# Cubist Models For Regression

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#### 1 Introduction

Cubist is an R port of the Cubist GPL C code released by RuleQuest at

http://rulequest.com/cubist-info.html

See the last section of this document for information on the porting. The other parts describes the functionality of the R package.

# 2 Model Trees

Cubist is a rule—based model that is an extension of Quinlan's M5 model tree. A tree is grown where the terminal leaves contain linear regression models. These models are based on the predictors used in previous splits. Also, there are intermediate linear models at each step of the tree. A prediction is made using the linear regression model at the terminal node of the tree, but is "smoothed" by taking into account the prediction from the linear model in the previous node of the tree (which also occurs recursively up the tree). The tree is reduced to a set of rules, which initially are paths from the top of the tree to the bottom. Rules are eliminated via pruning and/or combined for simplification.

This is explained better in Quinlan (1992). Wang and Witten (1997) attempted to recreate this model using a "rational reconstruction" of Quinlan (1992) that is the basis for the M5P model in Weka (and the R package RWeka).

An example of a model tree can be illustrated using the Boston Housing data in the mlbench package.

```
> library(Cubist)
> library(mlbench)
> data(BostonHousing)
> set.seed(1)
> inTrain <- sample(1:nrow(BostonHousing), floor(.8*nrow(BostonHousing)))</pre>
> trainingPredictors <- BostonHousing[ inTrain, -14]</pre>
> testPredictors <- BostonHousing[-inTrain, -14]</pre>
> trainingOutcome <- BostonHousing$medv[ inTrain]</pre>
               <- BostonHousing$medv[-inTrain]</pre>
> testOutcome
> modelTree <- cubist(x = trainingPredictors, y = trainingOutcome)</pre>
> modelTree
Call:
cubist.default(x = trainingPredictors, y = trainingOutcome)
Number of samples: 404
Number of predictors: 13
Number of committees: 1
Number of rules: 4
> summary(modelTree)
Call:
cubist.default(x = trainingPredictors, y = trainingOutcome)
Cubist [Release 2.07 GPL Edition] Fri Apr 22 22:44:58 2011
    Target attribute `outcome'
Read 404 cases (14 attributes) from undefined.data
Model:
 Rule 1: [88 cases, mean 13.81, range 5 to 27.5, est err 2.10]
    if
        nox > 0.668
    then
        outcome = 2.07 + 3.14 \, dis - 0.35 \, lstat + 18.8 \, nox + 0.007 \, b
                  - 0.12 ptratio - 0.008 age - 0.02 crim
 Rule 2: [153 cases, mean 19.54, range 8.1 to 31, est err 2.16]
    if
        nox <= 0.668
        1stat > 9.59
    then
```

```
outcome = 34.81 - 1 dis - 0.72 ptratio - 0.056 age - 0.19 lstat + 1.5 rm
                    -0.11 indus +0.004 b
  Rule 3: [39 cases, mean 24.10, range 11.9 to 50, est err 2.73]
    if
        rm <= 6.23
         1stat <= 9.59
    then
         outcome = 11.89 + 3.69 \text{ crim} - 1.25 \text{ lstat} + 3.9 \text{ rm} - 0.0045 \text{ tax}
                    - 0.16 ptratio
  Rule 4: [128 cases, mean 31.31, range 16.5 to 50, est err 2.95]
    if
         rm > 6.23
        lstat <= 9.59
    then
         outcome = -1.13 + 1.6 \text{ crim} - 0.93 \text{ lstat} + 8.6 \text{ rm} - 0.0141 \text{ tax}
                    - 0.83 ptratio - 0.47 dis - 0.019 age - 1.1 nox
Evaluation on training data (404 cases):
    Average | error |
                                       2.27
    Relative |error|
                                       0.34
    Correlation coefficient
                                      0.94
        Attribute usage:
           Conds Model
            78%
                  100%
                           lstat
            59%
                    53%
                           nox
            41%
                    78%
                           rm
                   100%
                           ptratio
                    90%
                           age
                    90%
                           dis
                    62%
                           crim
                    59%
                           b
                    41%
                           tax
                    38%
                           indus
```

Time: 0.0 secs

There is no formula method for cubist; the predictors are specified as matrix or data frame and the outcome is a numeric vector.

