Design of the HiRTOS Multi-core Real-Time Operating System

Germán Rivera jgrivera67@gmail.com

June 3, 2024

Contents

| 1 | Intr | oduct | ion | 1 | | | | | | | | | |
|---|---------------------------------|--------------------------|---|----|--|--|--|--|--|--|--|--|--|
| 2 | HiRTOS Overview 3 | | | | | | | | | | | | |
| | 2.1 RTOS Major Design Decisions | | | | | | | | | | | | |
| | 2.2 | | ation Kernel Major Design Decisions | 4 | | | | | | | | | |
| | 2.3 | | | | | | | | | | | | |
| 3 | HiR | TOS 2 | Z Specification | 9 | | | | | | | | | |
| | 3.1 HiRTOS Data Structures | | | | | | | | | | | | |
| | | 3.1.1 | Z Naming Conventions | 9 | | | | | | | | | |
| | | 3.1.2 | HiRTOS Configuration Parameters | 9 | | | | | | | | | |
| | | 3.1.3 | HiRTOS Target Platform Parameters | 10 | | | | | | | | | |
| | | 3.1.4 | HiRTOS Primitive Types | 10 | | | | | | | | | |
| | | 3.1.5 | HiRTOS Axiomatic Definitions | 12 | | | | | | | | | |
| | | 3.1.6 | HiRTOS State Variables | 12 | | | | | | | | | |
| | 3.2 | HiRT | OS Boot-time Initialization | 18 | | | | | | | | | |
| | 3.3 | HiRTOS Callable Services | | | | | | | | | | | |
| | | 3.3.1 | HiRTOS Threads Operations | 21 | | | | | | | | | |
| | | 3.3.2 | HiRTOS Mutex Operations | 22 | | | | | | | | | |
| | | 3.3.3 | HiRTOS Condition Variable Operations | 26 | | | | | | | | | |
| | | 3.3.4 | HiRTOS Software Timer Operations | 29 | | | | | | | | | |
| | 3.4 | HiRT | OS Thread Context Switching | 32 | | | | | | | | | |
| | | 3.4.1 | Asynchronous Thread Context Switch | 32 | | | | | | | | | |
| | | 3.4.2 | Synchronous Thread Context Switch | 34 | | | | | | | | | |
| | | 3.4.3 | TLA+/PlusCal Model of the HiRTOS Thread Scheduler | 36 | | | | | | | | | |
| 4 | HiR | TOS S | Separation Kernel Z Specification | 41 | | | | | | | | | |
| | 4.1 | Separa | ation Kernel Data Structures | 41 | | | | | | | | | |
| | | 4.1.1 | Separation Kernel Configuration Parameters | 41 | | | | | | | | | |
| | | 4.1.2 | Separation Kernel Primitive Types | 41 | | | | | | | | | |
| | | 4.1.3 | Separation Kernel State Variables | 42 | | | | | | | | | |
| | | 4.1.4 | Separation Kernel Boot-time Initialization | 44 | | | | | | | | | |
| | 4.2 | Separa | ation Kernel Callable Services | 45 | | | | | | | | | |

| 4.2.1 | Partition | Operations | | | | | | | | | | | | | | | | | | | | | | | | 4 | 5 |
|-------|-----------|------------|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|---|---|
|-------|-----------|------------|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|---|---|

Chapter 1

Introduction

This document describes the design of HiRTOS ("High Integrity" RTOS), a real-time operating system kernel (RTOS) written in SPARK Ada. HiRTOS targets safety-critical and security-sensitive embedded software applications that run in small multi-core microcontrollers. HiRTOS was designed using the Z notation, as a methodical way to capture correctness properties that can be expressed as programming contracts in SPARK Ada. Z is a software modeling notation based on discrete mathematics structures (such as sets, relations and functions) and predicate logic.

Although there are several popular RTOSes for embedded applications that run on small multi-core microcontrollers, most of them are not designed with high-integrity applications in mind, and are typically written in C, a notoriously unsafe language. So, it would be desirable to have an RTOS specifically designed for high-integrity applications, and written in a safer language, like Ada or its subset SPARK Ada, even if application code is written in C/C++. Modern versions of the Ada and SPARK languages have programming-by-contract constructs built-in in the language, which allows the programmer to express correctness properties, such as preconditions, postconditions, object state invariants and loop invariants, as code. However, one challenge when doing programming-by-contract is to be aware of all the correctness conditions that can be asserted in programming contracts. Describing software design in a formal notation, such as the Z notation [1, 2, 3], can help identify/elicit such correctness conditions in a more thorough and methodical way than just writing code.

Z is a software modeling notation based on discrete mathematics structures (such as sets, relations and functions) and predicate logic. With Z, data structures can be specified in terms of mathematical structures and their state invariants can be specified using mathematical predicates. The pre-conditions and post-conditions of the operations that manipulate the data structures can also be specified using predicates. Using Z for this purpose encourages a rigorous and methodical thought process to elicit correctness properties, in a systematic way. The *HiRTOS* Z model described here was checked with the **fuzz** tool [4], a Z type-checker, that catches Z type mismatches in predicates.

The code of HiRTOS is written in SPARK Ada [5], a high integrity subset of

the Ada programming language. The code of HiRTOS is available in GitHub at https://github.com/jgrivera67/HiRTOS. HiRTOS data types were modeled in Z at a level of abstraction that can be mapped directly to corresponding data types in SPARK Ada. This guided design decisions at the code level, resulting in a completely pointer-less implementation, that leverages the various Ada mechanisms to avoid having to use pointers.

Also, the HiRTOS thread scheduler was modeled in TLA+/PlusCal [15, 16] and the hiRTOS TLA+ model was verified using the TLC model checker [17].

Chapter 2

HiRTOS Overview

2.1 RTOS Major Design Decisions

- For API simplicity, mutexes and condition variables [7, 8] are the only synchronization primitives in *HiRTOS*, similar to the thread synchronization primitives of the C11 standard library [9]. Other synchronization primitives such as semaphores, event flags and message queues can be implemented on top of mutexes and condition variables.
- Unlike C11 mutexes, *HiRTOS* mutexes can change the priority of the thread owning the mutex. *HiRTOS* mutexes support both priority inheritance and priority ceiling [10].
- Unlike C11 condition variables, *HiRTOS* condition variables can also be waited on while having interrupts disabled, not just while holding a mutex. This prevents missing "thread wakeups", when signaling condition variables from interrupt service routines (ISRs), making it unnecessary to use semaphores for this purpose.
- *HiRTOS* atomic levels can be used to disable the thread scheduler or to disable interrupts at and below a given priority or to disable all interrupts.
- In a multi-core platform, there is one *HiRTOS* instance per CPU Core. Each *HiRTOS* instance is independent of each other. No resources are shared between *HiRTOS* instances. No communication/synchronization between CPU cores is supported by the current version of *HiRTOS*. If an application needs intercore communication, that would need to be provided outside of *HiRTOS*, using doorbell interrupts and mailboxes or shared memory, for example.
- Threads are bound to the CPU core in which they were created, for the lifetime of the thread. That is, no thread migration between CPU cores is supported.

- All RTOS objects such as threads, mutexes and condition variables are allocated internally by *HiRTOS* from statically allocated internal object pools. These object pools are just RTOS-private global arrays of the corresponding RTOS object types, sized at compile time via configuration parameters, whose values are application-specific. RTOS object handles provided to application code are just indices into these internal object arrays. No actual RTOS object pointers exposed to application code. No dynamic allocation/deallocation of RTOS objects is supported and no static allocation of RTOS objects in memory owned by application code is supported either. All this prevents HiRTOS internal state from being accidentally or intentionally corrupted from application code. RTOS objects can only be manipulated through the HiRTOS APIs.
- All application threads run in unprivileged mode by default. In unprivileged mode, a thread can only access its own stack. To access global variables or MMIO space, application threads must explicitly request either read-only or read-write permission to *HiRTOS* via a system call.
- ISRs are seen as hardware-scheduled threads that have higher priority than all software-scheduled threads. They can only be preempted by higher-priority ISRs. They cannot block waiting on mutexes or condition variables.

2.2 Separation Kernel Major Design Decisions

Besides being a fully functional RTOS, HiRTOS can be used as a separation kernel [11, 12]. A separation kernel can be seen as an RTOS that schedules partitions instead of threads. A partition is a spatial and temporal separation/isolation unit on which a bare-metal or RTOS-based firmware binary runs. A separation kernel requires that the target CPU supports hypervisor privilege mode and two-stage memory protection.

