

Bus-inter-city (BFS to build weighted directed graph and dijkstra)

```

int n, m;
vector<int> c, d, visited, dp;
vector<vector<int>> adj;
vector<long long> dis;
vector<vector<pair<int, int>> adj1;
void bfs(int i, int limit)
{
    fill(visited.begin(), visited.end(), 0);
    queue<pair<int, int>> q;
    visited[i] = 1;
    while (!q.empty())
    {
        int u = q.front().first;
        int depth = q.front().second;
        q.pop();
        if (u != i)
        {
            adj1[i].push_back({u, c[i]});
        }
        if (depth >= limit) continue;

        for (auto v : adj[u])
        {
            if (!visited[v])
            {
                visited[v] = 1;
                q.push({v, depth + 1});
            }
        }
    }
}
void dijkstra(int s)
{
    priority_queue<pair<long long, int>, vector<pair<long long, int>>, greater<pair<long long, int>> pq;
    dis[s] = 0;
    pq.push({0, s});

    for (int i = 0; i < n; i++)
    {
        int u = -1;

        while (!pq.empty())
        {
            u = pq.top().second;
            pq.pop();
            if (!visited[u]) break;
        }
        if (u == -1 || dis[u] == INT_MAX) break;
        visited[u] = 1;
        for (auto edge : adj1[u])
        {
            int v = edge.first;
            int w = edge.second;

            if (dis[u] + w < dis[v])
            {
                dis[v] = dis[u] + w;
                pq.push({dis[v], v});
            }
        }
    }
    int main()
    {
        cin >> n >> m;
        c.resize(n + 1, 0);
        d.resize(n + 1, 0);
        dp.resize(n + 1, 0);
        visited.resize(n + 1, 0);
        adj1.resize(n + 1, vector<pair<int>>());
        adj1.resize(n + 1, vector<pair<int, int>>());
        dis.resize(n + 1, INT_MAX);
        for (int i = 1; i <= n; i++)
        {
            cin >> c[i] >> d[i];
        }
        for (int i = 1; i <= m; i++)
        {
            int u, v;
            cin >> u >> v;
            adj1[u].push_back(v);
            adj1[v].push_back(u);
        }
        for (int i = 1; i <= n; i++)
        {
            bfs(i, d[i]);
        }
        fill(visited.begin(), visited.end(), 0);
        dijkstra(1);
        cout << dis[n] << "\n";
        return 0;
    }
}

amount.resize(n, vector<int>(X + 1, INT_MAX - 1));
for (int i = 0; i < n; i++) amount[i][0] = 0;
//base case i = 0, Money-exchange
//Knapsack inf
for (int j = 1; j <= X; j++)
{
    if ((j / d[0]) * d[0] == j)
    {
        amount[0][j] = j / d[0];
    }
}
for (int i = 1; i < n; i++)
{
    for (int j = 1; j <= X; j++)
    {
        amount[i][j] = amount[i - 1][j];
        if (j >= d[i])
        {
            amount[i][j] = min(amount[i][j],
                                amount[i][j - d[i]] + 1);
        }
    }
}
cout << (amount[n - 1][X] != INT_MAX - 1 ?
        amount[n - 1][X] : -1) << "\n";
return 0;

```

Make-span-schedule (topo sort and DP)

```

int n, m;
vector<vector<int>> adj;
vector<int> d;
vector<int> visited;
vector<int> order;
int hasCycle = 0;
int ans = 0;
vector<int> f;
void topo(int u)
{
    if (visited[u] == 2) return; // done
    if (visited[u] == 1)
    {
        hasCycle = 1;
        // cycle
        return;
    }
    visited[u] = 1;
    for (auto v : adj[u])
    {
        topo(v);
        if (hasCycle) return;
    }
    visited[u] = 2;
    order.push_back(u);
}
int main()
{
    cin >> n >> m;
    adj.resize(n + 1, vector<int>());
    num.resize(n + 1, 0);
    f.resize(n + 1, 0);
    for (int i = 1; i <= n; i++)
    {
        cin >> d[i];
    }
    adj.resize(n + 1, vector<int>());
    visited.resize(n + 1, 0);
    for (int i = 1; i <= n; i++)
    {
        int u, v;
        cin >> u >> v;
        adj[u].push_back(v);
    }
    for (int i = 1; i <= n; i++)
    {
        if (!visited[i]) topo(i);
    }
    reverse(order.begin(), order.end());
    for (auto u : order)
    {
        f[u] += d[u];
        for (auto v : adj[u])
        {
            f[v] = max(f[v], f[u]);
        }
        ans = max(ans, f[u]);
    }
    cout << ans << "\n";
    return 0;
}

