$$v(\mathbf{k}, a) = if(a)aH\delta(\mathbf{k}, a)\frac{\mathbf{k}}{k^2}$$