



<http://algs4.cs.princeton.edu>

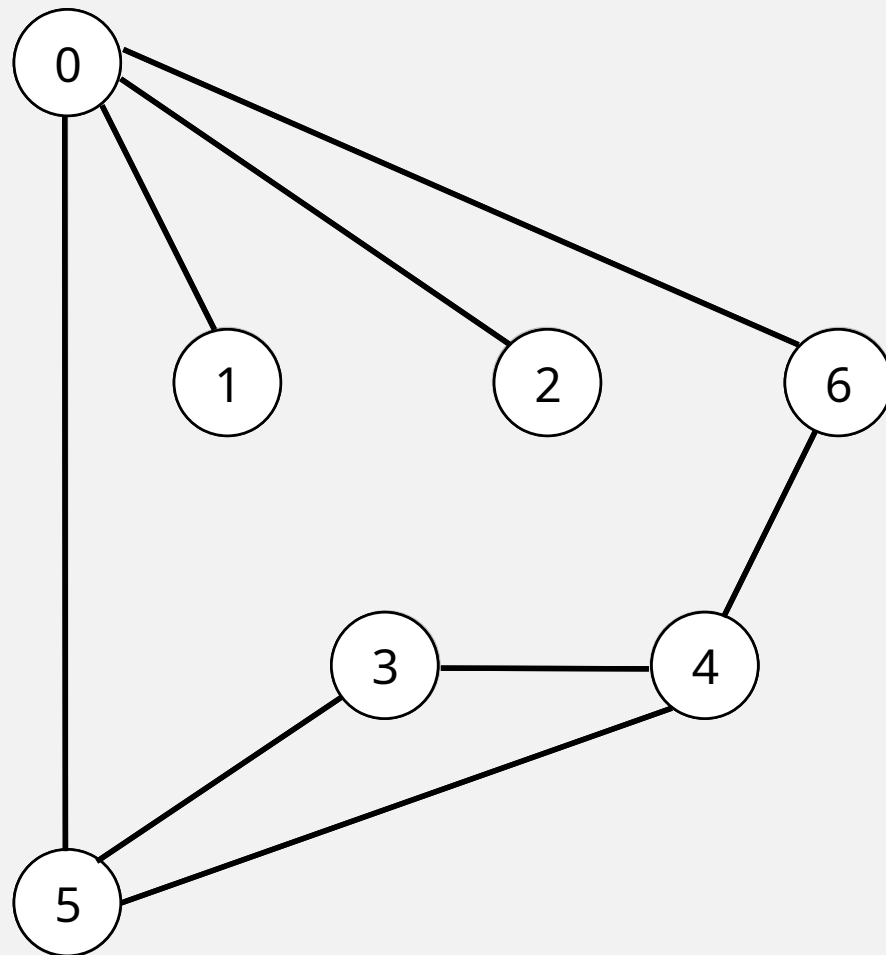
## 4.1 Connected Components Demo

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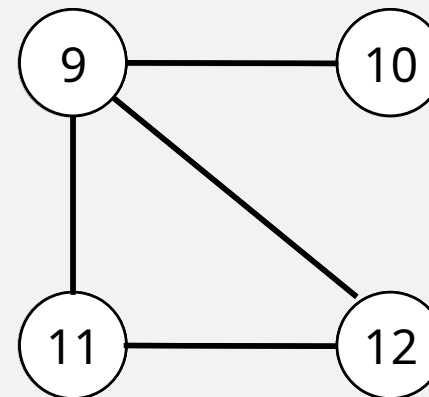
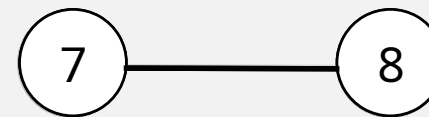
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**graph G**

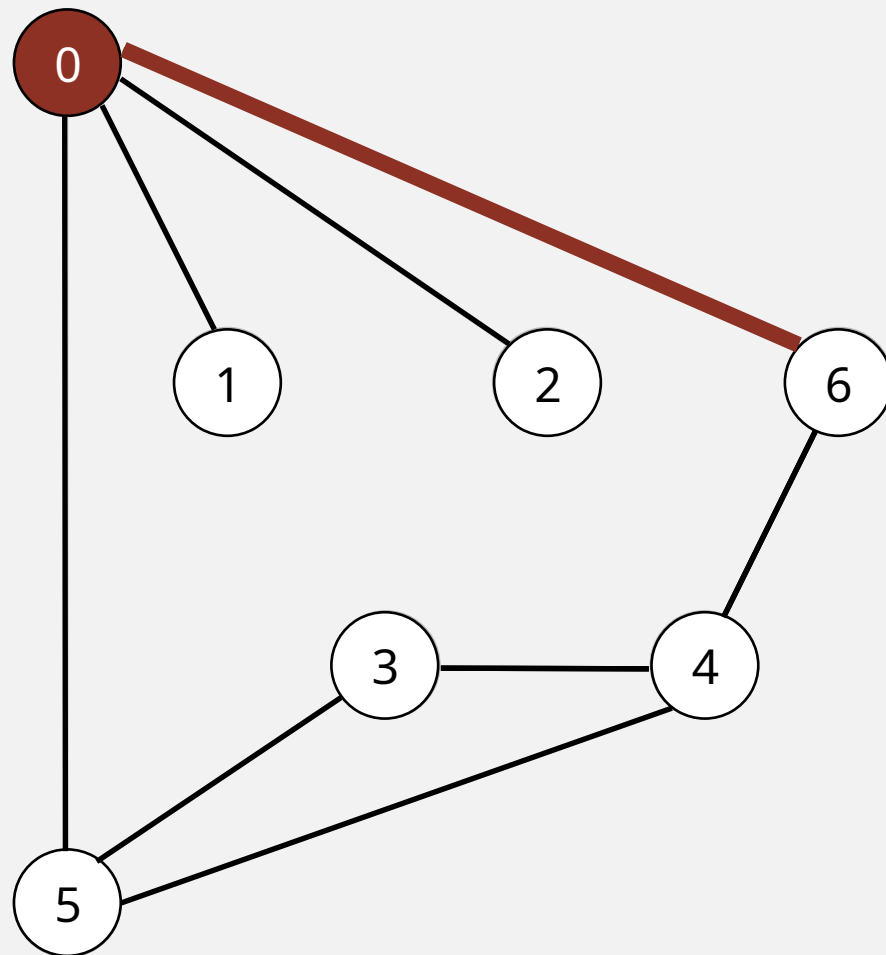


<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	F	-
1	F	-
2	F	-
3	F	-
4	F	-
5	F	-
6	F	-
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

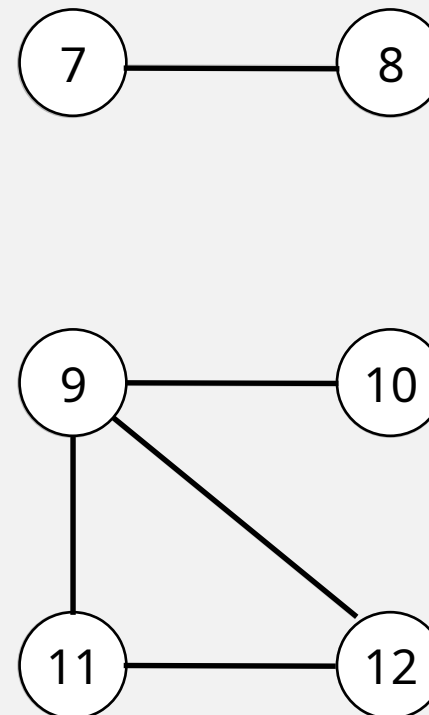
# Connected components demo



To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 0

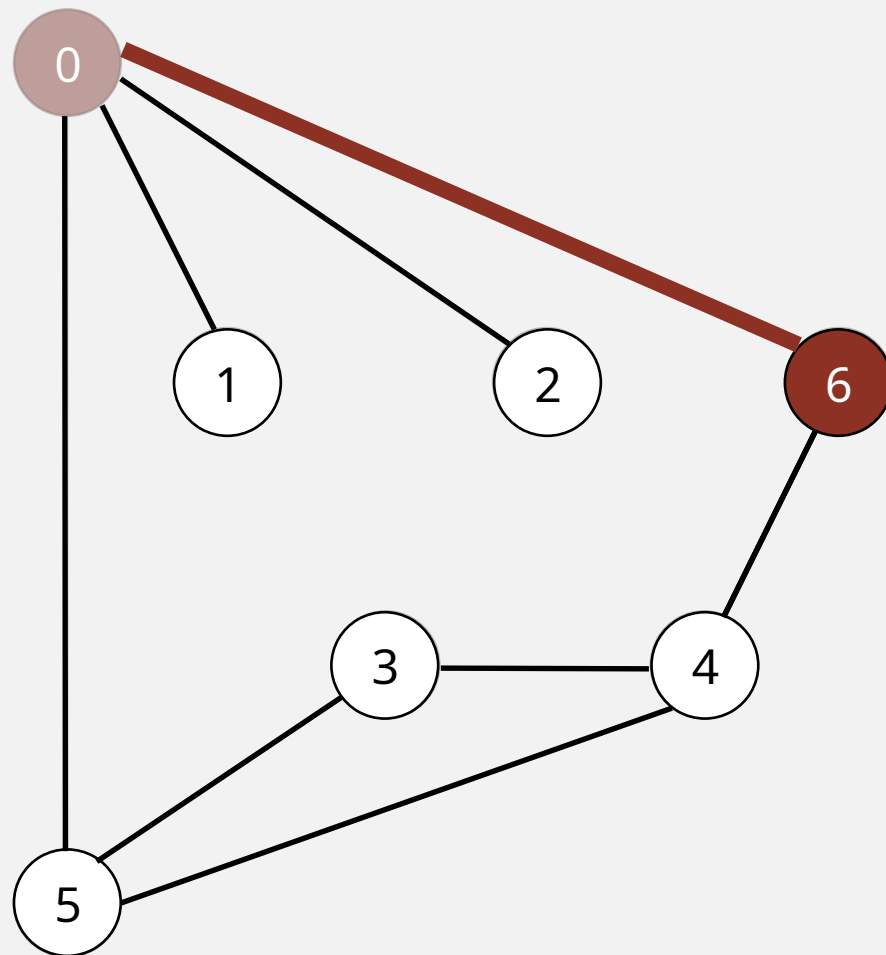


$v$	marked[]	id[]
0		
1	F	-
2	F	-
3	F	-
4	F	-
5	F	-
6	F	-
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

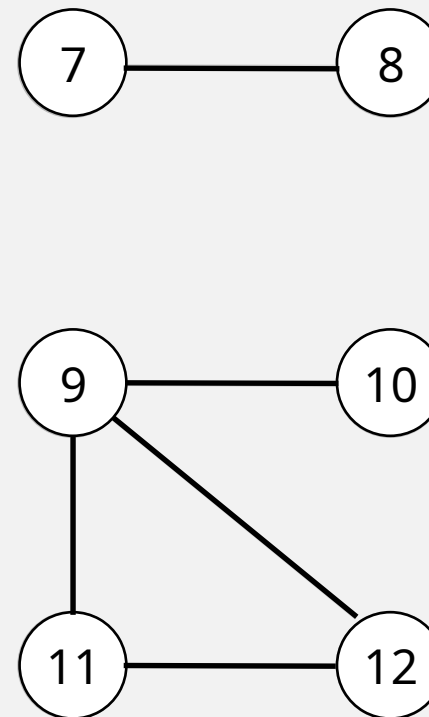
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 6

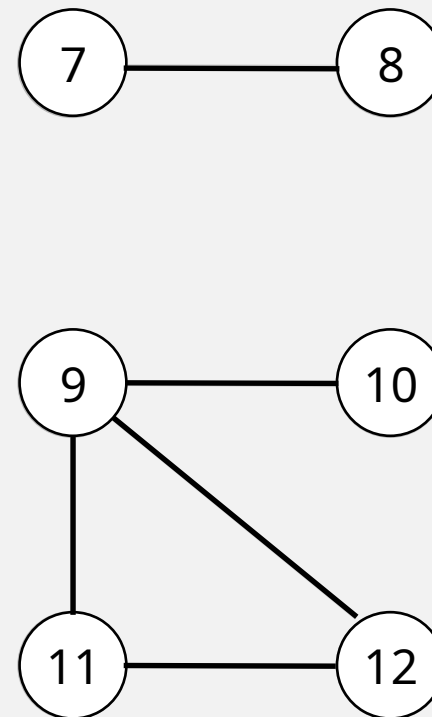
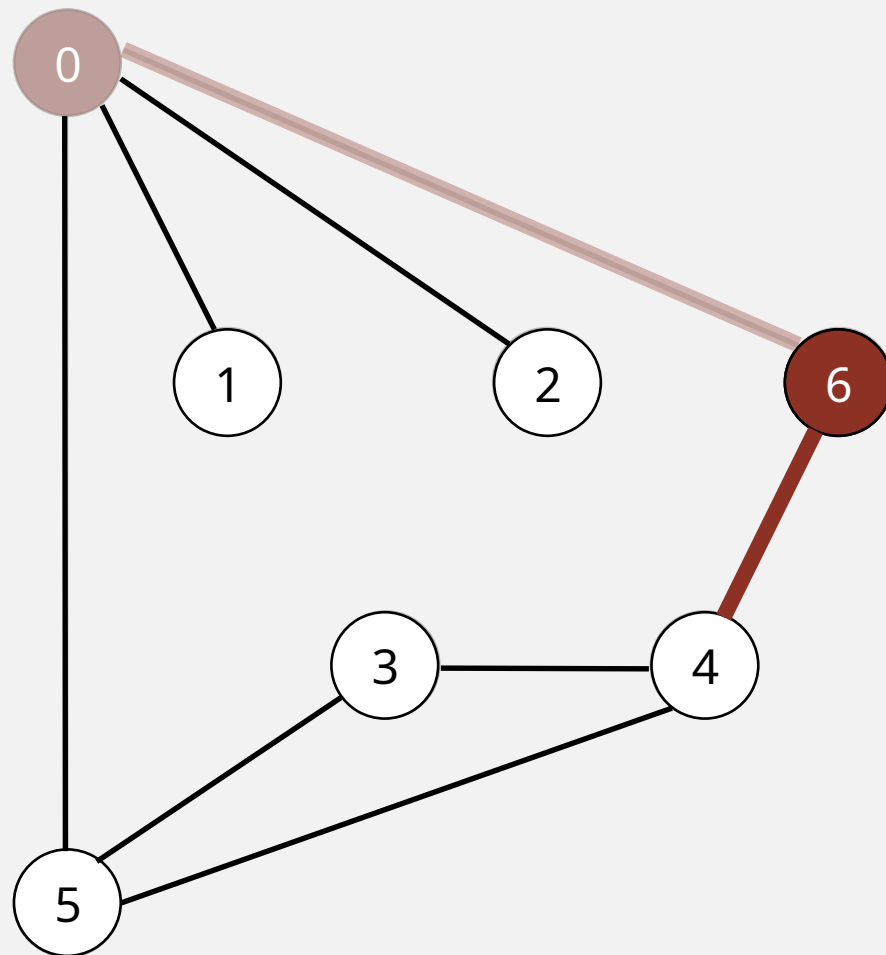


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	F	-
4	F	-
5	F	-
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



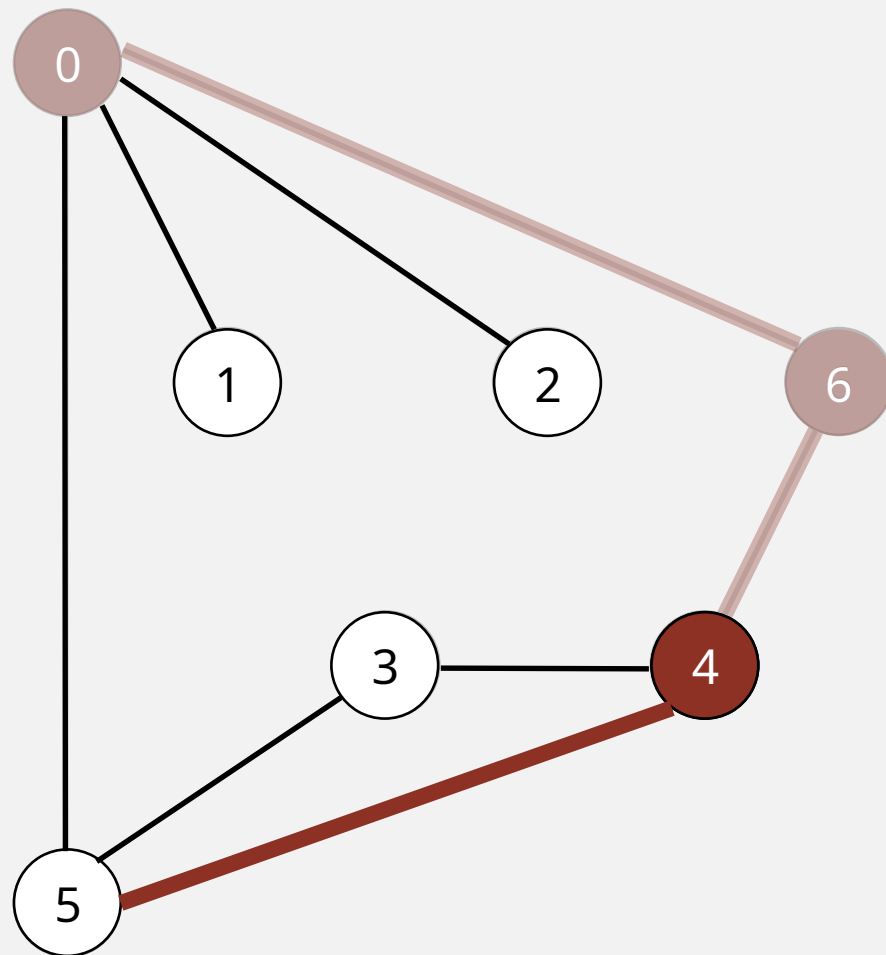
$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	F	-
4	F	-
5	F	-
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

visit 6

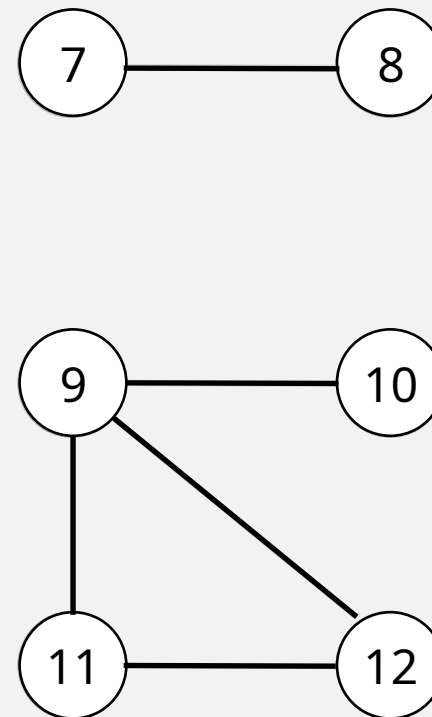
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 4

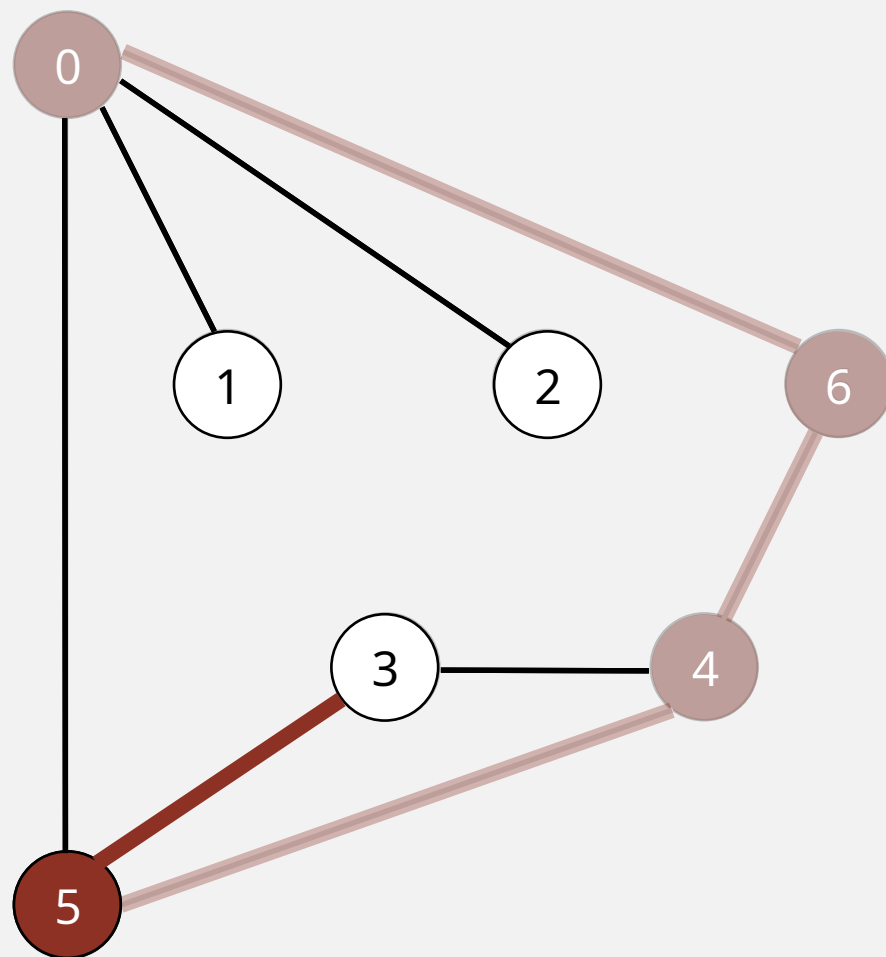


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	F	-
4	T	0
5	F	-
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

