Circular segment 1

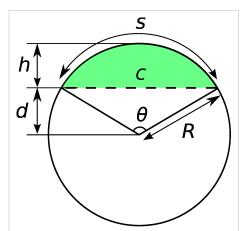
## Circular segment

In geometry, a **circular segment** (symbol: []) is an area of a circle informally defined as an area which is "cut off" from the rest of the circle by a secant or a chord.

#### **Formulas**

Let R be the radius of the circle,  $\theta$  is the central angle in radians,  $\alpha$  is the central angle in degrees, c the chord length, s the arc length, h the height of the segment, and d the height of the triangular portion.

- The radius is  $R = h + d = h/2 + c^2/8h$
- The arc length is  $s=\frac{\alpha}{180}\pi R=\theta R$
- The chord length is  $c=2R\sin{rac{ heta}{2}}=R\sqrt{2-2\cos{ heta}}$
- The height is  $h = R(1-\cos\frac{\theta}{2}) = R \sqrt{R^2 \frac{c^2}{4}}$
- The angle is  $\, \theta = 2 \arccos rac{d}{R} = 2 \arcsin rac{c}{2R} \,$



A circular segment (in green) is enclosed between a secant/chord (the dashed line) and the arc whose endpoints equal the chord's (the arc shown above the green area).

#### Area

The area of the circular segment is equal to the area of the circular sector minus the area of the triangular portion.

$$A = \pi R^2 \cdot \frac{\theta}{2\pi} - \frac{R^2 \sin \theta}{2} = \frac{R^2}{2} \left( \theta - \sin \theta \right) = \frac{R^2}{2} \left( \frac{\alpha \pi}{180} - \sin \frac{\alpha \pi}{180} \right)$$

#### **External links**

- Weisstein, Eric W., "Circular segment [1]", MathWorld.
- Definition of a circular segment <sup>[2]</sup> With interactive animation
- Formulae for area of a circular segment [3] With interactive animation

#### References

- [1] http://mathworld.wolfram.com/CircularSegment.html
- [2] http://www.mathopenref.com/segment.html
- [3] http://www.mathopenref.com/segmentarea.html

## **Article Sources and Contributors**

Circular segment Source: http://en.wikipedia.org/w/index.php?oldid=572716040 Contributors: Al Lemos, CWii, Canuckian89, Charles Matthews, Clovis Sangrail, Cpt jeltz, Duoduoduo, Elb2000, Giftlite, Gurglegogo, Götz, Henning Makholm, Iameukarya, Isnow, J'raxis, JPaestpreornJeolhlna, Jjhepburn, Kiensvay, La Pianista, Lutusp, Maksim-e, Marino-slo, Markhurd, Michael Hardy, MrOllie, Olaf, Perey, Pgartenburg1234, Python eggs, Rmashhadi, RuM, Sbesson, Skythiru, Sobreira, StuRat, SuneJ, Synethos, Vints, Walibi's are cool, Wellmann, Wernher, WikiHannibal, WillNess, ZooFari,  $\Sigma$ , 99 anonymous edits

# **Image Sources, Licenses and Contributors**

Image: Circularsegment.svg Source: http://en.wikipedia.org/w/index.php?title=File: Circularsegment.svg License: Public Domain Contributors: Sbesson

## License

Creative Commons Attribution-Share Alike 3.0 //creativecommons.org/licenses/by-sa/3.0/