



# HUST

**ĐẠI HỌC BÁCH KHOA HÀ NỘI**  
HANOI UNIVERSITY OF SCIENCE AND TECHNOLOGY

ONE LOVE. ONE FUTURE.



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# Applied Algorithm Lab

Make span schedule

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# Make span schedule

- Make a schedule for a project with many tasks.
- A project has  $n$  tasks  $1, \dots, n$ :
  - Task  $i$  has duration  $d(i)$  to be completed
  - Precedence constraints  $Q$ : for each  $(i, j)$  in  $Q$ , task  $j$  cannot be started before the completion of task  $i$ .
- **Objective:** Arrange task the project to complete as soon as possible.
- **Input:**  $n$ ,  $|Q|$ ,  $d(1), \dots, d(n)$ , the set  $Q$
- **Output:** The earliest completion time of the project.

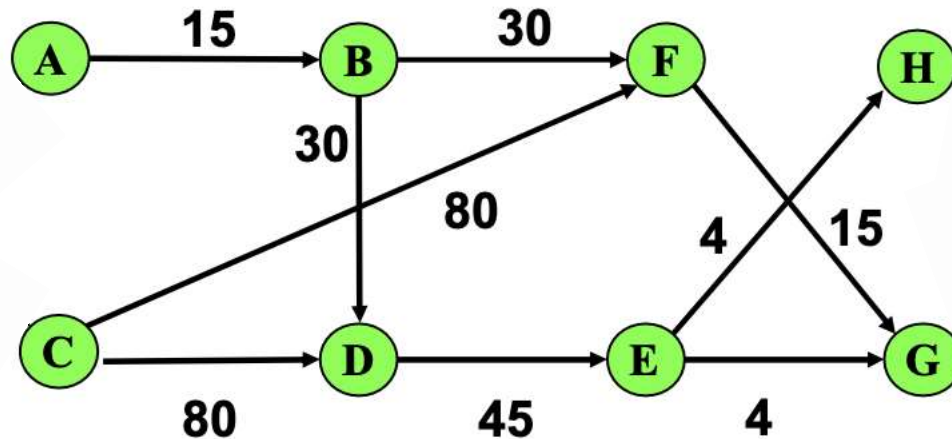
# Make span schedule

- Example

Input	Output
8 9 15 30 80 45 4 15 15 19 1 2 2 4 3 4 4 5 2 6 3 6 5 7 6 7 5 8	148

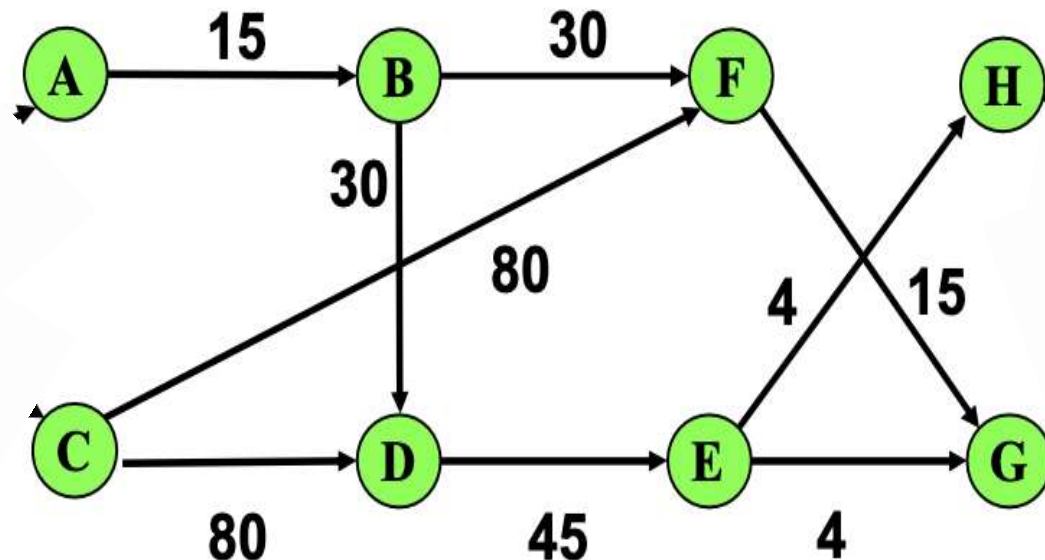
# Make span schedule

- Idea to solve: Formulate the problem using directed graph
  - A graph with  $n$  nodes as  $n$  tasks
  - If  $(i,j) \in Q$ , we draw an edge  $(i,j)$  on graph
    - weight of edge  $(i,j)$  is  $t[i]$
  - The node having in-degree 0 : we can perform the corresponding task since  $t = 0$



# Make span schedule

- Idea to solve: BFS
  - The node having in-degree 0  $\rightarrow$  not affected by any other, but may affect some other nodes
  - We use BFS to traverse, from a node  $y$  having in-degree 0
    - Use auxiliary variable  $\text{dist}[x]$ : the first starting time of  $x$
  - After BFS all node: retrieve the node with maximal  $\text{dist}[]$





A large graphic on the left side of the slide. It features a dark blue background with a circular pattern of red dots of varying sizes, creating a sense of depth and movement. The word "HUST" is centered within this graphic in a bold, white, sans-serif font.

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# THANK YOU !