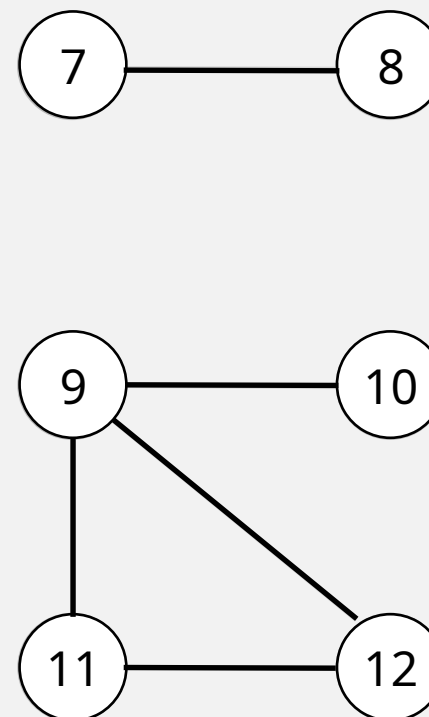
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 5

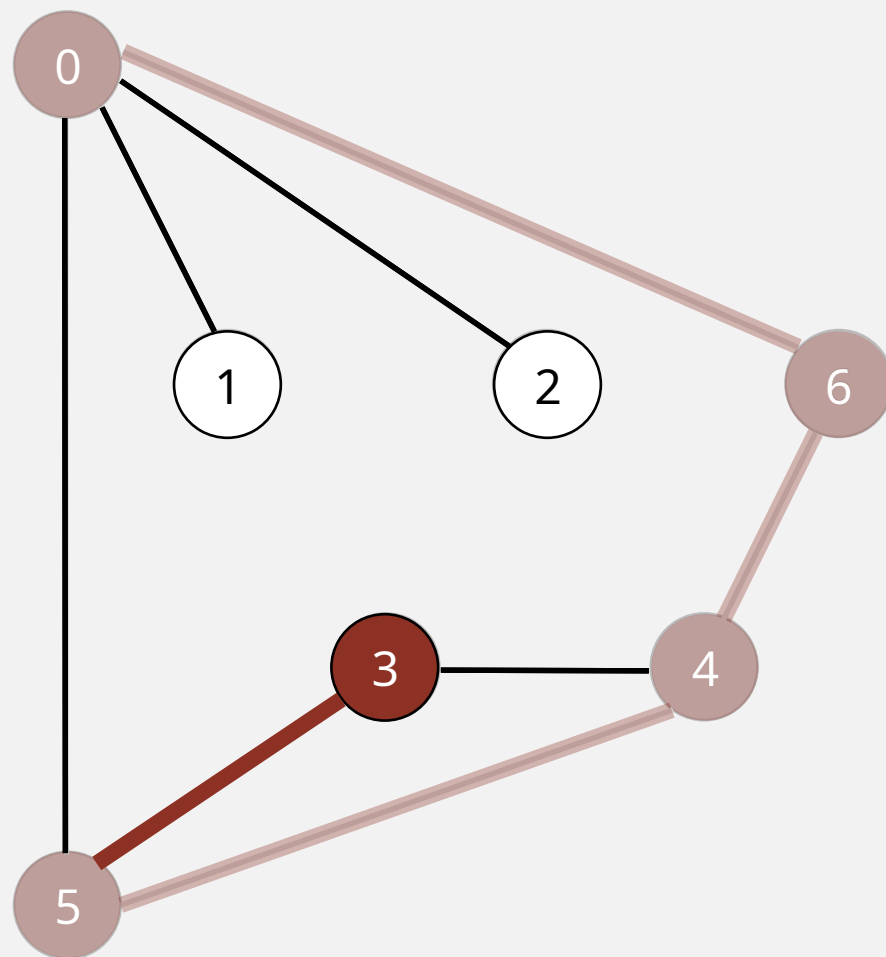


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	F	-
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

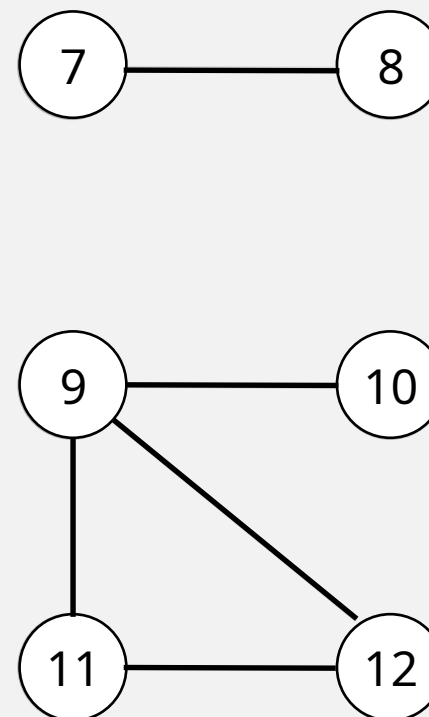
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**visit 3**



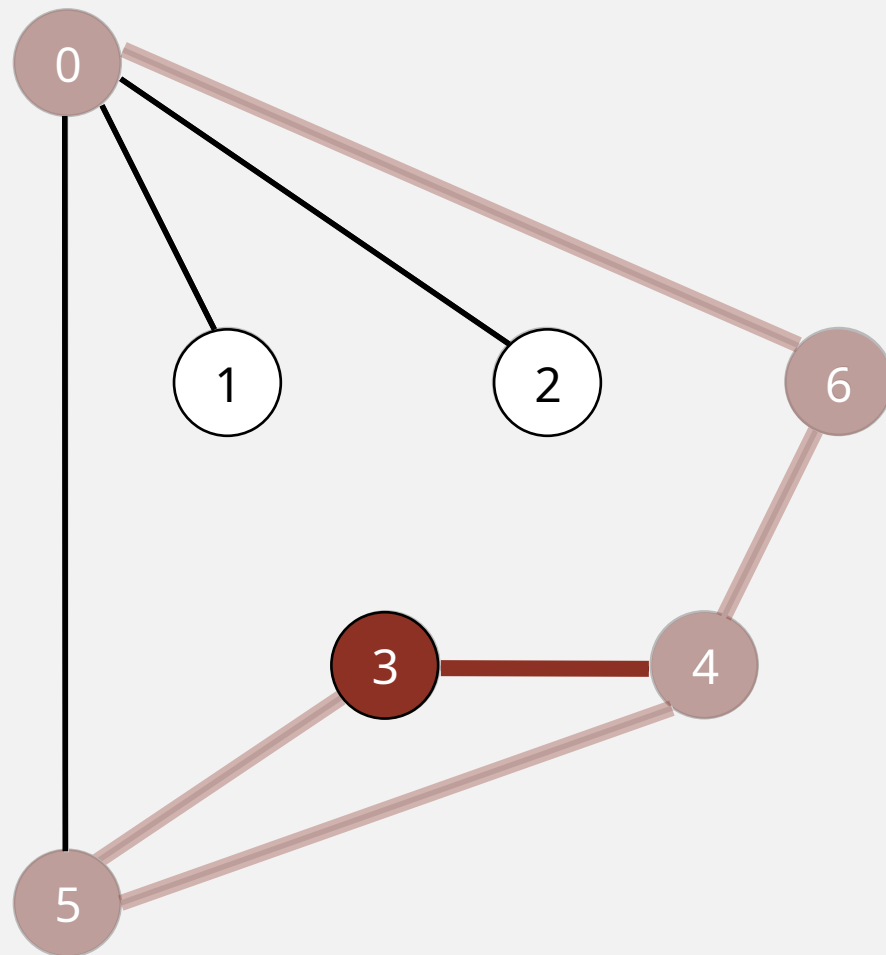
$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-



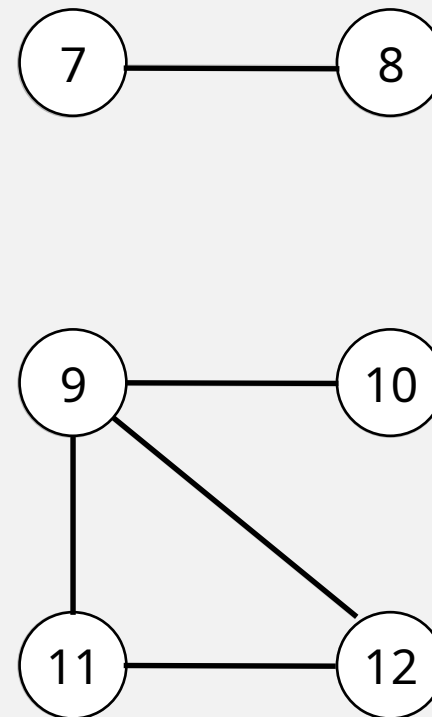
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**visit 3**

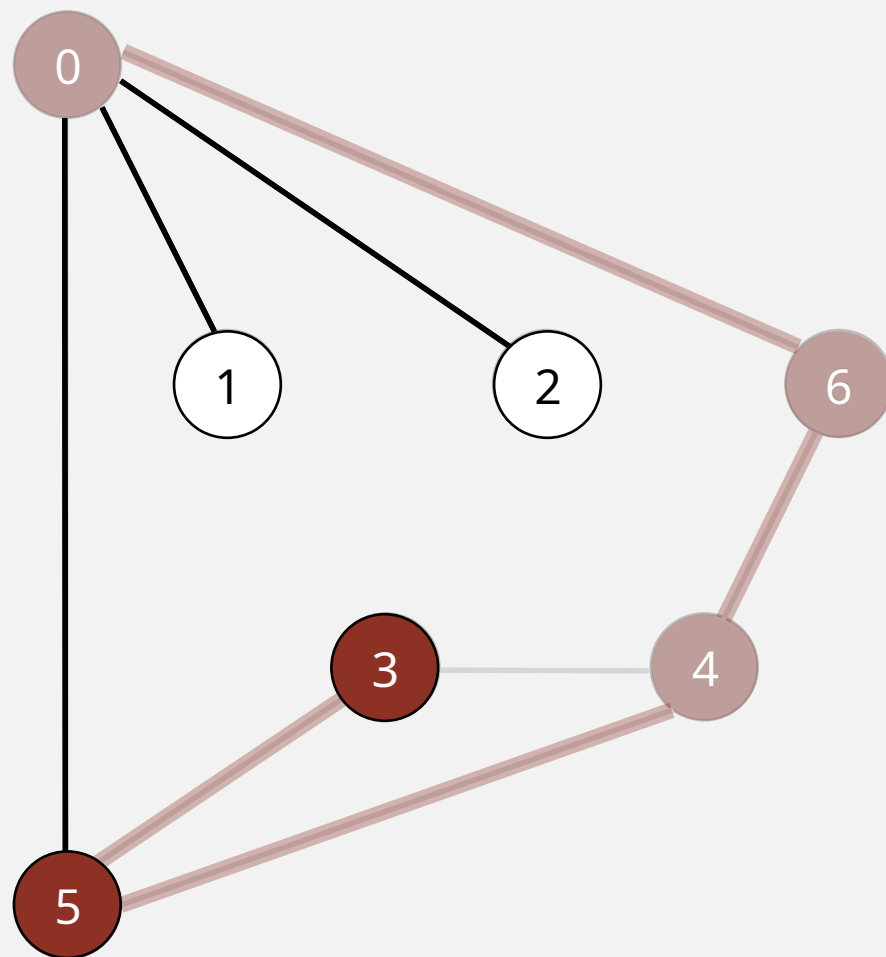


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

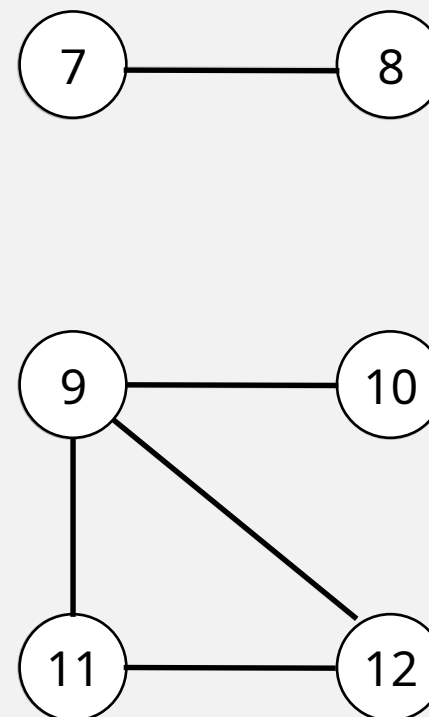
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**3 done**

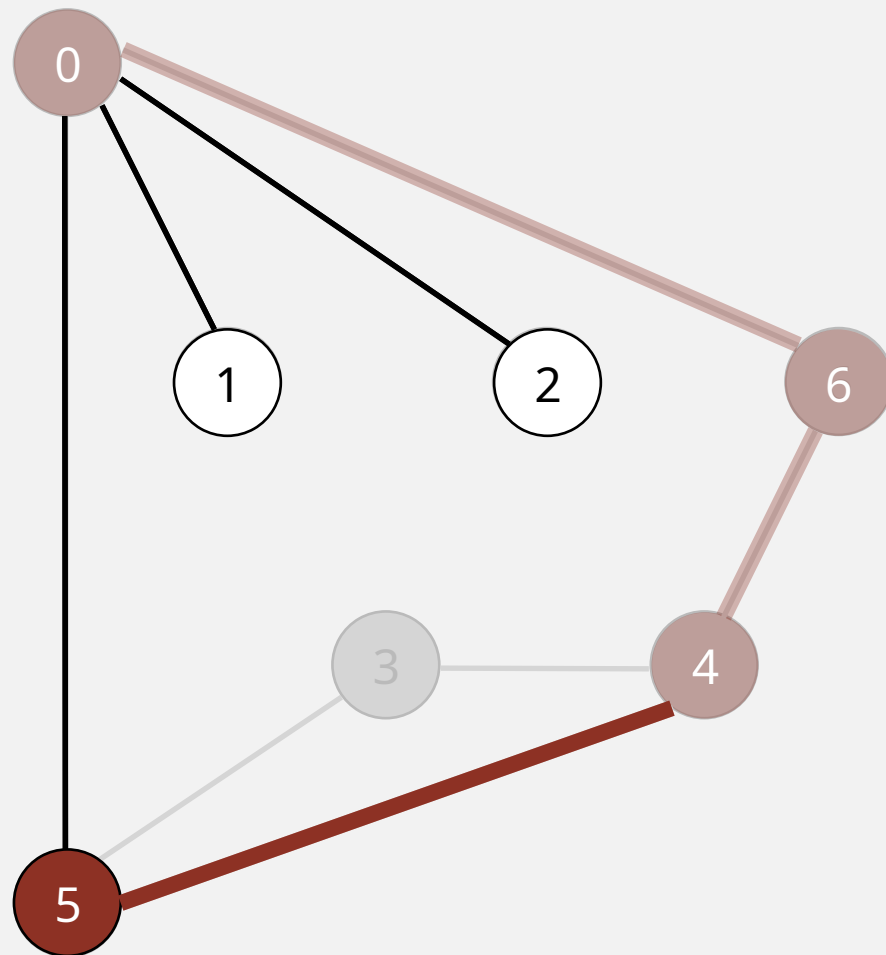


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

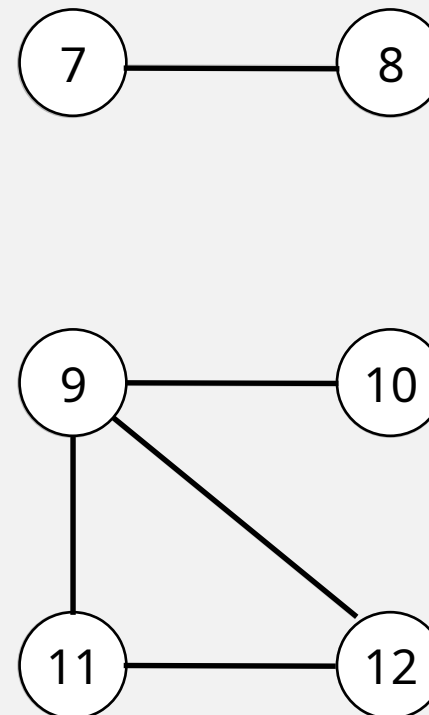
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**visit 5**

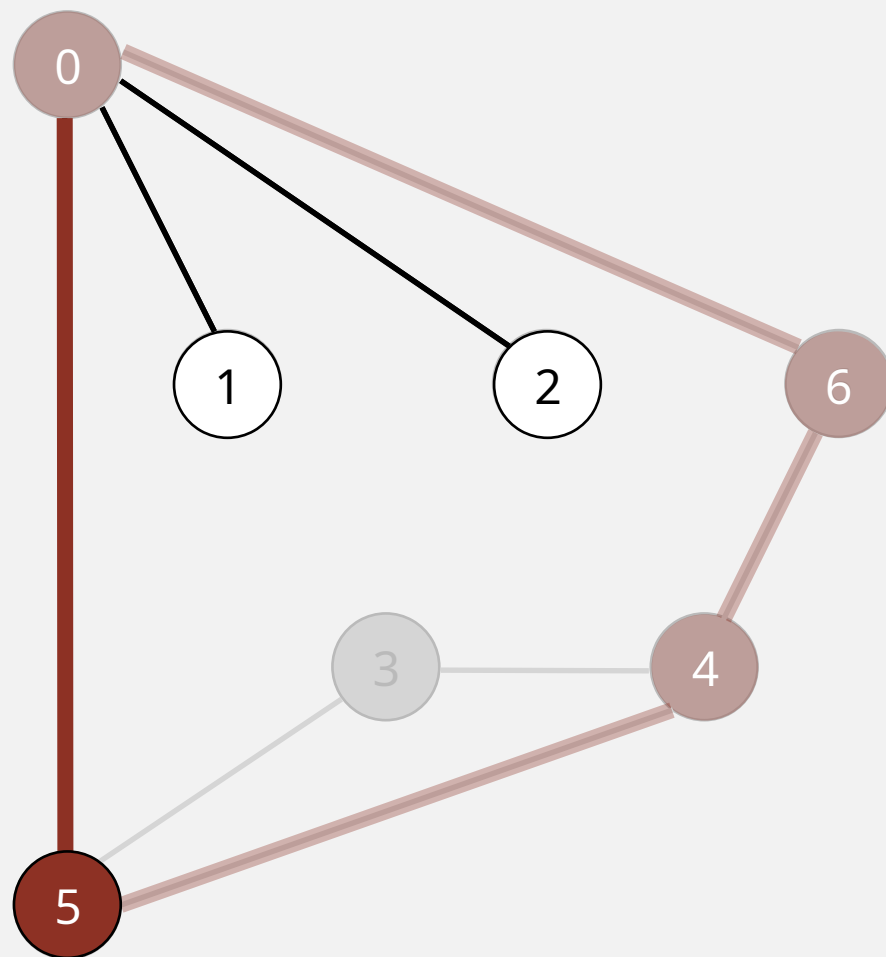


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

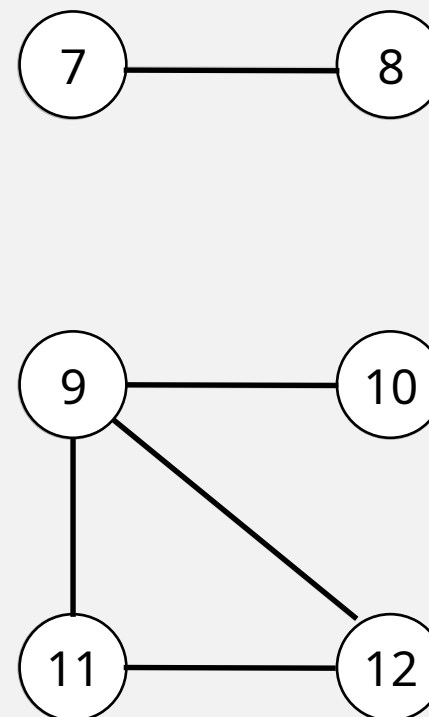
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 5