- In a multi-core platform, there is one separation kernel instance per CPU Core. Each instance is independent of each other. No resources are shared between separation kernel instances. No communication between CPU cores is supported yet. If needed by the application, inter-core communication would need to be provided outside of the HiRTOS separation kernel, using doorbell interrupts and mailboxes or shared memory, for example.
- Each separation-kernel instance consists of one or more partitions. A partition is a spatial and temporal separation/isolation unit on which a bare-metal or RTOS-based firmware binary runs. Each partition consists of one or more disjoint address ranges covering portions of RAM and MMIO space that only that partition can access. Isolation is enforced by a hypervisor-level memory protection unit (MPU). Also, each partition has its own interrupt vector table and its own set of physical interrupts. So, physical peripherals can be assigned to individual partitions (discrete device assignment). However, no device or

memory virtualisation is supported, as the target machine for the HiRTOS separation kernel is not required to have neither an MMU nor an IOMMU. The CPU core is time-sliced among the partitions running on the same separation kernel instance.

- Partitions are bound to the CPU core in which they were created. That is, no partition migration between CPU cores is supported.
- Partitions are created at boot time before starting the partition scheduler on the corresponding CPU core. Partitions cannot be destroyed or terminated.
- The separation kernel code itself runs in hypervisor privilege mode. All partitions run at a privilege lower than hypervisor mode. Partitions can communicate with the separation kernel via hypervisor calls and via traps to hypervisor mode triggered from special machine instructions such as WFI. The separation kernel can communicate with partitions, by forwarding interrupts targeted to the corresponding partition.

2.3 HiRTOS Code Architecture

To have wider adoption of an RTOS written in bare-metal Ada, providing a C/C++ programming interface is a must. Indeed, multiple interfaces or "skins" can be provided to mimic widely popular RTOSes such as FreeRTOS [13] and RTOS interfaces such as the CMSIS RTOS2 API [14]. As shown on figure 2.1, HiRTOS has a C/C++ interface layer that provides a FreeRTOS skin and and a CMSIS RTOS2 skin. Both skins are implemented on top of a native C skin. The native C skin is just a thin C wrapper that consists of a C header file containing the C functions prototypes of the corresponding Ada subprograms of the SPARK Ada native interface of HiRTOS.

In addition to the Ada native and C/C++ interfaces, HiRTOS could also provide an Ada runtime library (RTS) skin, as shown on figure 2.2, so that baremetal Ada applications that use Ada tasking features can run on top of HiRTOS. This can be especially useful, given the limited number of microcontroller platforms for which an available bare-metal Ada runtime library is provided with the GNAT Ada compiler.

HiRTOS has been architected to be easily portable to any single-core or multi-core microcontroller or bare metal platform for which a GNAT Ada cross compiler is available. All platform-dependent code is isolated in the HiRTOS porting layer, which provides platform-independent interfaces to the rest of the HiRTOS code. To avoid any dependency on a platform-specific bare-metal Ada runtime library, provided by the compiler, HiRTOS sits on top of a platform-independent portable minimal Ada runtime library. Currently, two porting layers have been implemented: one for the ARM Cortex-R52 multi-core processor, and the other for the RISCV-based ESP32-C3 microcontroller. To port HiRTOS to a new target platform, the platform-specific components of the porting layer would need to be implemented for the new platform.

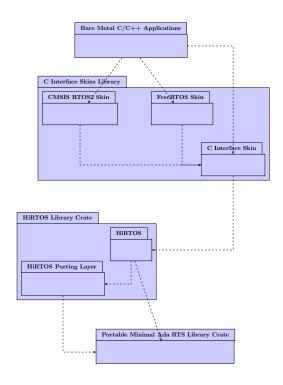


Figure 2.1: HiRTOS Code Architecture for $\mathrm{C/C}++$ Applications

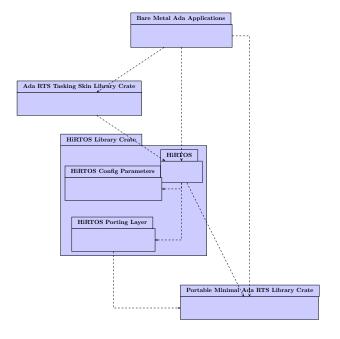


Figure 2.2: HiRTOS Code Architecture for Ada Applications

Figure 2.3 shows the major code components of HiRTOS. The HiRTOS code base is structured in three conceptual layers. The *HiRTOS API* layer, the *HiRTOS internals layer* and the *HiRTOS porting layer*.

The HiRTOS API layer contains the HiRTOS public interface components. The HiRTOS_Interrupt_Handling Ada package contains the services to be invoked from top-level interrupt handlers to notify HiRTOS of entering an exiting interrupt context. HiRTOS_Memory_Protection contains the services to protect ranges of memory and MMIO space. HiRTOS_Thread contains the services to create and manage threads.

The HiRTOS internals layer contains HiRTOS-private components that are hardware-independent.

The *HiRTOS porting layer* contains hardware-dependent components that provide hardware-independent interfaces to upper HiRTOS layers.

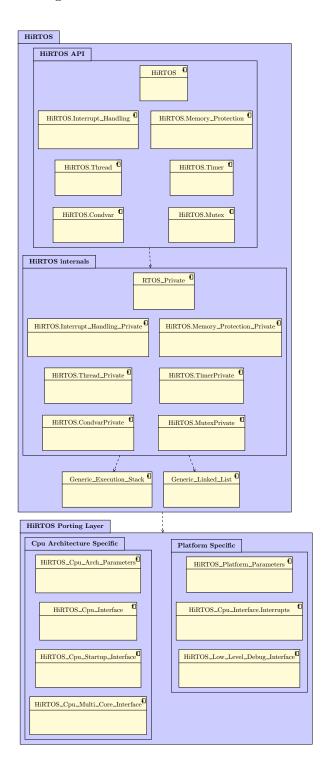


Figure 2.3: HiRTOS Code Components

Chapter 3

HiRTOS Z Specification

3.1 HiRTOS Data Structures

3.1.1 Z Naming Conventions

The following naming conventions are used in the Z model of HiRTOS:

- Z Primitive types are in uppercase.
- Z Composite types (schema types) start with uppercase.
- Z constants and variables start with lower case.
- \bullet Identifiers that start with the z prefix are meant to be modeling-only entities that do not physically correspond to code-level entities.

3.1.2 HiRTOS Configuration Parameters

Constants defined here represent compile-time configuration parameters for *HiRTOS*.

```
maxNumThreads: \mathbb{N}_1
maxNumMutexes: \mathbb{N}_1
maxNumCondvars: \mathbb{N}_1
maxNumTimers: \mathbb{N}_1
numThreadPriorities: \mathbb{N}_1
numTimerWheelSpokes: \mathbb{N}_1
maxNumThreads > 2
maxNumCondvars \geq maxNumThreads
maxNumTimers \geq maxNumThreads
```

The minimum number of threads that can be configured per CPU core is 2, which corresponds to the HiRTOS pre-defined threads: the idle thread and the tick timer

thread. Each thread has a built in timer, so the minimum number of timers that can be configured is maxNumThreads. Also, each thread has a built in condition variable, so the minimum number of condition variables that can be configured is maxNumThreads as well.

3.1.3 HiRTOS Target Platform Parameters

Constants defined here represent compile-time target platform parameters for HiR-TOS.

```
numCpus: \mathbb{N}_1

minMemoryAddress: \mathbb{N}

maxMemoryAddress: \mathbb{N}_1

numInterruptPriorities: \mathbb{N}_1

maxNumInterrupts: \mathbb{N}_1

minMemoryAddress < maxMemoryAddress
```

