HUST

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Applied Algorithm Lab

Gold mining

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- Given n gold warehouse in a straight line
 - Warehouse i stores an amount of a_i and located at point i in the line
- Objective: Find a subset of warehouse with largest sum of amount
- Constraint: distance between 2 warehouses must be in [L1, L2]
- Output: The amount found
- Example:

Input	Output
623	19
359674	explain: 3+9+7=19



- Idea to solve #1: Backtracking and Branch and bound
 - List all ways to choose a subset of gold warehouse
 - For each case, check if 2 consecutive warehouse has distance in [L1, L2]
 - if all pair satisfy distance constraint, update the amount if needed
 - Complexity: $O(2^n * n)$.
 - Some BnB technique can be applied:
 - While considering the i warehouse, the next ware house must be in [i + L1, i + L2].
 - Apply BnB for objective function
 - still can not pass full testcases...



- Idea to solve #2: Dynamic programming: Consider choosing warehoue i
 - Let F[i] be maximal amount available if we choose some warehouses from 1 to i-1 and choose warehouse i.
 - Base case: F[i] = a[i].
 - Formula:

$$F[i] = max_{j \in [i-L2, i-L1]}(a[i] + F[j]), \forall i \in [L1, n).$$

• return:

$$max_iF[i], \forall i \in [1, n].$$

• Complexity: $O(N^2)$.



- Idea to solve #3: Dynamic programming with priority queue
 - Priority queue: a queue with order. The element are sorted in order of priority
 - Improve to idea #2:
 - An element in priority queue: (j, F[j]) with F[j] be the priority.
 - element with big F[j] will be in the front
 - Considering ware house i: add (i − L1, F[i − L1]) to the queue.
 - Remove the top element of queue if i i.top > L2.
 - F[i] = a[i] + F.top.
 - Complexity: O(n*log(n)).



- Idea to solve #2: Dynamic programming with dequeue
 - Dequeue: a combination of stack and queue -> element can be add or remove in both the back and front of dequeue
 - Operation: push_back(), push_front(), pop_back(), pop_front()
 - Improvement: Element in queue: (x, F[x]). Traverse F[i] in order.
 - Remove all element j that $F[j] \leq F[i L1]$, then add F[i L1] to the queue.
 - Delete the top element of the queue until top \geq i L2.
 - F[i] = F[top] + a[i].
 - Complexity: O(n).





THANK YOU!