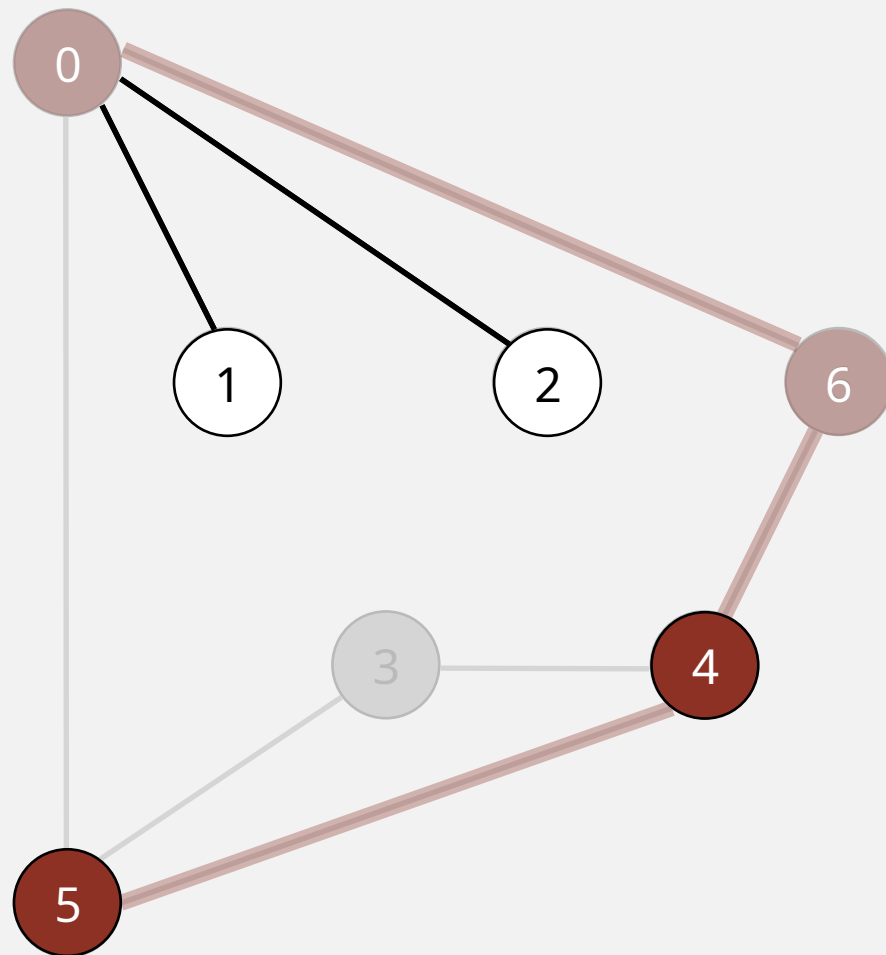


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

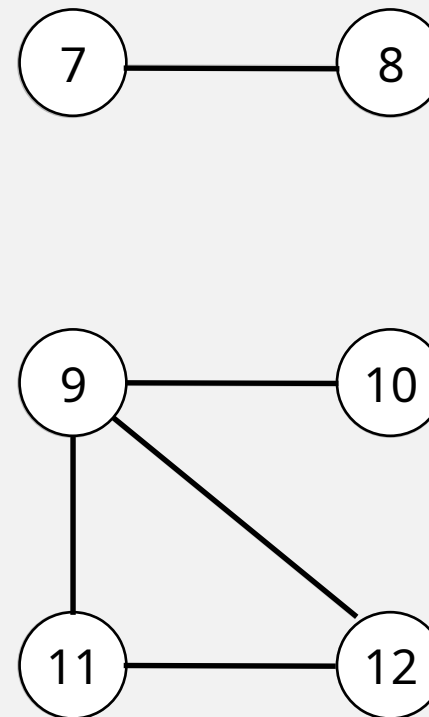
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**5 done**

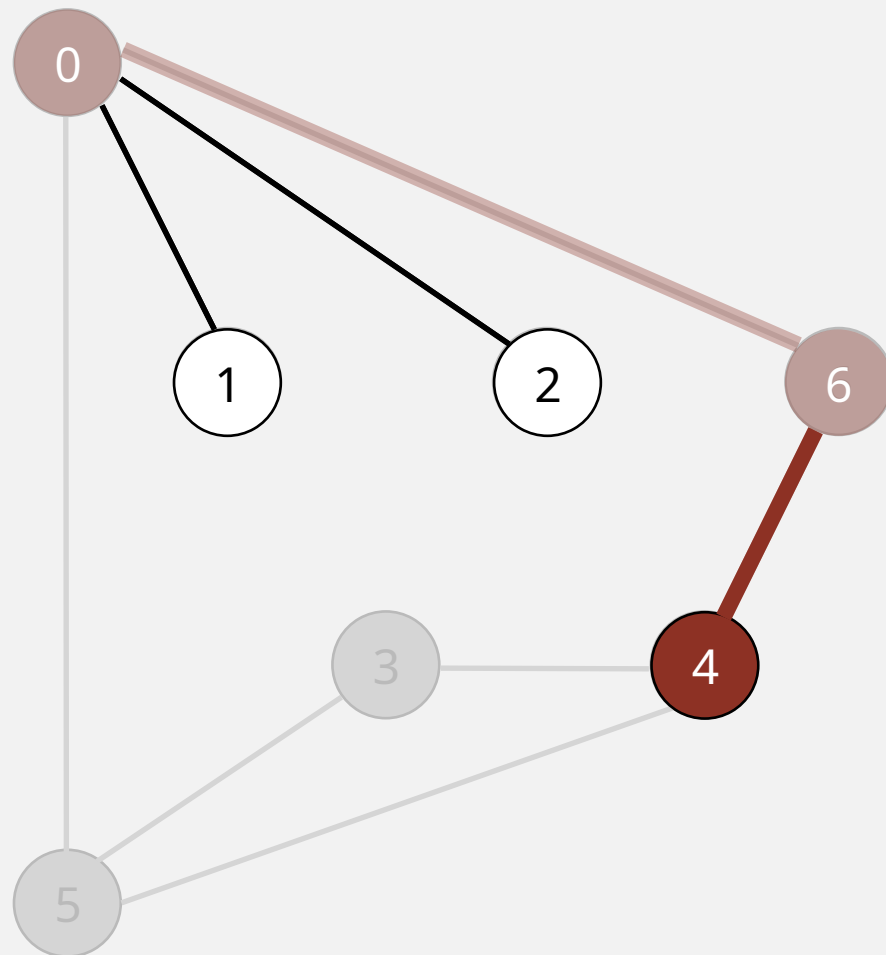


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

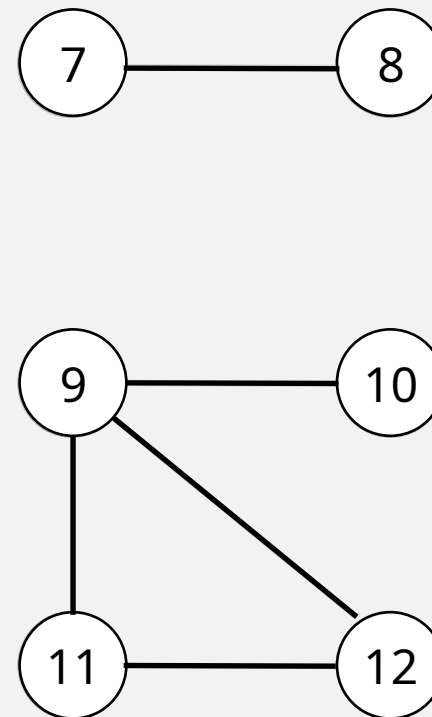
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**visit 4**

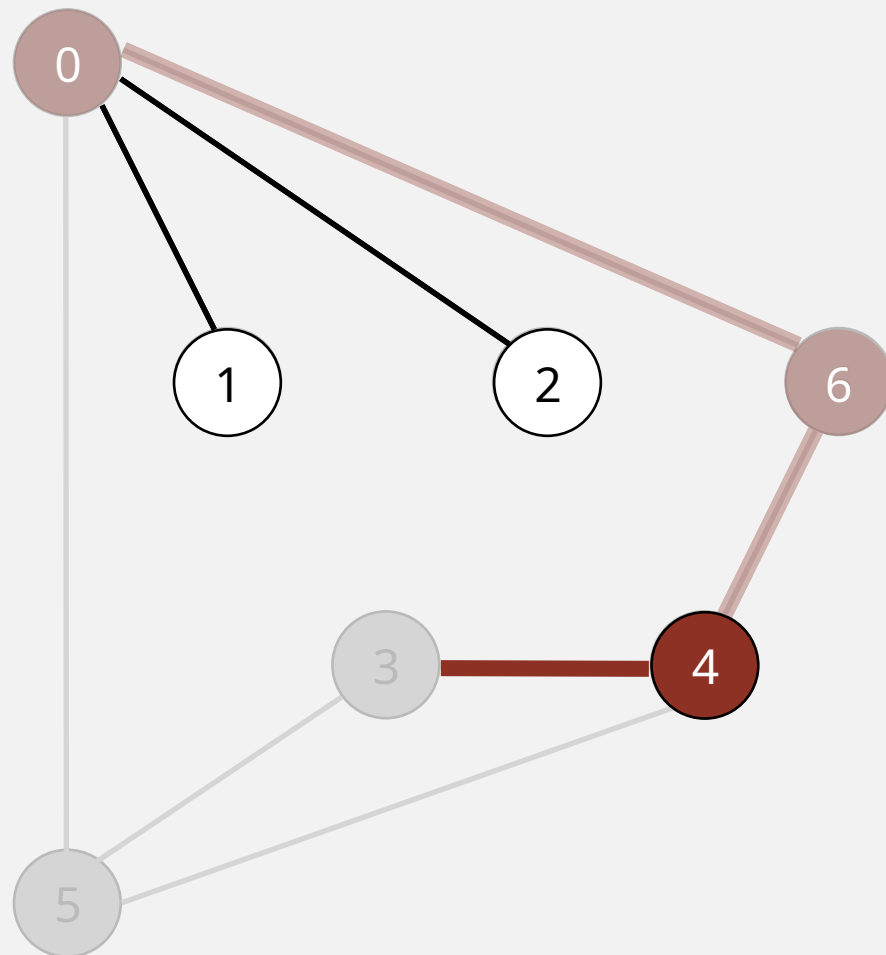


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

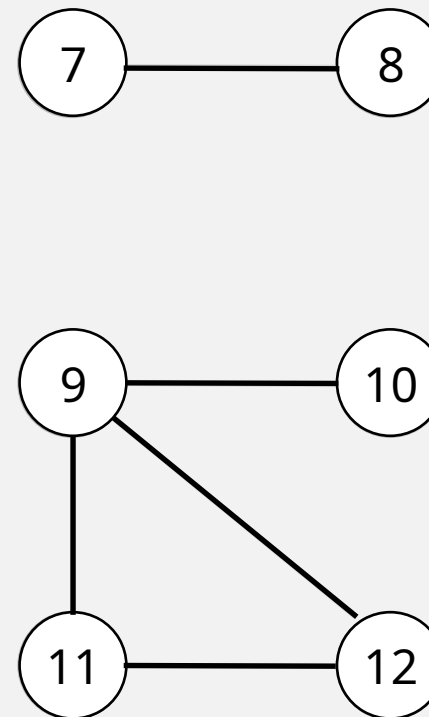
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 4

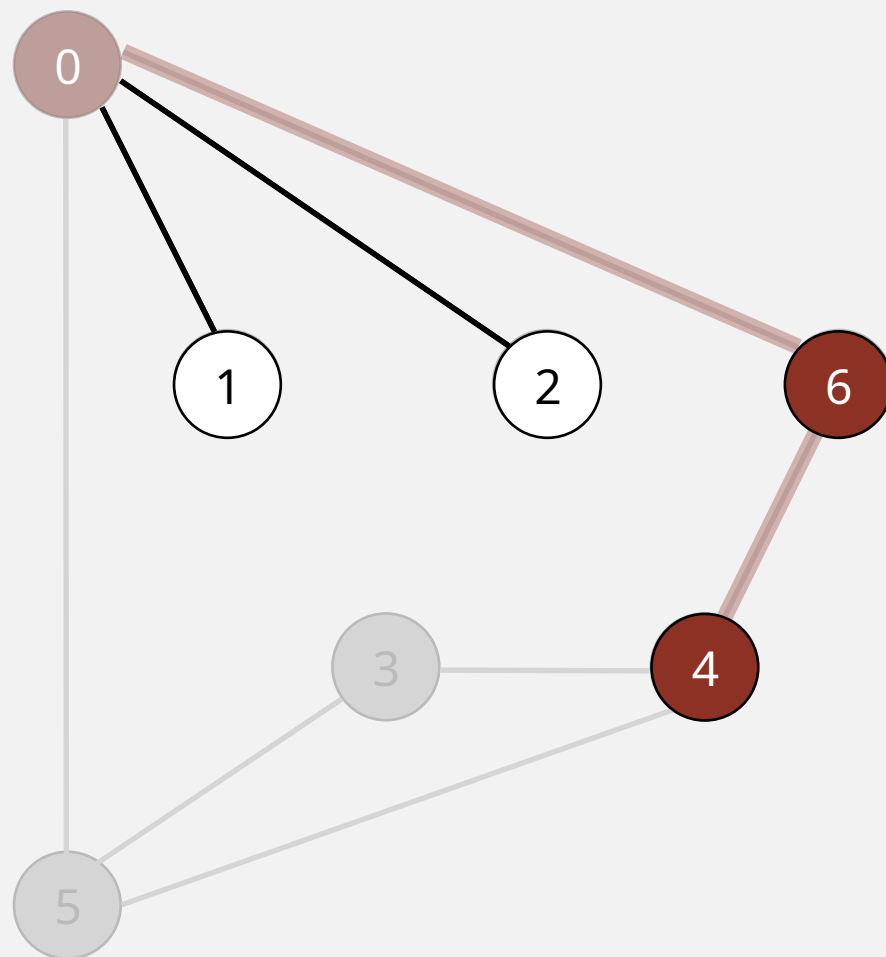


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

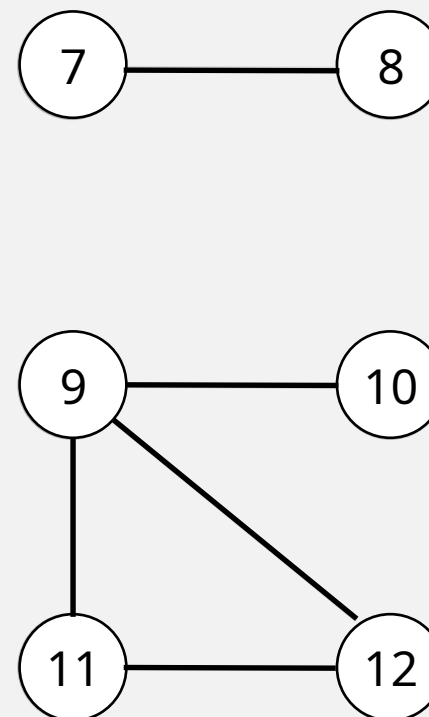
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**4 done**



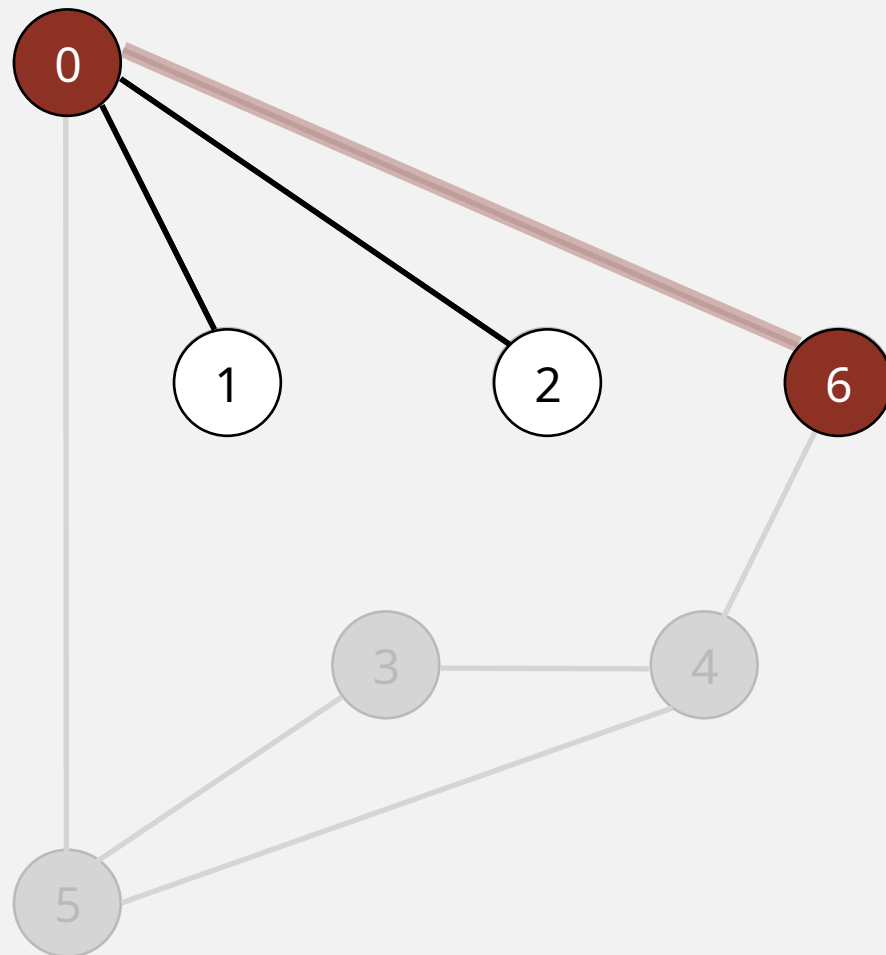
$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-



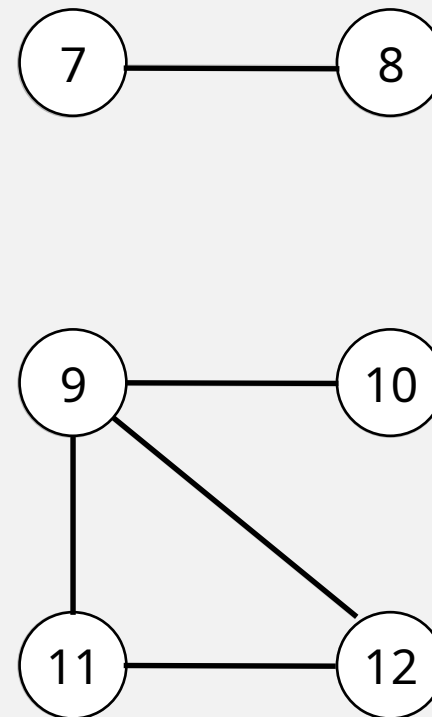
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**6 done**

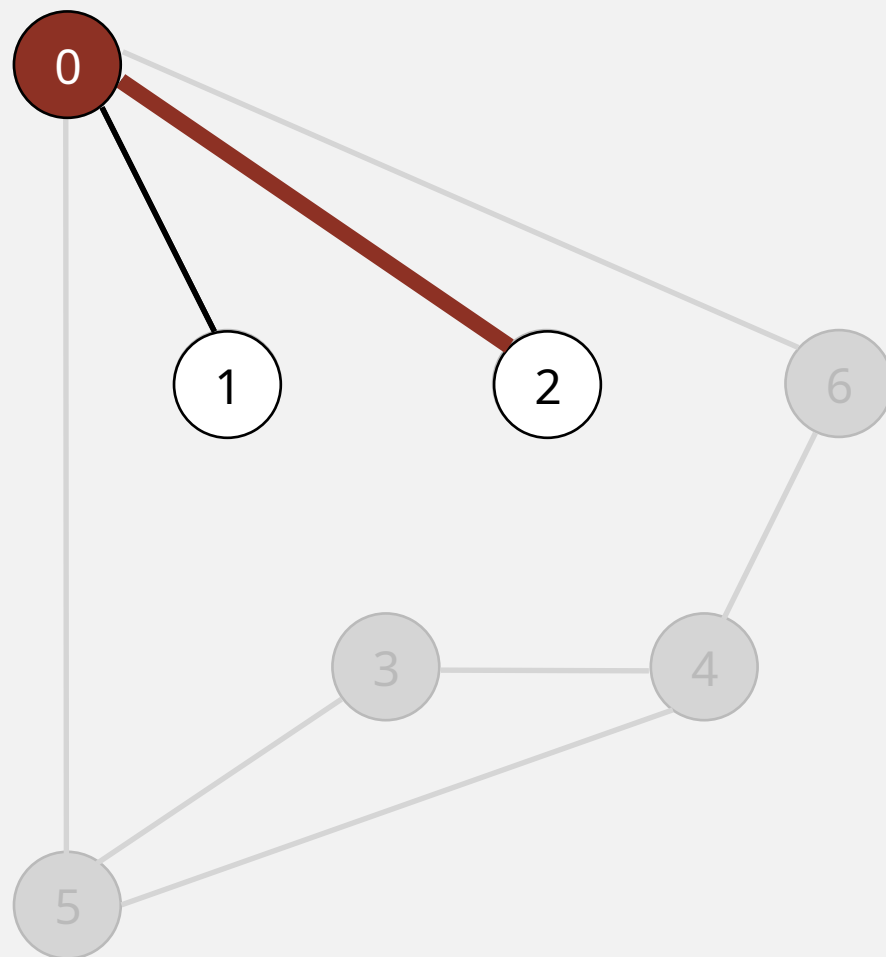


$v$	marked[]	id[]
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

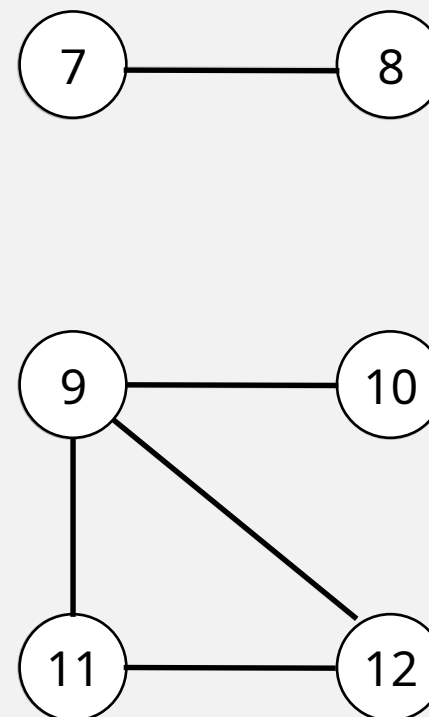
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**visit 0**

