0-2 0.26

5-7 0.28

2-7 0.34

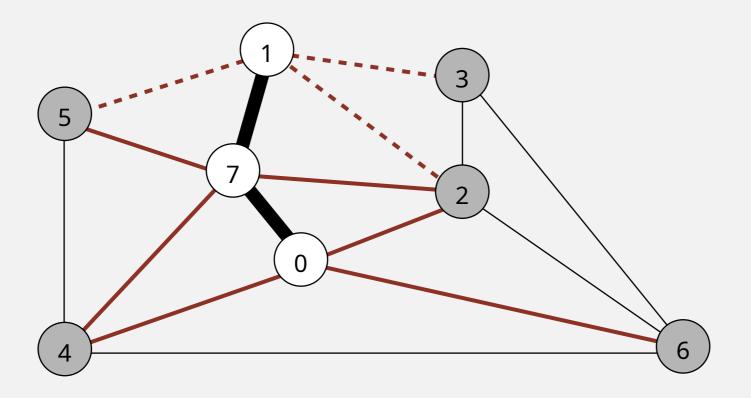
4-7 0.37

0-4 0.38

6-0 0.58

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

add to PQ all edges incident to 1



MST edges

0-7 1-7

edges on PQ
(sorted by weight)

0-2 0.26

5-7 0.28

* 1-3 0.29

* 1-5 0.32

2-7 0.34

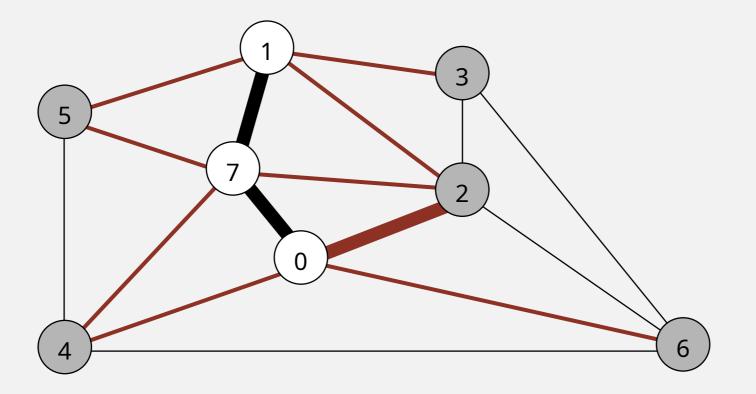
* 1-2 0.36

4-7 0.37

0-4 0.38

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete edge 0-2 and add to MST



MST edges

0-7 1-7

edges on PQ
(sorted by weight)

0-2 0.26

5-7 0.28

1-3 0.29

1-5 0.32

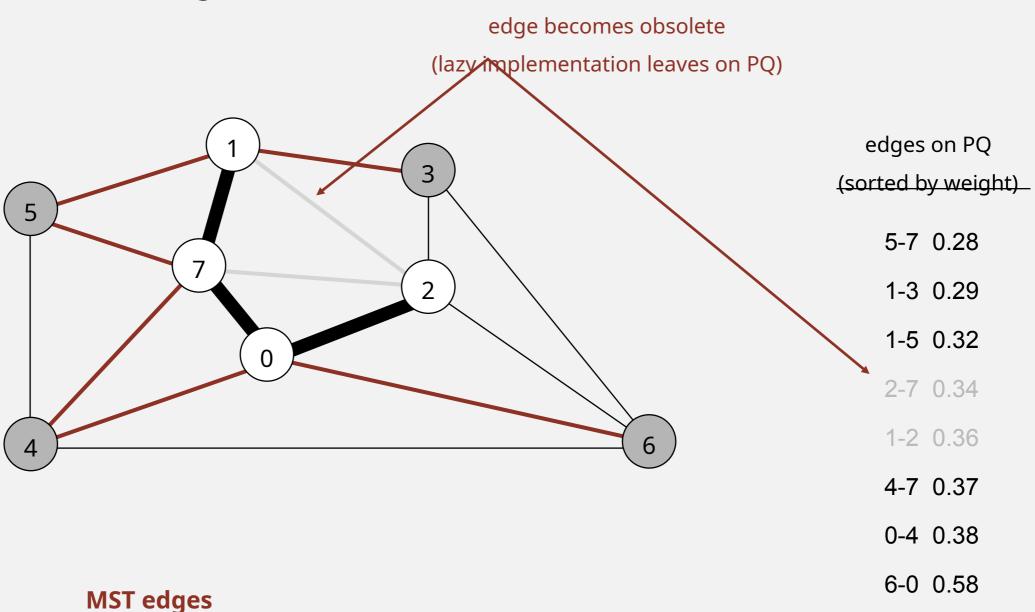
2-7 0.34

1-2 0.36

4-7 0.37

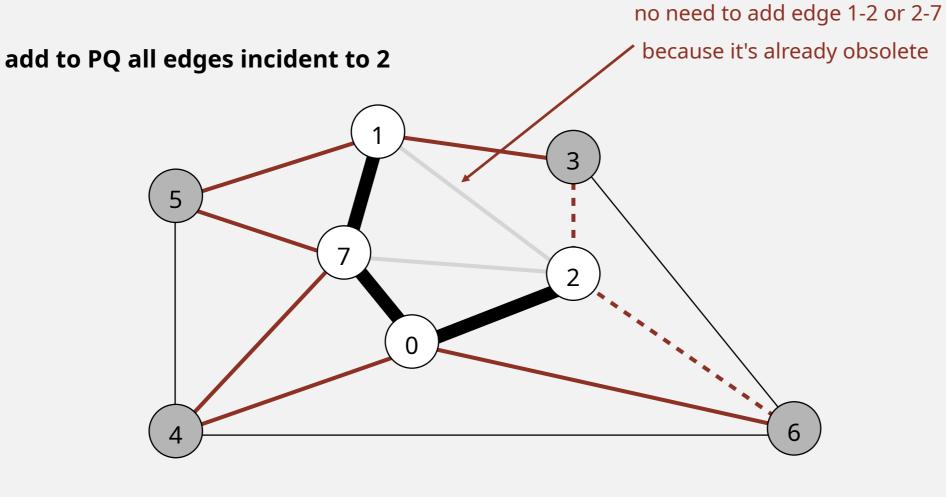
0-4 0.38

- Start with vertex 0 and greedily grow tree *T*.
- Add to *T* the min weight edge with exactly one endpoint in *T*.
- Repeat until V 1 edges.



0-7 1-7 0-2

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2

edges on PQ
(sorted by weight)

* 2-3 0.17

5-7 0.28

1-3 0.29

1-5 0.32

2-7 0.34

1-2 0.36

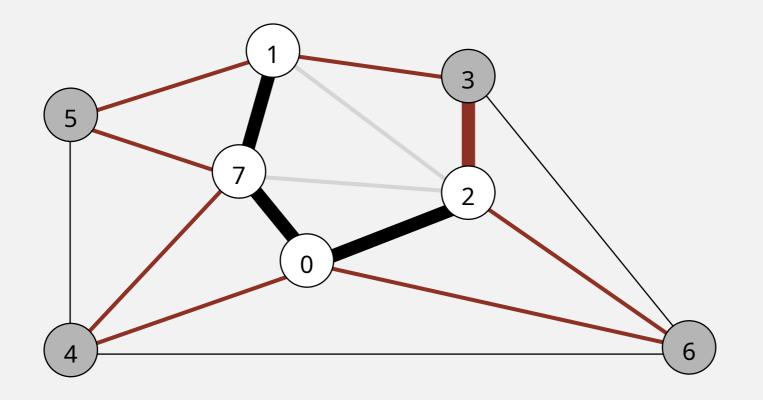
4-7 0.37

0-4 0.38

* 6-2 0.40

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 2-3 and add to MST



MST edges

0-7 1-7 0-2

edges on PQ
(sorted by weight)

* 2-3 0.17

5-7 0.28

1-3 0.29

1-5 0.32

2-7 0.34

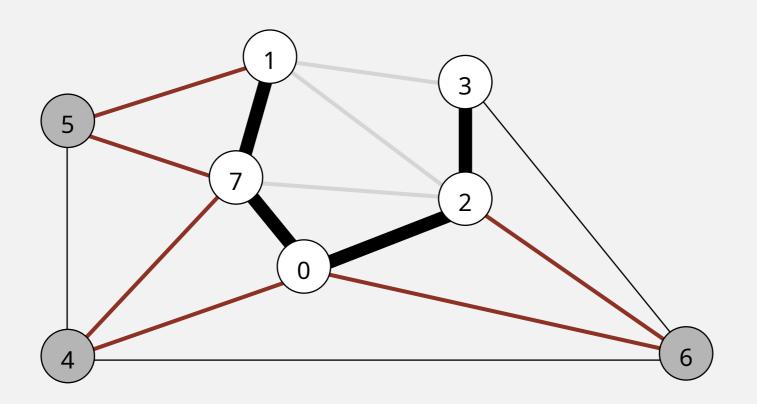
1-2 0.36

4-7 0.37

0-4 0.38

* 6-2 0.40

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3

edges on PQ
(sorted by weight)

