

Divide & Conquer — Core (Quick Guide)

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1) Count Inversions (Merge Sort)

- Split, count in left + right + cross inversions during merge.
- Time: $O(n \log n)$

2) Maximum Subarray (Divide & Conquer)

- Combine four quantities: total sum, best prefix, best suffix, best overall.
- Conquer: $\text{best} = \max(\text{left.best}, \text{right.best}, \text{left.bestSuffix} + \text{right.bestPrefix})$
- Time: $O(n)$

3) Majority Element (Boyer–Moore)

- Single pass candidate/vote.
- Time: $O(n)$, Space: $O(1)$
- If majority may not exist, verify candidate count at the end.

Tips

- Prefer divide & conquer when merging results from subproblems is efficient.
- Track minimal sufficient state (sum/pref/suf/best) to combine in $O(1)$.
- For inversions, the key is counting how many left elements remain when picking a right element.