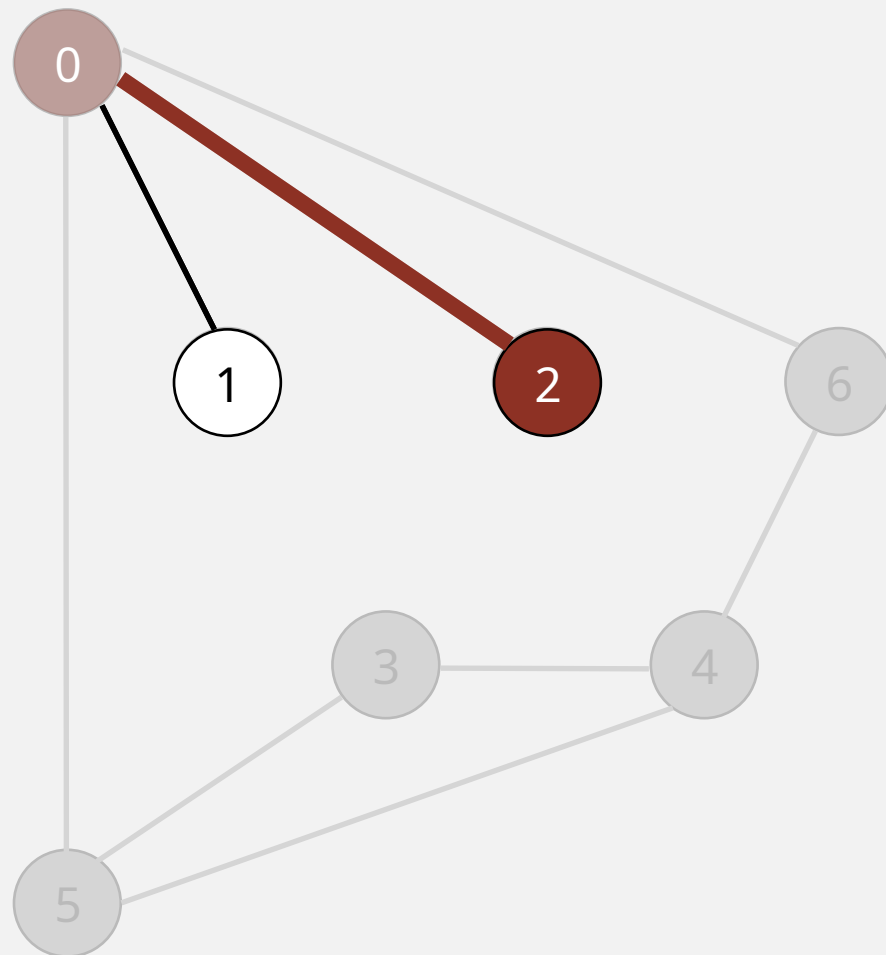


<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	F	-
2	F	-
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

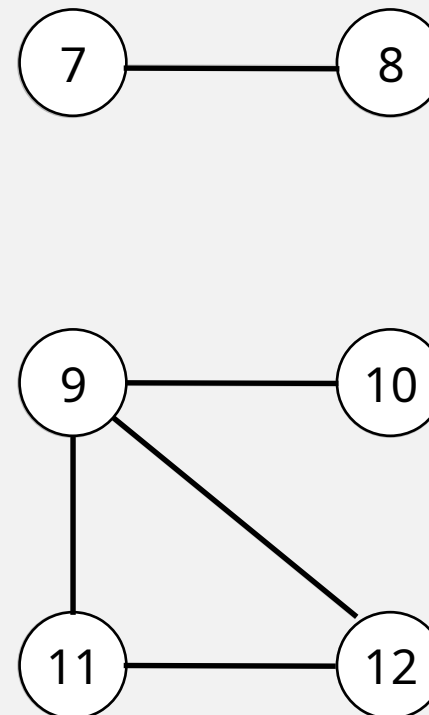
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



visit 2

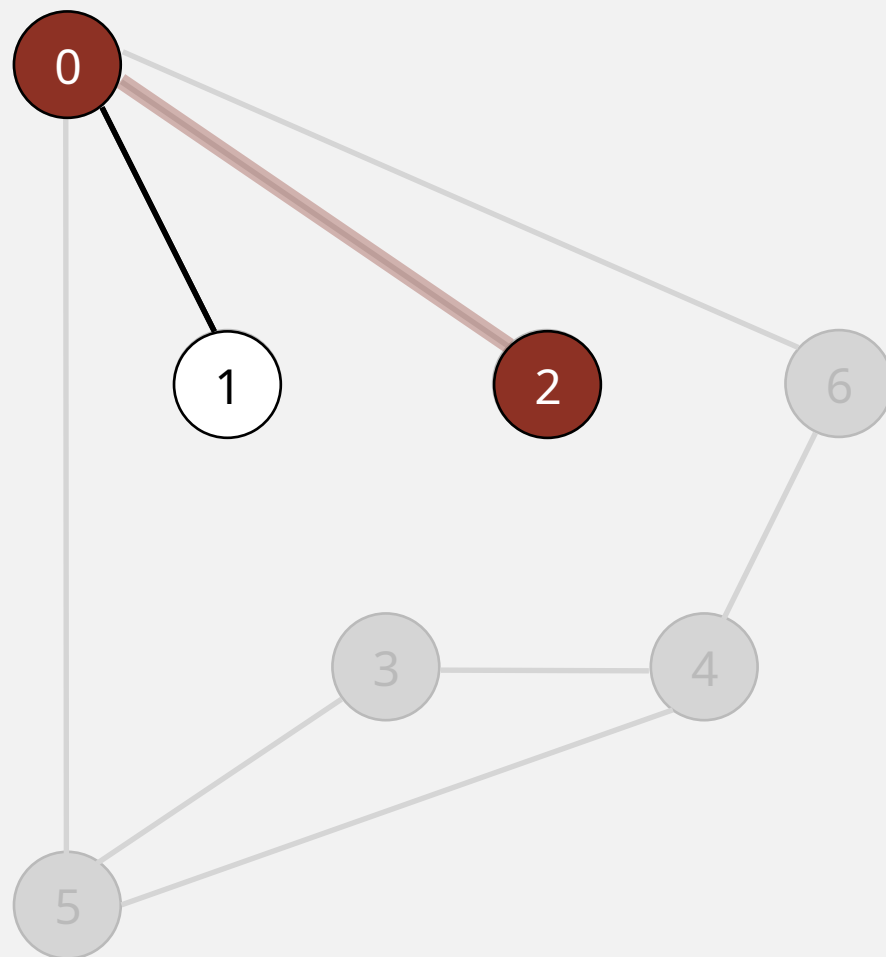


$v$	marked[]	id[]
0	T	0
1	F	-
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

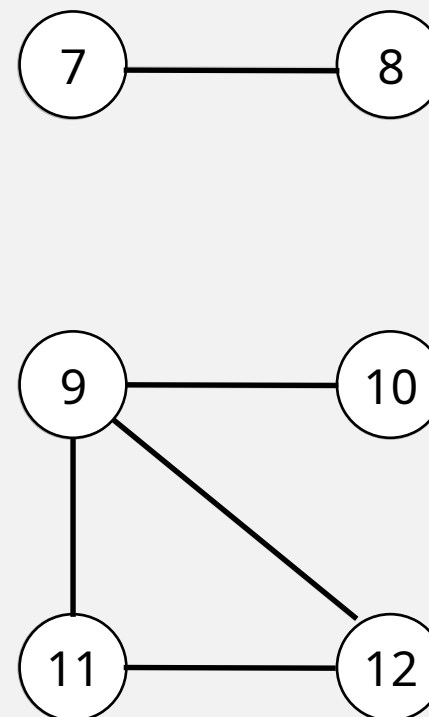
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**2 done**

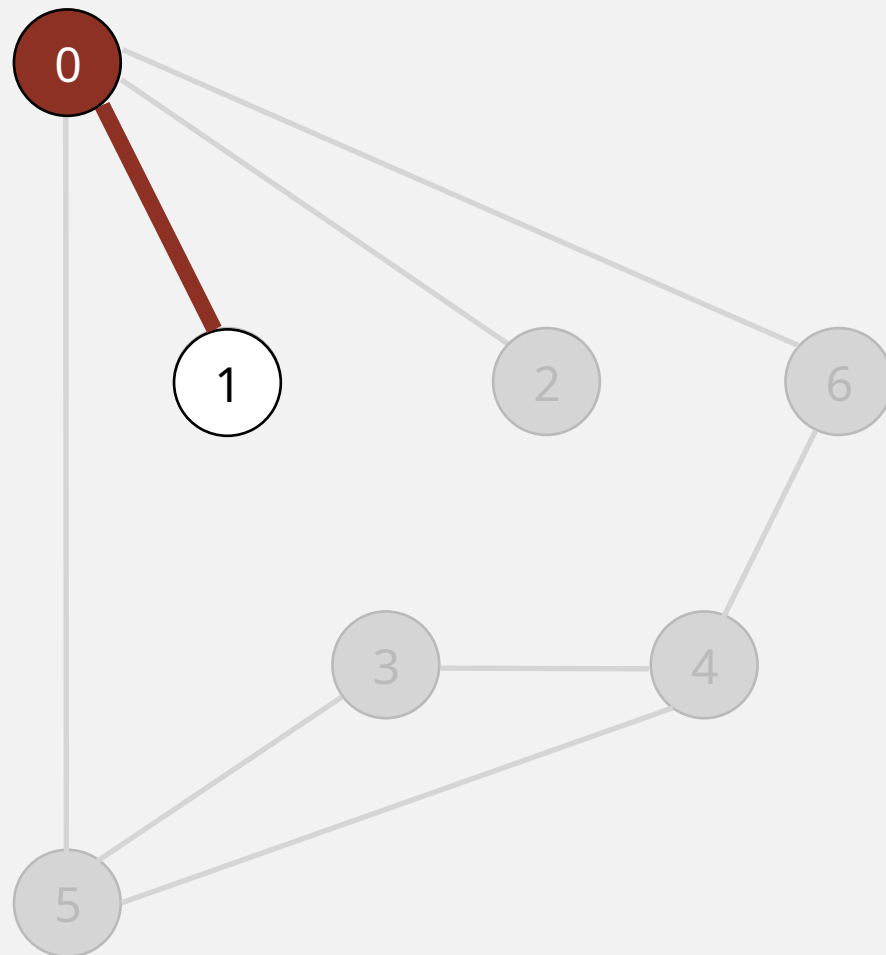


$v$	marked[]	id[]
0	T	0
1	F	-
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

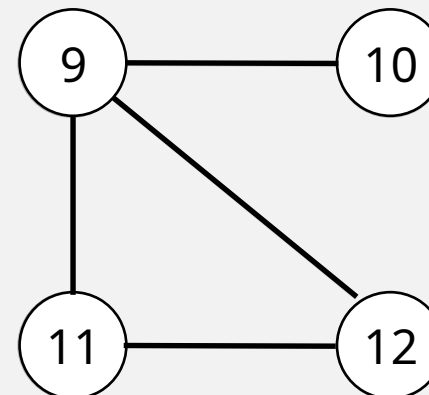
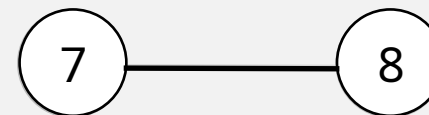
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**visit 0**

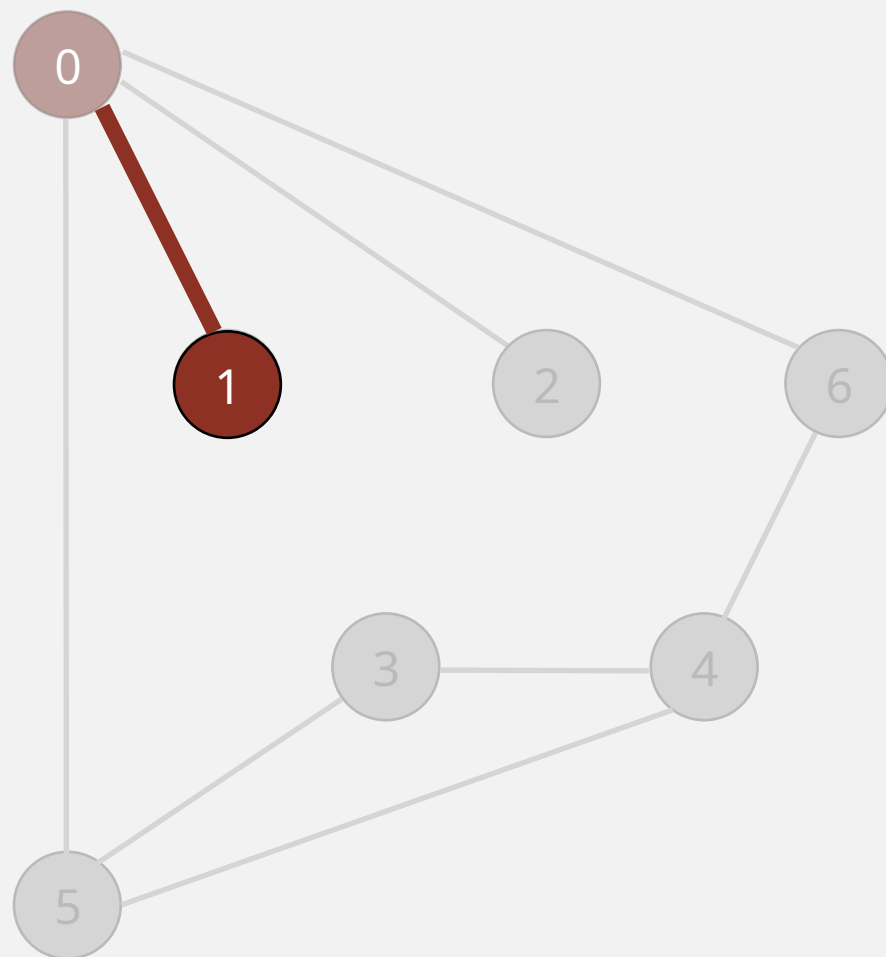


<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	F	-
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

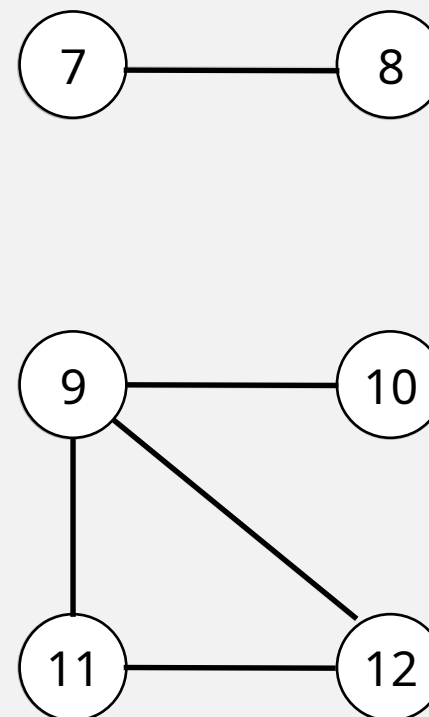
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**visit 1**

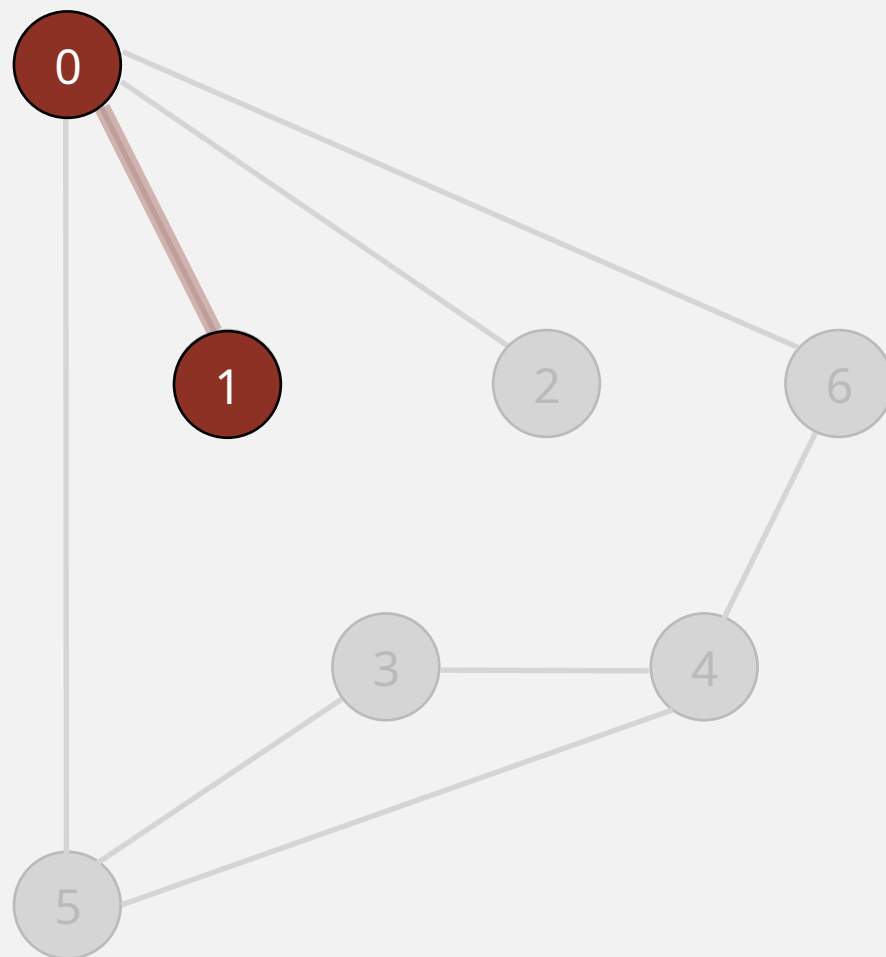


$v$	marked[]	id[]
0		
1		
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

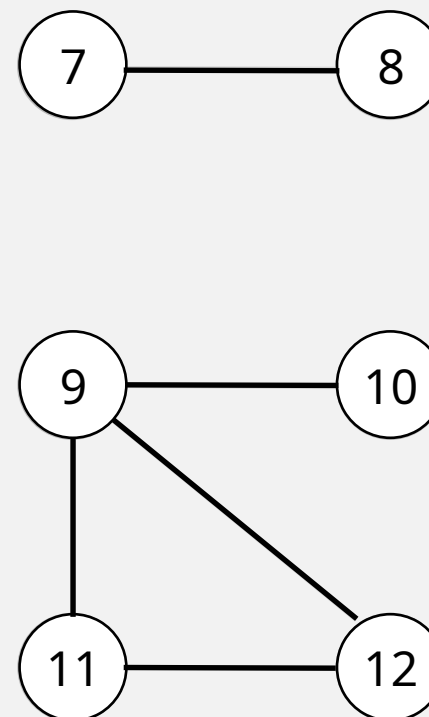
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**1 done**

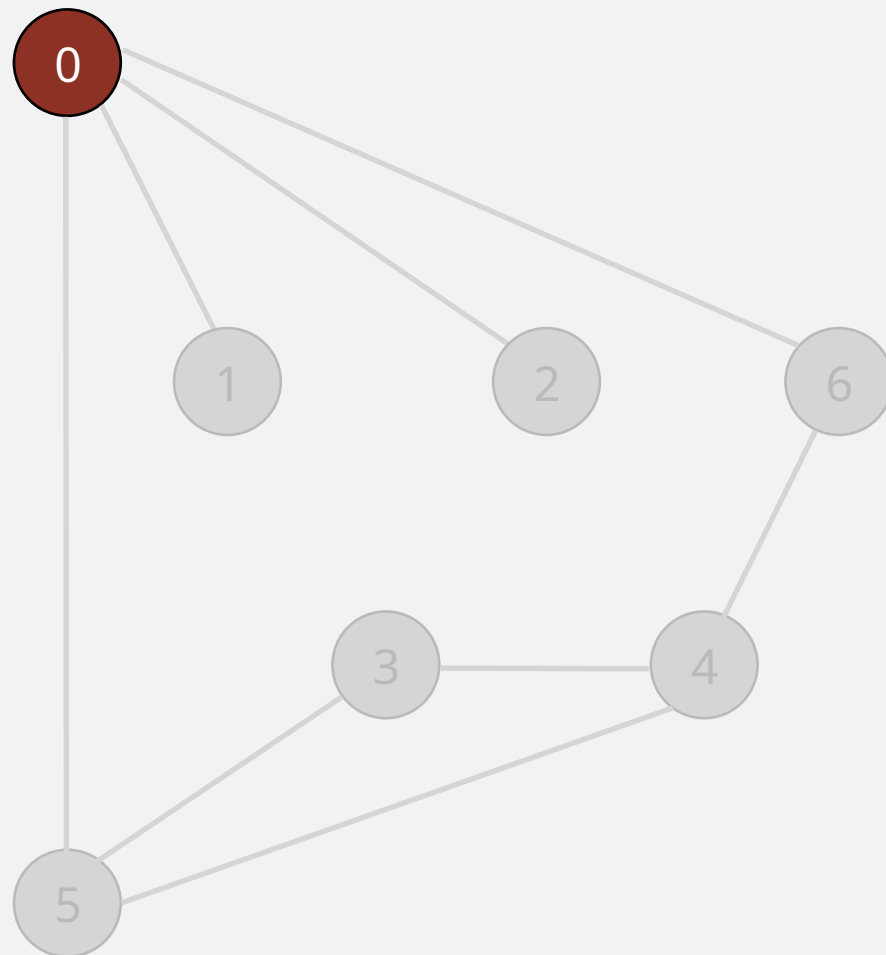


$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

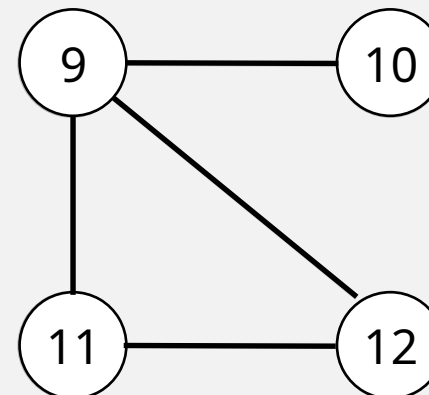
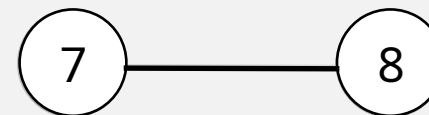
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**0 done**



