

Linear Data Chapter 1

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1. Let

$$\mathbf{A} = \begin{pmatrix} 15 & -14 & 13 & -12 & 11 \\ -10 & 9 & -8 & 7 & -6 \\ 5 & -4 & 3 & -2 & 1 \end{pmatrix} \text{ and } \mathbf{B} = \begin{pmatrix} 15 & -14 & 13 & -12 & 0 \\ -10 & 9 & -8 & 7 & -6 \\ 5 & -4 & 3 & -2 & 1 \end{pmatrix}$$

- Explicitly give (i.e., write down the numeral not just a formula) $A_{2,3}$.
 - Is \mathbf{A} a 5×3 matrix? Explain your answer.
 - Are \mathbf{A} and \mathbf{B} (mathematically) equal? Explain your answer.
2. Give an example of a data tensor with valence 3. (The example can be from the book or one you made up.)
3. Given the following set

$$X = \{2, 4, 6, 8\} \quad \text{and} \quad Y = \{1, 2, 3\},$$

explicitly give (e.g., write down the sets with numerical entries) of the outputs of the following requested set operations:

- (a) $X \cup Y$
- (b) $X \cap Y$
- (c) $X \setminus Y$

(You don't need to write written explanations for the set problems.)

4. Given the function $f : X \rightarrow Y$ (with X and Y as above) defined as

$$f(2) = 2, \quad f(4) = 1, \quad f(6) = 3, \quad f(8) = 2,$$

answer the following questions. Justify your answers.

- (a) Is f injective?
- (b) Is f surjective?
- (c) Is f bijective?

5. Using Python/Jupyter or Matlab/Matlab Live Script, perform the following:

- Define a matrix

$$\mathbf{M} = \begin{pmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{pmatrix}$$

- Define a (row) vector

$$\vec{x} = (0 \quad 0 \quad 0 \quad 0)$$

- Make the top row of \mathbf{M} equal to \vec{x} .

Hint: You only need 3 commands to perform the above tasks.