There is a predict method for the model:

```
> mtPred <- predict(modelTree, testPredictors)
> ## Test set RMSE
> sqrt(mean((mtPred - testOutcome)^2))
[1] 3.337924
> ## Test set R^2
> cor(mtPred, testOutcome)^2
[1] 0.8573504
```

# 3 Boosting

The Cubist model can also use a boosting–like scheme called *committees* where iterative model trees are created in sequence. The first tree follows the procedure described in the last section. Subsequent trees using a weighting scheme similar to gradient boosting where case weights are applied based on the errors from previous model trees. Unlike traditional boosting, stage weights for each committee are not used to average the predictions from each model tree; the final prediction is a simple average of the predictions from each model tree.

The committee option can be used to control number of model trees:

```
- 0.12 ptratio - 0.008 age - 0.02 crim
 Rule 1/2: [153 cases, mean 19.54, range 8.1 to 31, est err 2.16]
    if
        nox <= 0.668
        1stat > 9.59
    then
        outcome = 34.81 - 1 dis - 0.72 ptratio - 0.056 age - 0.19 lstat + 1.5 rm
                  -0.11 indus +0.004 b
 Rule 1/3: [39 cases, mean 24.10, range 11.9 to 50, est err 2.73]
    if
        rm <= 6.23
        lstat <= 9.59
    then
        outcome = 11.89 + 3.69 \text{ crim} - 1.25 \text{ lstat} + 3.9 \text{ rm} - 0.0045 \text{ tax}
                  - 0.16 ptratio
 Rule 1/4: [128 cases, mean 31.31, range 16.5 to 50, est err 2.95]
    if
        rm > 6.23
        1stat <= 9.59
    then
        outcome = -1.13 + 1.6 crim -0.93 lstat +8.6 rm -0.0141 tax
                  - 0.83 ptratio - 0.47 dis - 0.019 age - 1.1 nox
Model 2:
 Rule 2/1: [71 cases, mean 13.41, range 5 to 27.5, est err 2.62]
    if
        crim > 5.69175
        dis > 1.4254
    then
        outcome = 43.01 + 2.57 dis - 0.47 lstat - 0.7 ptratio - 2 rm
 Rule 2/2: [84 cases, mean 18.75, range 8.1 to 27.5, est err 2.25]
    if
        crim <= 5.69175
        nox > 0.532
        dis > 1.4254
        tax > 222
        ptratio > 17
        outcome = 44.08 + 1.19 crim - 0.43 lstat - 1.05 ptratio - 0.011 age
 Rule 2/3: [15 cases, mean 23.43, range 5 to 50, est err 5.62]
```

```
if
      dis <= 1.4254
      ptratio > 17
  then
      outcome = 174.86 - 100.95 dis - 1.07 lstat - 0.09 ptratio
Rule 2/4: [77 cases, mean 23.90, range 11.8 to 50, est err 2.35]
  if
      ptratio <= 17
      lstat > 5.12
  then
      outcome = -2.7 + 8.2 \text{ rm} - 0.0228 \text{ tax} - 1.68 \text{ dis} - 0.064 \text{ age} - 0.1 \text{ lstat}