3.1.4 *HiRTOS* Primitive Types

Below are the primitive types used in HiRTOS:

```
[CpuIdType] \\ \#CpuIdType = numCpus + 1 \\ [ThreadIdType] \\ \#ThreadIdType] \\ \#ThreadIdType = maxNumThreads + 1 \\ [MutexIdType] \\ \#MutexIdType = maxNumMutexes + 1 \\ [CondvarIdType] \\ \#CondvarIdType = maxNumCondvars + 1 \\ [TimerIdType] \\ \#TimerIdType = maxNumTimers + 1 \\ [InterruptIdType] \\ \#InterruptIdType = maxNumInterrupts + 1 \\ [Maximum Timers + 1] \\ [Maximum Tim
```

invalidCpuId: CpuIdType
invalidThreadId: ThreadIdType
invalidMutexId: MutexIdType
invalidCondvarId: CondvarIdType
invalidTimerId: TimerIdType
invalidInterruptId: InterruptIdType

```
[CpuRegistersType]
ValidCpuIdType == CpuIdType \setminus \{invalidCpuId\}
MemoryAddressType ==
    minMemoryAddress . . maxMemoryAddress
nullAddress == 0
ValidThreadIdType ==
    ThreadIdType \setminus \{invalidThreadId\}
ValidMutexIdType == MutexIdType \setminus \{invalidMutexId\}
ValidCondvarIdType ==
    CondvarIdType \setminus \{invalidCondvarId\}
ValidTimerIdType == TimerIdType \setminus \{invalidTimerId\}
ValidInterruptIdType ==
    InterruptIdType \setminus \{invalidInterruptId\}
ThreadPriorityType == 0 ... numThreadPriorities
invalidThreadPriority == numThreadPriorities
ValidThreadPriorityType ==
    ThreadPriorityType \setminus \{invalidThreadPriority\}
InterruptPriorityType == 0..numInterruptPriorities
invalidInterruptPriority == numInterruptPriorities
ValidInterruptPriorityType ==
    InterruptPriorityType \setminus \{invalidInterruptPriority\}
AtomicLevelType == 0 ... numInterruptPriorities + 1
atomicLevelNoInterrupts == min AtomicLevelType
atomicLevelSingleThread == max\ AtomicLevelType - 1
atomicLevelNone == max AtomicLevelType
InterruptNestingCounterType ==
    0...num Interrupt Priorities
ActiveInterruptNestingCounterType ==
    InterruptNestingCounterType \setminus \{0\}
CpuInterruptMaskingStateType ::=
    cpuInterruptsEnabled |
    cpuInterruptsDisabled
CpuPrivilegeType ::= cpuPrivileged \mid cpuUnprivileged
MemoryProtectionStateType ::=
    memoryProtectionOn \mid memoryProtectionOff
CpuExecutionModeType ::=
    cpuExecutingResetHandler
    cpuExecutingInterruptHandler |
    cpuExecutingThread
ThreadStateType ::= threadNotCreated \mid threadSuspended \mid
                       threadRunnable \mid threadRunning \mid
                       threadBlockedOnCondvar \mid threadBlockedOnMutex
ThreadSchedulerStateType ::=
    threadSchedulerStopped \mid threadSchedulerRunning
```

```
ThreadQueueType == iseq\ ValidThreadIdType
MutexListType == iseq\ ValidMutexIdType
TimerWheelSpokeIndexType == \\ 0..numTimerWheelSpokes
invalidTimerWheelSpokeIndex == \\ max\ TimerWheelSpokeIndexType
ValidTimerWheelSpokeIndexType == \\ TimerWheelSpokeIndexType \setminus \\ \{invalidTimerWheelSpokeIndex\}
TimerKindType ::= periodicTimer\ |\ oneShotTimer
TimerStateType ::= timerStopped\ |\ timerRunning
```

For interrupts, lower priority values represent higher priorities. For threads, lower priority values represent lower priorities.

3.1.5 *HiRTOS* Axiomatic Definitions

```
zAddressRange: \\ (MemoryAddressType \times MemoryAddressType) \mapsto \\ \mathbb{F}_1 \ MemoryAddressType \\ \forall x,y: MemoryAddressType \mid \\ (x,y) \in \operatorname{dom} zAddressRange \bullet \\ x < y \wedge zAddressRange(x,y) = x \dots y \\ \\ zCpuToISRstackAddressRange: \\ ValidCpuIdType \mapsto \\ (MemoryAddressType \times MemoryAddressType) \\ \hline \bigcap \{i: ValidCpuIdType \bullet \\ zAddressRange(zCpuToISRstackAddressRange(i))\} = \emptyset \\ \forall i: \operatorname{dom} zCpuToISRstackAddressRange \bullet \\ \#(zAddressRange(zCpuToISRstackAddressRange(i))) \geq 2 \\ \\ interruptPriorities: \\ InterruptIdType \rightarrow InterruptPriorityType \\ \\ \end{cases}
```

3.1.6 *HiRTOS* State Variables

The *HiRtos* schema represents the multi-core RTOS state variables (internal data structures). All HiRTOS objects such as threads, mutexes, condition variables and software timers are statically allocated internally by HiRTOS.

```
HiRtos\_
rtos Cpu Instances:
      ValidCpuIdType \rightarrow HiRtosCpuInstanceType
zAllCreatedThreadInstances: \mathbb{F}\ ThreadType
\#rtosCpuInstances \ge 1
\forall i : dom \ rtosCpuInstances \bullet
      (rtosCpuInstances(i)).cpuId = i
zAllCreatedThreadInstances =
     \bigcup \{ i : ValidCpuIdType \bullet \}
           ran(rtosCpuInstances(i)).threads
\bigcap \{ i : ValidCpuIdType \bullet \}
      ran(rtosCpuInstances(i)).threads \} = \emptyset
\bigcap \{ thread : zAllCreatedThreadInstances \bullet \}
      zAddressRange(thread.stack)\} = \emptyset
\bigcap \{ i : ValidCpuIdType \bullet \}
     ran(rtosCpuInstances(i)).mutexes \} = \emptyset
\bigcap \{ i : ValidCpuIdType \bullet \}
     ran(rtosCpuInstances(i)).condvars \} = \emptyset
\bigcap \{ i : ValidCpuIdType \bullet \}
     ran(rtosCpuInstances(i)).timers \} = \emptyset
\bigcap \{t : zAllCreatedThreadInstances \bullet zAddressRange(t.stack)\} = \emptyset
```

Per-CPU HiRTOS Instance

The state variables and internal data structures of each per-CPU ${\it HiRTOS}$ instance are described below:

```
. HiRtosCpuInstanceType .
cpuId: CpuIdType
currentCpuContext: CpuRegistersType
threadSchedulerState: ThreadSchedulerStateType
currentAtomicLevel: AtomicLevelType
currentCpuExecutionMode: CpuExecutionModeType
currentThreadId: ThreadIdType
timerTicksSinceBoot: \mathbb{N}
idle Thread Id: Valid Thread Id Type
tickTimerThreadId: ValidThreadIdType
interruptNestingLevelStack:InterruptNestingLevelStackType
threads: ValidThreadIdType \implies ThreadType
mutexes: ValidMutexIdType > MutexType
condvars: ValidCondvarIdType \implies CondvarType
timers: ValidTimerIdType \rightarrowtail TimerType
runnable Threads Queue: Thread Priority Queue Type
timerWheel: TimerWheelType
zCpuInterruptMaskingState:CpuInterruptMaskingStateType
zCpuPrivilege: CpuPrivilegeType
zMemoryProtectionState: MemoryProtectionStateType
\{ idleThreadId, tickTimerThreadId \} \subseteq dom threads
tickTimerThreadId \neq idleThreadId
threadSchedulerState = threadSchedulerRunning \Rightarrow
(\forall threadId : (dom threads \setminus \{ currentThreadId \}) \bullet
     (threads(threadId)).currentPriority \leq (threads(currentThreadId)).currentPriority)
zCpuInterruptMaskingState = cpuInterruptsEnabled \Leftrightarrow
     currentAtomicLevel > atomicLevelNoInterrupts
zCpuInterruptMaskingState = cpuInterruptsDisabled \Rightarrow zCpuPrivilege = cpuPrivileged
currentAtomicLevel < atomicLevelNone \Rightarrow zCpuPrivilege = cpuPrivileged
\bigcap \{ t : \operatorname{ran} threads \bullet \{ t.builtinCondvarId \} \} = \emptyset
\bigcap \{ t : \text{ran } threads \bullet \{ t.builtinTimerId \} \} = \emptyset
\forall t : \text{ran } threads \bullet (t.id = (threads^{\sim})(t) \land
(t.ownedMutexes \neq \emptyset \Rightarrow
t.currentPriority = max \{ m : ran \ t.ownedMutexes \bullet (mutexes(m)).ceilingPriority \}) \}
\forall m : \text{ran } mutexes \bullet m.id = mutexes^{\sim}(m)
\forall c : \text{ran } condvars \bullet c.id = condvars^{\sim}(c)
\forall ti : ran \ timers \bullet \ ti.id = timers^{\sim}(ti)
\forall p : ValidThreadPriorityType \bullet
     \forall threadId : ran(runnableThreadsQueue.threadQueues(p)) \bullet
```

