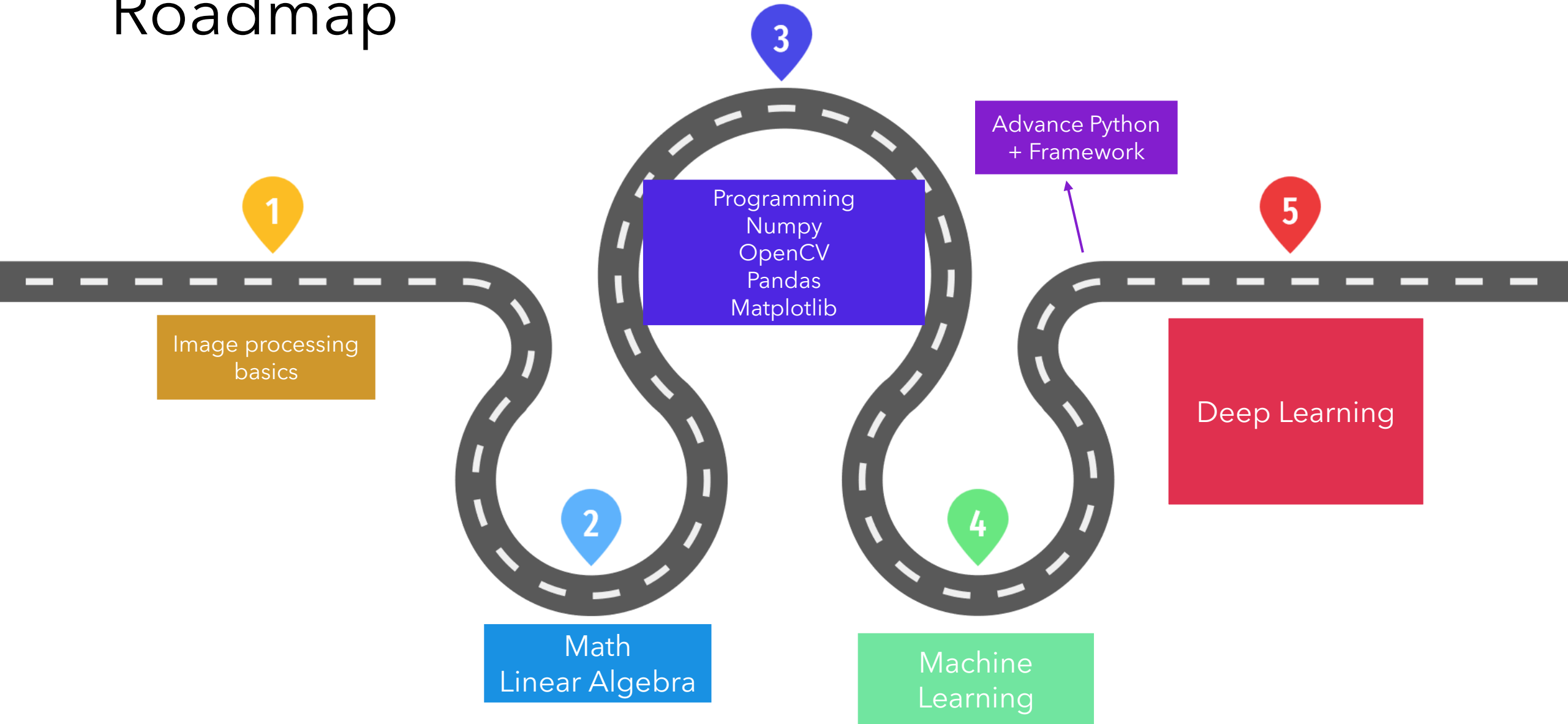


Computer Vision

CVI620

Session 16
03/2025

Roadmap



What is Left?

11 sessions

1. Optimization and Loss Function
2. Code + Logistic Regression
3. ML and Images
4. Perceptron and Neural Networks
5. Deep Neural Networks
6. Convolution Neural Networks (CNN)
7. Advanced CNNs
8. Project
9. Segmentation
10. Introduction to object detection and image generation methods with AI
11. Project