```

SCC

```

int n, m;
vector<vector<int>> adj;
vector<int> num;
vector<int> low;
stack<int> SCC;
vector<int> onStack;
int current_num = 0, cnt = 0;
vector<vector<int>> res;
void dfs(int u)
{
    current_num++;
    num[u] = current_num;
    low[u] = current_num;
    SCC.push(u);
    onStack[u] = 1;
    for (auto v : adj[u])
    {
        if (num[v] == 0)
        {
            dfs(v);
            if (hasCycle) return;
        }
        else if (onStack[v] == 1)
        {
            low[u] = min(low[u], num[v]);
        }
    }
    if (low[u] == num[u])
    {
        cnt++;
        vector<int> res1;
        while (!onStack[u])
        {
            int v = SCC.top();
            SCC.pop();
            onStack[v] = false;
            res1.push_back(v);
            if (v == u) break;
        }
        sort(res1.begin(), res1.end());
        res.push_back(res1);
    }
}
int main()
{
    cin >> n >> m;
    adj.resize(n + 1, vector<int>());
    num.resize(n + 1, 0);
    low.resize(n + 1, 0);
    onStack.resize(n + 1, 0);
    for (int i = 1; i <= n; i++)
    {
        cin >> d[i];
    }
    adj.resize(n + 1, vector<int>());
    visited.resize(n + 1, 0);
    for (int i = 1; i <= n; i++)
    {
        int u, v;
        cin >> u >> v;
        adj[u].push_back(v);
    }
    for (int i = 1; i <= n; i++)
    {
        if (!visited[i]) dfs(i);
    }
    reverse(order.begin(), order.end());
    for (auto u : order)
    {
        int v;
        if (u == edge.first)
        {
            v = edge.second;
        }
        else if (u == edge.second)
        {
            v = edge.first;
        }
        else if (u == edge.first || u == edge.second)
        {
            v = edge.first;
        }
        else
        {
            v = edge.second;
        }
        if (v == u) break;
    }
    cout << ans << "\n";
    return 0;
}

```

Hungary

```

const long long INF = 1e18; // Giá trị vô cùng lớn cho long long
int n, m, k, sz;
vector<vector<long long>> a; // Ma trận chỉ phái (dãy đầu)
vector<long long> u, v, minv;
vector<int> p, way; // p: hung matching, way: mang truy vết
int main()
{
    if (!!(cin >> n >> m >> k)) return 0;

    sz = max(n, m);
    a.assign(sz + 1, vector<long long>(sz + 1, 0));
    for (int i = 0; i < k; i++)
    {
        int x, y, w;
        cin >> x >> y >> w;
        if (a[x][y] == 0) a[x][y] = -w;
        else a[x][y] = min(a[x][y], -(long long)w);
    }

    u.assign(sz + 1, 0);
    v.assign(sz + 1, 0);
    p.assign(sz + 1, 0);
    way.assign(sz + 1, 0);
    for (int i = 1; i <= sz; i++) cout << " " << i << endl;
    p[0] = 1;
    int j0 = 0;
    minv.assign(sz + 1, INF);
    vector<bool> used(sz + 1, false);

    do
    {
        used[j0] = true;
        int i0 = p[j0];
        long long delta = INF;
        int j1;
        for (int j = 1; j <= sz; j++)
        {
            if (!used[j])
            {
                if (v == u)
                {
                    sort(res.begin(), res.end());
                    res.push_back(res1);
                    cout << endl;
                    break;
                }
            }
        }
        if (i0 == j0) break;
        int v = a[i0][j0] - u[i0] - v[j0];
        if (v < minv[j0])
        {
            minv[j0] = v;
            way[j0] = j0;
        }
        if (minv[j0] < delta)
        {
            delta = minv[j0];
            j1 = j0;
        }
    }
    while (j1 != j0);
    cout << endl;
    cout << way[0] << endl;
    return 0;
}