5-7 0.28

1-3 0.29

1-5 0.32

2-7 0.34

1-2 0.36

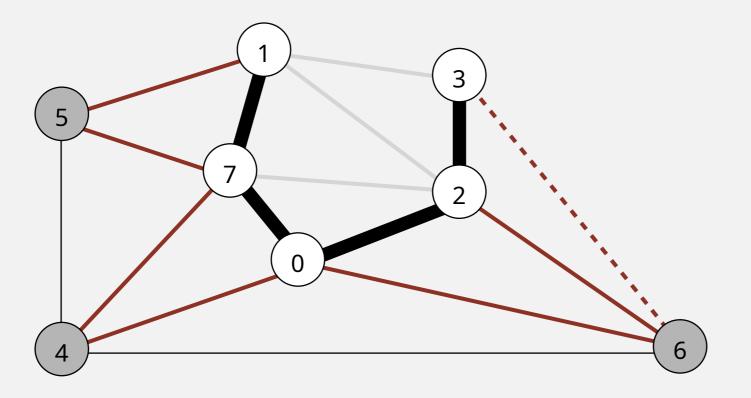
4-7 0.37

0-4 0.38

6-2 0.40

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

add to PQ all edges incident to 3



MST edges

0-7 1-7 0-2 2-3

edges on PQ (sorted by weight)

5-7 0.28

1-3 0.29

1-5 0.32

2-7 0.34

1-2 0.36

4-7 0.37

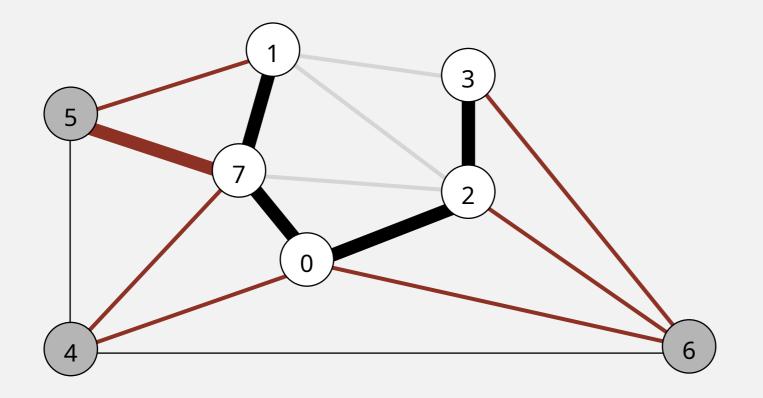
0-4 0.38

6-2 0.40

* 3-6 0.52

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 5-7 and add to MST



MST edges

0-7 1-7 0-2 2-3

edges on PQ
(sorted by weight)

5-7 0.28

1-3 0.29

1-5 0.32

2-7 0.34

1-2 0.36

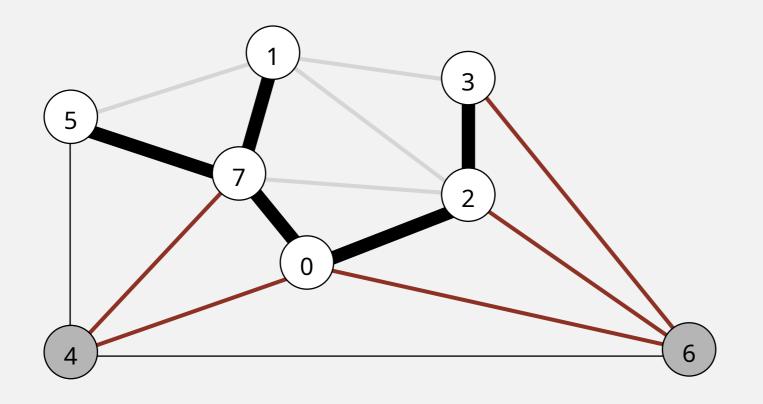
4-7 0.37

0-4 0.38

6-2 0.40

3-6 0.52

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3 5-7

edges on PQ
(sorted by weight)

1-3 0.29

1-5 0.32

2-7 0.34

1-2 0.36

4-7 0.37

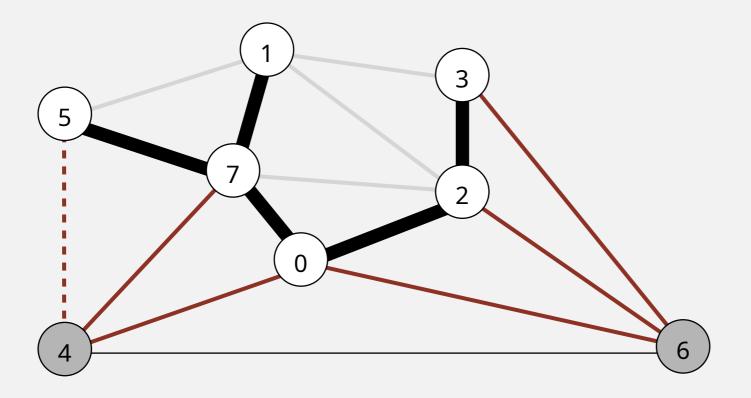
0-4 0.38

6-2 0.40

3-6 0.52

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

add to PQ all edges incident to 5



MST edges

0-7 1-7 0-2 2-3 5-7

edges on PQ (sorted by weight)

1-3 0.29

1-5 0.32

2-7 0.34

* 4-5 0.35

1-2 0.36

4-7 0.37

0-4 0.38

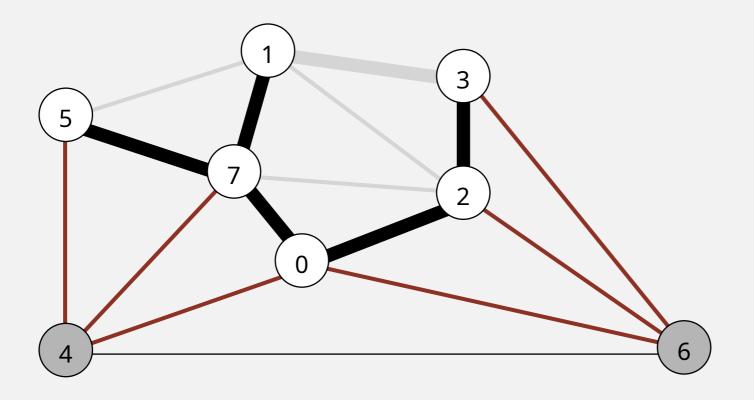
6-2 0.40

3-6 0.52

6-0 0.58

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 1-3 and discard obsolete edge



MST edges

0-7 1-7 0-2 2-3 5-7

edges on PQ
(sorted by weight)

1-3 0.29

1-5 0.32

2-7 0.34

4-5 0.35

1-2 0.36

4-7 0.37

0-4 0.38

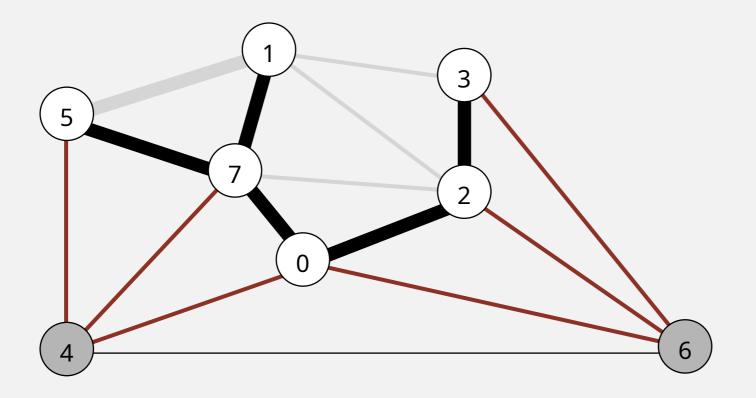
6-2 0.40

3-6 0.52

6-0 0.58

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 1-5 and discard obsolete edge



MST edges

0-7 1-7 0-2 2-3 5-7

edges on PQ
(sorted by weight)

1-5 0.32

2-7 0.34

4-5 0.35

1-2 0.36

4-7 0.37

0-4 0.38

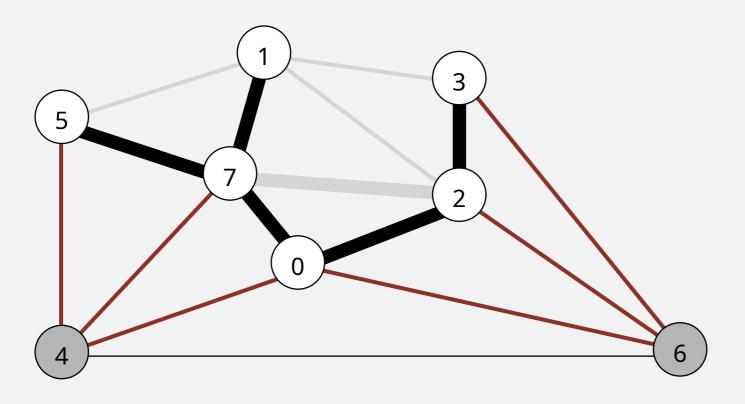
6-2 0.40

3-6 0.52

6-0 0.58

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 2-7 and discard obsolete edge



6-2 0.40

edges on PQ

(sorted by weight)

2-7 0.34

4-5 0.35

1-2 0.36

4-7 0.37

0-4 0.38

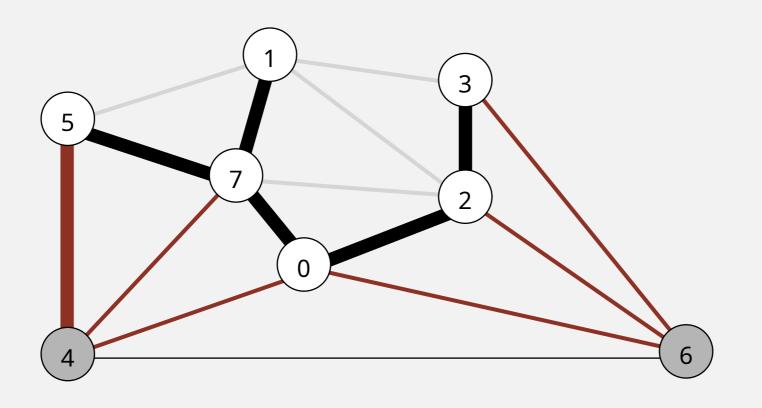
3-6 0.52

6-0 0.58

MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 4-5 and add to MST



edges on PQ
(sorted by weight)