                 - 0.24 ptratio - 3.7 nox + 0.009 zn - 0.02 crim - 0.02 indus
                 + 0.001 b
Rule 2/5: [128 cases, mean 25.56, range 14.4 to 50, est err 3.12]
      crim <= 5.69175
      nox <= 0.532
      ptratio > 17
  then
      outcome = -14.6 + 2.4 \text{ crim} + 7 \text{ rm} - 0.075 \text{ age} + 0.23 \text{ lstat} - 0.42 \text{ dis}
                 - 0.17 ptratio
Rule 2/6: [16 cases, mean 27.91, range 15.7 to 39.8, est err 5.25]
  if
      tax <= 222
      lstat > 5.12
  then
      outcome = 274.62 - 12.31 ptratio - 0.212 age - 0.03 lstat
Rule 2/7: [18 cases, mean 30.49, range 22.5 to 50, est err 3.76]
  if
      rm <= 6.861
      lstat <= 5.12
  then
      outcome = -58.67 + 10.99 crim + 13.3 rm - 0.08 dis - 0.02 lstat
                 - 0.05 ptratio
Rule 2/8: [19 cases, mean 41.54, range 31.2 to 50, est err 3.64]
  if
      rm > 6.861
      age <= 71
      lstat <= 5.12
  then
```

```
outcome = -57.01 + 14.2 \text{ rm} - 0.23 \text{ dis} - 0.05 \text{ lstat} - 0.13 \text{ ptratio}
                    -2.2 \text{ nox} + 0.006 \text{ zn} - 0.01 \text{ crim}
  Rule 2/9: [14 cases, mean 43.48, range 22.8 to 50, est err 5.55]
    if
         age > 71
         lstat <= 5.12
    then
         outcome = -24.48 + 1.99 \text{ crim} + 0.467 \text{ age} + 3.5 \text{ rm}
Model 3:
  Rule 3/1: [88 cases, mean 13.81, range 5 to 27.5, est err 2.29]
    if
         nox > 0.668
    then
         outcome = -12.77 + 5.44 \text{ dis} + 22.7 \text{ nox} - 0.18 \text{ lstat} + 0.013 \text{ b}
                    -0.07 crim
  Rule 3/2: [10 cases, mean 17.64, range 11.7 to 27.5, est err 11.51]
    if
         nox <= 0.668
         b <= 179.36
         outcome = -2.19 + 0.149 + 0.76 lstat
  Rule 3/3: [156 cases, mean 19.68, range 8.1 to 33.8, est err 2.23]
    if
         nox <= 0.668
         1stat > 9.53
         outcome = 28.86 - 1.08 dis - 0.27 lstat - 0.067 age + 2.6 rm
                    - 0.62 ptratio
  Rule 3/4: [164 cases, mean 29.68, range 11.9 to 50, est err 3.44]
    if
         1stat <= 9.53
    then
         outcome = 6.37 + 4.09 \text{ crim} - 0.75 \text{ lstat} + 7.6 \text{ rm} - 0.0303 \text{ tax}
                    - 0.78 ptratio - 0.14 dis - 2.2 nox + 0.001 b
Model 4:
  Rule 4/1: [335 cases, mean 19.44, range 5 to 50, est err 2.60]
    if
```

```
rm <= 7.079
        lstat > 5.12
    then
        outcome = 50.33 - 0.0168 \text{ tax} - 0.39 \text{ lstat} + 0.32 \text{ rad} - 12.7 \text{ nox}
                   - 0.65 ptratio - 0.59 dis - 0.11 crim
  Rule 4/2: [18 cases, mean 30.49, range 22.5 to 50, est err 4.90]
    if
        rm <= 6.861