```

Edmond-karp (max flow)

```

int n, m;
vector<vector<int>> capacity;
vector<vector<int>> adj;
int bfs(int source, int sink, vector<int>& parent)
{
    fill(parent.begin(), parent.end(), -1);
    parent[source] = source;
    queue<pair<int, int>> q;
    q.push({source, INT_MAX});
    while (!q.empty())
    {
        int u = q.front().first;
        int flow = q.front().second;
        q.pop();
        for (int v : adj[u])
        {
            if (parent[v] == -1 && capacity[u][v] > 0)
            {
                parent[v] = u;
                int new_flow = min(flow, capacity[u][v]);
                q.push({v, new_flow});
            }
        }
    }
    return 0;
}
int edmond_karp(int source, int sink)
{
    int max_flow = 0;
    vector<int> parent(n + 1);
    int new_flow;
    while ((new_flow = bfs(source, sink, parent)) > 0)
    {
        max_flow += new_flow;
        int cur = sink;
        while (cur != source)
        {
            int prev = parent[cur];
            capacity[prev][cur] -= new_flow;
            capacity[cur][prev] += new_flow;
            cur = prev;
        }
    }
    return max_flow;
}
int main()
{
    cin >> n >> m;
    capacity.resize(n + 1, vector<int>(n + 1, 0));
    adj.resize(n + 1);
    for (int i = 1; i <= m; i++)
    {
        int u, v, c;
        cin >> u >> v >> c;
        capacity[u][v] += c;
        adj[u].push_back(v);
        adj[v].push_back(u);
    }
    int source, sink;
    cin >> source >> sink;
    cout << edmond_karp(source, sink) << "\n";
    return 0;
}

```

Max-matching-bipartite

```

int n, m;
vector<vector<int>> adj;
// adj[task] = list of staffs
// that can do this task
vector<int> matchTask;
// matchTask[staff] = task
// assigned to this staff (0 if none)
vector<bool> visited;
// Kuhn's algorithm
// (DFS to find augmenting path)
bool dfs(int task)
{
    for (int staff : adj[task])
    {
        if (visited[staff]) continue;
        visited[staff] = true;
        // If staff is free or we can
        // reassign their current task
        if (matchTask[staff] == 0 ||
            !dfs(matchTask[staff]))
        {
            matchTask[staff] = task;
            return true;
        }
    }
    return false;
}
int main()
{
    cin >> n >> m;
    adj.resize(n + 1);
    matchTask.resize(m + 1, 0);
    for (int i = 1; i <= n; i++)
    {
        int k;
        cin >> k;
        for (int j = 0; j < k; j++)
        {
            int staff;
            cin >> staff;
            adj[i].push_back(staff);
        }
    }
    for (int i = 1; i <= n; i++)
    {
        if (dfs(i))
        {
            cout << i << " ";
        }
    }
    cout << endl;
    return 0;
}

```

Total-path-lengths

```

int n;
vector<vector<pair<int, int>>> a(MAX + 1);
vector<int> subtree_size(MAX + 1, 1);
vector<int> visited(MAX + 1, 0);
vector<long long> answer(MAX + 1, 0);

void dfs(int u, int depth)
{
    visited[u] = 1;
    answer[1] += depth;
    for (auto path : a[u])
    {
        int v = path.first;
        int w = path.second;
        if (visited[v] == 0)
        {
            dfs(v, depth + subtree_size[v] * w); // or +1
            subtree_size[u] += subtree_size[v];
        }
    }
}

void dfs2(int u)
{
    visited[u] = 1;
    for (auto path : a[u])
    {
        int v = path.first;
        int w = path.second;
        if (visited[v] == 0)
        {
            // Cân tính answer[v] TRUE khi gọi đệ quy xuống v
            answer[v] = answer[u] - w * subtree_size[v] * w; // 1 : weight
            dfs2(v);
        }
    }
}

int main()
{
    cin >> n;
    for (int i = 1; i < n; i++)
    {
        int u, v, w;
        cin >> u >> v >> w;
        a[u].push_back(make_pair(v, w));
        a[v].push_back(make_pair(u, w));
    }
    bfs(1);
    int Max = 0;
    int start = 1;
    for (int i = 1; i <= n; i++)
    {
        if (Max < distances[i])
        {
            Max = distances[i];
            start = i;
        }
    }
    distances[i] = 0;
    visited[i] = 0;
    bfs(start);
    Max = 0;
    for (int i = 1; i <= n; i++)
    {
        if (Max < distances[i])
        {
            Max = distances[i];
        }
    }
    cout << Max << "\n";
    return 0;
}

```