4-5 0.35

1-2 0.36

4-7 0.37

0-4 0.38

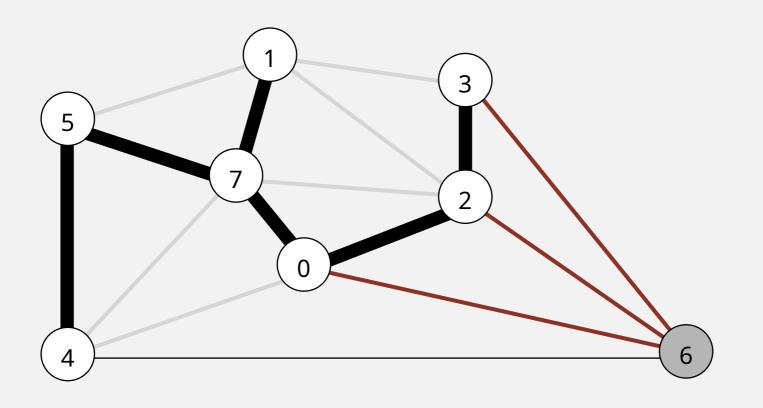
6-2 0.40

3-6 0.52

6-0 0.58

MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



edges on PQ
(sorted by weight)

1-2 0.36

4-7 0.37

0-4 0.38

6-2 0.40

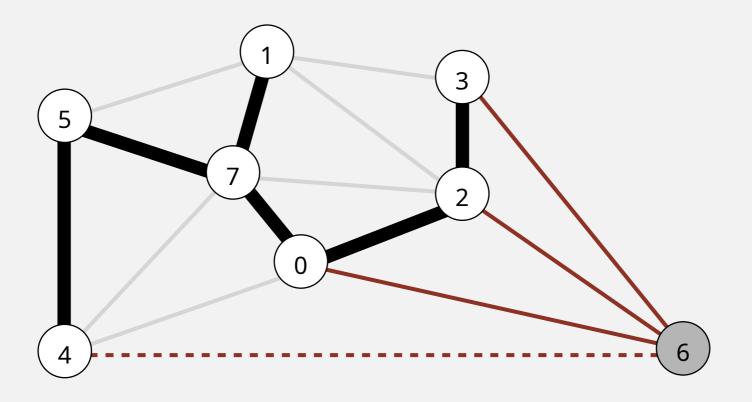
3-6 0.52

6-0 0.58

MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

add to PQ all edges incident to 4



edges on PQ
(sorted by weight)

1-2 0.36

4-7 0.37

0-4 0.38

6-2 0.40

3-6 0.52

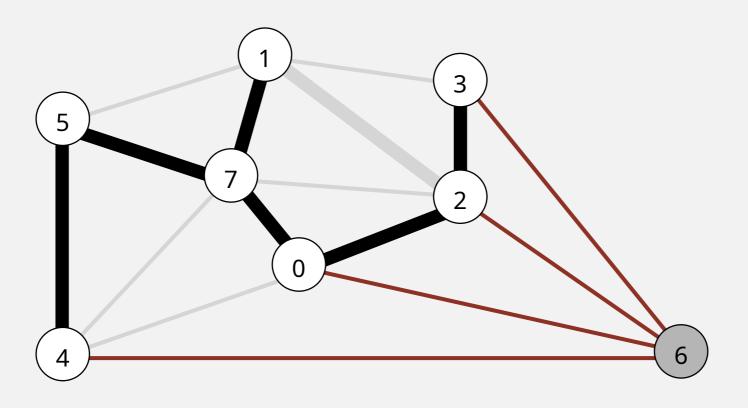
6-0 0.58

* 6-4 0.93

MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 1-2 and discard obsolete edge



edges on PQ
(sorted by weight)

1-2 0.36

4-7 0.37

0-4 0.38

6-2 0.40

3-6 0.52

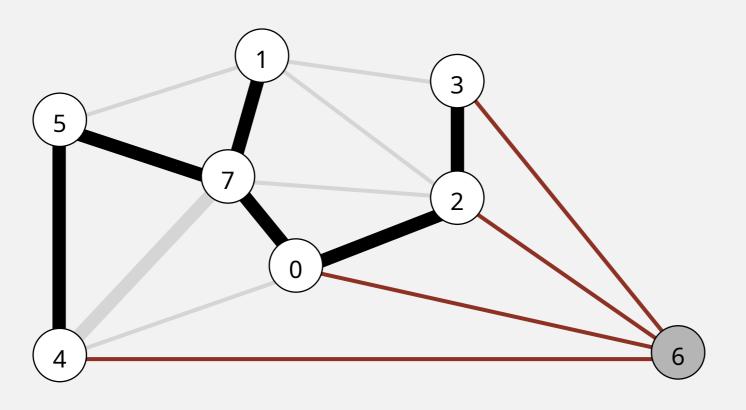
6-0 0.58

6-4 0.93

MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 4-7 and discard obsolete edge



edges on PQ (sorted by weight)

4-7 0.37

0-4 0.38

6-2 0.40

3-6 0.52

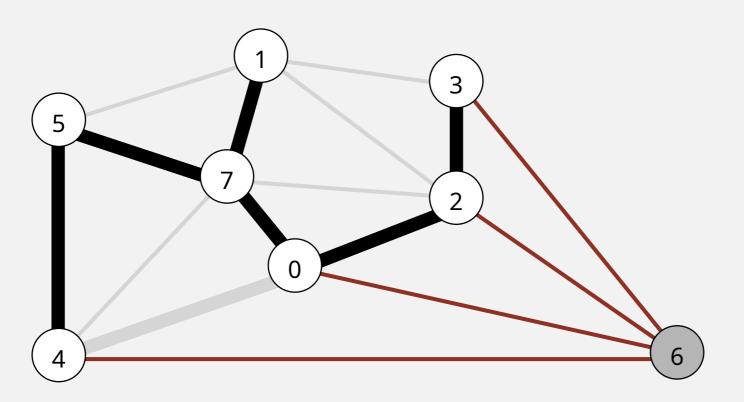
6-0 0.58

6-4 0.93

MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 0-4 and discard obsolete edge



edges on PQ (sorted by weight)

0-4 0.38

6-2 0.40

3-6 0.52

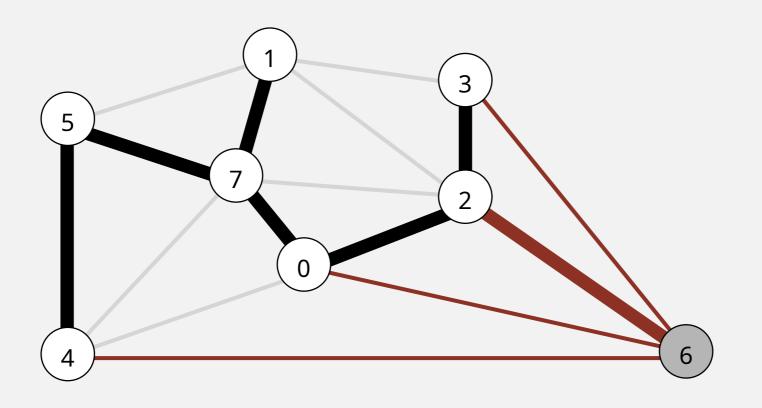
6-0 0.58

6-4 0.93

MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 6-2 and add to MST



edges on PQ (sorted by weight)

6-2 0.40

3-6 0.52

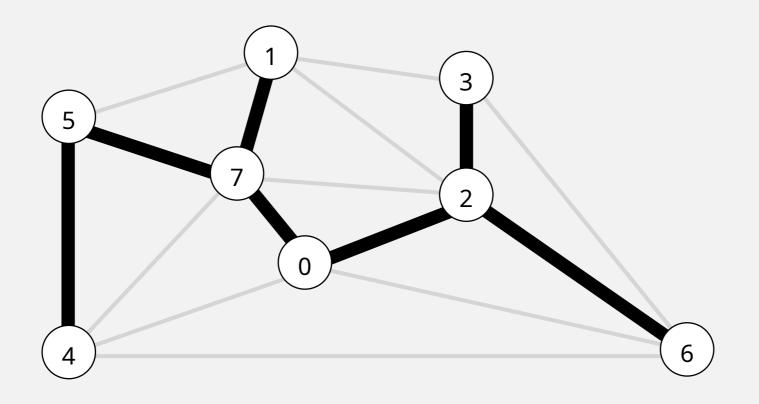
6-0 0.58

6-4 0.93

MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

delete 6-2 and add to MST



edges on PQ (sorted by weight)

3-6 0.52

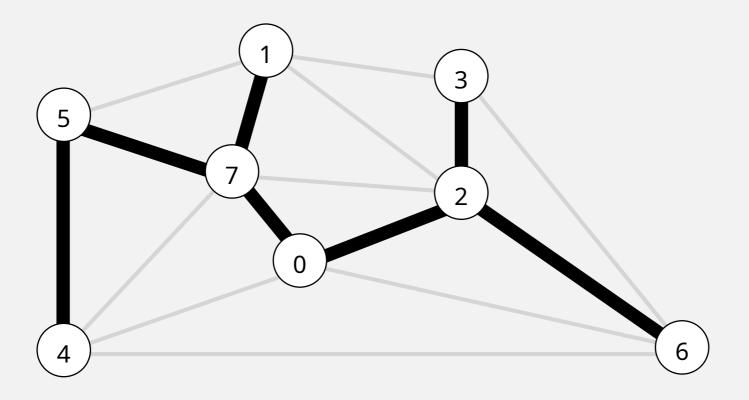
6-0 0.58

6-4 0.93

MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

stop since V-1 edges



edges on PQ (sorted by weight)

