

CSC373 Notes

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§1 Day 1: Intro (Jan 06, 2026)

This was taken off the slides from past years.

§1.1 About this Class

This class is about designing algorithms to solve problems.

We will be:

(i) Designing fast algorithms

- Divide and conquer
- Greedy algorithms
- Dynamic programming
- Network flow
- Linear programming

(ii) Proving no fast algorithms are likely possible

- Reductions and NP-completeness

(iii) Solving problems where no fast algorithms are possible

- Approximation algorithms
- Randomized algorithms

When we analyze an algorithm, we do correctness and running-time proofs.

§2 Day 2: Intro Redux (Jan 08, 2026)

This course is now about the thought process behind solutions of problems. We use the **RAM Computational Model**.

A proof is a convincing argument:

- Convince your TA for marks
- Convince employer that your program does what it claim it does
- Convince yourself that you're not producing word salad

Sometimes, formal verification is used for mission-critical applications, where unit tests may not have sufficient coverage. We use semi-formal proofs in this course, to prove specific results (as opposed to more general ones, like in math).

§2.1 Divide & Conquer

The general framework is to:

- (i) Break a problem into two smaller subproblems of the same type
- (ii) Solve each problem recursively and independently
- (iii) Quickly combine solutions from subproblems to form a solution to a bigger part of the problem

'Quick/cheap' means that the step count is in $O(f(n))$ where f is a polynomial.

Recurrence relations are often encountered while analyzing the running time of divide-and-conquer algorithms. We take the master theorem from (CLRS) for granted, a general result about the asymptotic behavior of certain types of recurrences.

Theorem 2.1 (CLRS Master Theorem)

Let $a \geq 1, b > 1$. Have $f(n)$ be a function, and let $T(n)$ be defined on the non-negative integers by the recurrence $T(n) = aT(n/b) + f(n)$, where n/b is interpreted as $\lceil \frac{n}{b} \rceil$ or $\lfloor \frac{n}{b} \rfloor$. Then $T(n)$ has the following asymptotic bounds:

1. If $f(n) \in O(n^{\log_b a - \varepsilon})$ for some constant $\varepsilon > 0$, then $T(n) = \Theta(n^{\log_b a})$
2. If $f(n) \in \Theta(n^{\log_b a})$, then $T(n) = \Theta(n^{\log_b a} \log_2 n)$
3. If $f(n) = \Omega(n^{\log_b a + \varepsilon})$ for some constant $\varepsilon > 0$, and if $af(n/b) \leq cf(n)$ for some constant $c < 1$ and all sufficiently large n , then $T(n) \in \Theta(f(n))$

n/b describes the size of the subproblems, and $f(n)$ describes the step count required to merge/divide the subproblems to form a solution of size n . The Master Theorem handles the leaf-heavy, balanced, and root-heavy case in that order.

Example 2.2

Algorithms considered divide-and-conquer include:

- Closest pair in \mathbb{R}^2 , with non-degeneracy assumption
- Karatsuba's Algorithm
- Strassen's Algorithm

There was also a brief discussion about galactic algorithms.