

THEORETICAL EXERCISE 5

ANSWER 1

- a) $8\text{MB} = 64000000 \text{ bit}$
 $64000000 * 10^{-5} = 640 \text{ dollars Ram}$
 $1\text{MB} = 8000000 \text{ bit}$
 $8000000 * 10^{-4} = 800 \text{ dollars Cache}$
Ram is cheaper than cache.

b) RAM

$$1320 = H * 1200 + (1 - H)(100 + 1200)$$
$$1320 = 1200H + 1300 - 1300H$$
$$1320 = 1300 - 100H$$
$$100H = -20$$
$$H = -20/100 = -0,2$$

CACHE

$$110 = H * 100 + (1 - H)(100 + 1200)$$
$$110 = 100H + 1300 - 1300H$$
$$110 = 1300 - 1200H$$
$$1200H = 1190$$
$$H = 1190/1200 = 0,99$$

- c) $0,901 = H * 100 + (1 - H)(100 + 1200)$
 $0,901 = 1300 - 1200H$
 $1200H = 1300 - 0,901$
 $H = (1300 - 0,901)/1200 = 1,082$
Performance improved.

ANSWER 2

- a) Cache = Numbers of blocks * Size of each Word
Cache = $2K * 128 = 2^1 * 2^{10} * 2^7 = 2^{18}$ words
Physical address = $\log_2(2^{18}) = 18$
Word offset = $\log_2(128) = 7$
Number of lines(cache) = 64
Line number = $\log_2(64) = 6$
Tag = $18 - (7 + 6) = 5$ bits S=6bits W=7bits

b) Cache=Numbers of blocks*Size of each Word

$$\text{Cache} = 2K * 128 = 2^1 * 2^{10} * 2^7 = 2^{18} \text{ words}$$

$$\text{Physical Address} = \log_2(2^{18}) = 18$$

$$\text{Word offset} = \log_2(128) = 7$$

$$\text{Tag} = 18 - 7 = 11 \text{ bits} \quad W = 7 \text{ bits}$$

c) Cache= Numbers of blocks*Size of each Word

$$\text{Cache} = 2K * 128 = 2^1 * 2^{10} * 2^7 = 2^{18} \text{ words}$$

$$\text{Physical Address} = \log_2(2^{18}) = 18$$

$$\text{Word offset} = \log_2(128) = 7$$

$$\text{Number of lines(cache)} = 64$$

$$\text{Number of sets(cache)} = 64 / 4 = 16$$

$$\text{Set number} = \log_2(16) = 4$$

$$\text{Tag} = 18 - (7 + 4) = 7 \text{ bits} \quad S = 4 \text{ bits} \quad W = 7 \text{ bits}$$

ANSWER 3

a) Block size=16 bytes

$$\text{Lines} = 8 \text{ KB} / 16 \text{ B} = 2^{13} / 2^4 = 2^9 \quad r = 9$$

$$\text{Blocks} = 64 \text{ MB} / 16 \text{ B} = 2^{26} / 2^4 = 2^{22} \quad s = 22$$

$$\text{Words} = 16 \text{ B} / 1 \text{ B} = 2^4 \quad w = 4$$

$$\text{Number of addressable unit}(2^{s+w}) = 2^{26}$$

$$\text{Address length}(s+w) = 26$$

$$\text{Block size} 2^w = 2^4$$

$$\text{Number of blocks in main memory}(2^s) = 2^{22}$$

b) Direct mapping

$$\text{Tag} = 22 - 9 = 13$$

c) Associative mapping

$$\text{Tag} = 22$$

d) Set Associative

$$\text{Tag} = 22 - 1 = 21$$

e) 0011 1111 0100 1010 1101 0110 1001

3 F 4 A D 6 9

Direct Mapping

$$\text{Tag} = 0011 \ 1111 \ 0100 = 7E9$$

$$\text{Word} = 1001 = 9$$

Associative Mapping

$$\text{Tag} = 0011 \ 1111 \ 0100 \ 1010 \ 110101 = \text{FD2B5}$$

$$\text{Word} = 1001 = 9$$

Set Associative Mapping

Tag=0011 1111 0100 1010 11010=6E95A

Word=1001=9

ANSWER 4

a) Miss ratio = $97/386=0,251$

Hit ratio= $1-0,251=0,749$

b) Hit time=8ns → Access time of cache

Miss time=23ns → Access time of cache+Access time of ram

c) Non-overlapped

Effective Access Time= $H*Access(cache)+M*(Access(cache)+Access(ram))$

= $0,749*8+0,251*23$

= 11,76

Overlapped

Effective Access Time= $H*Access(cache)+M*Access(ram)$

= $0,749*8+0,251*15$

=9,75

ANSWER 5

a) 101010101100 → Hit

b) 1100110011001100 → Hit

c) 1010101100 → Miss

d) 01010110000000 → Miss

e) 0000110 → Miss

f) 0110000 → Miss

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