(threads(threadId)).currentPriority = p

```
ThreadPriorityQueueType\_
thread Queues:
     ValidThreadPriorityType \rightarrow ThreadQueueType
waiting Threads Count : \mathbb{N}
waiting Threads Count =
\#(\bigcup \{p : ValidThreadPriorityType \bullet threadQueues(p)\})
InterruptNestingLevelStackType \_
interrupt Nesting Levels:
     ActiveInterruptNestingCounterType \rightarrow
     InterruptNestingLevelType
currentInterruptNestingCounter:
     InterruptNestingCounterType
zCpuId:ValidCpuIdType
\forall x : dom interruptNestingLevels \bullet
     (interruptNestingLevels(x)).interruptNestingCounter = x
     (interruptNestingLevels(x)).savedStackPointer \in
     zAddressRange(zCpuToISRstackAddressRange(zCpuId))
dom interruptNestingLevels =
1... current Interrupt Nesting Counter
InterruptNestingLevelType \_
interruptId: InterruptIdType
interruptNestingCounter: ActiveInterruptNestingCounterType
savedStackPointer: MemoryAddressType
atomicLevel: AtomicLevelType
atomicLevel \leq interruptPriorities(interruptId)
TimerWheelType_{-}
wheel Spokes Hash Table:\\
     ValidTimerWheelSpokeIndexType \rightarrow \mathbb{F}\ ValidTimerIdType
current Wheel Spoke Index: Valid Timer Wheel Spoke Index Type
\forall i, j : ValidTimerWheelSpokeIndexType \mid i \neq j \bullet
     wheelSpokesHashTable(i) \cap wheelSpokesHashTable(j) = \emptyset
```

 $.\ TimerType$ $_$

id: Timer IdType

timerKind: TimerKindType timerState: TimerStateType $timerWheelRevolutions: \mathbb{N}$ $timerWheelRevolutionsLeft: \mathbb{N}$

 $expiration Callback Addr: Memory Address Type \\ wheel Spoke Index: Timer Wheel Spoke Index Type$

 $timerWheelRevolutionsLeft \leq timerWheelRevolutions$

 $timerState = timerRunning \Rightarrow expirationCallbackAddr \neq nullAddress$

```
Thread Type _
id: ThreadIdType
state: ThreadStateType
current Priority: Thread Priority Type
basePriority: ThreadPriorityType
atomicLevel: AtomicLevelType
builtinTimerId: TimerIdType
builtin Condvar Id: Condvar Id Type
waiting On Condvar Id: Condvar Id Type
waiting OnMutexId: MutexIdType
ownedMutexes : iseq ValidMutexIdType
savedStackPointer: MemoryAddressType
stack: AddressRangeType
stack Saved Cpu Context: Cpu Registers Type \\
privilegedNestingCounter : \mathbb{N}
timeSliceLeftUs: \mathbb{N}
state \neq threadNotCreated \Rightarrow
     (id \neq invalidThreadId \land
     builtinTimerId \neq invalidTimerId \land
     builtinCondvarId \neq invalidCondvarId \land
     basePriority \neq invalidThreadPriority \land
     currentPriority \neq invalidThreadPriority \land
     savedStackPointer \in zAddressRange(stack))
currentPriority \geq basePriority
state = threadBlockedOnCondvar \Leftrightarrow
     waitingOnCondvarId \neq invalidCondvarId
state = threadBlockedOnMutex \Leftrightarrow
     waitingOnMutexId \neq invalidMutexId
waitingOnCondvarId \neq invalidCondvarId \Rightarrow
     waitingOnMutexId = invalidMutexId
waitingOnMutexId \neq invalidMutexId \Rightarrow
     waitingOnCondvarId = invalidCondvarId
waitingOnMutexId \notin ran\ ownedMutexes
```

```
\begin{tabular}{l} CondvarType & & \\ id: CondvarIdType \\ wakeupAtomicLevel: AtomicLevelType \\ wakeupMutexId: MutexIdType \\ waitingThreadsQueue: ThreadPriorityQueueType \\ \hline \\ wakeupAtomicLevel \neq atomicLevelNone \Rightarrow wakeupMutexId = invalidMutexId \\ \hline \end{tabular}
```

```
 \begin{aligned} &MutexType \\ &id: MutexIdType \\ &ownerThreadId: ThreadIdType \\ &recursiveCount: \mathbb{N} \\ &ceilingPriority: ThreadPriorityType \\ &waitingThreadsQueue: ThreadPriorityQueueType \\ \end{aligned} \\ &waitingThreadsQueue.waitingThreadsCount \neq 0 \Rightarrow \\ &ownerThreadId \neq invalidThreadId \\ &ceilingPriority \neq invalidThreadPriority \Rightarrow \\ &(\forall p: ValidThreadPriorityType \mid \\ &waitingThreadsQueue.threadQueues(p) \neq \emptyset \bullet \\ &p \leq ceilingPriority) \end{aligned}
```

3.2 HiRTOS Boot-time Initialization

When HiRTOS. Initialize is called for each CPU core, the idle thread and the tick timer thread for that CPU are created, but the thread scheduler is not started yet:

```
HiRtosInitialize HiRtos'
HiRtosCpuInstanceInitialize
cpuId?: CpuIdType
cpuId' = cpuId?
\theta HiRtosCpuInstanceType' = rtosCpuInstances'(cpuId?)
interruptNestingLevelStack'.zCpuId = cpuId?
```

```
HiRtosCpuInstanceInitialize \ \_
HiRtosCpuInstanceElaboration
idleThreadId' \neq invalidThreadId
tickTimerThreadId' \neq invalidThreadId
tickTimerThreadId' \neq idleThreadId'
dom threads' = \{ idleThreadId', tickTimerThreadId' \}
dom\ condvars' =
\{(threads'(idleThreadId')).builtinCondvarId,
(threads'(tickTimerThreadId')).builtinCondvarId }
dom timers' =
\{(threads'(idleThreadId')).builtinTimerId,
(threads'(tickTimerThreadId')).builtinTimerId }
zCpuInterruptMaskingState' = cpuInterruptsEnabled
zCpuPrivilege' = cpuUnprivileged
zMemoryProtectionState' = memoryProtectionOn
runnable Threads Queue'. thread Queues (min Valid Thread Priority Type)
    = \langle idleThreadId' \rangle
runnable Threads Queue'. thread Queues (max Valid Thread Priority Type)
     = \langle tickTimerThreadId' \rangle
\forall p : ValidThreadPriorityType \setminus
         \{ min\ ValidThreadPriorityType, max\ ValidThreadPriorityType \} \bullet 
     runnable Threads Queue'.thread Queues(p) = \emptyset
```

```
HiRtosCpuInstanceElaboration \_
HiRtosCpuInstanceType'
Interrupt Nesting Level Stack Elaboration \\
threadSchedulerState' = threadSchedulerStopped
current Thread Id' = invalid Thread Id
currentAtomicLevel' = atomicLevelNone
currentCpuExecutionMode' = cpuExecutingResetHandler
idleThreadId' = invalidThreadId
tickTimerThreadId' = invalidThreadId
threads' = \emptyset
condvars' = \emptyset
timers' = \emptyset
timerTicksSinceBoot' = 0
InterruptNestingLevelStackElaboration _
InterruptNestingLevelStackType'
InterruptNestingLevelElaboration
currentInterruptNestingCounter' = 1
\forall x : ActiveInterruptNestingCounterType \bullet
     interruptNestingLevels'(x) = \theta InterruptNestingLevelType'
InterruptNestingLevelElaboration
InterruptNestingLevelType'
interruptId' = invalidInterruptId
interruptNestingCounter' = 0
```

savedStackPointer' = nullAddress

atomicLevel' = atomicLevelNone

```
TimerWheelElaboration TimerWheelType' ran wheelSpokesHashTable' = { \emptyset } currentWheelSpokeIndex' = min ValidTimerWheelSpokeIndexType
```

3.3 HiRTOS Callable Services

3.3.1 HiRTOS Threads Operations

Create a new thread

A thread can be created by calling HiRTOS.Thread.Create_Thread. Threads are allocated from the pool of thread objects of the calling CPU:

```
InitializeNewThread\_
Thread Type'
condvarId!: ValidCondvarIdType
timerId!: ValidTimerIdType
threadId!: ValidThreadIdType
threadId! \neq invalidThreadId
id' = threadId!
builtinTimerId' = timerId!
builtinCondvarId' = condvarId!
state' = threadRunnable
atomicLevel' = atomicLevelNone
ThreadPriorityQueueInitialize\_
ThreadPriorityQueueType'
\forall p : ValidThreadPriorityType \bullet
    threadQueues'(p) = \emptyset
DequeueHighestPriorityThread\_
\Delta ThreadPriorityQueueType
highest Priority Thread Id!: Valid Thread Id Type
(let highestPrio ==
    max (dom(threadQueues > \emptyset)) \bullet
     highestPriorityThreadId! = head (threadQueues(highestPrio)) \land
     threadQueues'(highestPrio) = tail(threadQueues(highestPrio)))
```

3.3.2 *HiRTOS* Mutex Operations

Create a new mutex

A mutex can be created by calling HiRTOS.Mutex.Create. Mutexes are allocated from the pool of mutex objects of the calling CPU:

```
CreateMutex \Delta HiRtosCpuInstanceType InitializeNewMutex mutexId! \notin dom\ mutexes mutexId! \in dom\ mutexes' \theta\ MutexType' = mutexes'(mutexId!)
```

If ceilingPriority? is invalidThreadPriority that means that the mutex follows the priority inheritance protocol. Otherwise, it follows the priority ceiling protocol. In the priority inheritance protocol, if the thread trying to acquire a busy mutex has higher priority than the thread currently owning the mutex, the owning thread gets its priority raised to the priority of the waiting thread. In the priority ceiling protocol, when a thread acquires a mutex, if the mutex's ceiling priority is higher than the thread's priority, the thread gets its priority raised to the ceiling priority.

