

DATA SCIENCE WITH R

HYPOTHESIS TESTING

Introduction to Hypothesis Testing

Basic Framework of a Hypothesis Test



Distance Measures

Central Limit Theorem

Types of Hypothesis Tests

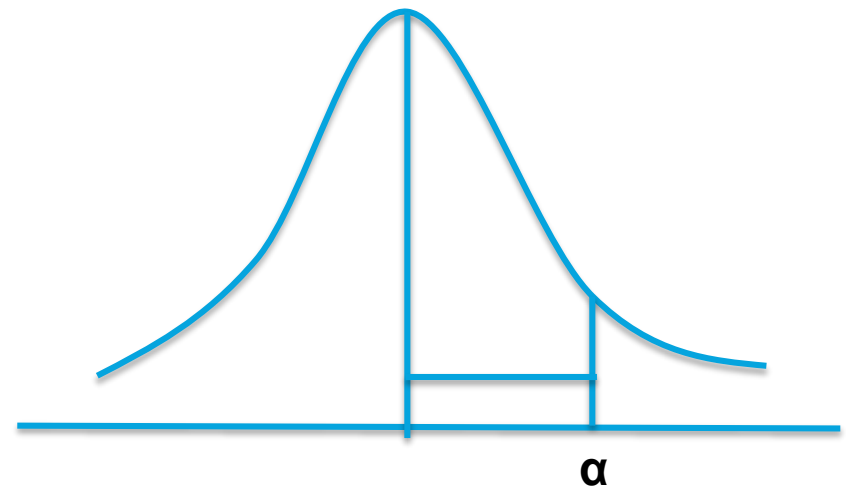


Distance Measures

Another way to think about the test is to look at distance from mean

Critical Value:

