

# CSCI 2270

## Data Structures and Algorithms

### Lecture 16

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Office hours: ECCS 128

Wed 1-2pm

Fri 2-3pm

# Administrivia

Thursday 2-3 office hours have moved to Friday 2-3

HW2 will post on Monday

linked list implementation of a biiig integer in any base

Read 10.2, Linked Lists

Skim Free Trees B.5.1

Read Rooted and Ordered Trees, B.5.2

Read Binary Search Trees, 12.1-12.4

Next week's lab: binary search trees

Colloquia: check the videos link if you need review...

# Queues

Finish 'wrapped' array based queue

# Trees

Trees are like linked lists that can branch out (but never in)

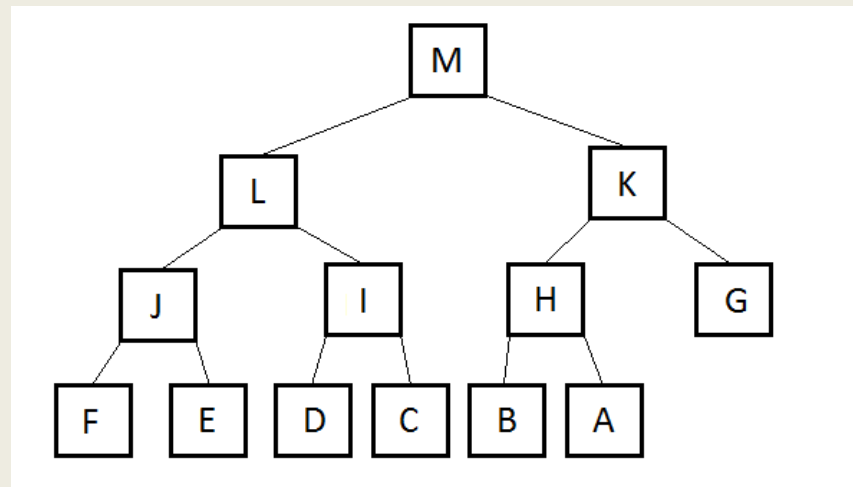
Tree nodes have more than one next pointer

Instead of a head\_ptr, we keep a pointer to the tree's root

nodes farthest from the root are the leaves

Hierarchy: parent/child, ancestor, sibling

Trees contain subtrees (recursive structure)



# Binary trees

Binary tree nodes:

- contain data;

- have 2 children per node (n-ary tree: n children)

- We call the children the left and right subtrees

Used to represent arithmetic expressions

# Tree height

Empty tree: height = 0

Else tree height is = 1 + height of largest subtree

(what's important about this definition?)

If binary tree is full, no nodes are missing at any height

height  $h \geq 0$ ; tree has  $2^h - 1$  nodes

if tree has  $n$  nodes, height is  $\log_2(n+1)$

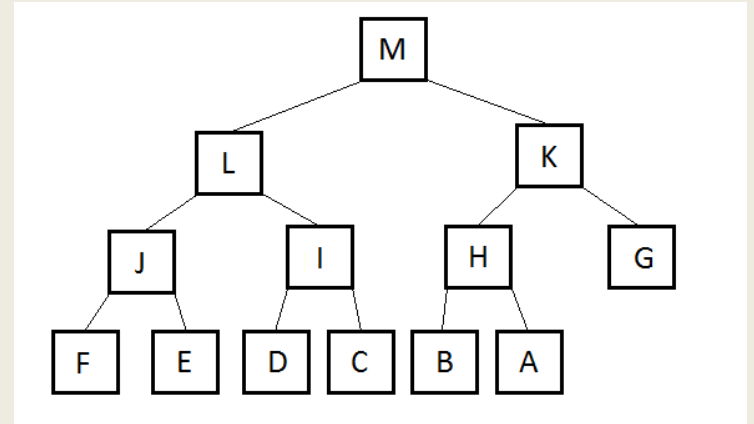
If it's complete, then the last row can be partially filled in,

left to right, with no skipped children.