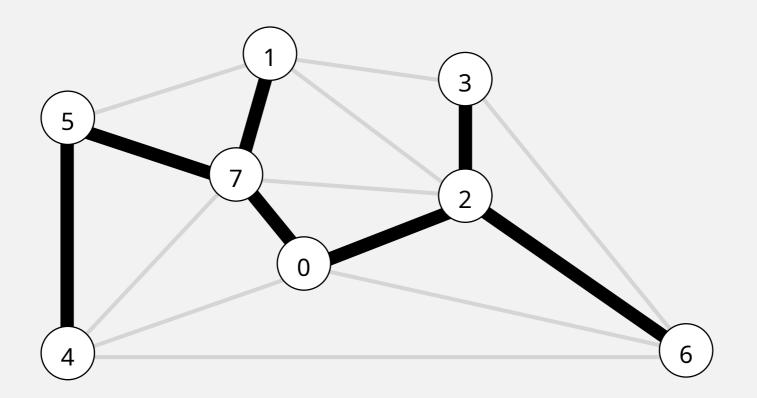
3-6 0.52

6-0 0.58

6-4 0.93

MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges



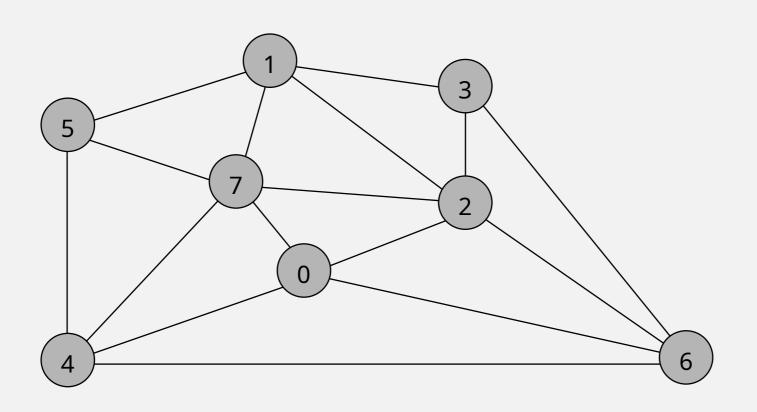
ROBERT SEDGEWICK | KEVIN WAYNE

http://algs4.cs.princeton.edu

PRIM'S ALGORITHM DEMO

- Prim's algorithm
- lazy implementation
- eager implementation

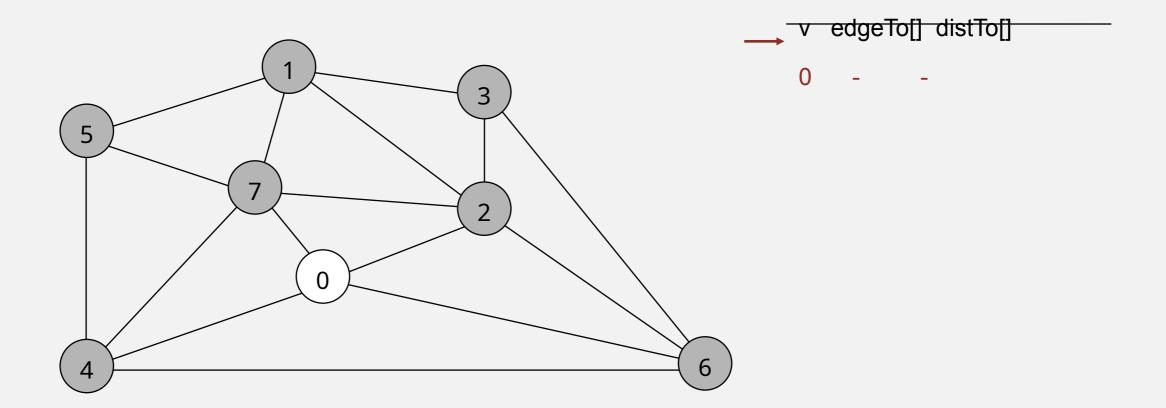
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



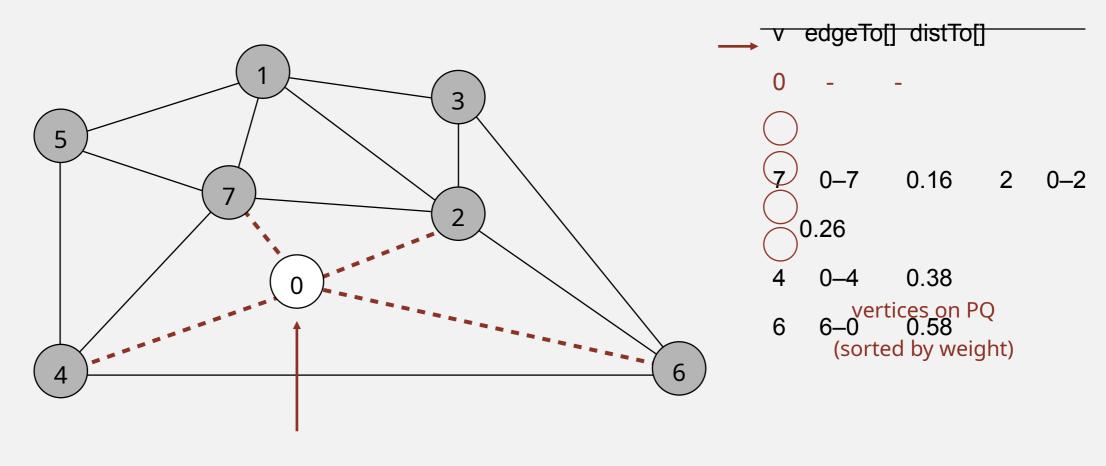
an edge-weighted graph

- 0-7 0.16
- 2-3 0.17
- 1-7 0.19
- 0-2 0.26
- 5-7 0.28
- 1-3 0.29
- 1-5 0.32
- 2-7 0.34
- 4-5 0.35
- 1-2 0.36
- 4-7 0.37
- 0-4 0.38
- 6-2 0.40
- 36 0 52