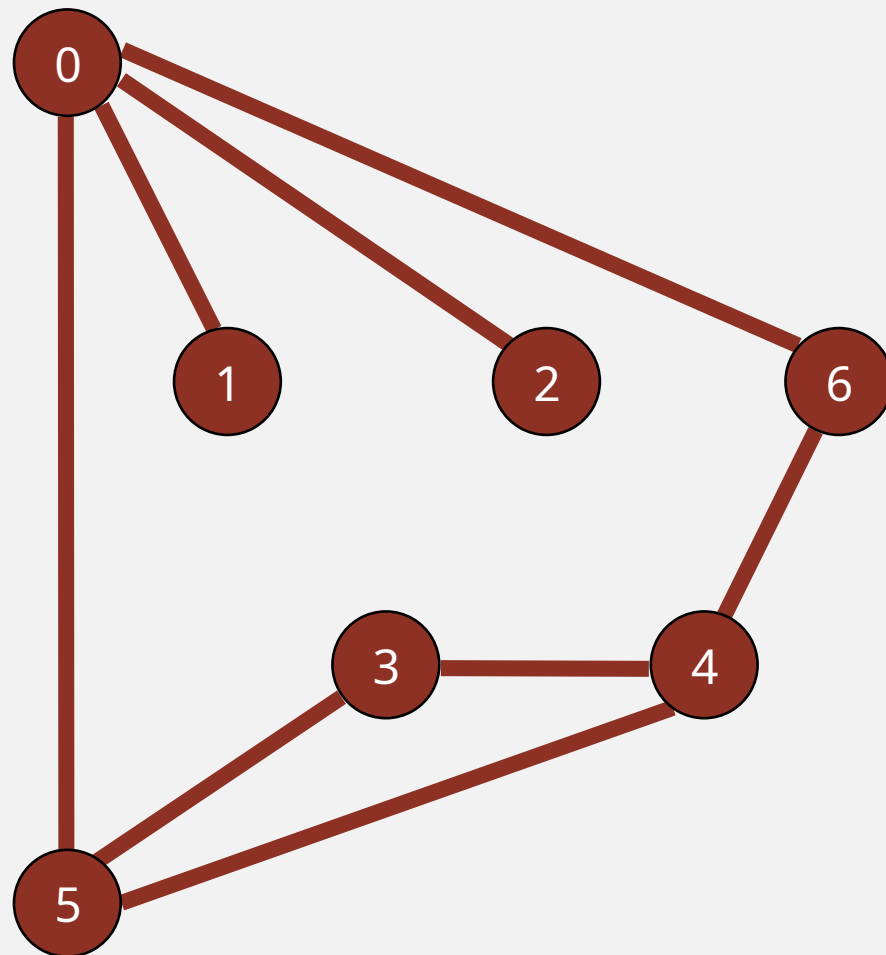
<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-



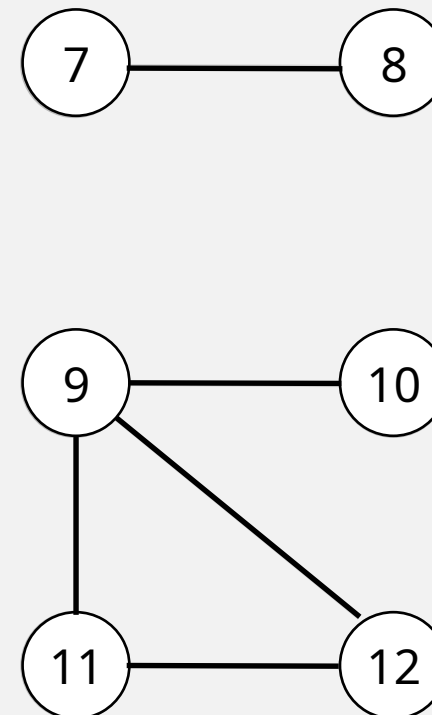
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**connected component: 0 1 2 3 4 5 6**



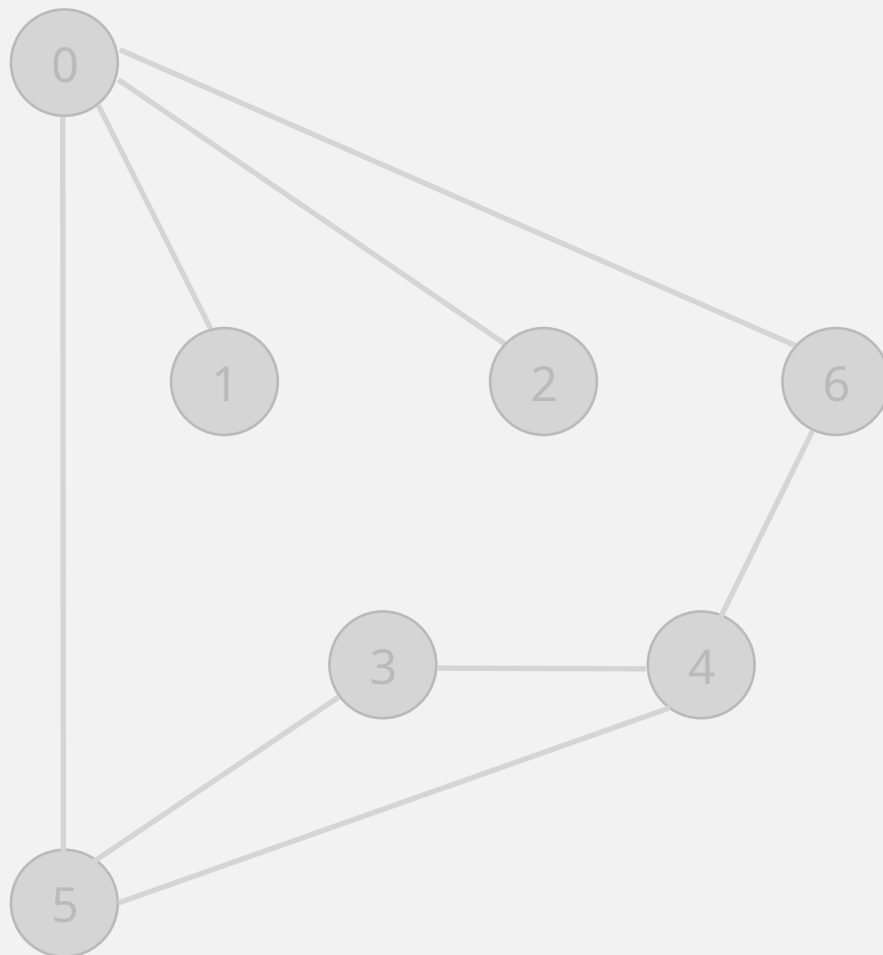
connected  
component

$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

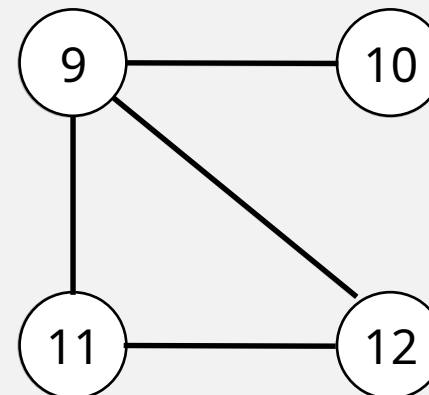
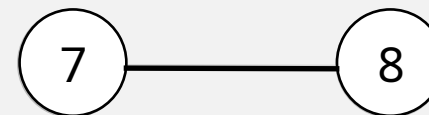
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



check 1 2 3 4 5 6

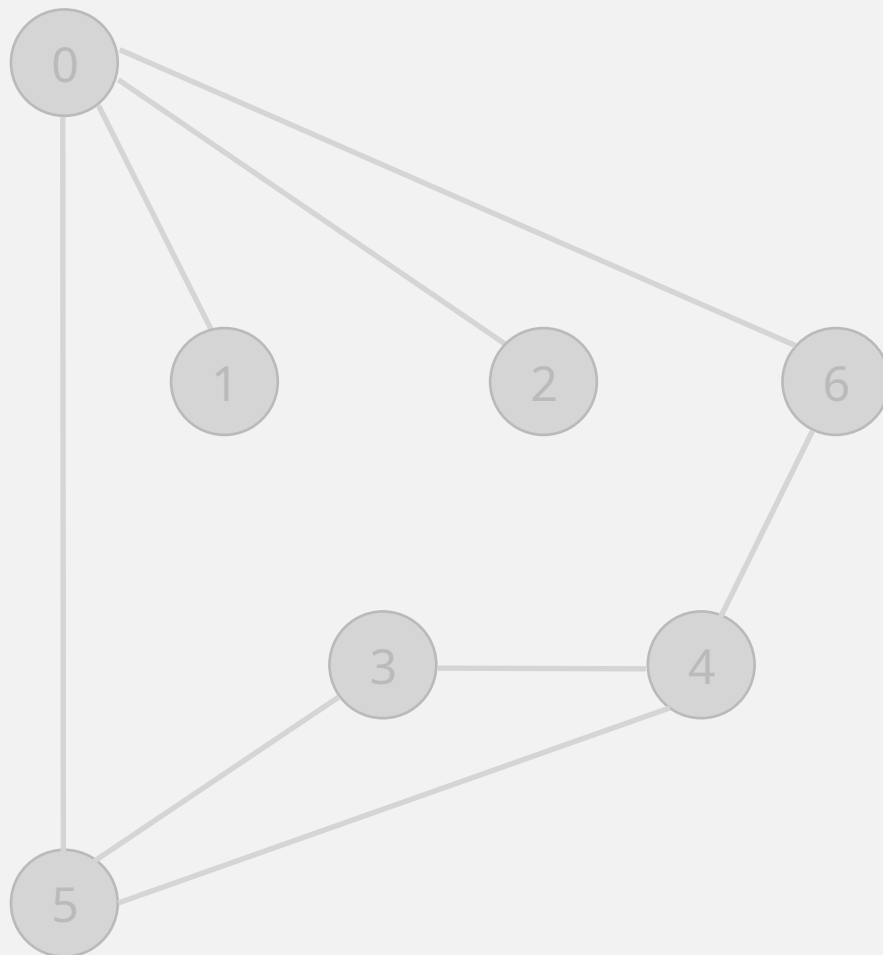


<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	F	-
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

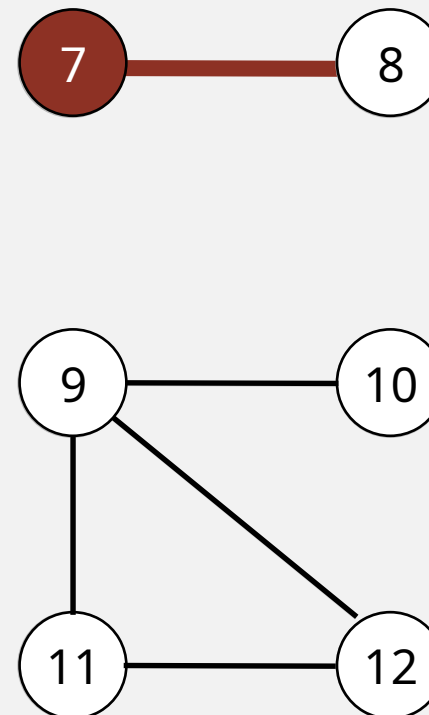
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**visit 7**

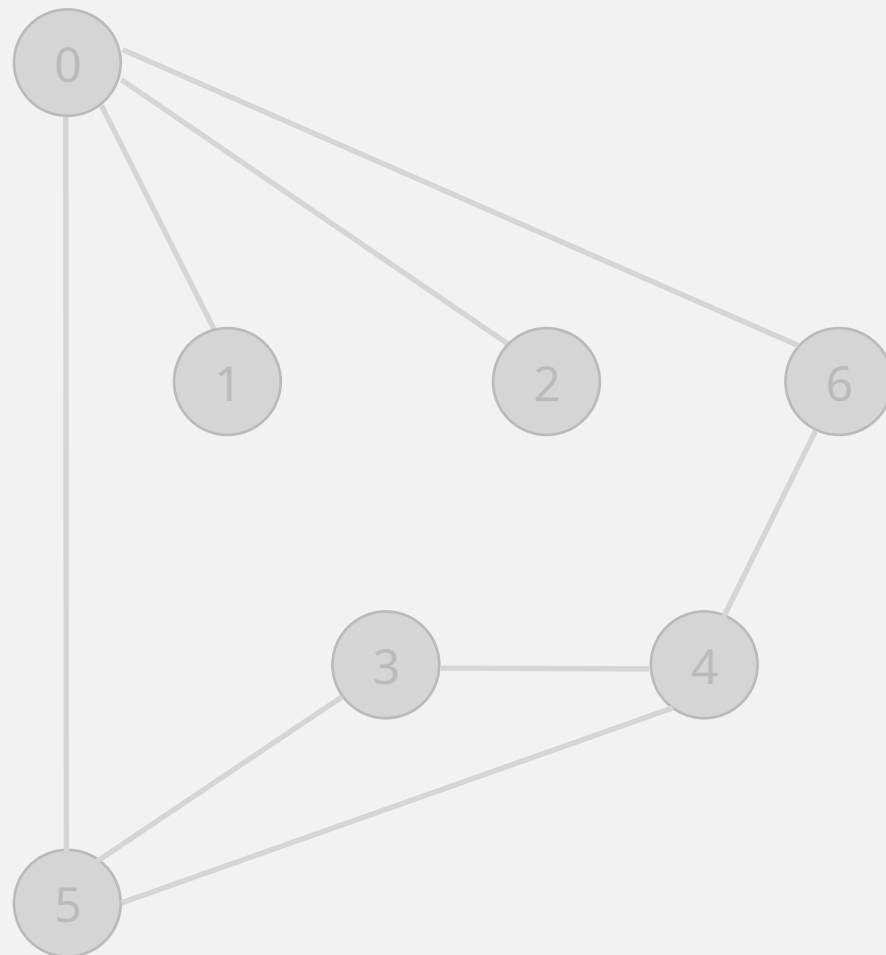


$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	F	-
9	F	-
10	F	-
11	F	-
12	F	-

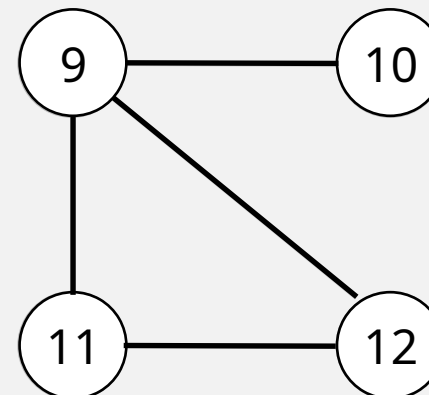
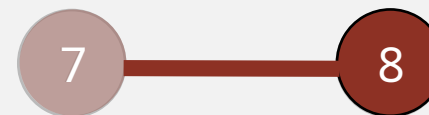
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**visit 8**

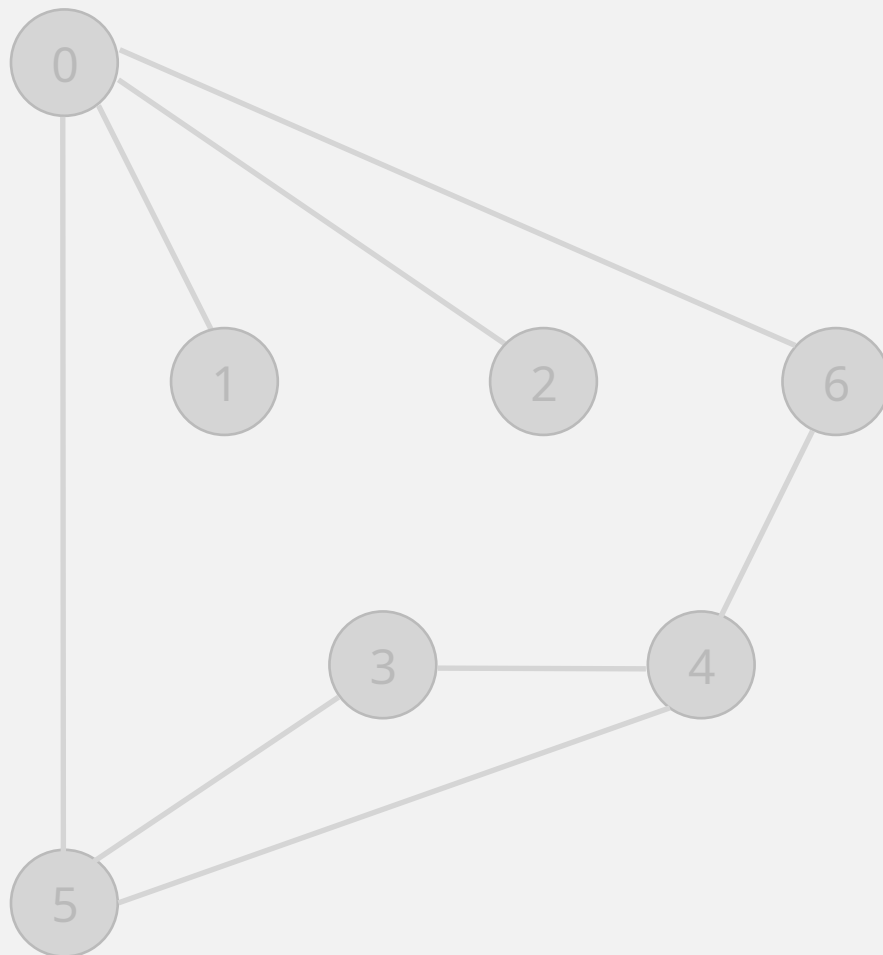


<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	F	-
10	F	-
11	F	-
12	F	-

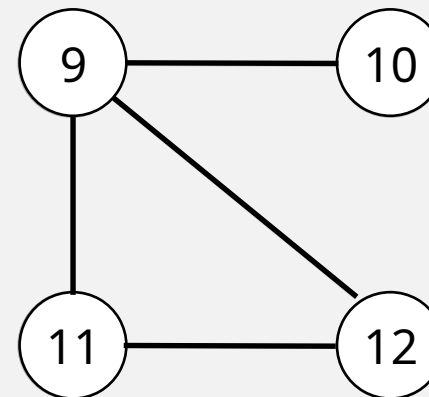
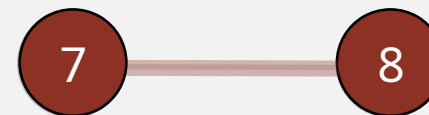
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**8 done**