        lstat <= 5.12
        outcome = 20.98 + 8.17 crim - 0.54 lstat + 0.23 rad + 1.3 rm
  Rule 4/3: [5 cases, mean 31.10, range 13.8 to 50, est err 24.23]
    if
        dis <= 1.2852
        lstat > 5.12
    then
        outcome = 36.25
  Rule 4/4: [35 cases, mean 36.15, range 22.5 to 50, est err 3.57]
    if
        age <= 71
        lstat <= 5.12
    then
        outcome = -67.2 + 15.9 \text{ rm} - 1.04 \text{ rad} - 0.005 \text{ b} - 0.05 \text{ lstat} - 0.05 \text{ dis}
  Rule 4/5: [43 cases, mean 39.37, range 15 to 50, est err 6.47]
    if
        rm > 7.079
    then
        outcome = -132.71 + 0.323 b + 9.1 rm - 0.48 rad - 1.4 ptratio
                   - 0.0015 tax - 0.03 lstat
  Rule 4/6: [14 cases, mean 43.48, range 22.8 to 50, est err 5.19]
    if
        age > 71
        lstat <= 5.12
        outcome = -34.38 + 0.6 age -0.75 lstat + 6.1 rm -0.047 b + 0.16 rad
Model 5:
  Rule 5/1: [86 cases, mean 13.32, range 5 to 23.2, est err 2.71]
    if
```

```
nox > 0.659
        1stat > 9.53
    then
         outcome = -28.42 + 7.76 \text{ dis} + 35.5 \text{ nox} + 0.017 \text{ b} - 0.12 \text{ lstat}
                    - 0.18 ptratio + 0.4 rm - 0.01 age - 0.03 crim + 0.02 rad
                    - 0.0006 tax
  Rule 5/2: [154 cases, mean 19.76, range 8.1 to 33.8, est err 2.34]
    if
        nox <= 0.659
        lstat > 9.53
    then
        outcome = 32.87 - 1.36 dis - 0.1 age + 2.5 rm - 0.68 ptratio - 0.1 lstat
                    -2.8 \text{ nox} - 0.03 \text{ crim} + 0.002 \text{ b} + 0.01 \text{ rad}
  Rule 5/3: [138 cases, mean 28.31, range 16.5 to 50, est err 2.52]
    if
         dis > 2.6403
        1stat <= 9.53
    then
         outcome = -34.37 + 11.1 \text{ rm} + 0.81 \text{ crim} - 0.2 \text{ lstat} - 0.0064 \text{ tax}
                    - 0.03 age - 0.3 ptratio - 0.17 dis + 0.03 rad - 2.2 nox
                    + 0.002 b
  Rule 5/4: [26 cases, mean 36.97, range 11.9 to 50, est err 11.81]
    if
         dis <= 2.6403
        lstat <= 9.53
    then
        outcome = -1.18 + 2.48 \text{ crim} + 3.6 \text{ rm}
  Rule 5/5: [21 cases, mean 41.33, range 21.9 to 50, est err 10.93]
    if
        nox > 0.573
        1stat <= 9.53
    then
         outcome = 61.04 + 4.95 crim - 51.6 nox - 0.0226 tax - 0.48 lstat
                    + 4.3 rm - 0.64 ptratio
Evaluation on training data (404 cases):
    Average |error|
                                       1.94
    Relative |error|
                                       0.29
    Correlation coefficient
                                       0.96
```