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

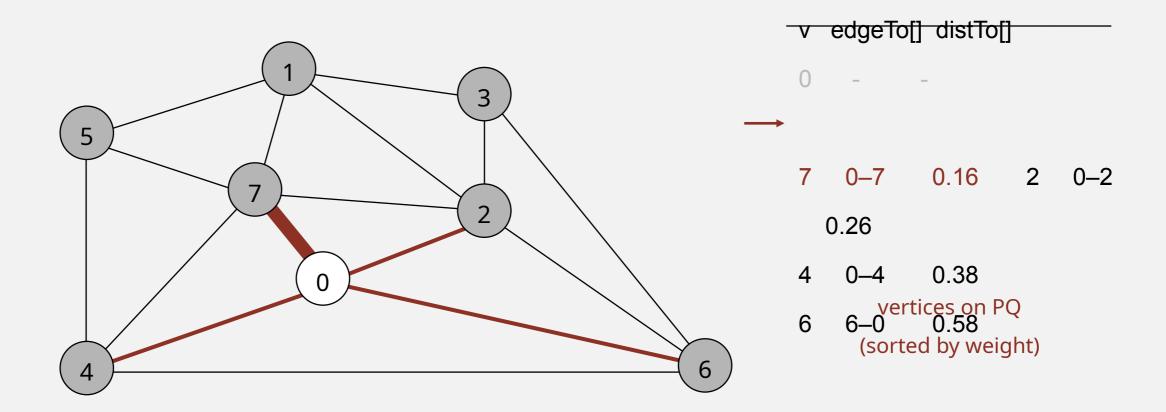


- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

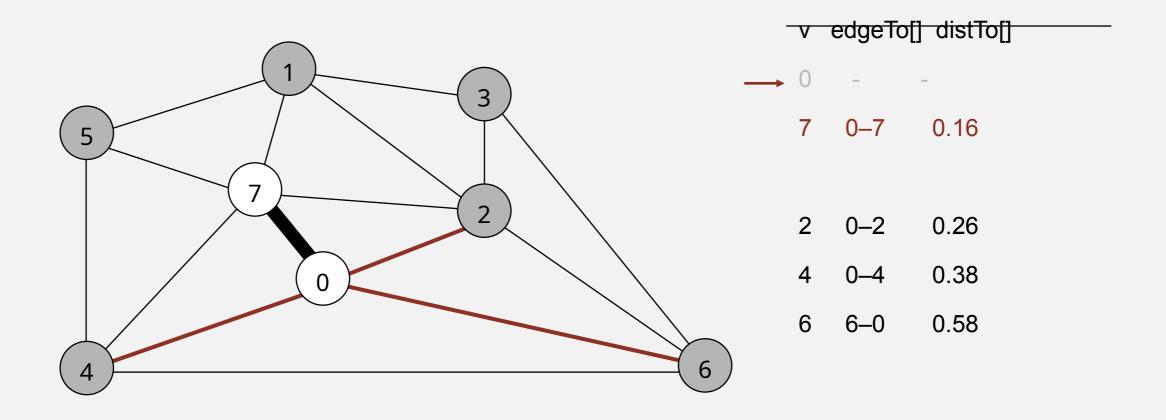


add vertices 7, 2, 4, and 6 to PQ

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



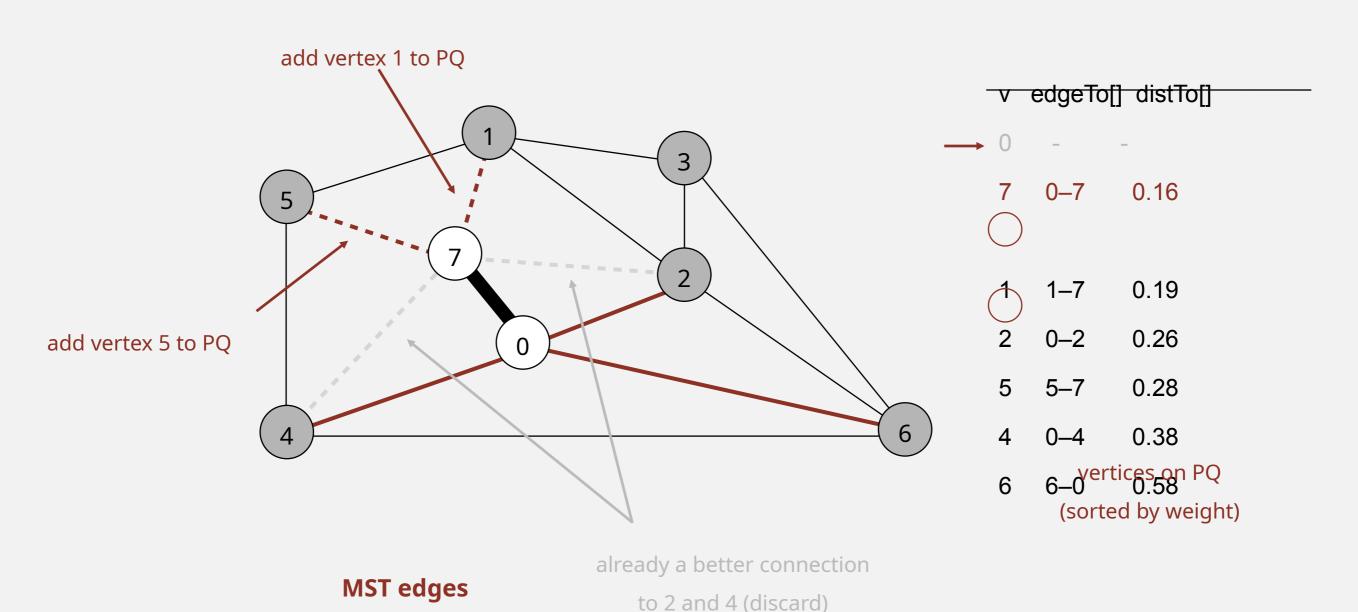
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



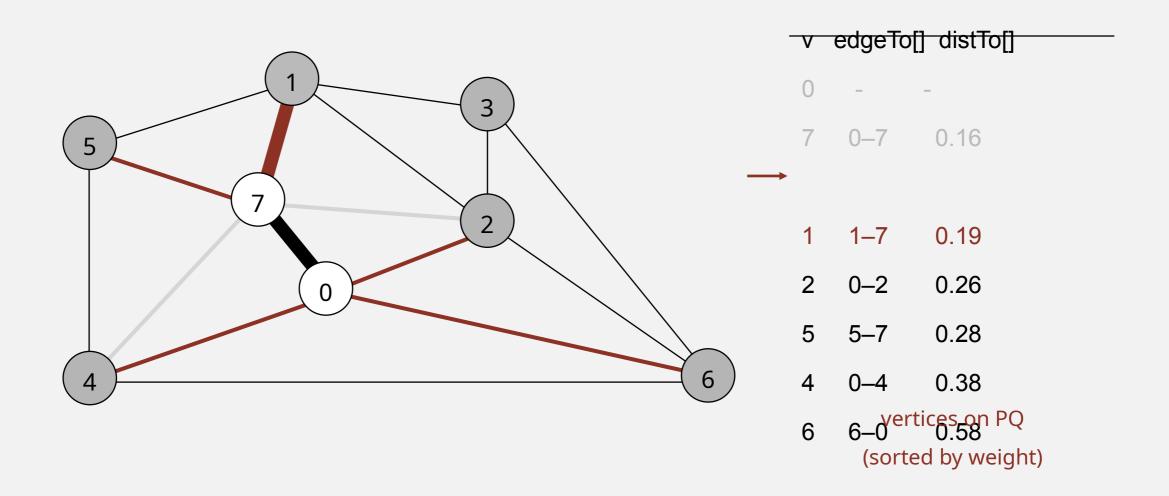
MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

0-7

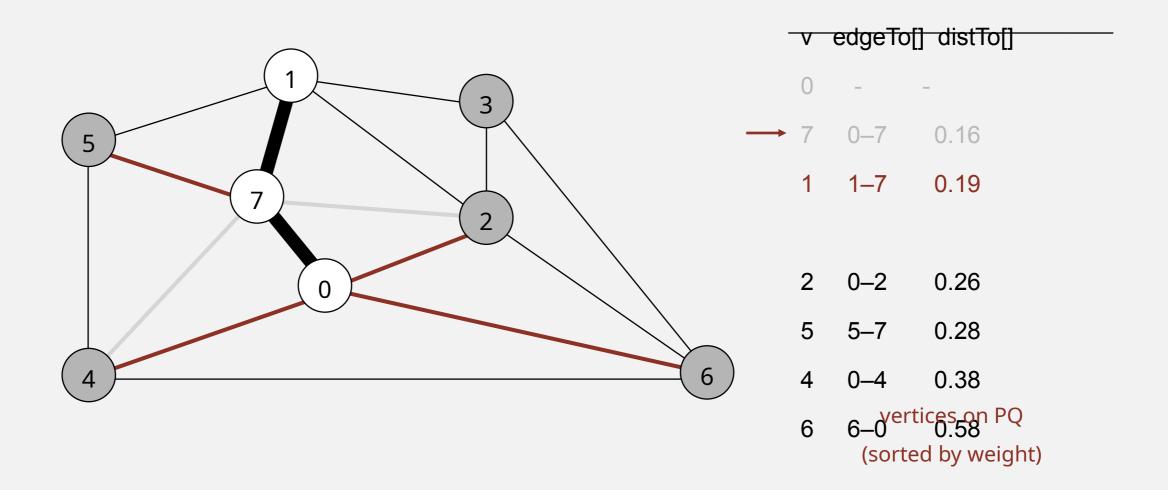


- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



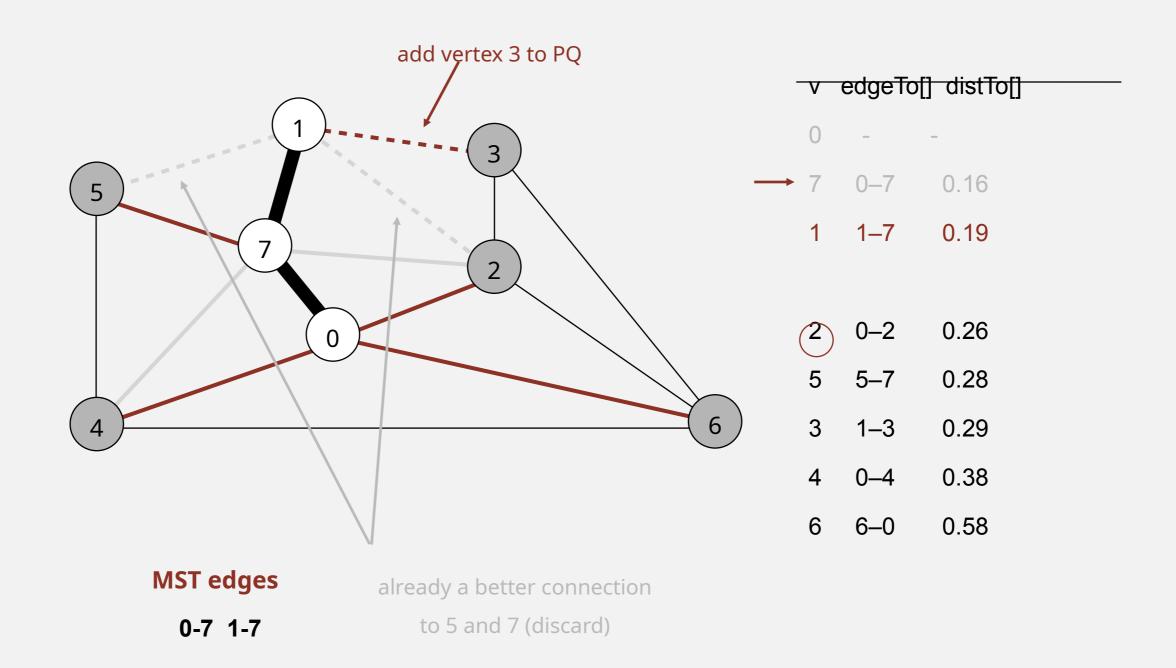
MST edges

- Start with vertex 0 and greedily grow tree T.
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- Repeat until V 1 edges.

