Tutorial on the R package ReplicationSuccess

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Theory

Installation

Linux / Windows

- Mac

Replication studies

Direct replication

- Repeating original study using the same methodology
- → Tool to assess credibility of scientific discoveries
- → Regulatory requirement

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Replication crisis

- Low replicability of many scientific discoveries
- → Increased interest in meta-science
- → Large-scale replication projects

- 2015: Reproducibility project psychology

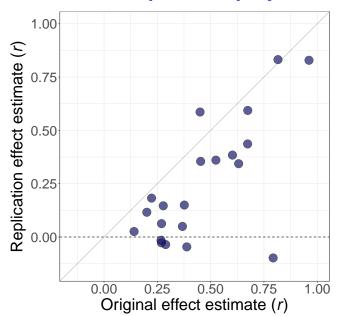
- 2015: Reproducibility project psychology
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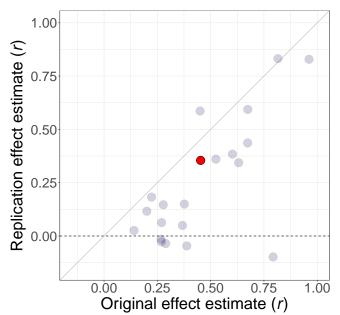
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Social sciences replication project



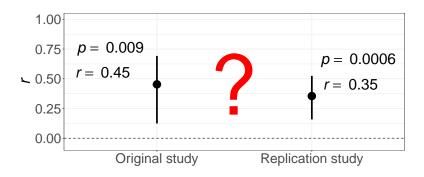
Social sciences replication project



Morewedge et al. (2010). Science

Original discovery

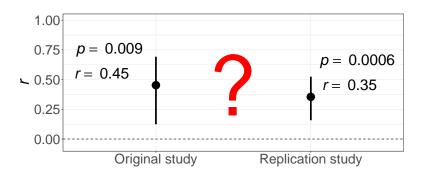
"Repeatedly imagining eating a food subsequently reduces the actual consumption of that food"



When is a replication successful?

Some proposed criteria

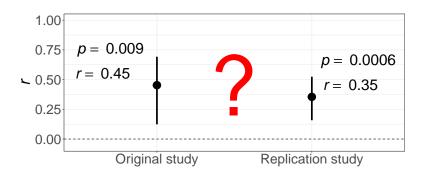
1. Statistical significance



When is a replication successful?

Some proposed criteria

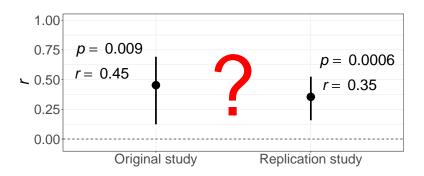
- 1. Statistical significance
- 2. Compatibility of effect estimates



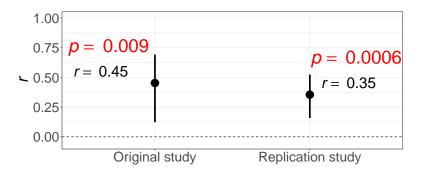
When is a replication successful?

Some proposed criteria

- 1. Statistical significance
- 2. Compatibility of effect estimates
- 3. Sceptical p-value

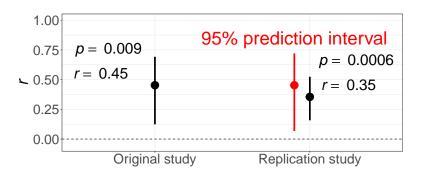


Are original and replication estimates statistically significant?



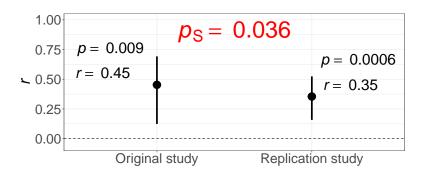
2. Compatibility of effect estimates

Is the replication estimate contained in its prediction interval?



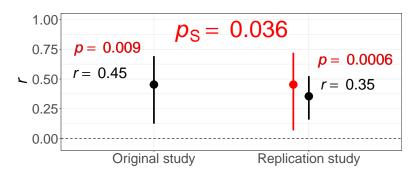
3. Sceptical p-value

?At which level can we convince a sceptic who argues that the original study is no longer signficant at that level?



Drawbacks of classical approaches

- Signficiance can always be achieved by increasing sample size
- Estimates can be compatible but provide no information about true effect



Design of replication studies

Sample size of replication study

- Direct replication → procedures of replication study as closely matched as possible to original study
- But proper sample size calculation is essential and depends on analysis strategy

Design of replication studies

What is used in practice

- Standard power calculation
- Depending on the projects, goal is to have between 80% and 95% power in the replication study to detect the effect estimate from the original study
- Shrinkage of the original effect estimate is sometimes used (e.g. in Camerer et al. (2018))

Design of replication studies

Issues with this method

- Uncertainty of original effect estimate is ignored
- Heterogeneity between original and replication study is not taken into account
- Arbitrary shrinkage methods

Package

To add: small intro to package (goal, structure etc)

Statistical framework of package

- Effect estimates are assumed to be normally distributed
 - → usually fulfilled after suitable transformation
 - \rightarrow Fisher's z-transformation for correlation coefficients r
- Design prior
 - → Conditional: ignores uncertainty of original study
 - \rightarrow Predictive: reflects that there is still uncertainty about the true effect after the original experiment

Statistical framework of package

- Relative quantities (as opposed to absolute quantities)
 - → p-value or test statistic of original study
 - \rightarrow Relative sample size n_r/n_o
- Example for Morewedge et al. (2010):
 - $-p_0 = 0.009$
 - $-p_r = 0.0006$
 - -c = 3

Application

Application

- 1. Statistical significance
- 2. Comparison of effect estimates
- 3. Reverse Bayes methods

Two functions:

- powerSignificance() and sampleSizeSignificance()

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- powerSignificance() and sampleSizeSignificance()

Main arguments

- po or to
- c
- power
- designPrior
- shrinkage

Exercise 1

We have five original studies that we want to replicate. Their *p*-values are 0.0001, 0.001, 0.005, 0.01, 0.03 and 0.05, respectively. We decide to simply use the same sample size as in the original study.

- Please compute the conditional and predictive power of the five replication studies and plot it.
- What do you notice?
- What happens if we decide to take less subjects in the replication study as compared to the original study?

Exercise 2

We now know that taking the same sample size as in the original study is not optimal and want to perform a proper sample size calculation.

- Please compute and plot the relative replication sample sizes of the six studies to achieve a power of 80% with the conditional and the predictive design prior.
- What happens if the desired power is now 90%?

Exercise 3

We now know that taking the same sample size as in the original study is not optimal and want to perform a proper sample size calculation.

- Please compute and plot the relative replication sample sizes of the six studies to achieve a power of 80% with the conditional and the predictive design prior.
- What happens if the desired power is now 90%?

Comparison of effect size

- predictionInterval - sampleSizePI - sampleSizePIwidth

Reverse Bayes

– pSceptical – powerReplicationSuccess – sampleSizeReplicationSuccess

Outlook

- Interim - Heterogeneity - EB shrinkage

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