

Stack & Monotonic Stack — Illustrated Guide

Monotonic Stack Patterns

- Decreasing stack (values downwards): helps find "next greater" to the right.
- Increasing stack (values upwards): helps compute spans or areas (histogram).
- Always consider pushing indices (not values) to derive widths and distances.

Included Problems

- 1) Next Greater Element — decreasing stack of indices
- 2) Daily Temperatures — decreasing stack of temperatures
- 3) Largest Rectangle in Histogram — increasing stack; sentinel 0 flush
- 4) Stock Span — decreasing stack of prices
- 5) Valid Parentheses — classic push/pop matching

Complexities

All stack scans are $O(n)$ time (each index pushed/popped ≤ 1), $O(n)$ space.

Implementation Tips

- For histogram area: $\text{width} = \text{current_index} - \text{last_smaller_index} - 1$
- For distance-to-next-warmer: store indices to compute $i - j$
- Append sentinel when you need to flush remaining stack content