The *CreatedMutexMutableOperation* schema below is used in the specifications of all the mutable operations that can be performed on mutexes that were previously created by a call to HiRTOS.Mutex.Create:

```
Created Mutex Mutable Operation
\Delta HiRtos
\Delta HiRtos CpuInstance Type
\Delta Mutex Type
cpuId?: CpuId Type
mutexId?: Valid Mutex Id Type
\theta HiRtos CpuInstance Type = rtos CpuInstances (cpuId?)
\theta HiRtos CpuInstance Type' = rtos CpuInstances' (cpuId?)
\theta Mutex Type = mutexes (mutexId?)
\theta Mutex Type' = mutexes' (mutexId?)
```

Acquire a mutex

A thread acquires a mutex by calling HiRTOS.Mutex.Acquire, according to the contract specified by the *AcquireMutex* schema:

```
Created Mutex Mutable Operation \\ owner Thread Id = invalid Thread Id \lor \\ (owner Thread Id = current Thread Id \Rightarrow \\ recursive Count' = recursive Count + 1) \\ owner Thread Id' = current Thread Id \\ (ceiling Priority \neq invalid Thread Priority \land \\ (threads (current Thread Id)).current Priority < \\ ceiling Priority) \Rightarrow \\ (threads' (current Thread Id)).current Priority = \\ ceiling Priority \\ (threads' (current Thread Id)).owned Mutexes = \\ (threads (current Thread Id)).owned Mutexes \land \langle mutex Id? \rangle \\ \\
```

```
Wait On Unavailable Mutex
Created Mutex Mutable Operation
Dequeue Highest Priority Thread
runnable Threads Queue = \theta Thread Priority Queue Type
runnable Threads Queue' = \theta Thread Priority Queue Type'
ownerThreadId \neq invalidThreadId
currentThreadId \neq ownerThreadId
currentThreadId' \neq currentThreadId
(let oldCurrentPriority ==
    (threads(currentThreadId)).currentPriority \bullet
(ceilingPriority = invalidThreadPriority \land
oldCurrentPriority >
    (threads(ownerThreadId)).currentPriority) \Rightarrow
(threads'(ownerThreadId)).currentPriority =
    oldCurrentPriority
currentThreadId' \neq ownerThreadId \Rightarrow
((threads'(currentThreadId')).currentPriority \ge
    (threads'(ownerThreadId)).currentPriority \lor
(threads'(ownerThreadId)).state \in \{threadBlockedOnMutex, threadBlockedOnCondvar\}\}
Λ
(threads'(currentThreadId)).state = threadBlockedOnMutex
currentThreadId \in
    ran(waiting Threads Queue'.thread Queues(old Current Priority)))
ceilingPriority \neq invalidThreadPriority \Rightarrow
((threads(currentThreadId)).currentPriority \leq
    (threads'(ownerThreadId)).currentPriority \land
(threads'(ownerThreadId)).state \in \{threadBlockedOnMutex, threadBlockedOnCondvar\}\}
currentThreadId' \neq currentThreadId
currentThreadId' = highestPriorityThreadId!
```

```
AcquireMutex \triangleq \\ AcquireAvailableMutex \lor WaitOnUnavailableMutex
```

Release a mutex

A thread releases a mutex by calling HiRTOS.Mutex.Release, according to the contract specified by the *ReleaseMutex* schema:

3.3.3 *HiRTOS* Condition Variable Operations

Create a new condition variable

A condition variable can be created by calling HiRTOS.Condvar.Create. Condvars are allocated from the pool of condvar objects of the calling CPU:

```
CreateCondvar \Delta HiRtosCpuInstanceType InitializeNewCondvar condvarId! \notin dom\ condvars' condvarId! \in dom\ condvars' condvars'(condvarId!) = \theta\ CondvarType'
```

```
InitializeNewCondvar \\ CondvarType'\\ ThreadPriorityQueueInitialize\\ condvarId!: ValidCondvarIdType\\ \\ waitingThreadsQueue' = \theta ThreadPriorityQueueType'\\ condvarId! \neq invalidCondvarId\\ id' = condvarId!\\ \\ wakeupAtomicLevel' = atomicLevelNone\\ \\ wakeupMutexId' = invalidMutexId
```

The *CreatedCondvarMutableOperation* schema below is used in the specifications of all the mutable operations that can be performed on condition variables that were previously created by a call to HiRTOS.Condvar.Create:

```
 \begin{array}{l} Created Condvar Mutable Operation \\ \Delta HiRtos \\ \Delta HiRtos Cpu Instance Type \\ \Delta Condvar Type \\ cpu Id?: Cpu Id Type \\ condvar Id?: Valid Condvar Id Type \\ \\ \hline rtos Cpu Instances (cpu Id?) = \theta HiRtos Cpu Instance Type \\ rtos Cpu Instances' (cpu Id?) = \theta HiRtos Cpu Instance Type' \\ condvars (condvar Id?) = \theta Condvar Type \\ condvars' (condvar Id?) = \theta Condvar Type' \\ \end{array}
```

Wait on a condition variable

A thread waits on a condition variable by calling HiRTOS.Condvar.Wait, according to the contract specified by the *WaitOnCondvar* schema:

Signal a condition variable

A thread signals a condition variable by calling HiRTOS.Condvar.Signal, according to the contract specified by the *SignalCondvar* schema. Signaling a condition variable wakes up the highest priority thread waiting on the condition variable.

Broadcast on a condition variable

A thread broadcasts on a condition variable by calling HiRTOS.Condvar.Broadcast, according to the contract specified by the *BroadcastCondvar* schema. Broadcasting on a condition variable wakes up all threads waiting on the condition variable.

```
BroadcastCondvar\\ CreatedCondvarMutableOperation\\ (\forall \, p: ValidThreadPriorityType \mid \\ waitingThreadsQueue.threadQueues(p) \neq \emptyset \bullet \\ waitingThreadsQueue'.threadQueues(p) = \emptyset \land \\ runnableThreadsQueue'.threadQueues(p) = \\ runnableThreadsQueue.threadQueues(p) \cap \\ waitingThreadsQueue.threadQueues(p))
```

3.3.4 *HiRTOS* Software Timer Operations

Create a new software timer

A software timer can be created by calling HiRTOS.Timer.Create. Timers are allocated from the pool of timer objects of the calling CPU:

```
Create Timer \\ \Delta HiRtos CpuInstance Type \\ InitializeNew Timer \\ timerId! \notin \text{dom } timers \\ timerId! \in \text{dom } timers' \\ timers'(timerId!) = \theta Timer Type'
```

```
InitializeNewTimer \\ TimerType'\\ timerId!: ValidTimerIdType \\ \\ timerId! \neq invalidTimerId\\ id' = timerId!\\ timerKind' = oneShotTimer\\ timerState' = timerStopped\\ timerWheelRevolutions' = 0\\ timerWheelRevolutionsLeft' = 0\\ expirationCallbackAddr' = nullAddress\\ wheelSpokeIndex' = invalidTimerWheelSpokeIndex
```

The CreatedTimerMutableOperation schema below is used in the specifications

of all the mutable operations that can be performed on software timers that were previously created by a call to HiRTOS.Timer.Create:

Start a software timer

A software timer is started by calling HiRTOS.Timer.Start_Timer, according to the contract specified by the *StartTimer* schema:

```
Created Timer Mutable Operation \\ expiration Time Us?: \mathbb{N} \\ expiration Callback Addr?: Memory Address Type \\ timer Kind?: Timer Kind Type \\ \\ expiration Callback Addr? \neq null Address \\ expiration Callback Addr' = expiration Callback Addr? \\ timer Kind' = timer Kind? \\ (\textbf{let } expiration Time Ticks == expiration Time Us? \textbf{div } Tick Timer Period Us \bullet \\ wheel Spoke Index' = \\ (timer Wheel. current Wheel Spoke Index + expiration Time Ticks) \textbf{mod } num Timer Wheel Revolutions' = expiration Time Ticks \textbf{div } num Timer Wheel Spokes \land \\ timer Wheel Revolutions Left' = timer Wheel Revolutions' \land \\ timer Wheel'. wheel Spokes Hash Table (wheel Spoke Index') = \\ timer Wheel. wheel Spokes Hash Table (wheel Spoke Index') \cup \{ timer Id? \})
```