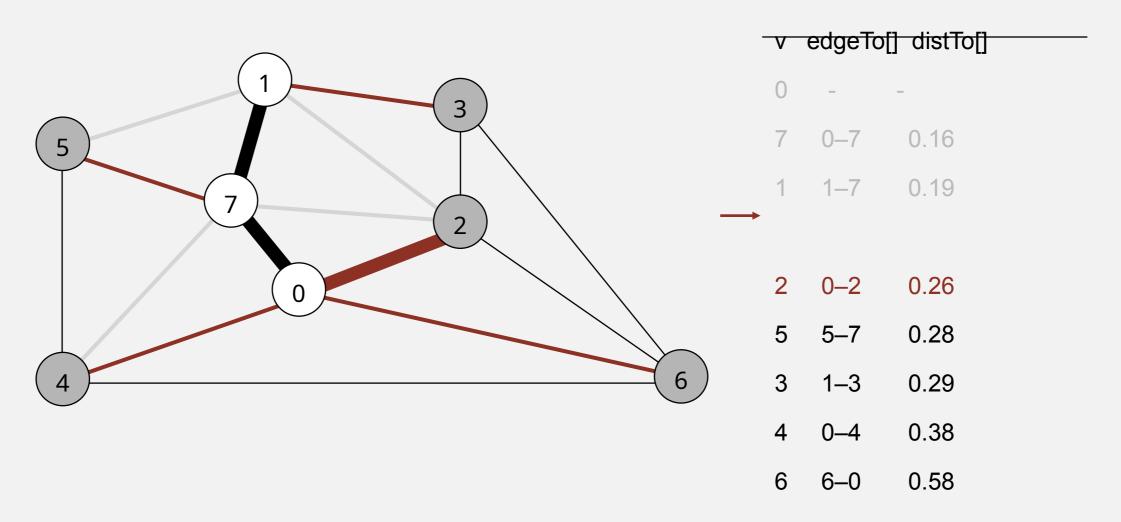


MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.

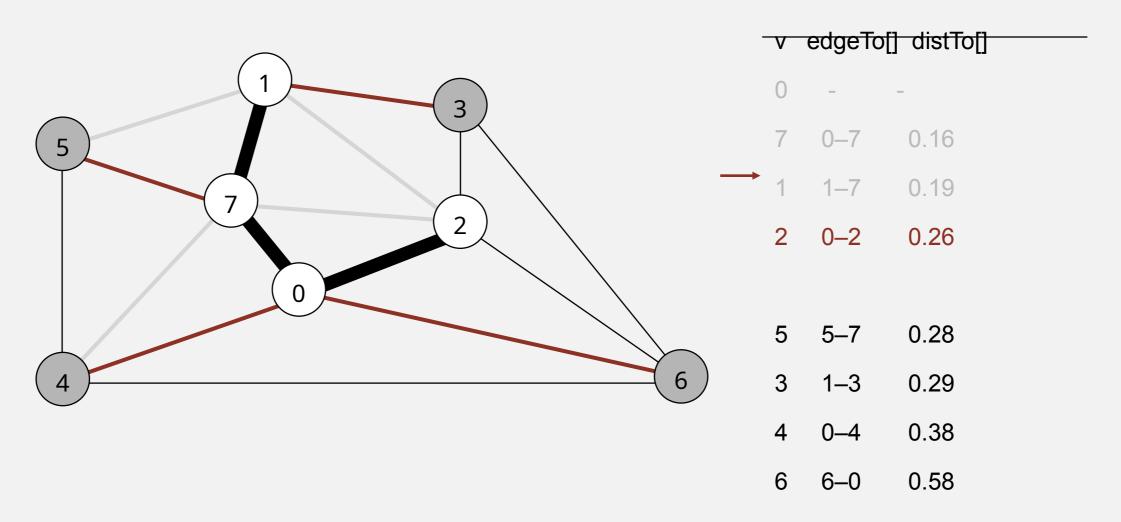


- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



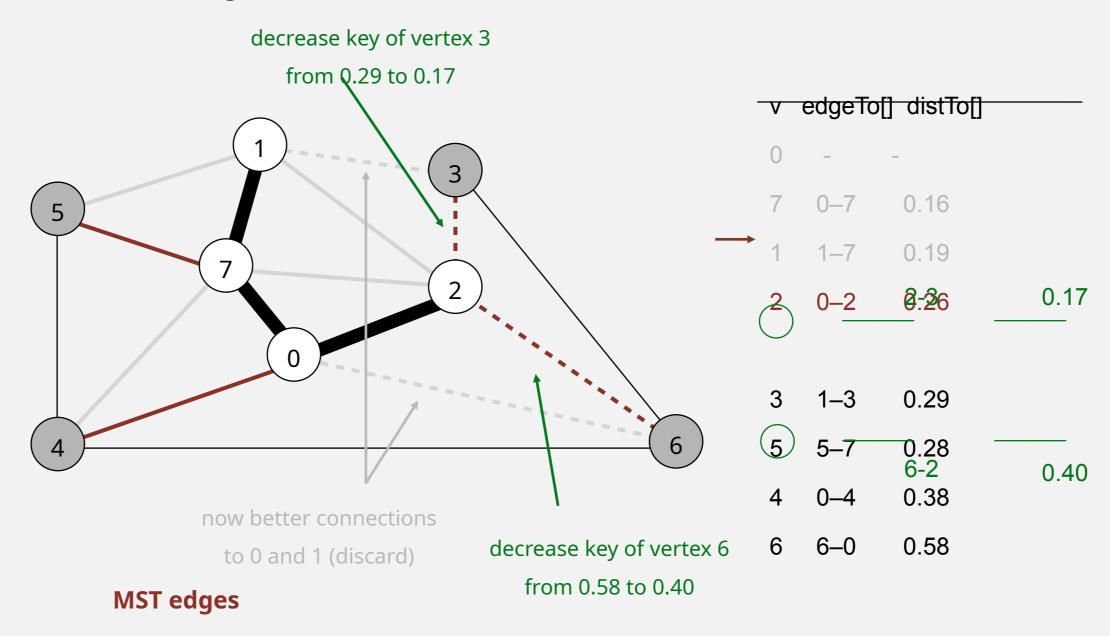
MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



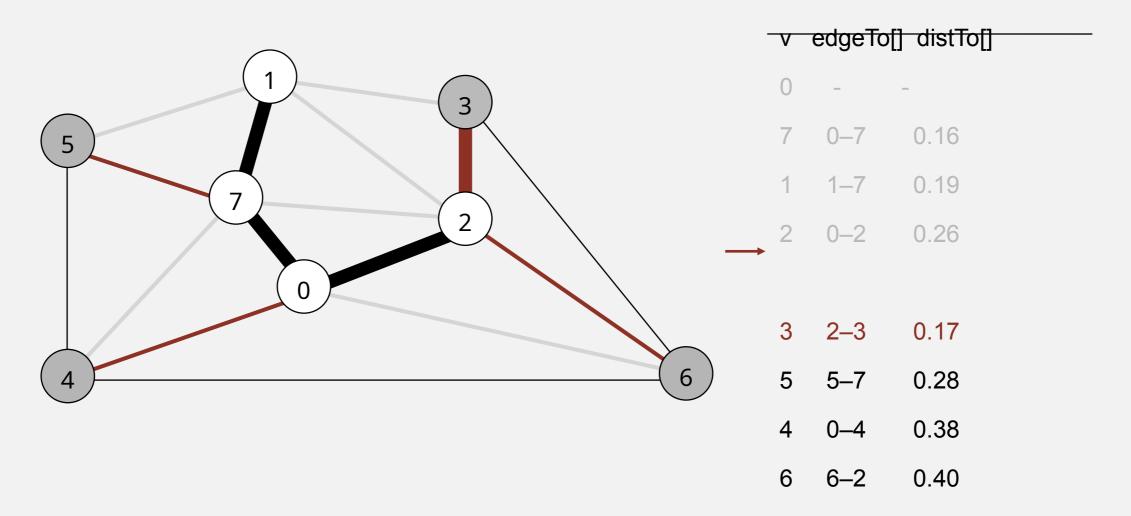
MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



0-7 1-7 0-2

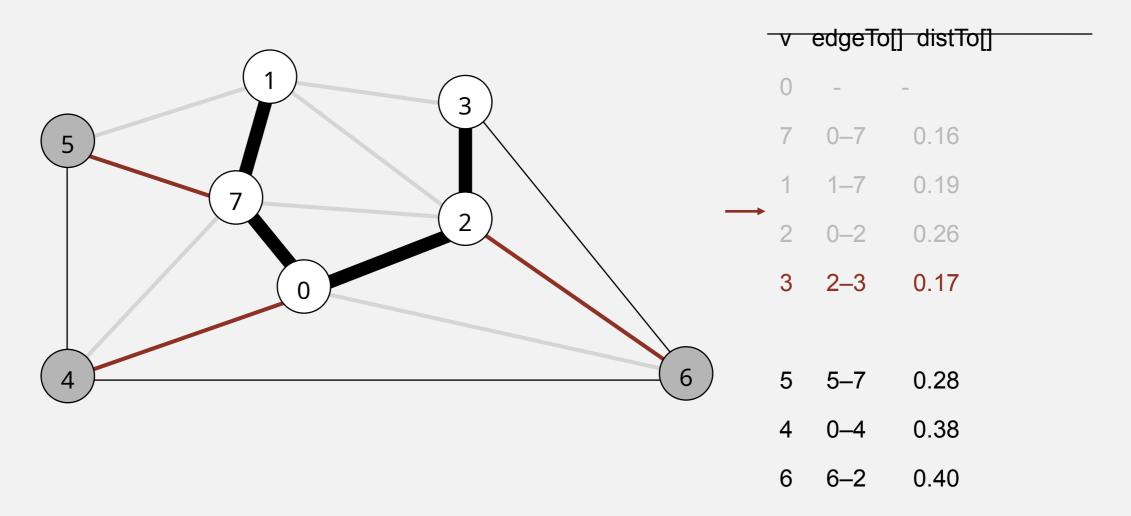
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