Opposite of complete tree (degenerate case) looks like a list

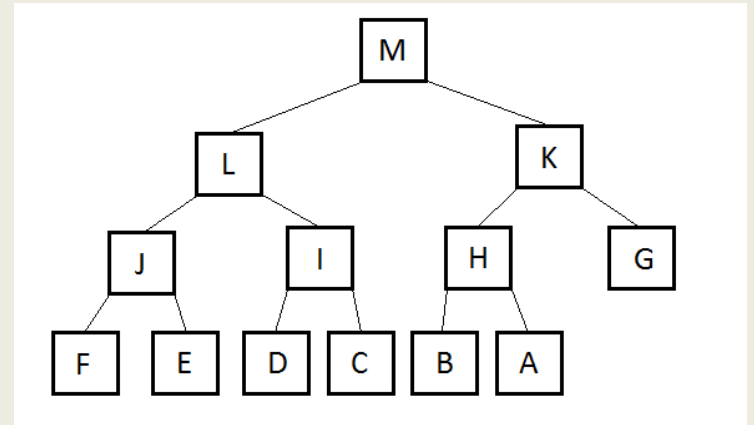
# Tree traversals

Recursive process



```
preorder_print (const binary_tree_node* bintree)
{
    if (bintree is not empty)
    {
        print out data at root
        preorder_print(left subtree of bintree's root)
        preorder_print(right subtree of bintree's root)
    }
}
```

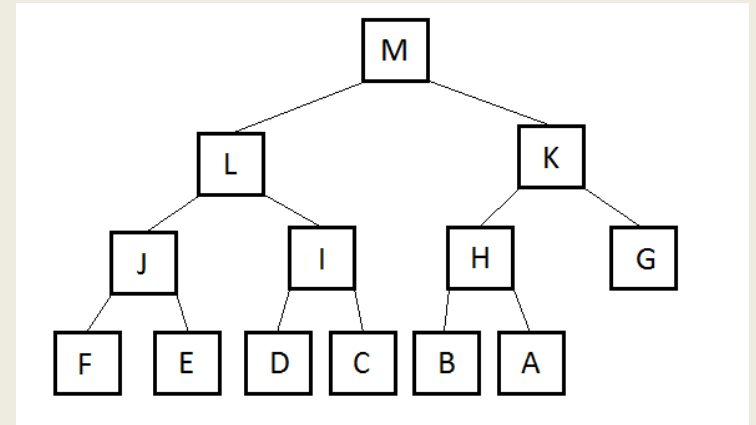
# Tree traversals



```
inorder_print (const binary_tree_node* bintree) :  
    if (bintree is not empty)  
    {  
        inorder_print(left subtree of bintree's root)  
        print out data at root  
        inorder_print(right subtree of bintree's root)  
    }
```



# Tree traversals



```
postorder_print (const binary_tree_node* bintree) :  
    if (bintree is not empty)  
    {  
        postorder_print(left subtree of bintree's root)  
        postorder_print(right subtree of bintree's root)  
        print out data at root  
    }
```

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Binary search trees: special binary trees

- can* work faster than lists

- data at n is  $\geq$  values in n's left subtree

- data at n is  $<$  values in n's right subtree

# Binary *search* tree: search

Recall that      data in node  $n$  is  $\geq$  data in  $n$ 's left subtree  
                    data in node  $n$  is  $<$  data in  $n$ 's right subtree

```
search(const binary_tree_node* bstree, int target) :  
    if (bstree is empty)  
        target not found, boo!  
    else if (target equals data item at root)  
        target found, yay!  
    else if (target < data item at root)  
        search(left subtree of bstree, target)  
    else  
        search(right subtree of bstree, target)
```

# Binary search tree: insert

Find where item would go and then put it there as a new leaf

Shape of tree depends on order in which items are inserted

# Trees offer the chance for $\log(n)$ performance if you're lucky

For a binary search tree of  $n$  nodes,

Search:  $O(\log n)$  average,  $O(n)$  worst case

Insert:  $O(\log n)$  average,  $O(n)$  worst case

Remove:  $O(\log n)$  average,  $O(n)$  worst case

Traverse:  $O(n)$

Another tree ADT, the B-tree, ensures that the tree is perfectly full—guarantees the  $O(\log n)$  performance, worst case