Distance from mean, beyond which the null will be rejected

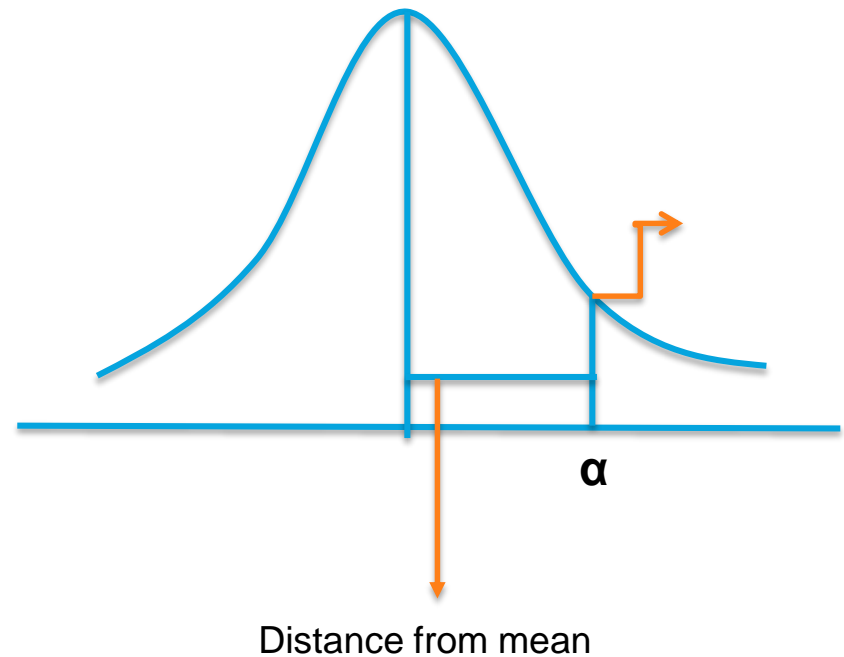


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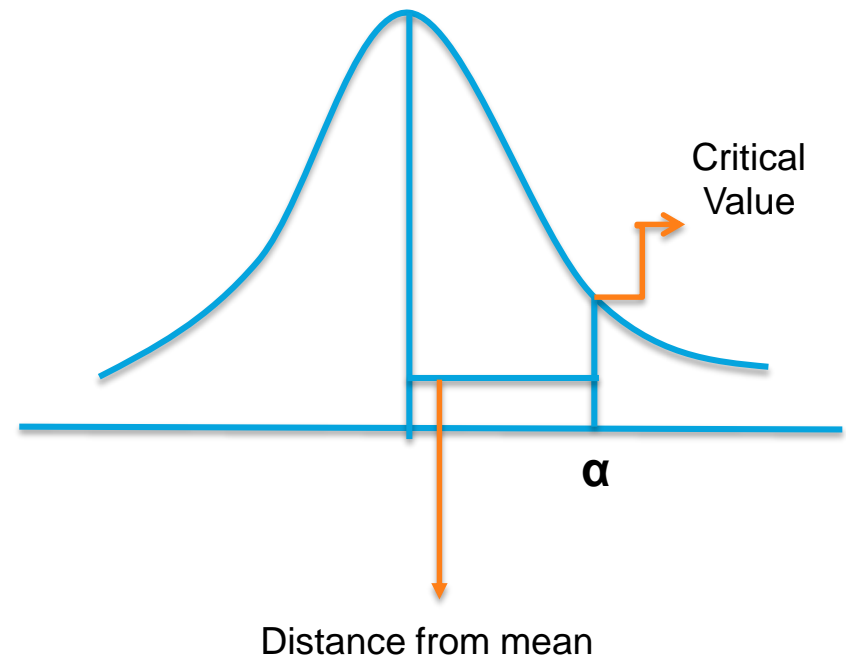


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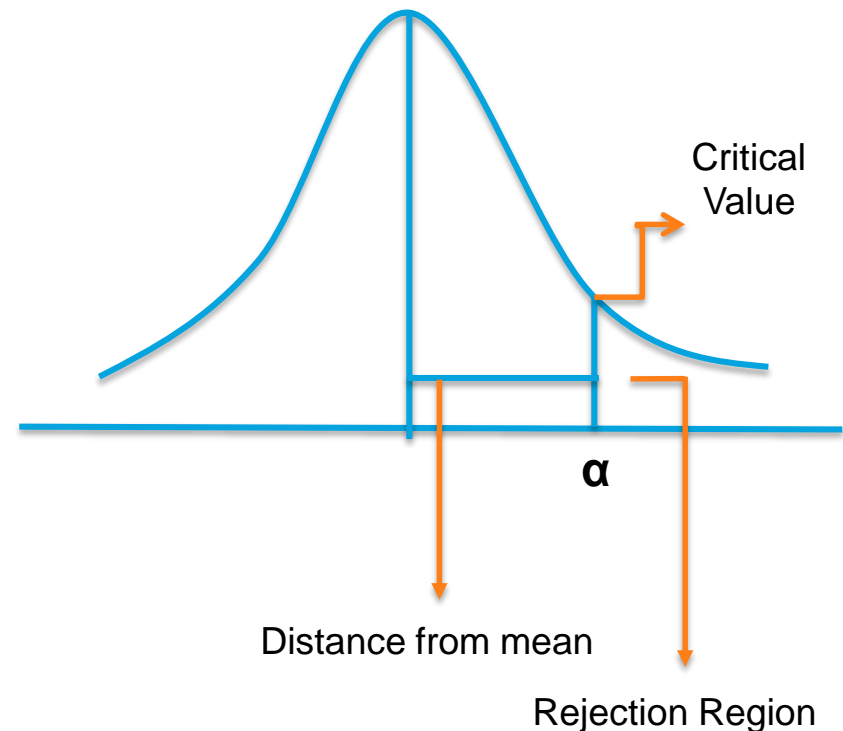
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Critical Value:

Distance from mean, beyond which the null will be rejected

Rejection Region:

Values of the test statistic (distance) that are unlikely if null is true, associated with the probability distribution



Distance Measures

Test Statistic:

A function of the random sample,
usually measured as standardized
distance from mean