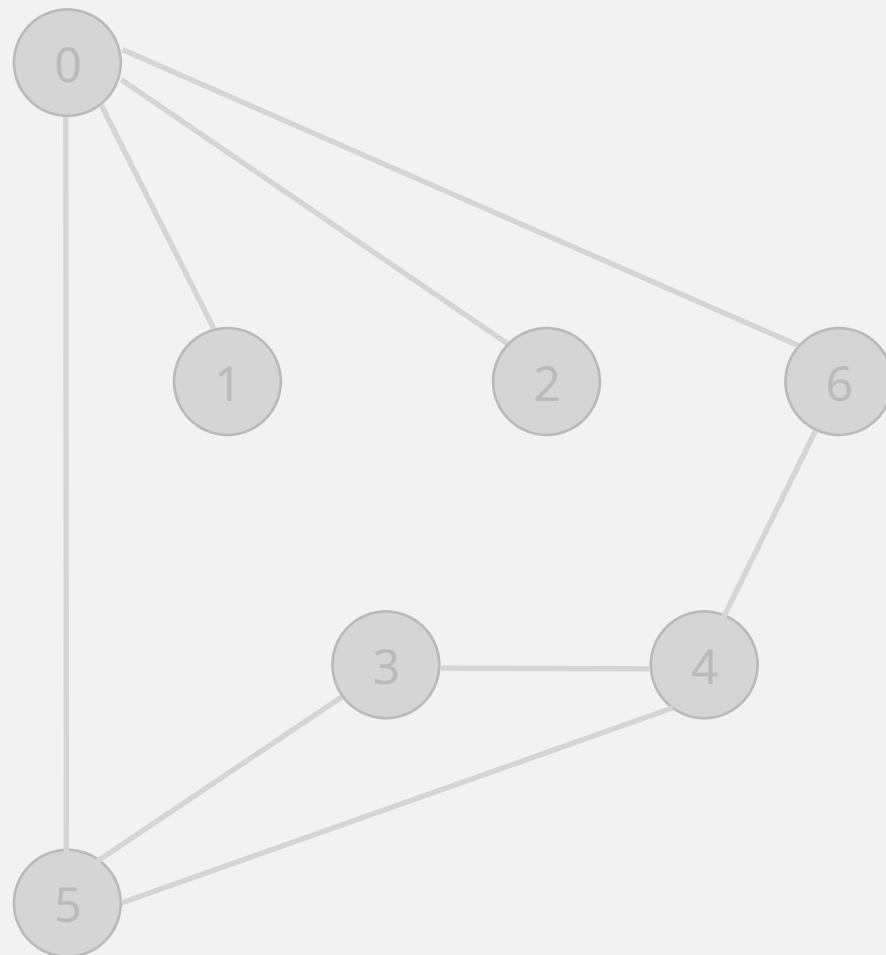


$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	F	-
10	F	-
11	F	-
12	F	-

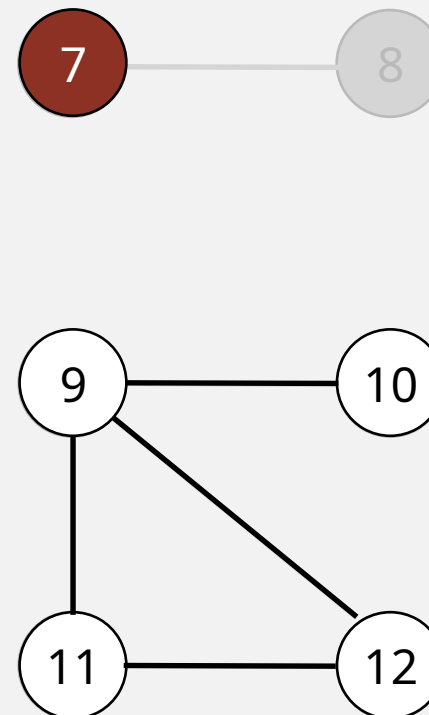
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**7 done**

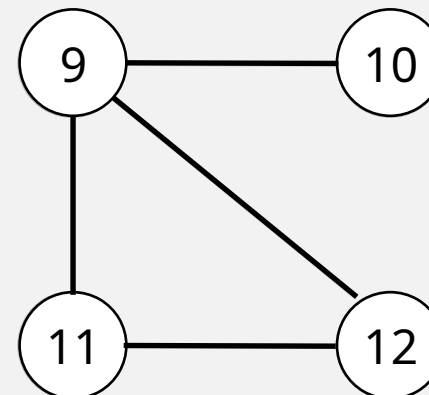
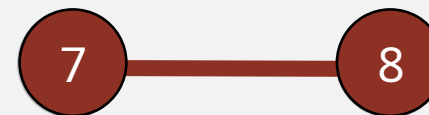
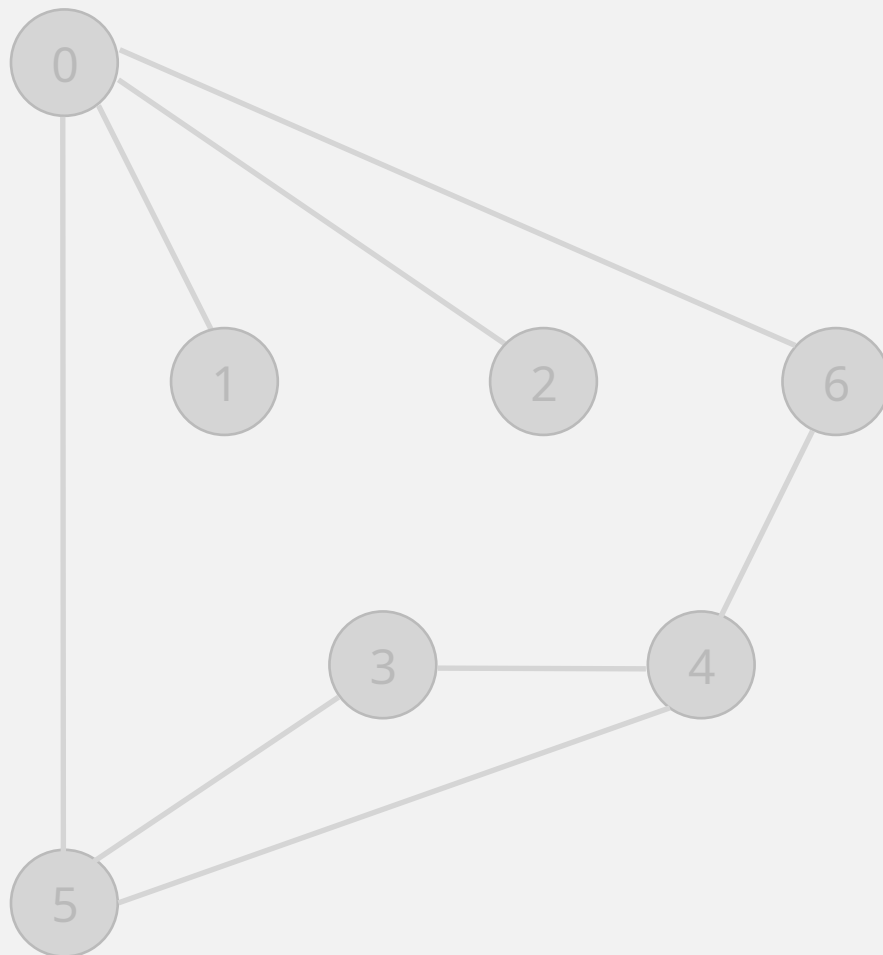


<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	<b>T</b>	<b>1</b>
8	<b>T</b>	<b>1</b>
9	F	-
10	F	-
11	F	-
12	F	-

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



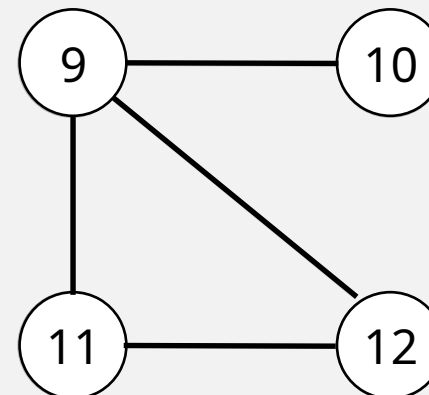
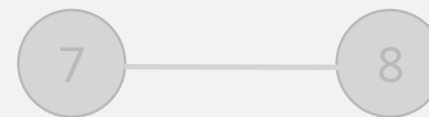
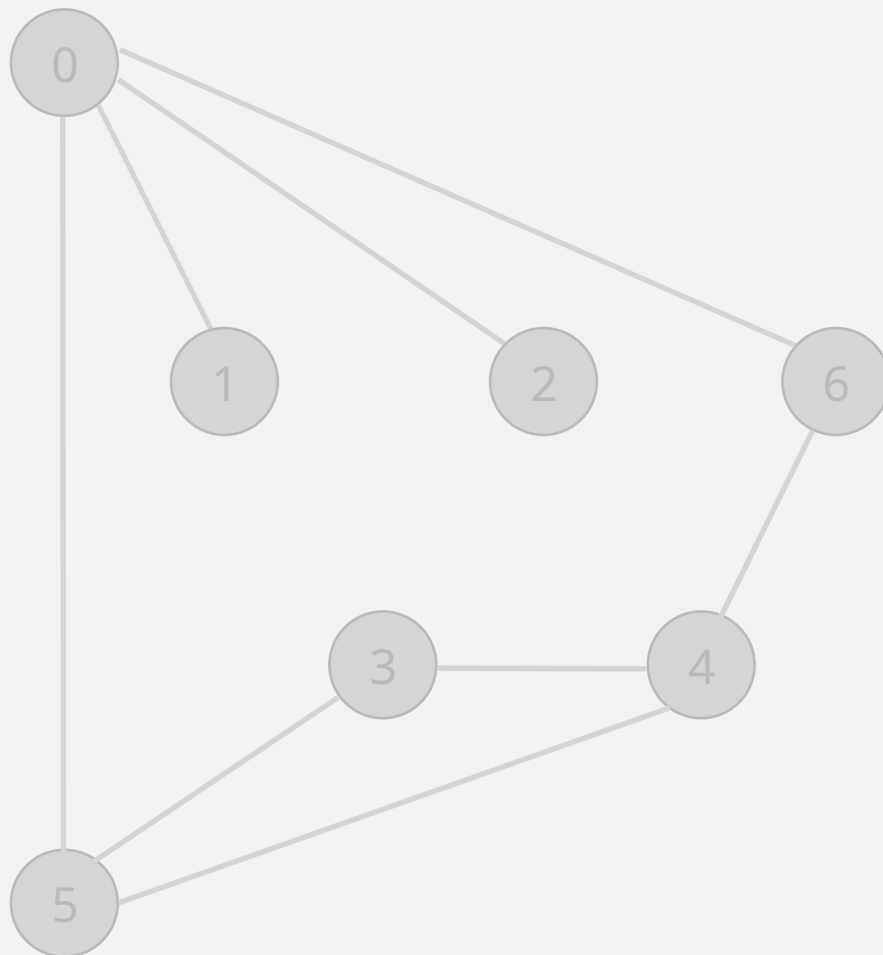
**connected component: 7 8**

<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	<b>T</b>	<b>1</b>
8	<b>T</b>	<b>1</b>
9	F	-
10	F	-
11	F	-
12	F	-

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	F	-
10	F	-
11	F	-
12	F	-

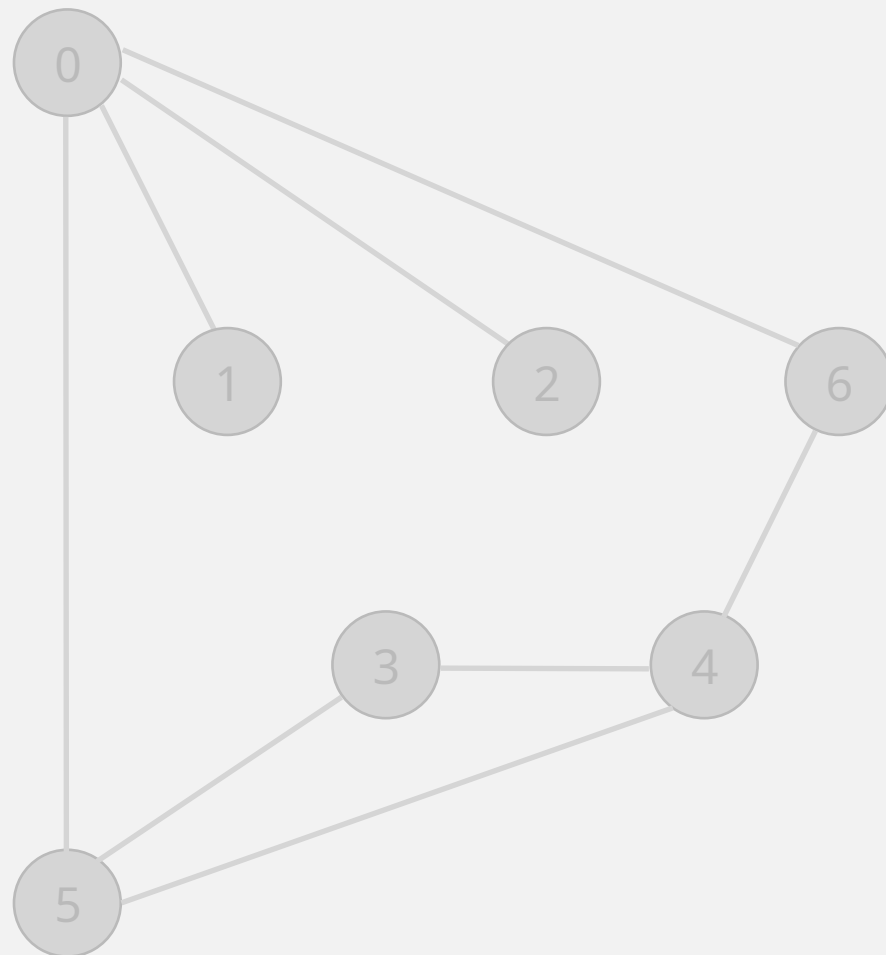
**check 8**



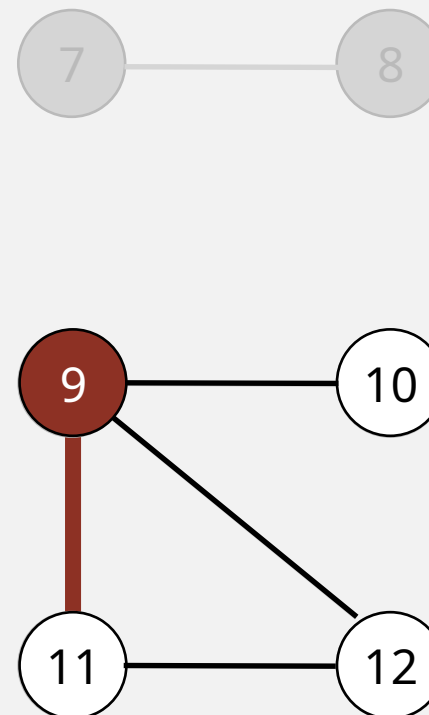
# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



**visit 9**

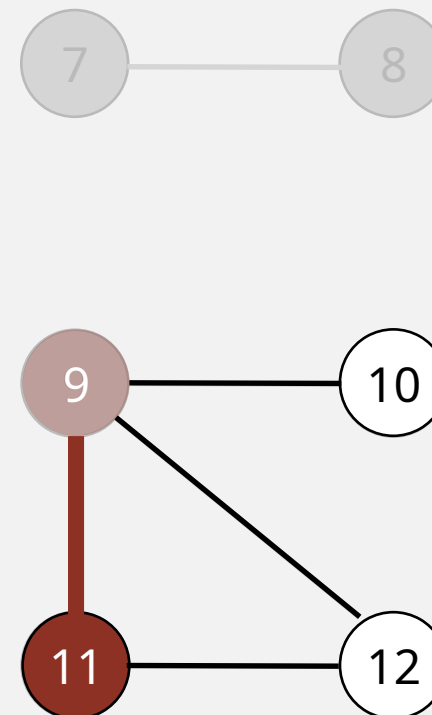
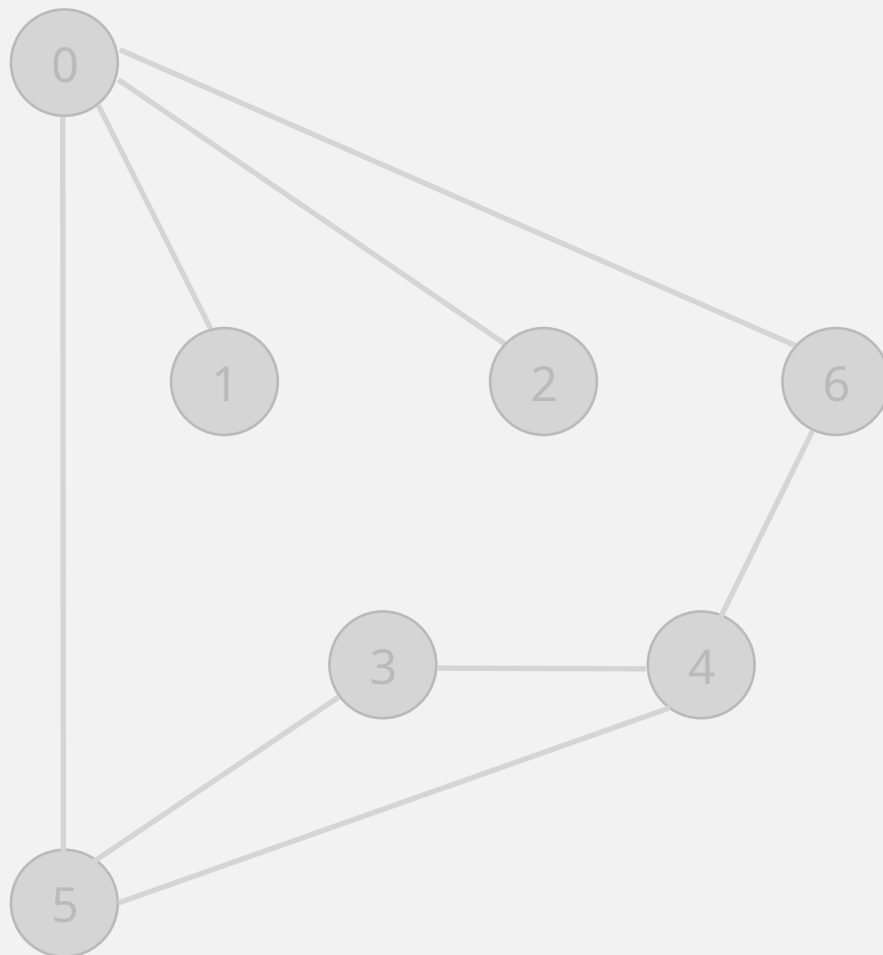


<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	-
11	F	-
12	F	-

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



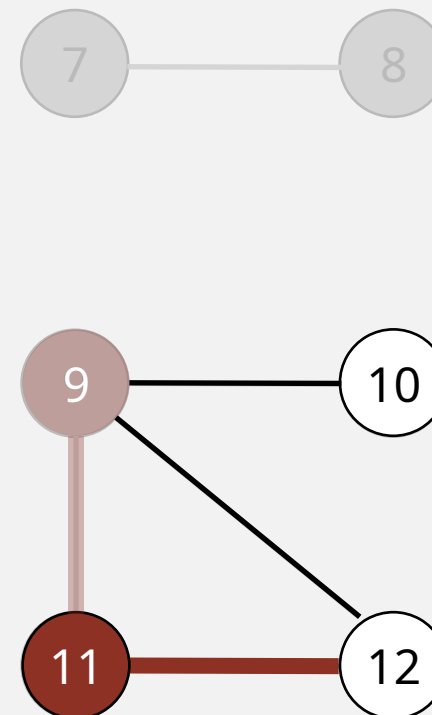
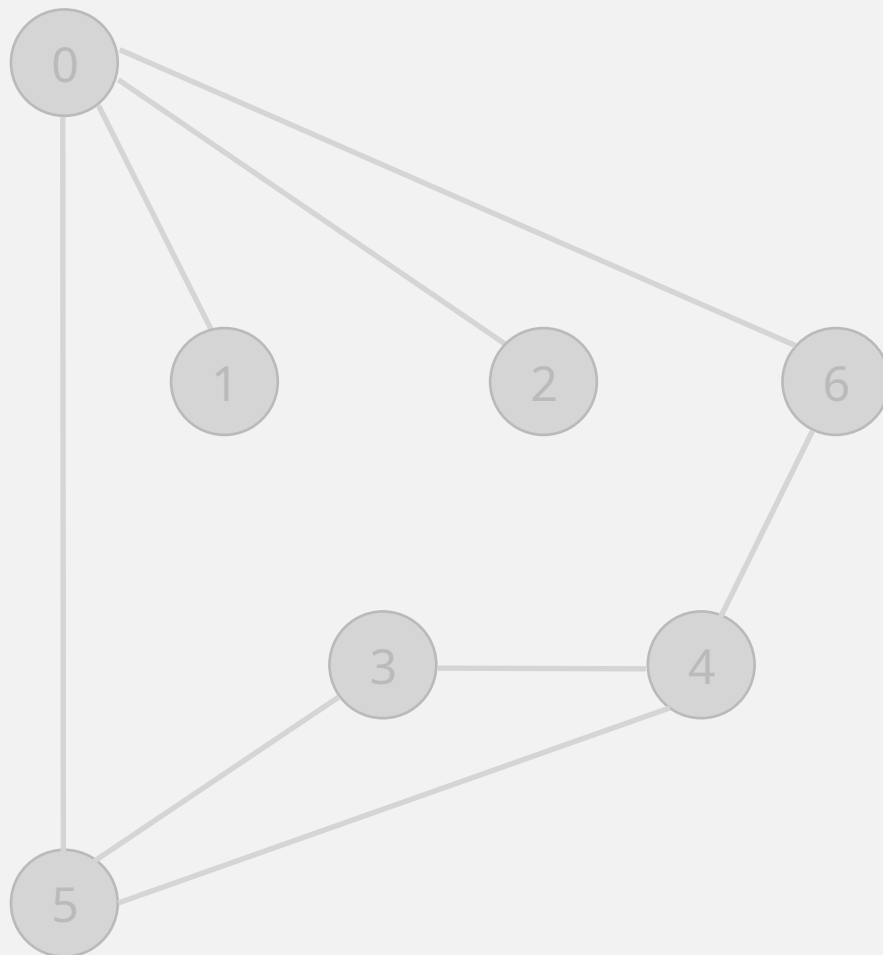
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	-
11	T	2
12	F	-