0-7 1-7 0-2 2-3

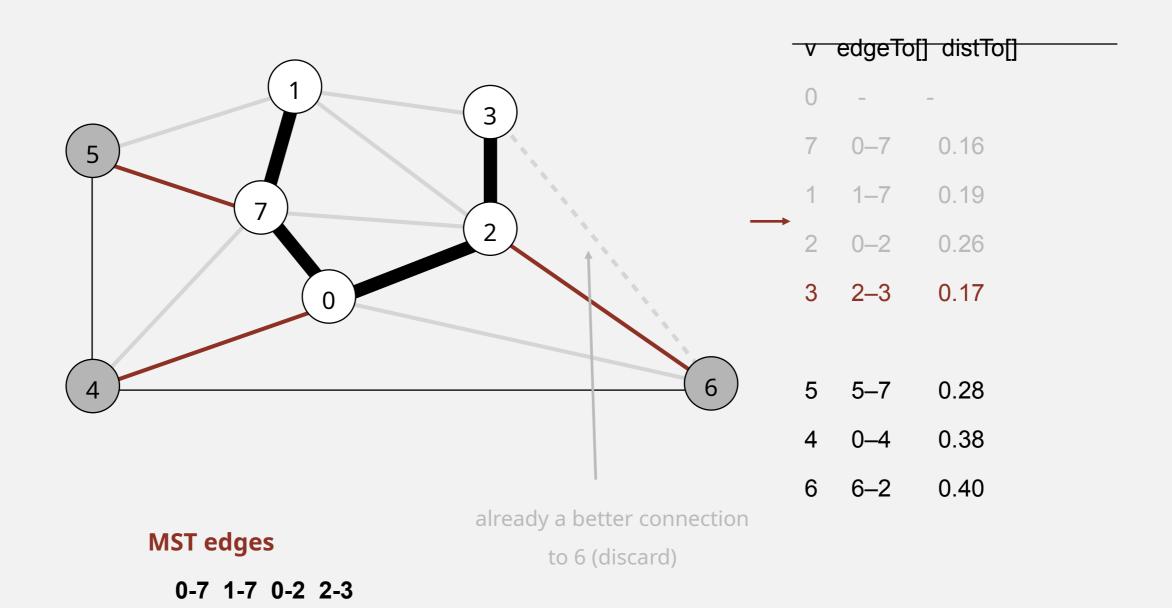
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



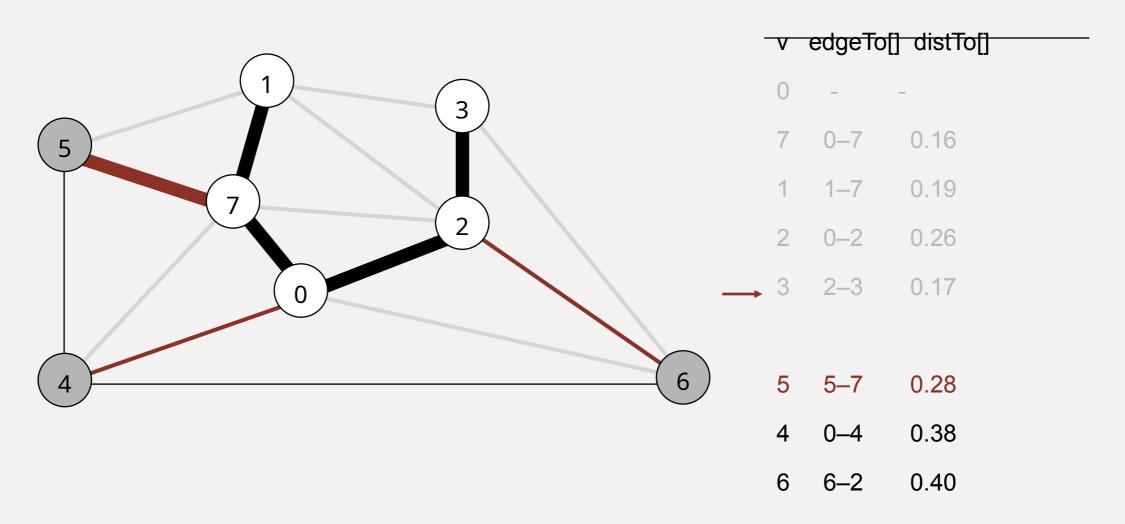
MST edges

0-7 1-7 0-2 2-3

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



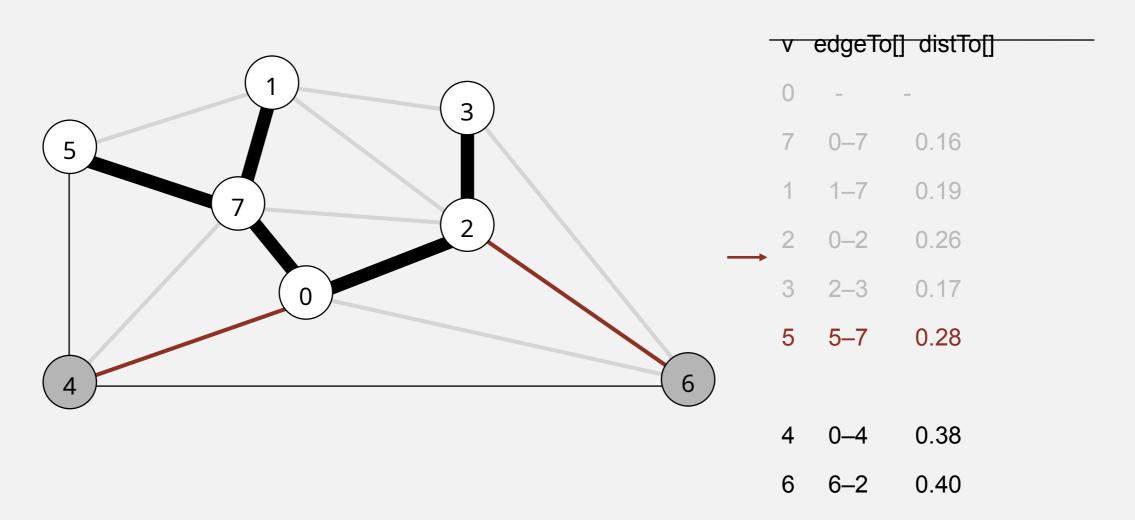
- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



MST edges

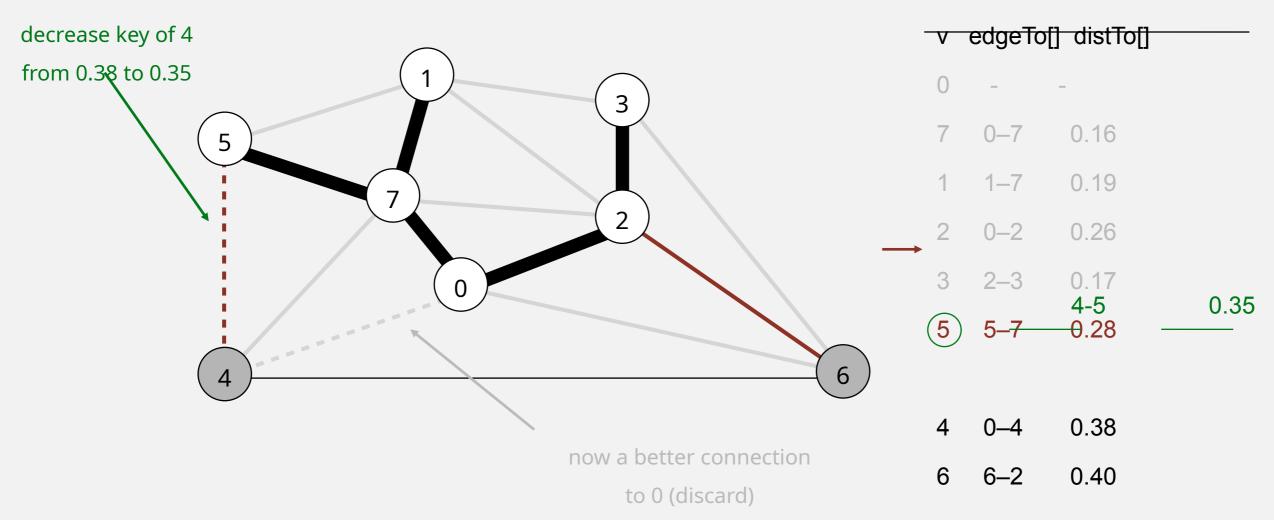
0-7 1-7 0-2 2-3

- Start with vertex 0 and greedily grow tree T.
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- Repeat until V 1 edges.