Stop a software timer

A software timer is stopped by calling HiRTOS.Timer.Stop_Timer, according to the contract specified by the *StopTimer* schema:

```
StopTimer \_ \_ \\ CreatedTimerMutableOperation \\ expirationCallbackAddr' = nullAddress \\ timerWheel'.wheelSpokesHashTable(wheelSpokeIndex) = \\ timerWheel.wheelSpokesHashTable(wheelSpokeIndex) \setminus \{\ timerId?\} \\
```

Pointer-less Linked list

Thread queues, mutex lists and timer sets are refined as pointer-less linked lists. Pointer-less linked lists use array indices instead of physical pointers. The *GenericLinkedLists* schema represents a generic pointer-less linked list in which the links that chain the list toegether are values of type *ElementIdType* which corresponds to indices of some object array.

```
GenericLinkedList[ElementIdType]_{\perp}
head: ElementIdType
tail: Element Id Type
length: \mathbb{N}
nextElement: ElementIdType \implies ElementIdType
prevElement: ElementIdType \implies ElementIdType
length \leq \#ElementIdType
length = \#(dom \ nextElement)
dom nextElement = dom prevElement
dom nextElement = dom prevElement
length \leq 1 \Leftrightarrow head = tail
length \ge 2 \Leftrightarrow
     th \ge 2 \Leftrightarrow (nextElement^{length-1}(head) = tail \land prevElement^{length-1}(tail) = head)
nextElement^+ \cap id\ ElementId\ Type = \emptyset
prevElement^+ \cap id\ ElementIdType = \emptyset
\forall x : dom \ nextElement \bullet
     (x \neq tail \Rightarrow prevElement(nextElement(x)) = x) \land
     (x \neq head \Rightarrow nextElement(prevElement(x)) = x)
```

ThreadQueueType which is an injective sequence is refined as the RefinedThreadQueueType schema:

 $\mathit{MutexListType}$ which is also an injective sequence is refined as the $\mathit{RefinedMutexListType}$ schema:

```
RefinedMutexListType \_
GenericLinkedList[MutexIdType]
nextElement(tail) = invalidMutexId
prevElement(tail) = invalidMutexId
length = 0 \Leftrightarrow head = invalidMutexId
tail = invalidMutexId \Leftrightarrow head = invalidMutexId
```

The set of timers associated with each timerwheel spoke is refined as the $\mathit{TimerListType}$ schema:

```
TimerListType \_
GenericLinkedList[TimerIdType]
nextElement(tail) = invalidTimerId
prevElement(tail) = invalidTimerId
length = 0 \Leftrightarrow head = invalidTimerId
tail = invalidTimerId \Leftrightarrow head = invalidTimerId
```

3.4 HiRTOS Thread Context Switching

3.4.1 Asynchronous Thread Context Switch

In HiRTOS, thread preemption is implemented by invoking the thread scheduler on the exit path of an interrupt handler. When an interrupt fires while a thread is running, the executing thread's CPU context is saved on thread's stack by the interrupt handler prolog. Then, before calling the actual interrupt handler, the stack is switched to the interrupt handling stack. After the interrupt handler returns, the

interrupt handler epilog invokes the HiRTOS thread scheduler, to select the highest priority runnable thread. Then, if the newly selected thread is different from the one that was running before the interrupt, the extended context of the old thread is saved and the extended context of the new thread is restored.

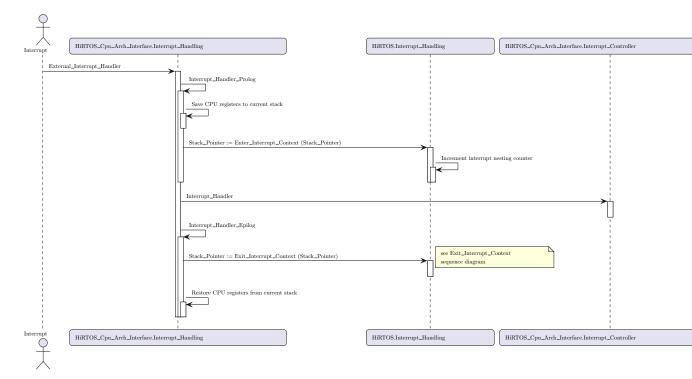


Figure 3.1: HiRTOS Asynchronous Thread Context Switch - part 1

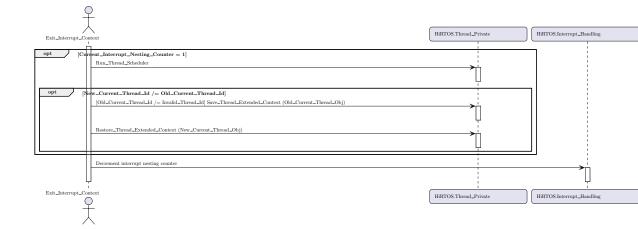


Figure 3.2: HiRTOS Asynchronous Thread Context Switch - part 2

3.4.2 Synchronous Thread Context Switch

In HiRTOS, a synchronous thread context switch occurs in the following cases:

- When a thread calls HiRTOS.Condvar.Wait
- When a thread calls HiRTOS.Condvar.Signal or HiRTOS.Condvar.Broadcast, and there are threads waiting on the condition variable
- When a thread calls HiRTOS.Mutex.Acquire and the mutex is not available
- When a thread calls HiRTOs.Mutex.Release and there are threads waiting to acquire the mutex
- When a thread calls HiRTOS. Thread. Thread_Delay_Until (calls HiRTOS. Condvar. Wait)
- When a thread calls HiRTOS.Thread.Suspend_Current_Thread
- When a thread calls HiRTOS. Thread. Resume_Thread
- When a thread calls HiRTOS.Restore_Atomic_Level and the old atomic level is Atomic_Level_None

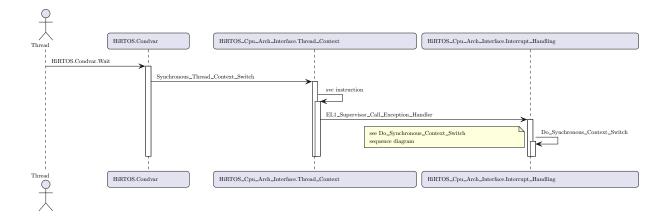


Figure 3.3: HiRTOS Synchronous Thread Context Switch - part 1

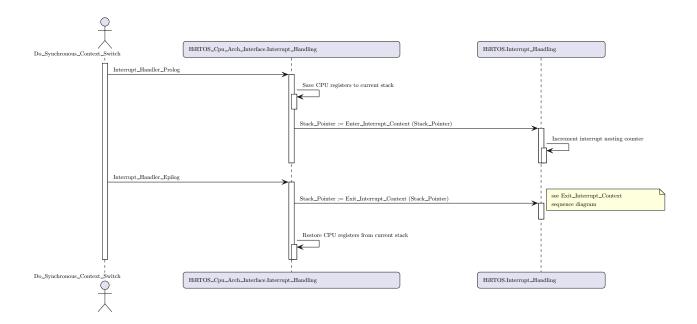


Figure 3.4: HiRTOS Synchronous Thread Context Switch - part 2

A special case is the initial thread context switch, which occurs when the HiRTOS thread scheduler is started, when the application calls HiRTOS.Start_Thread_Scheduler.

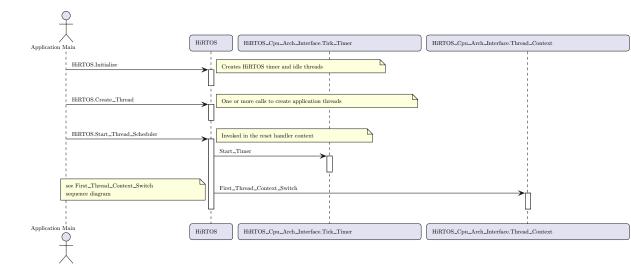


Figure 3.5: HiRTOS Initial Thread Context Switch - part 1

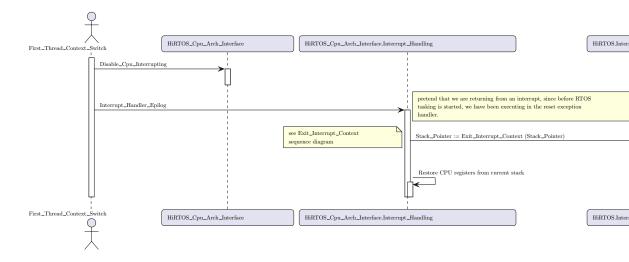


Figure 3.6: HiRTOS Initial Thread Context Switch - part 2

3.4.3 TLA+/PlusCal Model of the HiRTOS Thread Scheduler

The HiRTOS thread scheduler has been modeled in TLA+/PlusCal [15, 16]. The HiRTOS TLA+/PlusCal model can be found here. The following safety invariants were verified with the TLC model checker [17]:

• There can be at most only one "running" thread

```
HiRTOS. Interrupts_Enabled =>
     IF HiRTOS. Current_Thread_Id /= "Invalid_Thread_Id" THEN
        \label{eq:cardinality} $$ (\{ t \in Thread_Objects[t]. State = "Running" \}) = 1 $$
        /\ HiRTOS. Current_Thread_Id =
           CHOOSE t \in Threads: Thread_Objects[t]. State = "Running"
    ELSE
        { t \in Threads: Thread_Objects[t].State = "Running" } = {}
• The running thread is not in any queue
  (HiRTOS. Interrupts_Enabled /\
  HiRTOS. Current_Thread_Id /= "Invalid_Thread_Id") =>
     (/\ Thread_Objects [HiRTOS. Current_Thread_Id]. State = "Running"
      /\ Thread_Objects [HiRTOS. Current_Thread_Id]. Waiting_On_Condvar_Id =
            "Invalid_Condvar_Id"
      /\ Thread_Objects [HiRTOS. Current_Thread_Id]. Waiting_On_Mutex_Id =
            "Invalid_Mutex_Id"
      /\ ~Is_Thread_In_Priority_Queue (HiRTOS. Runnable_Threads_Queue,
                                       HiRTOS. Current_Thread_Id)
      ~Is_Thread_In_Priority_Queue (Mutex_Objects [m]. Waiting_Threads_Queue,
                                         HiRTOS. Current_Thread_Id)
      /\ \A cv \in Condvars :
           ~Is_Thread_In_Priority_Queue (Condvar_Objects [cv]. Waiting_Threads_Queue,
                                         HiRTOS. Current_Thread_Id)
• All Runnable threads are in the Runnable threads queue and no other queue
 HiRTOS. Interrupts_Enabled =>
 \A t \in Threads: Thread_Objects[t]. State = "Runnable" =>
     /\ Thread_Objects[t]. Waiting_On_Condvar_Id = "Invalid_Condvar_Id"
    /\ Thread_Objects[t]. Waiting_On_Mutex_Id = "Invalid_Mutex_Id"
     /\ Is_Thread_In_Priority_Queue (HiRTOS. Runnable_Threads_Queue, t)
     /\ Is_Thread_In_Priority_Queue_In_Only_One_Queue(
           HiRTOS. Runnable_Threads_Queue, t)
     ~Is_Thread_In_Priority_Queue (Mutex_Objects [m]. Waiting_Threads_Queue, t)
     /\ \ A \ cv \ \ in \ Condvars :
           ~Is_Thread_In_Priority_Queue(
              Condvar_Objects [cv]. Waiting_Threads_Queue, t)
• Each thread blocked on a mutex in only one mutex's wait queue and no other
 queue
 HiRTOS. Interrupts_Enabled =>
 \A t \in Threads :
 LET
     thread_obj == Thread_Objects[t]
```

```
IN
   thread_obj.State = "Blocked_On_Mutex" =>
   /\ thread_obj.Waiting_On_Mutex_Id /= "Invalid_Mutex_Id"
   /\ thread_obj.Waiting_On_Condvar_Id = "Invalid_Condvar_Id"
   /\ (LET
         mutex_obj == Mutex_Objects[thread_obj.Waiting_On_Mutex_Id]
       IN
         /\ Is_Thread_In_Priority_Queue (mutex_obj. Waiting_Threads_Queue,
         /\ Is_Thread_In_Priority_Queue_In_Only_One_Queue(
               mutex_obj.Waiting_Threads_Queue, t))
   /\ ~Is_Thread_In_Priority_Queue (HiRTOS. Runnable_Threads_Queue, t)
   /\ \A m \in Mutexes \ { thread_obj.Waiting_On_Mutex_Id } :
         ~Is_Thread_In_Priority_Queue(
            Mutex_Objects [m]. Waiting_Threads_Queue, t)
   /\ \A cv \in Condvars :
          ~Is_Thread_In_Priority_Queue(
            Condvar_Objects [cv]. Waiting_Threads_Queue, t)
```

• Each thread blocked on a condvar is in only one condvarś wait queue and no other queue

```
HiRTOS. Interrupts_Enabled =>
\A t \ in Threads :
LET
   thread_obj = Thread_Objects[t]
IN
   thread_obj.State = "Blocked_On_Condvar" =>
   /\ thread_obj.Waiting_On_Condvar_Id /= "Invalid_Condvar_Id"
   /\ thread_obj. Waiting_On_Mutex_Id = "Invalid_Mutex_Id"
   /\ (LET
        condvar_obj == Condvar_Objects[thread_obj.Waiting_On_Condvar_Id]
       IN
         /\ Is_Thread_In_Priority_Queue(
               condvar_obj.Waiting_Threads_Queue, t)
         /\ Is_Thread_In_Priority_Queue_In_Only_One_Queue(
               condvar_obj.Waiting_Threads_Queue, t))
   /\ ~Is_Thread_In_Priority_Queue(HiRTOS.Runnable_Threads_Queue, t)
   /\ \A cv \in Condvars \ { thread_obj.Waiting_On_Condvar_Id } :
         ~Is_Thread_In_Priority_Queue(
            Condvar_Objects [cv]. Waiting_Threads_Queue, t)
   ~Is_Thread_In_Priority_Queue(
            Mutex_Objects [m]. Waiting_Threads_Queue, t)
```

• Each mutex that is currently owned by a thread must be in the list of mutexes owned by that thread

```
HiRTOS.Interrupts_Enabled =>
\A m \in Mutexes :
```

```
LET
    t == Mutex_Objects[m].Owner_Thread_Id
IN
    t /= "Invalid_Thread_Id" =>
        m \in Range(Thread_Objects[t].Owned_Mutexes)
```

• If a mutex is not owned by a thread, its wait queue should be empty

```
HiRTOS.Interrupts_Enabled =>
\A m \in Mutexes :
   Mutex_Objects[m].Owner_Thread_Id = "Invalid_Thread_Id" =>
        Is_Thread_Priority_Queue_Empty(Mutex_Objects[m].Waiting_Threads_Queue)
```

• The thread owning a mutex can never have lower priority than any thread waiting for the mutex

• A thread not owning any mutex and not waiting on a condvar always has its current priority set to its base priority

```
HiRTOS. Interrupts_Enabled =>
\A t \in Threads :
   (Thread_Objects[t]. Owned_Mutexes = <<>> /\
        Thread_Objects[t]. State /= "Blocked_On_Condvar") =>
        Thread_Objects[t]. Current_Priority = Thread_Objects[t]. Base_Priority
```

Also, the following liveness properties were verified with TLC:

• Interrupts are not disabled indefinitely

```
~HiRTOS. Interrupts_Enabled => <> HiRTOS. Interrupts_Enabled
```

• Every thread waiting to acquire a mutex, eventually gets it:

```
\A t \in Threads:
Thread_Objects[t].State = "Waiting_On_Mutex" =>
<>(Thread_Objects[t].State = "Runnable")
```

• Every thread waiting on a condvar is eventually awaken:

```
\A t \in Threads:
Thread_Objects[t].State = "Waiting_On_Mutex" =>
<>(Thread_Objects[t].State = "Runnable")
```

Chapter 4

HiRTOS Separation Kernel Z Specification

4.1 Separation Kernel Data Structures

4.1.1 Separation Kernel Configuration Parameters

Constants defined here represent compile-time configuration parameters for the *HiR-TOS* Separation kernel.

```
maxNumPartitionsPerCpu : \mathbb{N}_1

TickTimerPeriodUs : \mathbb{N}_1

PartitionTimeSliceTicks : \mathbb{N}_1
```

4.1.2 Separation Kernel Primitive Types

Below are the primitive types used in HiRTOS:

```
[PartitionIdType] \\ \#PartitionIdType = maxNumPartitionsPerCpu + 1 \\ | invalidPartitionId : PartitionIdType \\ ValidPartitionIdType == \\ | PartitionIdType == \\ | PartitionIdType \setminus \{invalidPartitionId\} \\ | PartitionQueueType == iseq ValidPartitionIdType \\ | PartitionStateType ::= partitionNotCreated \mid \\ | partitionRunnable \mid partitionRunning \mid \\ | partitionSuspended \\ | PartitionSchedulerStateType ::= \\ | partitionSchedulerStopped \mid partitionSchedulerRunning \\ | AddressRangeType == MemoryAddressType \times MemoryAddressType \\ | PartitionSchedulerStype == MemoryAddressType \times MemoryAddressType \\ | PartitionSchedulerStype == M
```

