HUST

ĐẠI HỌC BÁCH KHOA HÀ NỘI

HANOI UNIVERSITY OF SCIENCE AND TECHNOLOGY

ONE LOVE. ONE FUTURE.

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Applied Algorithm Lab

Nurse

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Nurse

- Schedule working timetable for a nurse in N consecutive days $1, \dots, N$.

  This is divided into series of consecutive working days (call working period)

- **Constraints:**
  - Only 1 day off between 2 working period
  - A working period has length in segment $[K1, K2]$
- **Input:** $N, K1, K2$
- **Output:** Number of valid ways to schedule
- Example: Input: 6 2 3

  Output: 4 Explain: 110111 111011

  110110 011011

Nurse

- **Idea to solve #1:** Brute-force
  - A timetable can be considered as a binary sequence with length N
  - List all binary sequence and check if they are valid or not
  - Complexity: $O(n\ 2^n)$ (checking costs $O(n)$)
  - Applying Branch and Bound technique: after the first bit 1 must be K1 bit 1, if there are K2 bit 1 then the next bit must be 0 to separate 2 working periods

Nurse

- **Idea to solve #2:** dynamic programming
  - Consider the problem: Scheduling for day i depends on the earlier days
  - Observe 2 cases: day i working and off
  - Consider 2 arrays $S_0[N]$ and $S_1[N]$
    - $S_0[i]$: number of ways to schedule i days that day i off
    - $S_1[i]$: number of ways to schedule i days that day i work
  - Recursive formula:

$S_0[i] = S_1[i-1];$ *// day i off = day i-1 working*

$S_1[i] = \sum_{j=K1}^{K2} S_0[i-j]$ *// day i working= end of 1 working period*

  - Base cases: $S_0[1] = S_1[K1] = S_0[0] = 1$;
  - return: $S_0[n] + S_1[n]$
  - Complexity: O(n(K2-K1))

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THANK YOU !