**visit 11**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



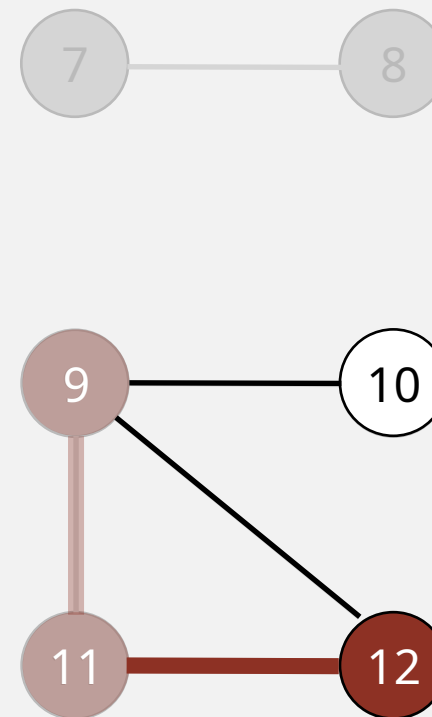
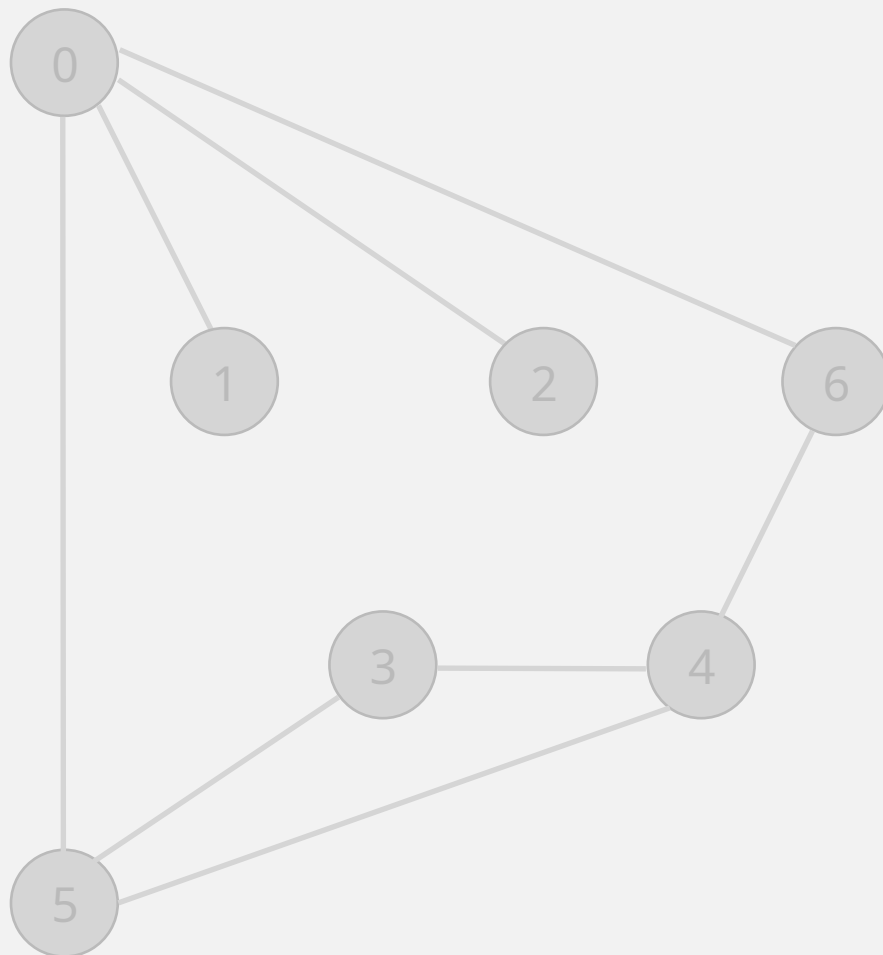
<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	<b>T</b>	<b>2</b>
10	F	-
11	<b>T</b>	<b>2</b>
12	F	-

**visit 11**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



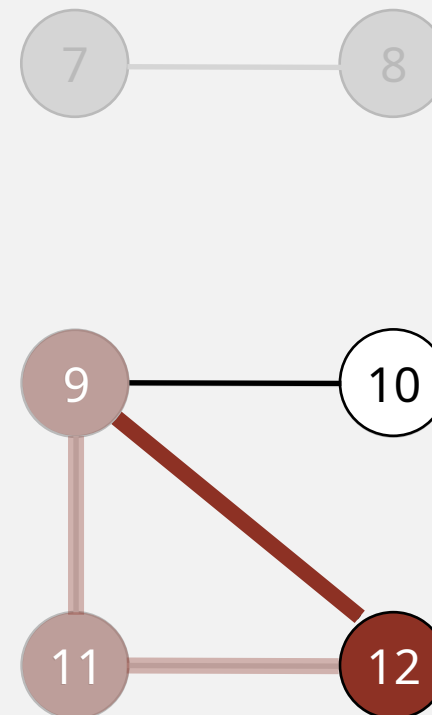
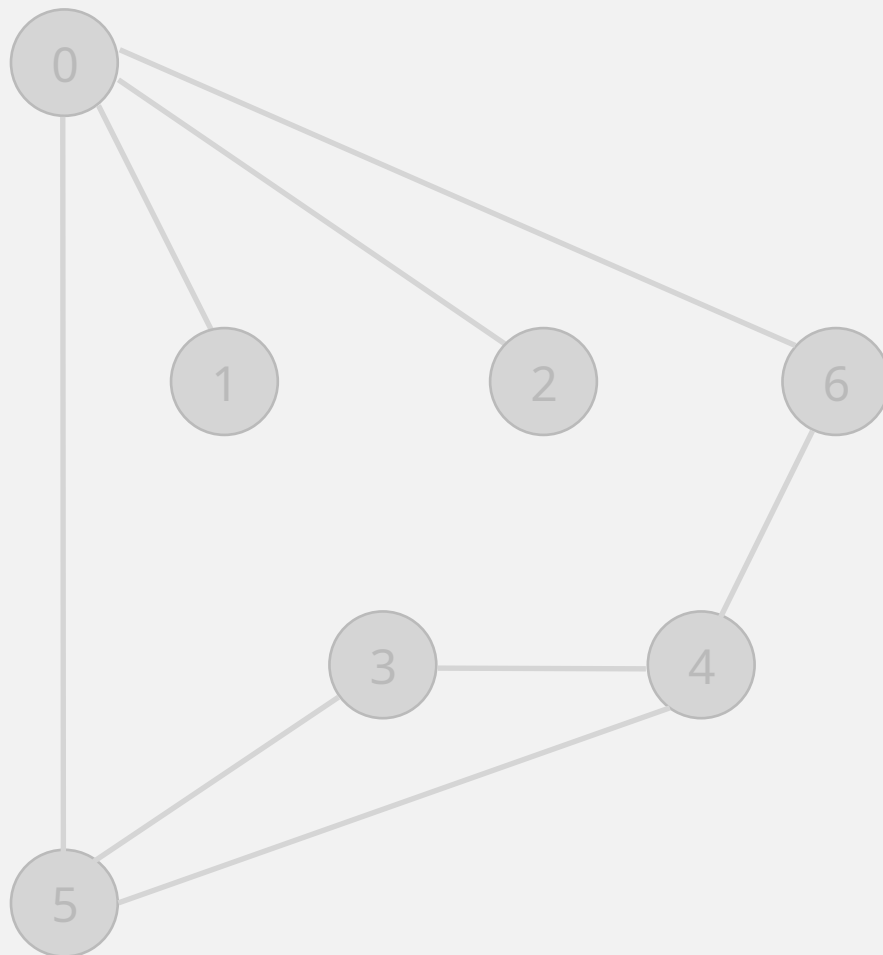
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	<span style="border: 1px solid red; border-radius: 50%; padding: 2px;">T</span>	<span style="border: 1px solid red; border-radius: 50%; padding: 2px;">2</span>
10	F	-
11	T	2
12	T	2

**visit 12**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



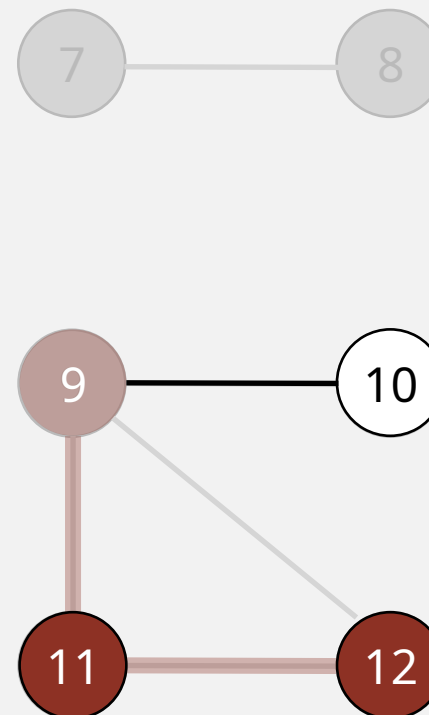
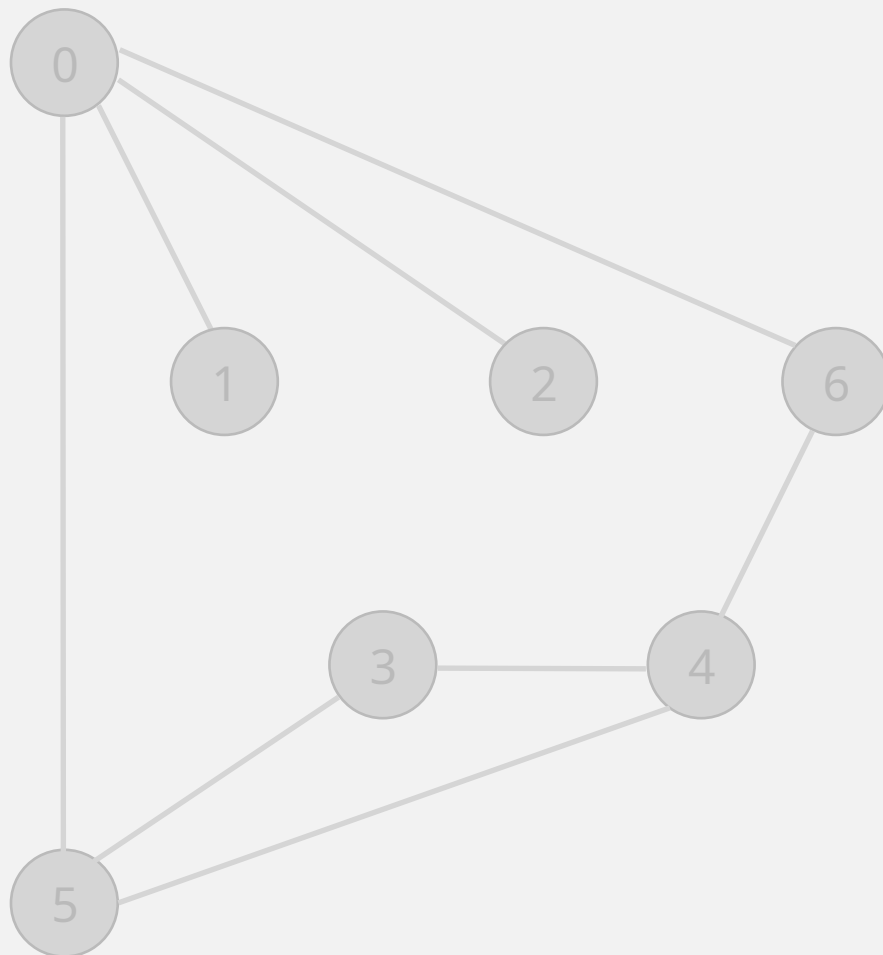
$v$	marked[]	id[]
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	F	-
11	T	2
12	T	2

**visit 12**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



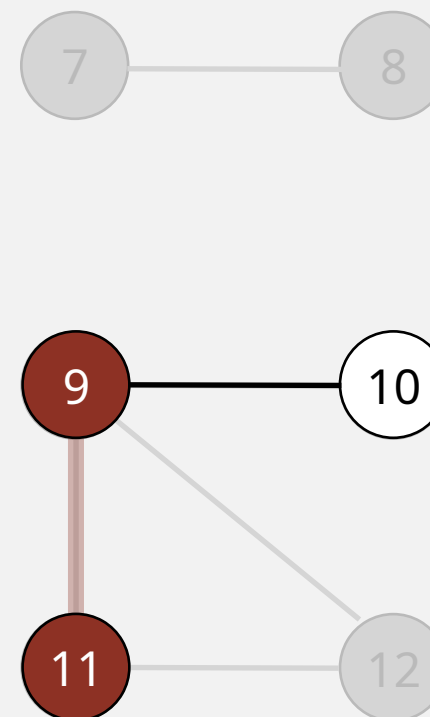
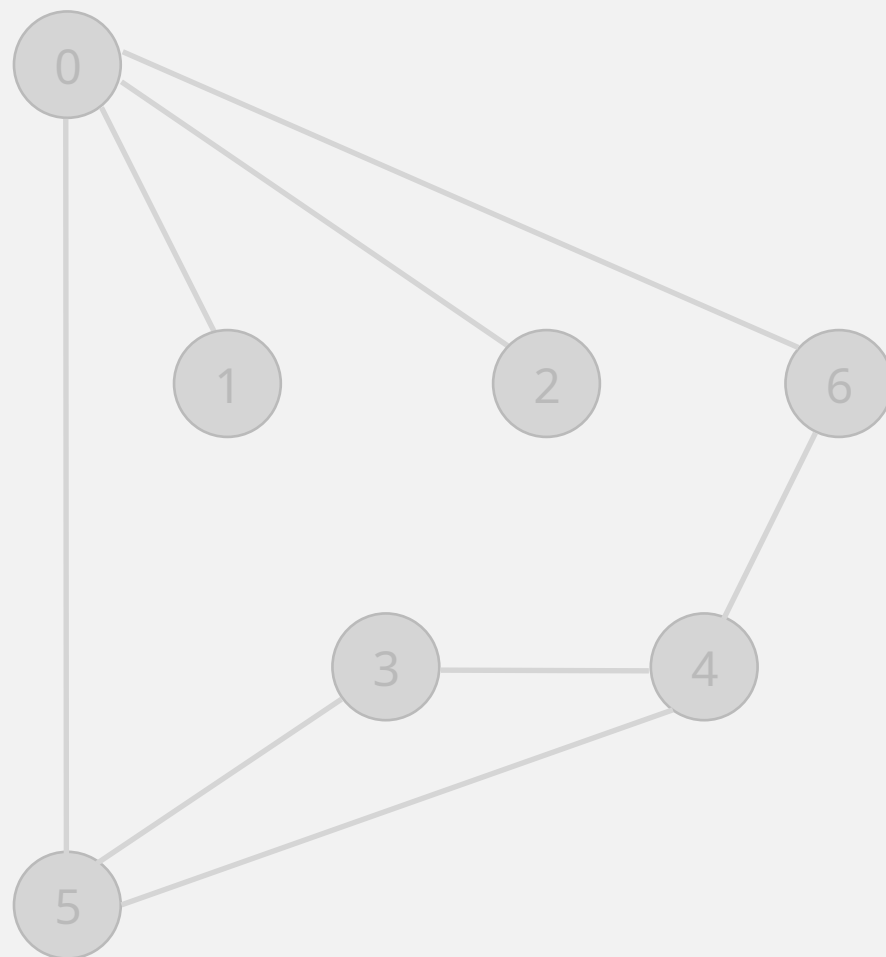
<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	<b>T</b>	<b>2</b>
10	F	-
11	<b>T</b>	<b>2</b>
12	<b>T</b>	<b>2</b>

**12 done**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



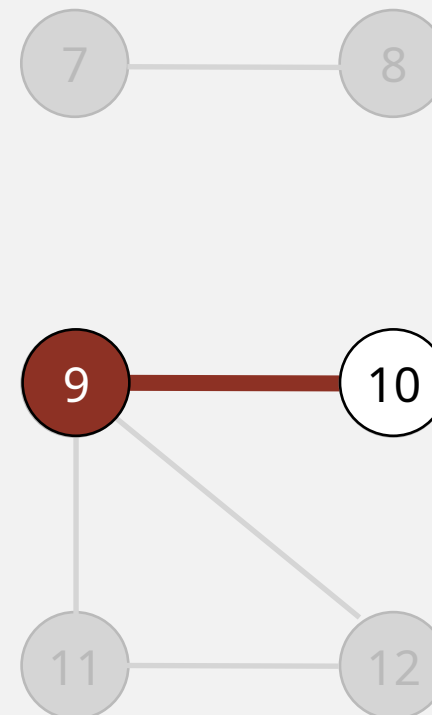
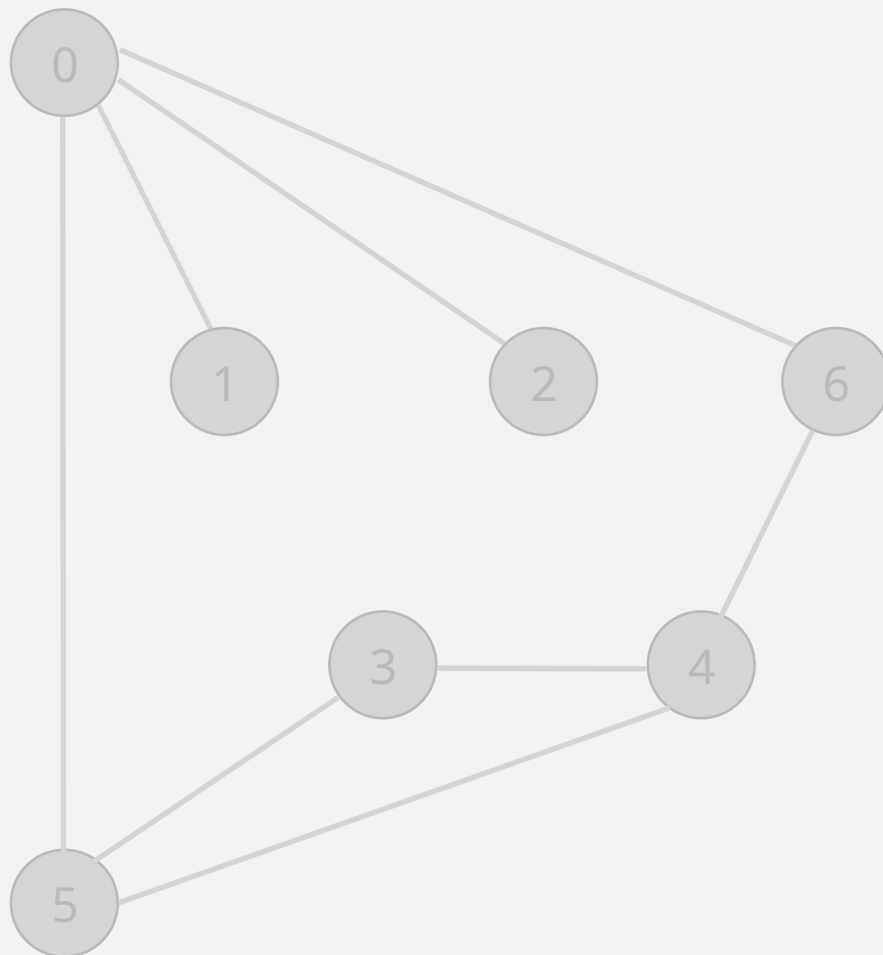
<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	<b>T</b>	<b>2</b>
10	F	-
11	<b>T</b>	<b>2</b>
12	<b>T</b>	<b>2</b>

**11 done**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	<b>T</b>	<b>2</b>
10	F	-
11	<b>T</b>	<b>2</b>
12	<b>T</b>	<b>2</b>

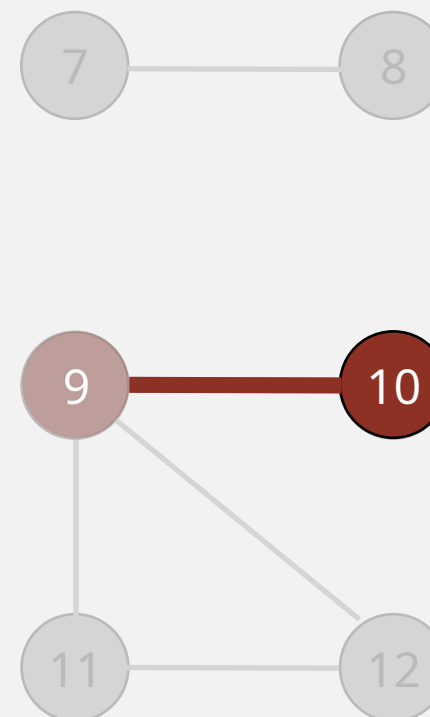
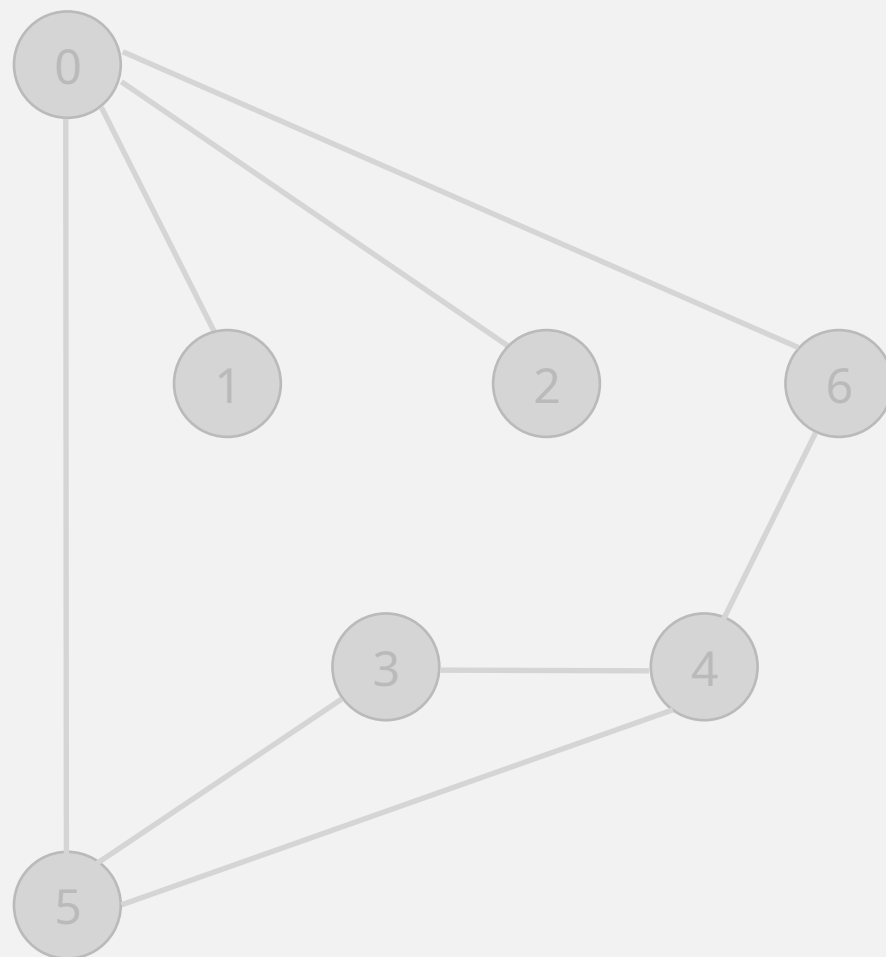
**visit 9**



# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



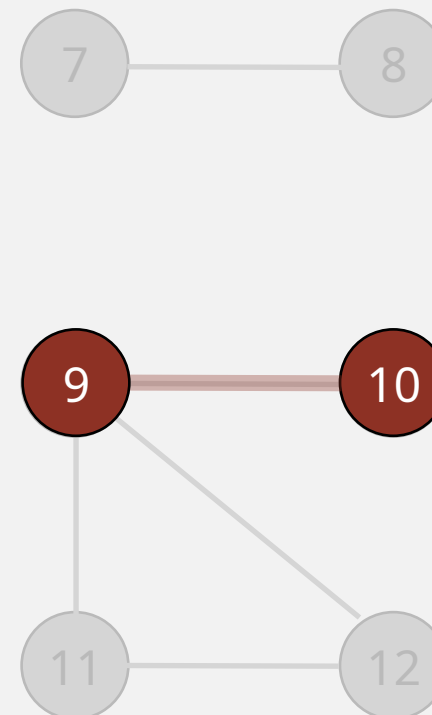
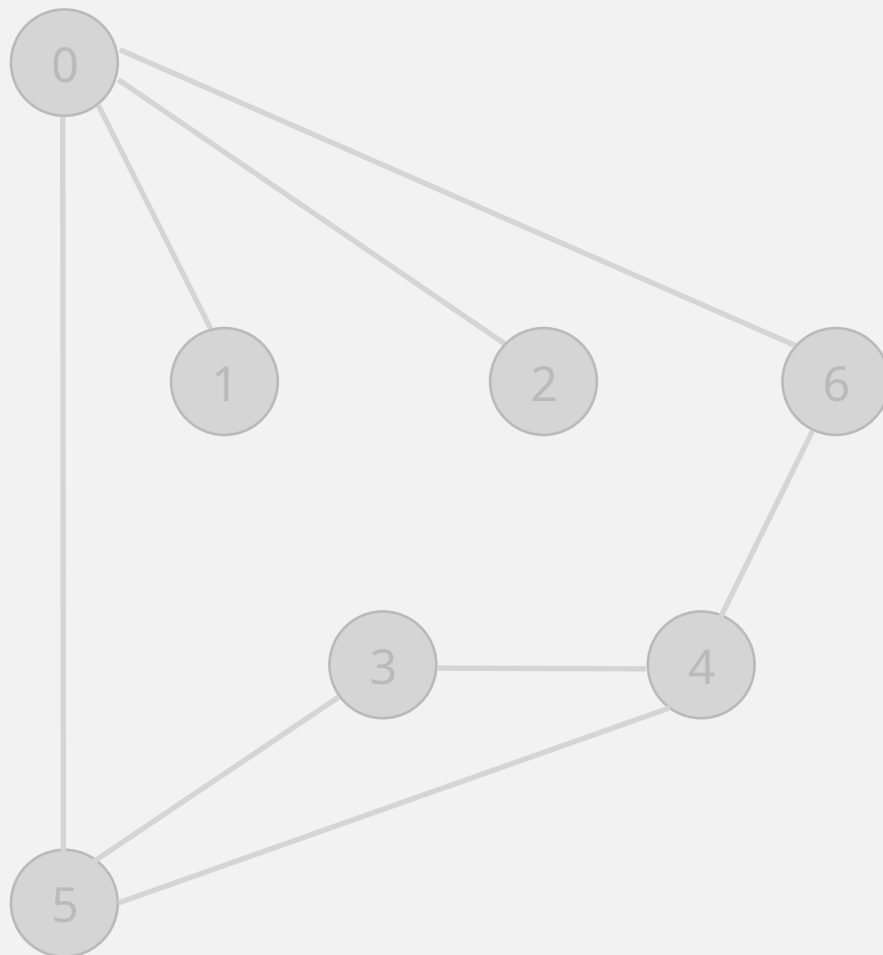
<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

**visit 10**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



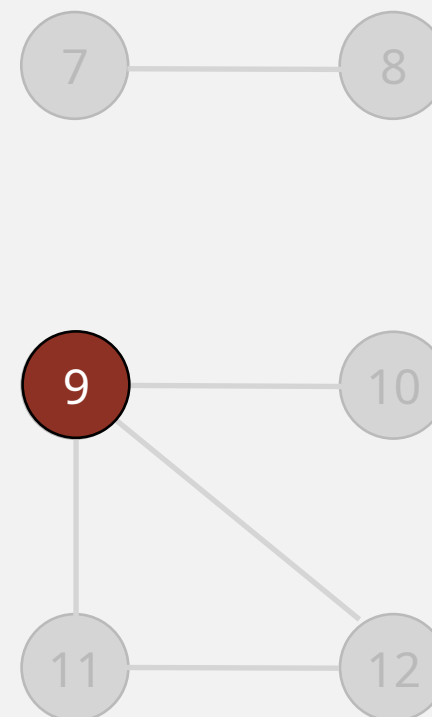
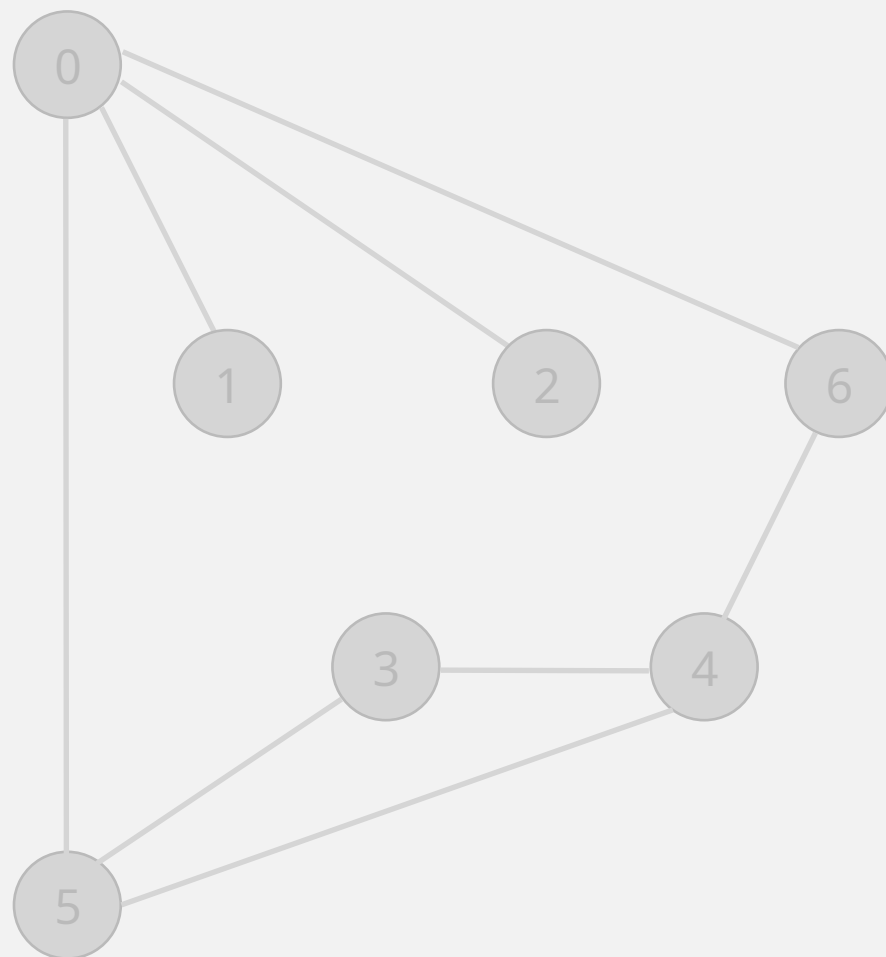
<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	<b>T</b>	<b>2</b>
10	<b>T</b>	<b>2</b>
11	<b>T</b>	<b>2</b>
12	<b>T</b>	<b>2</b>

**10 done**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



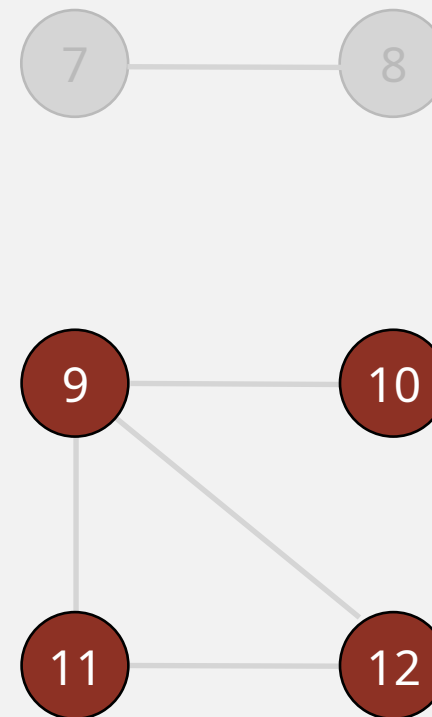
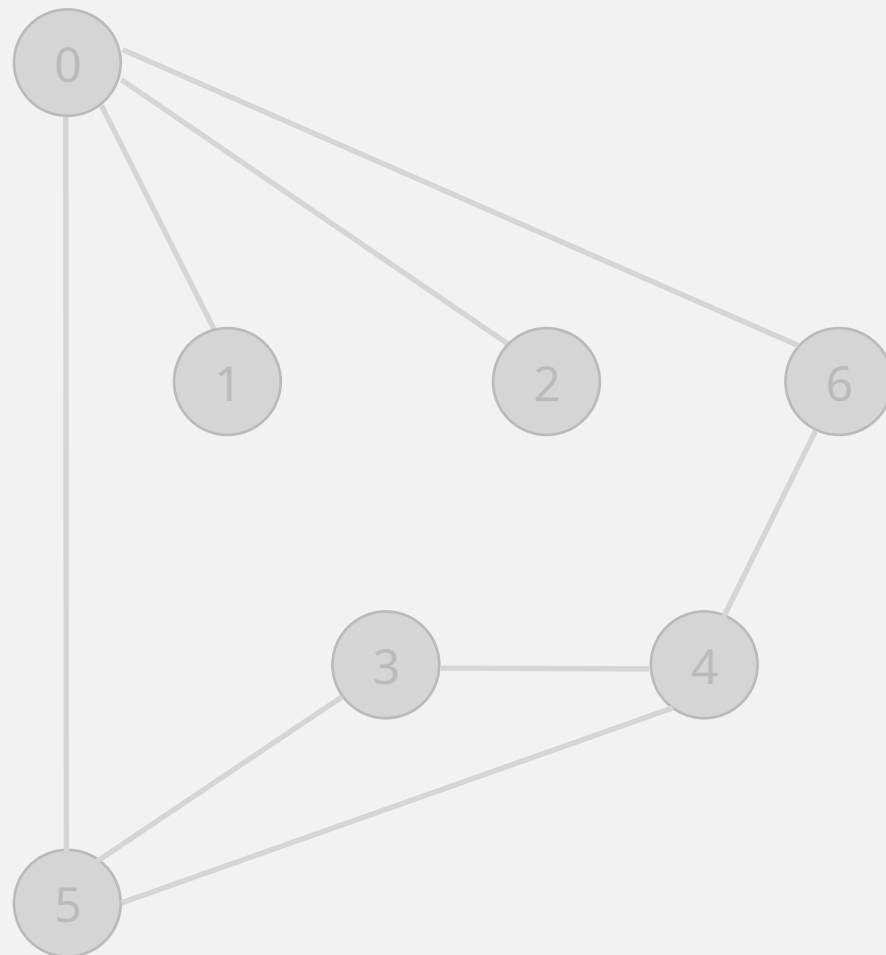
<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	<b>T</b>	<b>2</b>
10	<b>T</b>	<b>2</b>
11	<b>T</b>	<b>2</b>
12	<b>T</b>	<b>2</b>

**9 done**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



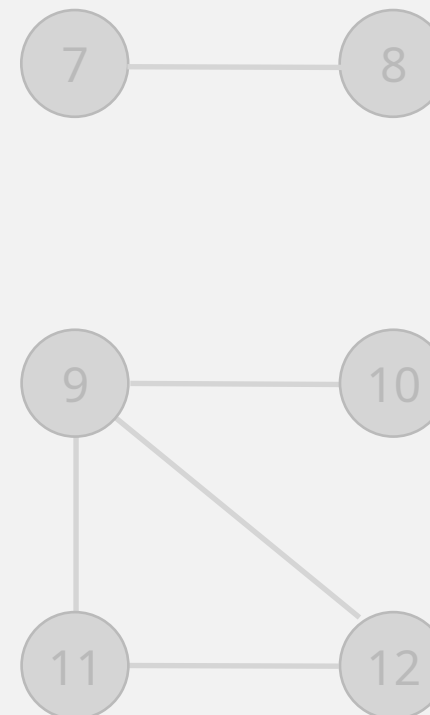
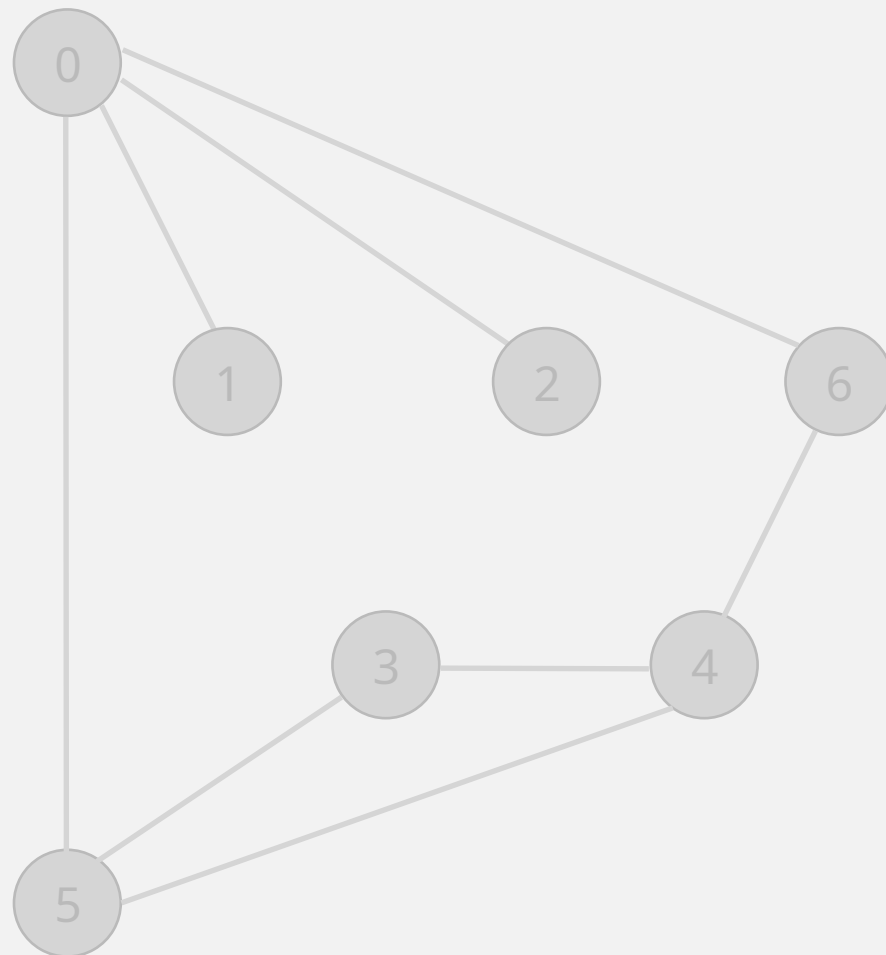
**connected component: 9 10 11 12**

<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



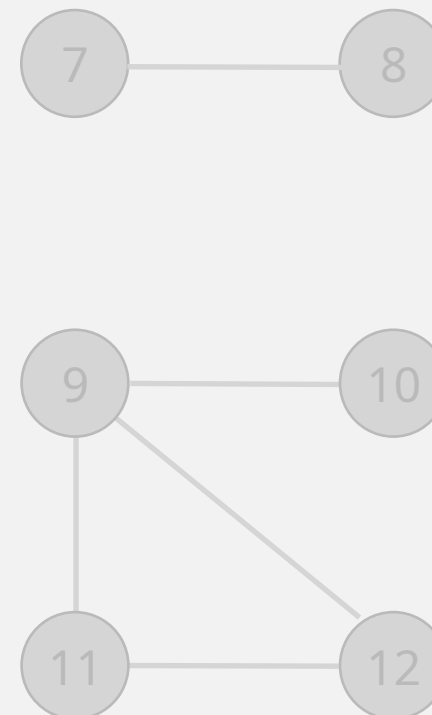
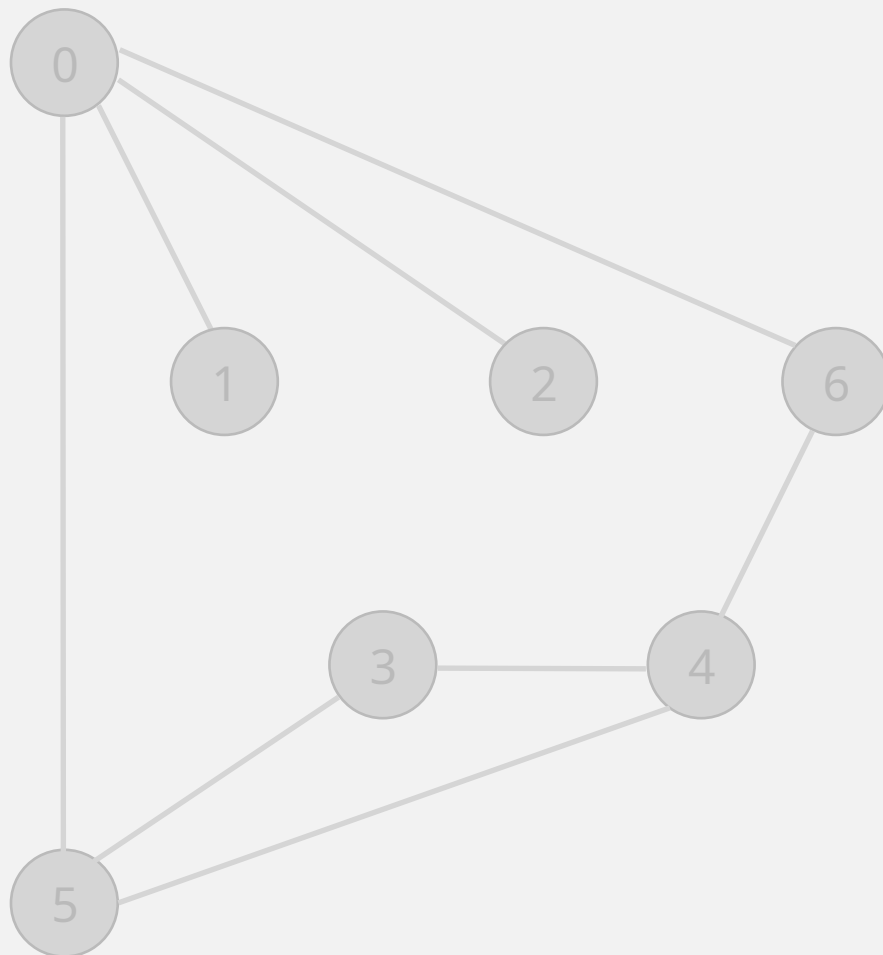
<u>v</u>	<u>marked[]</u>	<u>id[]</u>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

**check 10 11 12**

# Connected components demo

To visit a vertex  $v$ :

- Mark vertex  $v$  as visited.
- Recursively visit all unmarked vertices adjacent to  $v$ .



<b>v</b>	<b>marked[]</b>	<b>id[]</b>
0	T	0
1	T	0
2	T	0
3	T	0
4	T	0
5	T	0
6	T	0
7	T	1
8	T	1
9	T	2
10	T	2
11	T	2
12	T	2

**done**