#### Attribute usage: Conds Model 75% 98% lstat 45% 61% nox 28% 70% rm16% 86% dis 14% 90% ptratio 13% 76% crim 5% 48% 4% 58% age 49% b 38% rad 11% indus 4% zn

Time: 0.1 secs

For this model:

```
> cmPred <- predict(committeeModel, testPredictors)
> ## RMSE
> sqrt(mean((cmPred - testOutcome)^2))
[1] 2.863727
> ## R^2
> cor(cmPred, testOutcome)^2
[1] 0.8967124
```

## 4 Instance–Based Corrections

Another innovation in Cubist is the use of a nearest–neighbor to adjust the predictions from the rule–based model. First, a model tree (with or without committees) is created. Once a sample is predicted by this model, Cubist can find it's nearest neighbors and determine the average of these training set points. See Quinlan (1993a) for the details of the adjustment.

The development of rules and committees is independent of the choice of using instances. The original C code allowed the program to choose whether to use instances, not use them or let the program decide. Our approach is to build a model with the cubist function that is ignorant to the decision about instances. When samples are predicted, the argument neighbors can be used to adjust the rule—based model predictions (or not).

We can add instances to the previously fit committee model:

```
> instancePred <- predict(committeeModel, testPredictors, neighbors = 5)
> ## RMSE
> sqrt(mean((instancePred - testOutcome)^2))
[1] 2.685944
> ## R^2
> cor(instancePred, testOutcome)^2
[1] 0.9125262
```

Note that the previous models used the implicit default of neighbors = 0 for their predictions.

To tune the model over different values of neighbors and committees, the train function in the caret package can be used to optimize these parameters.

# 5 Exporting the Model

As previously mentioned, this code is a port of the command—line C code. To run the C code, the training set data must be converted to a specific file format as detailed on the RuleQuest website. Two files are created. The file.data file is a header—less, comma delimited version of the data (the file part is a name given by the user). The file.names file provides information about the columns (eg. levels for categorical data and so on). After running the C program, another text file called file.models, which contains the information needed for prediction.

Once a model has been built with the R cubist package, the exportCubistFiles can be used to create the .data, .names and .model files so that the same model can be run at the command-line.

## 6 Current Limitations

There are a few features in the C code that are not yet operational in the R package:

- variable usage/importance haven't been ported into R objects
- only continuous and categorical predictors can be used (the C allows for other data types)
- there is an option to let the C code decide on using instances or not. The choice is more explicit in this package
- non-standard name are not currently checked
- the C code supports binning of predictors

Many of these features will be implemented in the future.

# 7 About the Cubist C Code and Our Approach

This section may be interesting or important to those of you who care about the implementation (if you exist at all).

The cubist sources are written to take specific data files from the file system, pull them into memory, run the computations, then write the results to a text file that is also saved to the file system. The code makes use of a lot of global variables (especially for the data). The code has been around for a while and, after reading it, one can tell that the author put in a lot of time to catch many special cases. At Pfizer, we have pushed millions of samples through the non–GPL code without any substantive errors.

So the approach here is to pass in the training data as strings that mimic the formats that one would use with the command line version and get back the textual representation that would be saved to the .model file also as a string. The prediction function would then pass the model text string (and the data text string if instances are used) to the C code for prediction.

We did this for a few reasons. First, this approach would require us to re—write main() and touch as little of the original code as possible (otherwise we would have to write a parser for the data and try to get it into the global variable structure with complete fidelity). Second, most modeling functions implicitly assume that the data matrix is all numeric, thus factors are converted to dummy variables etc. Cubist doesn't want categorical data split into dummy variables based on how it does splits. Thus, we would have to pass in the numeric and categorical predictors separately unless we want to get really fancy.

## 8 Session Information

- R version 2.11.1 (2010-05-31), x86\_64-apple-darwin9.8.0
- Locale: en\_US.UTF-8/en\_US.UTF-8/C/C/en\_US.UTF-8/en\_US.UTF-8
- Base packages: base, datasets, graphics, grDevices, methods, stats, utils
- Other packages: Cubist 0.02, lattice 0.18-8, mlbench 2.1-0, reshape2 1.1
- Loaded via a namespace (and not attached): grid 2.11.1, plyr 1.2.1, stringr 0.4, tools 2.11.1

#### 9 References

Quinlan. Learning with continuous classes. Proceedings of the 5th Australian Joint Conference On Artificial Intelligence (1992) pp. 343-348

- Quinlan. Combining instance-based and model-based learning. Proceedings of the Tenth International Conference on Machine Learning (1993a) pp. 236-243
- Quinlan. C4.5: Programs For Machine Learning (1993b) Morgan Kaufmann Publishers Inc. San Francisco, CA
- Wang and Witten. Inducing model trees for continuous classes. Proceedings of the Ninth European Conference on Machine Learning (1997) pp. 128-137

http://rulequest.com/cubist-info.html