Test Statistic $Z : (X - \mu)/\sigma$

$$X = 2.68$$

$$\mu = 2.5$$

$$\sigma = 0.12$$

$$Z = (2.68 - 2.5)/0.12 \quad \mathbf{1.5}$$



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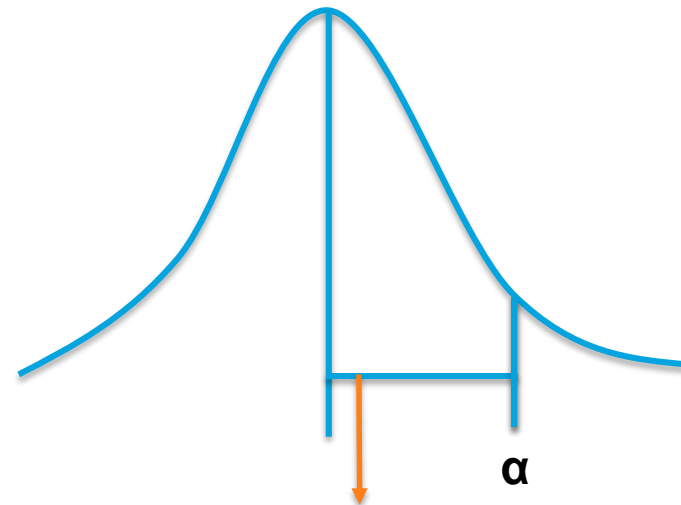
$$\mu = 2.5$$

$$\sigma = 0.12$$

$$Z = (2.68 - 2.5) / 0.12 \quad \mathbf{1.5}$$

Critical Distance:

Distance equivalent to Sig Level



Critical Distance



Distance Measures



Probability Content from $-\infty$ to Z

Z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981



Distance Measures

Test Statistic $Z : (X - \mu)/\sigma$

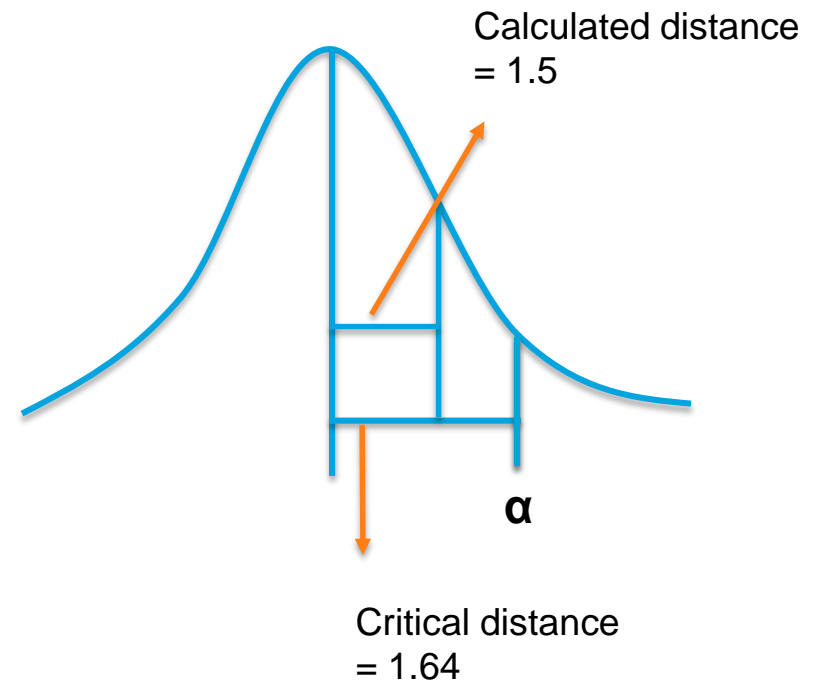
$X = 2.68$

$\mu = 2.5$

$\sigma = 0.12$

$Z = (2.68 - 2.5)/0.12$ **1.5**

Critical distance = 1.64



Distance Measures

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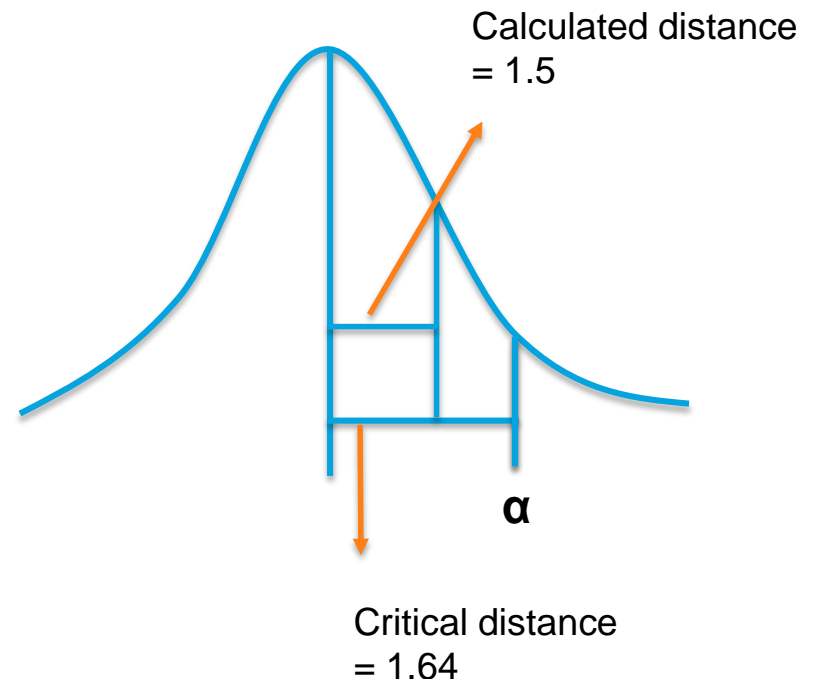
$\mu = 2.5$

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$Z = (2.68 - 2.5)/0.12$ **1.5**

Critical distance = 1.64

Since outcome is closer to mean than critical ($1.5 > 1.64$) , we fail to reject the null



Distance Measures



Probability Content from $-\infty$ to Z

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Distance Measures

1. If you have access to Excel / SAS / Calculators

- Directly calculate p – values to decide
- If calculated p-value is less than significance level: **Reject the null**

2. If you don't have access to Excel / Calculators

- Use distance measures to reject (or not reject) the null hypothesis, or probability tables
- If calculated Test Statistic is further away from the mean than the critical value: **Reject the null**



Distance Measures

IMPORTANT TO NOTE:



Distance Measures

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Confidence level

- This is $(1 - \text{significance level})$, and is used to show how confident you are about your conclusion.



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- This is $(1 - \text{significance level})$, and is used to show how confident you are about your conclusion.
 - If null hypothesis is rejected at a 5% level of significance, you are 95% confident about your conclusion.



Distance Measures

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Confidence level

- This is $(1 - \text{significance level})$, and is used to show how confident you are about your conclusion.
 - If null hypothesis is rejected at a 5% level of significance, you are 95% confident about your conclusion.
 - If significance level is set to 1%, confidence level will be?



Distance Measures

IMPORTANT TO NOTE:

Choosing significance level



Distance Measures

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Choosing significance level

- Most often set to 5%



Distance Measures

IMPORTANT TO NOTE:

Choosing significance level

- Most often set to 5%
- May choose to set stricter levels depending on business requirements



Distance Measures

IMPORTANT TO NOTE:

Choosing significance level

- Most often set to 5%
- May choose to set stricter levels depending on business requirements
- May also choose to relax (but less often)



Distance Measures

IMPORTANT TO NOTE:

Statistically Significant Result

- A result is said to be statistically significant if it is unlikely to have occurred by chance.



Recap

- Hypothesis Testing is a statistical technique used to make decisions based on data



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- It relies on calculation of the random chance probability of seeing an observed outcome (sample based mean) to test a hypothesis



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 2. Decide on a significance level



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 3. Calculate p-value



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 2. Decide on a significance level
 3. Calculate p-value
 4. Compare to significance level



Recap

- Hypothesis Testing is a statistical technique used to make decisions based on data
- It relies on calculation of the random chance probability of seeing an observed outcome (sample based mean) to test a hypothesis
- **Essential steps of hypothesis testing:**
 1. Set up null and alternate hypothesis
 2. Decide on a significance level
 3. Calculate p-value
 4. Compare to significance level
 5. Reject null if p-value is less than significance level



THANK YOU