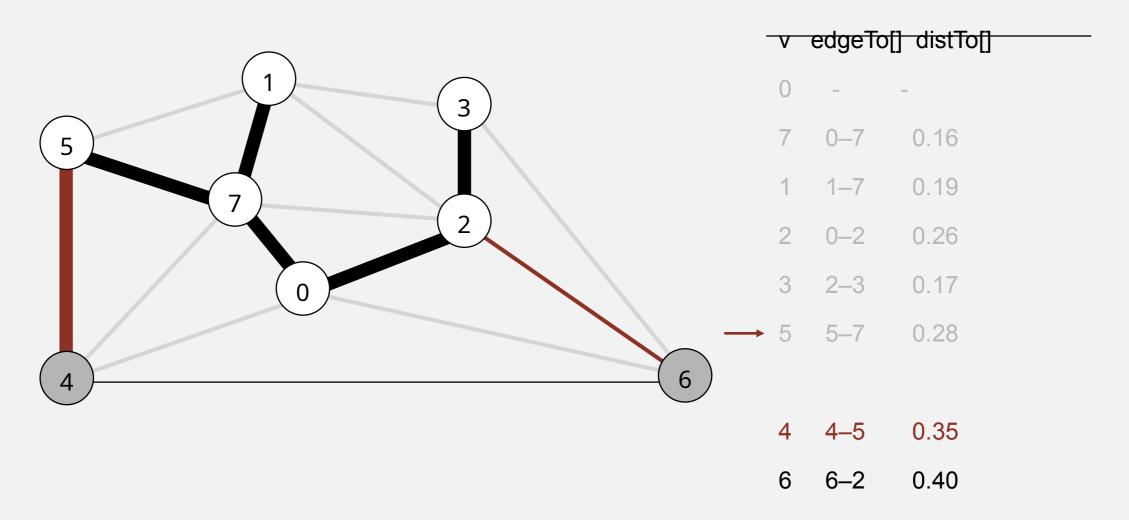
MST edges

- Start with vertex 0 and greedily grow tree T.
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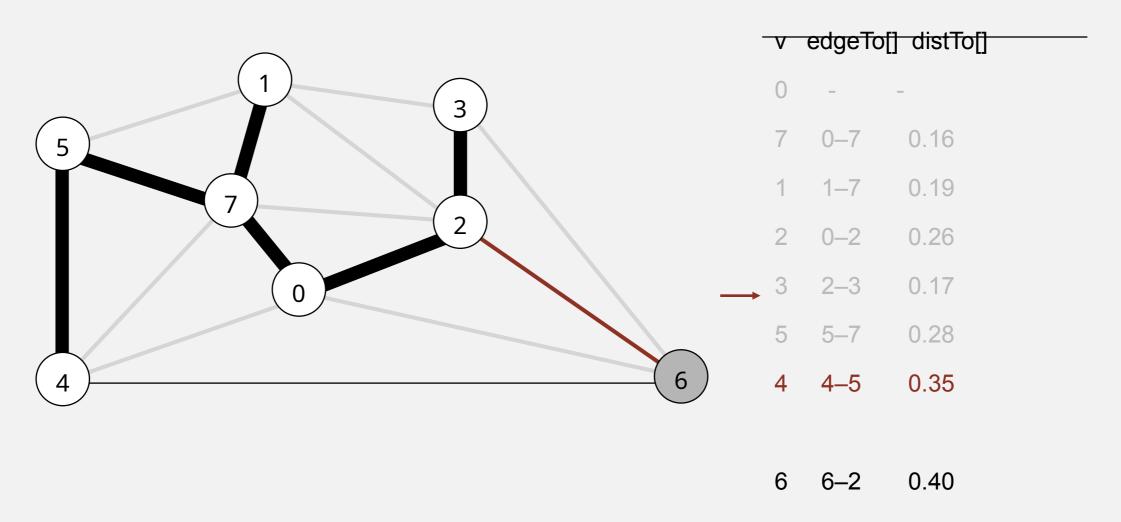
MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



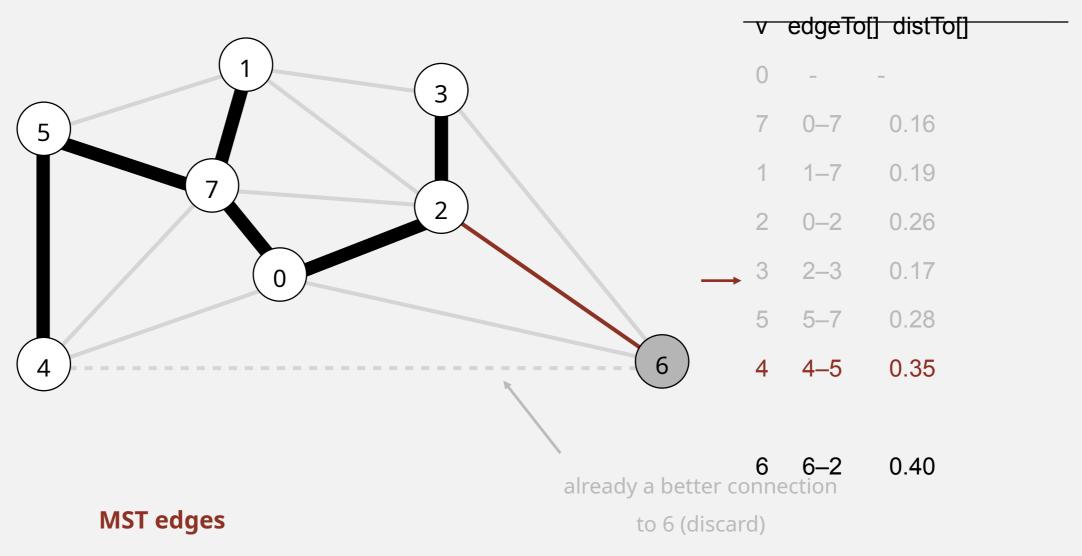
MST edges

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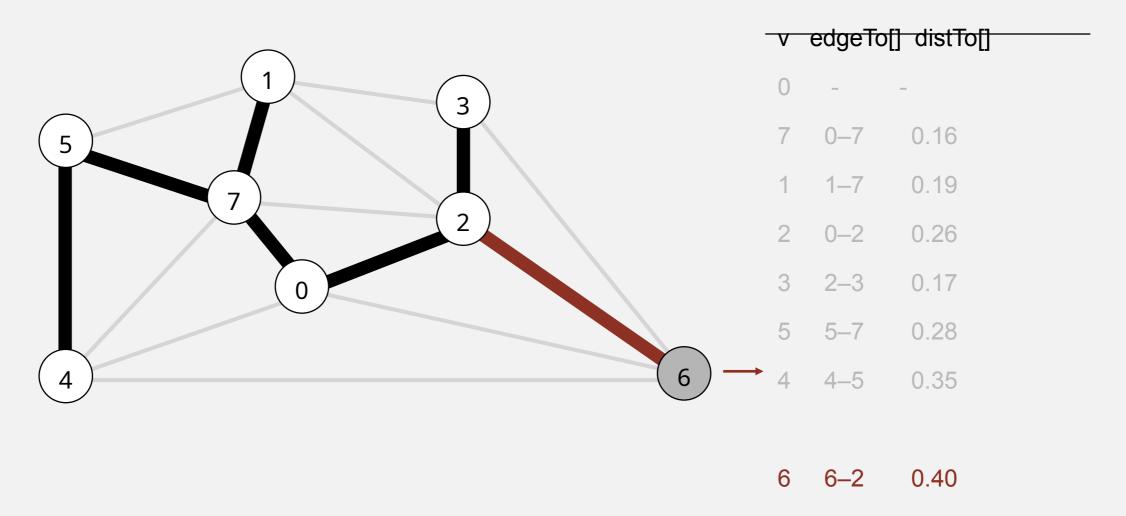


MST edges

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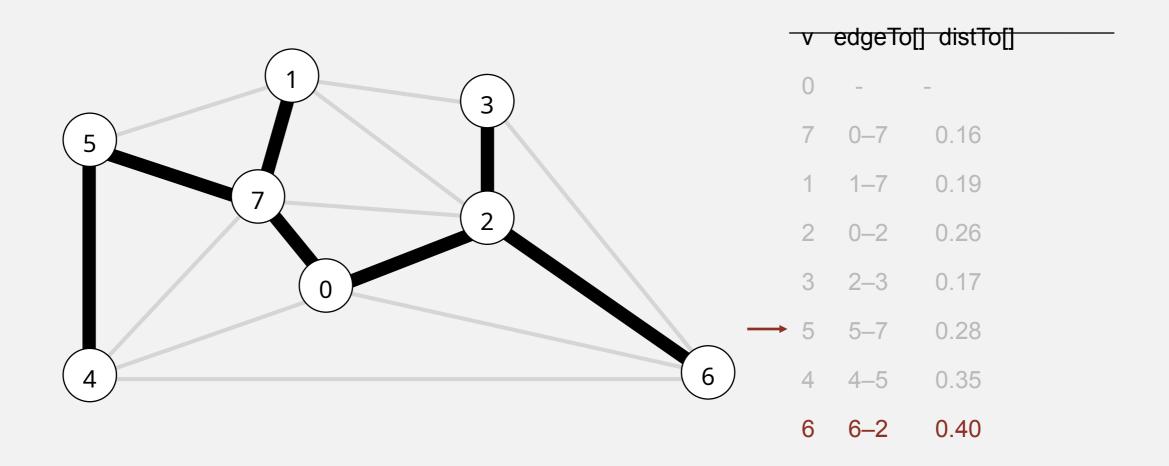


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- Repeat until V 1 edges.



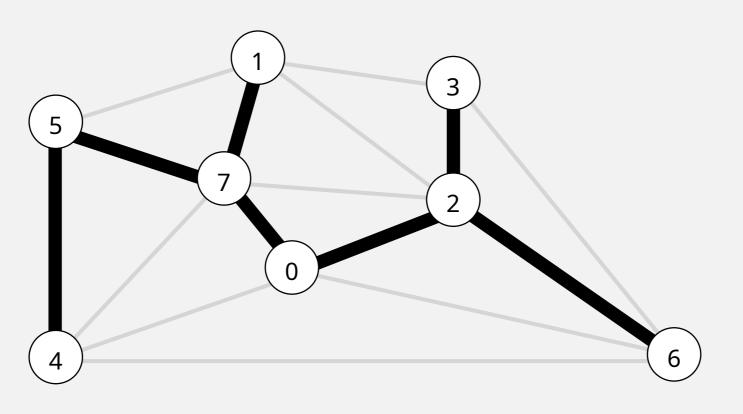
MST edges

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- Repeat until V 1 edges.



MST edges

- Start with vertex 0 and greedily grow tree T.
- Add to T the min weight edge with exactly one endpoint in T.
- Repeat until V 1 edges.



v edgeTo[] distTo[]		
v euge roll distroll		
0	-	-
7	0–7	0.16
1	1–7	0.19
2	0–2	0.26
3	2–3	0.17
5	5–7	0.28
4	4–5	0.35
6	6–2	0.40

MST edges