4.1.3 Separation Kernel State Variables

The HiRtosSeparationKernel schema represents the internal data structures of the HiRTOS separation kernel.

```
\begin{tabular}{l} HiRtosSeparationKernelCpuInstances: \\ separationKernelCpuInstances: \\ ValidCpuIdType & SeparationKernelCpuInstanceType \\ zAllCreatedPartitionInstances: & PartitionType \\ \hline \#separationKernelCpuInstances & \\ (separationKernelCpuInstances & \\ (separationKernelCpuInstances(i)).cpuId & i \\ \hline zAllCreatedPartitionInstances & \\ & \forall i: ValidCpuIdType & \\ & & \text{ran} (separationKernelCpuInstances(i)).partitions \} \\ \hline \cap \{i: ValidCpuIdType & \\ & & \text{ran} (separationKernelCpuInstances(i)).partitions \} & \\ \hline \cap \{r: \bigcup \{p: zAllCreatedPartitionInstances & p.savedHypervisorLevelMpuRegions \} & \\ & zAddressRange(r)\} & = \emptyset \\ \hline \end{tabular}
```

Per-CPU Separation Kernel Instance

The state variables and internal data structures of each per-CPU *HiRTOS* separation kernel instance are described below:

```
Separation Kernel Cpu Instance Type _
cpuId: ValidCpuIdType
interruptStack: AddressRangeType
partitionSchedulerState: PartitionSchedulerStateType
currentPartitionId: PartitionIdType
timerTicksSinceBoot: \mathbb{N}
runnable Partitions Queue: Partition Queue Type
partitions: ValidPartitionIdType \implies PartitionType
zCurrentCpuContext: CpuRegistersType
zCurrentHypervisorLevelMpuRegions: \mathbb{F}_1 \ AddressRangeType
zCurrentSupervisorLevelMpuRegions: \mathbb{F} AddressRangeType
zCurrentSupervisorLevelInterruptVectorTableAddr: MemoryAddressType
zCurrentSupervisorLevelInterruptsEnabled: \mathbb{F}\ ValidInterruptIdType
zCurrentHighestInterruptPriorityDisabled: InterruptPriorityType
zAddressRange(interruptStack) \neq \emptyset
currentPartitionId \neq invalidPartitionId \Rightarrow
     currentPartitionId \in dom \ partitions \land
     zCurrentHypervisorLevelMpuRegions =
         (partitions(currentPartitionId)).savedHypervisorLevelMpuRegions \land
     zCurrentSupervisorLevelInterruptVectorTableAddr =
         (partitions(currentPartitionId)).savedInterruptVectorTableAddr
\forall p : \text{ran } partitions \bullet
    \bigcap \{i: p.savedHypervisorLevelMpuRegions \bullet zAddressRange(i)\} = \emptyset
\exists_1 j : zCurrentHypervisorLevelMpuRegions \bullet
          zAddressRange(i) \subseteq zAddressRange(i)
```

```
Partition Type _
id: Partition IdType
failover Partition Id: Partition Id Type
state: Partition State Type
timeSliceLeftUs: \mathbb{N}
savedCpuContext: CpuRegistersType
savedHypervisorLevelMpuRegions: \mathbb{F}_1 AddressRangeType
saved Supervisor Level MpuRegions: \mathbb{F}\ Address Range\ Type
savedInterruptVectorTableAddr: MemoryAddressType
savedInterruptsEnabled: \mathbb{F} InterruptIdType
saved Highest Interrupt Priority Disabled: Interrupt Priority Type
state \neq partitionNotCreated \Rightarrow
     id \neq invalidPartitionId
failoverPartitionId \neq invalidPartitionId \Rightarrow
     failoverPartitionId \neq id
\bigcap \{i : savedHypervisorLevelMpuRegions \bullet zAddressRange(i)\} = \emptyset
\emptyset \notin \{ i : savedHypervisorLevelMpuRegions \bullet zAddressRange(i) \} 
\exists_1 j : savedHypervisorLevelMpuRegions \bullet
          zAddressRange(i) \subseteq zAddressRange(j)
```

4.1.4 Separation Kernel Boot-time Initialization

At boot time, the HiRTOS separation kernel is initialized when the HiRTOS.Separation_Kernel.Initialize *HiRTOS* API is called on every CPU core:

```
HiRtosSeparationKernelInitialize \_
HiRtosSeparationKernel'
SeparationKernelCpuInstanceInitialize
cpuId?: CpuIdType
cpuId' = cpuId?
\theta SeparationKernelCpuInstanceType' = separationKernelCpuInstances'(cpuId?)
```

```
SeparationKernelCpuInstanceElaboration \\ SeparationKernelCpuInstanceType' \\ zAddressRange(interruptStack') \neq \emptyset \\ partitionSchedulerState' = partitionSchedulerStopped \\ currentPartitionId' = invalidPartitionId \\ timerTicksSinceBoot' = 0 \\ runnablePartitionsQueue' = \langle \rangle \\ partitions' = \emptyset
```

4.2 Separation Kernel Callable Services

4.2.1 Partition Operations

Create a new partition

A partition can be created by calling HiRTOS. Separation_Kernel.Partition.Create_Partition. Partitions are allocated from the pool of partition objects of the calling CPU:

```
InitializeNewPartition \_
PartitionType'
partitionId!: ValidPartitionIdType

id' = partitionId!
failoverPartitionId' = invalidPartitionId
state' = partitionRunnable
savedHypervisorLevelMpuRegions' \neq \emptyset
savedSupervisorLevelMpuRegions' = \emptyset
savedInterruptsEnabled' = \emptyset
```

Bibliography

- [1] Mike Spivey, "Z Reference Card", 1992 https://github.com/Spivoxity/fuzz/blob/master/doc/refcard3-pub.pdf
- [2] Mike Spivey, "The Z Reference Manual", second edition, Prentice-Hall, 1992 http://spivey.oriel.ox.ac.uk/~mike/zrm/zrm.pdf
- [3] Jonathan Jacky, "The Way of Z", Cambridge Press, 1997 http://staff.washington.edu/jon/z-book/index.html
- [4] Mike Spivey, "The Fuzz checker" https://github.com/Spivoxity/fuzz
- [5] John W. McCormick, Peter C. Chapin, "Building High Integrity Applications with SPARK", Cambridge University Press, 2015 https://www.amazon.com/Building-High-Integrity-Applications-SPARK/ dp/1107040736
- [6] AdaCore, "Formal Verification with GNATprove" https://docs.adacore.com/spark2014-docs/html/ug/en/gnatprove.html
- [7] Andrew D. Birrel, "An Introduction to Programming with Threads", Digital Equipment Corporation, Systems Research Center, 1989 http://birrell.org/andrew/papers/035-Threads.pdf
- [8] Andrew D. Birrel et al, "Synchronization Primitives for a Multiprocessor: A Formal Specification", Digital Equipment Corporation, Systems Research Center, 1987 https://dl.acm.org/doi/pdf/10.1145/37499.37509
- [9] ISO, "N2731: Working draft of the C23 standard, section 7.26", October 2021 http://www.open-std.org/jtc1/sc22/wg14/www/docs/n2596.pdf#page=345&zoom=100,102,113
- [10] Lui Sha et al, "Priority Inheritance Protocols: An Approach to Real-Time Synchronization", IEEE Transactions on Computers, September 1990 https://www.csie.ntu.edu.tw/~r95093/papers/Priority%20Inheritance% 20Protocols%20An%20Approach%20to%20Real-Time%20Synchronization.pdf

- [11] John Rushby, "Design and Verification of Secure Systems", ACM SIGOPS Operating Systems Review, 1981 https://www.csl.sri.com/users/rushby/papers/sosp81.pdf
- [12] John Rushby, "Partitioning in Avionics Architectures: Requirements, Mechanisms, and Assurance", Technical Report. 1999
 https://www.tc.faa.gov/its/worldpac/techrpt/ar99-58.pdf
- [13] FreeRTOS https://www.freertos.org/
- [14] CMSIS-RTOS API v2 (CMSIS-RTOS2)
 https://www.keil.com/pack/doc/CMSIS/RTOS2/html/group__CMSIS__RTOS.
 html
- [15] Leslie Lamport, "Specifying Systems: The TLA+ Language and Tools for Hardware and Software Engineers", Addison Wesley, 2003 https://lamport.azurewebsites.net/tla/book.html?back-link=learning.html#book
- [16] 'Hillel Wayne, '''Practical TLA+: Planning Driven Development", APress, 2018 https://link.springer.com/book/10.1007/978-1-4842-3829-5
- [17] Leslie Lamport, "The TLA+ Toolbox" https://lamport.azurewebsites.net/tla/toolbox.html