Agenda

Multiple Linear
Regression

Optimization

Gradient Descend

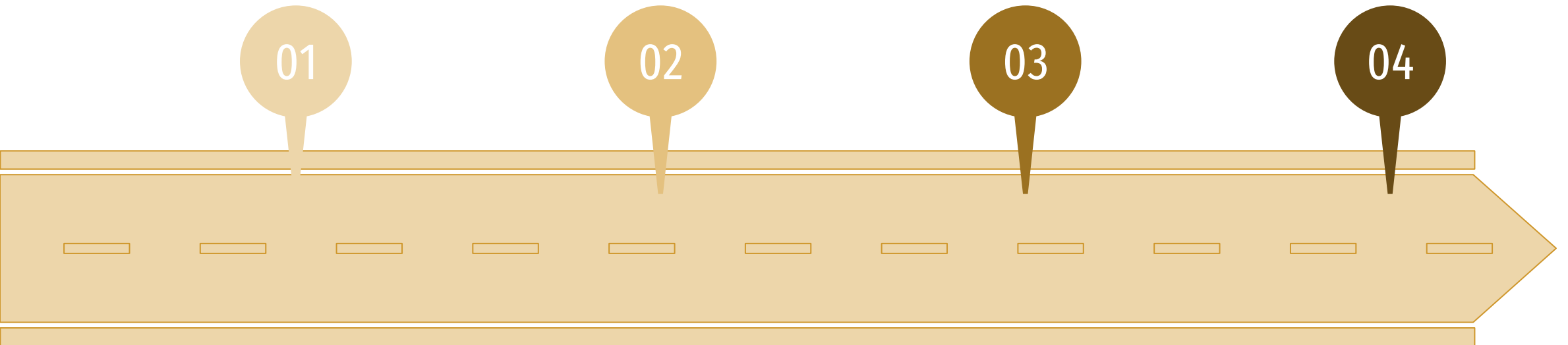
Example
Code

01

02

03

04



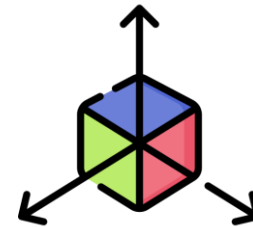
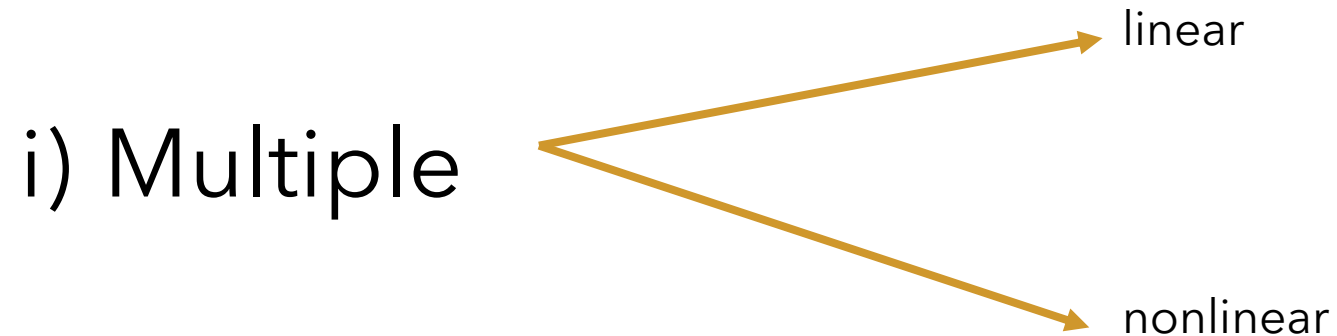
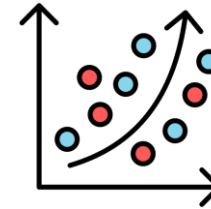
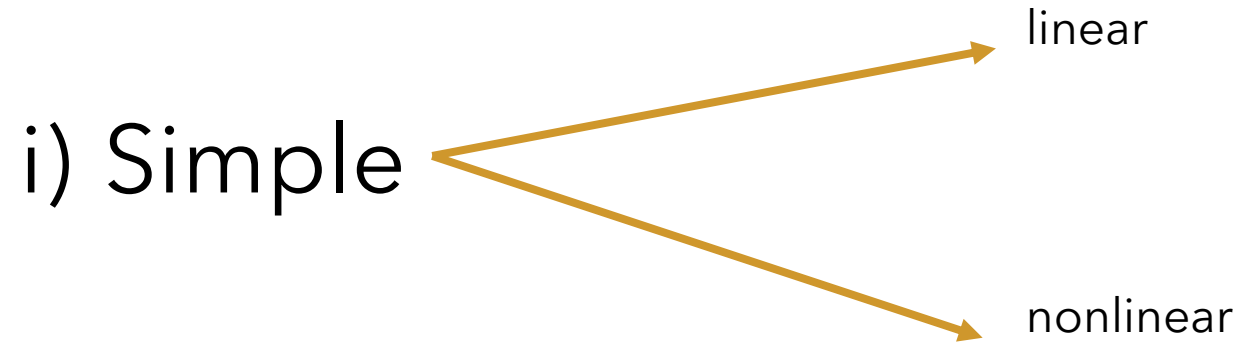
Difficult





Questions from Session 15 Videos?

Regression



Polynomial

Simple vs Multiple

Simple
Linear
Regression

$$y = b_0 + b_1 * x_1$$

Multiple
Linear
Regression

$$y = b_0 + b_1 * x_1 + b_2 * x_2 + \dots + b_n * x_n$$

Simple vs Multiple

Simple
Linear
Regression

$$y = b_0 + b_1 * x_1$$

Multiple
Linear
Regression

$$y = b_0 + b_1 * x_1 + b_2 * x_2 + \dots + b_n * x_n$$

Still calculate derivative and
solve variable values!

Multiple Linear Regression

```
import pandas as pd
import numpy as np
from sklearn.model_selection import train_test_split
from sklearn.linear_model import LinearRegression
from sklearn.metrics import mean_absolute_error, mean_squared_error

dataset = pd.read_csv('S16/petrol_consumption.csv')
X = dataset[['Petrol_tax', 'Average_income', 'Paved_Highways', 'Population_Driver_licence(%)']]
y = dataset['Petrol_Consumption']

X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)

regressor = LinearRegression()
regressor.fit(X_train, y_train)
coeff_df = pd.DataFrame(regressor.coef_, X.columns, columns=['Coefficient'])
print(coeff_df)

y_pred = regressor.predict(X_test)
df = pd.DataFrame({'Actual': y_test, 'Predicted': y_pred})

print('Mean Absolute Error:', mean_absolute_error(y_test, y_pred))
print('Mean Squared Error:', mean_squared_error(y_test, y_pred))
```



Problem

- Some datasets have millions of features -> impossible to calculate
- They are not always linear
- Some problems do not have closed form formulas

Problem

- Some datasets have millions of features -> impossible to calculate
- They are not always linear
- Some problems do not have closed form formal

Solution -> Optimization

Optimization



Start random in space

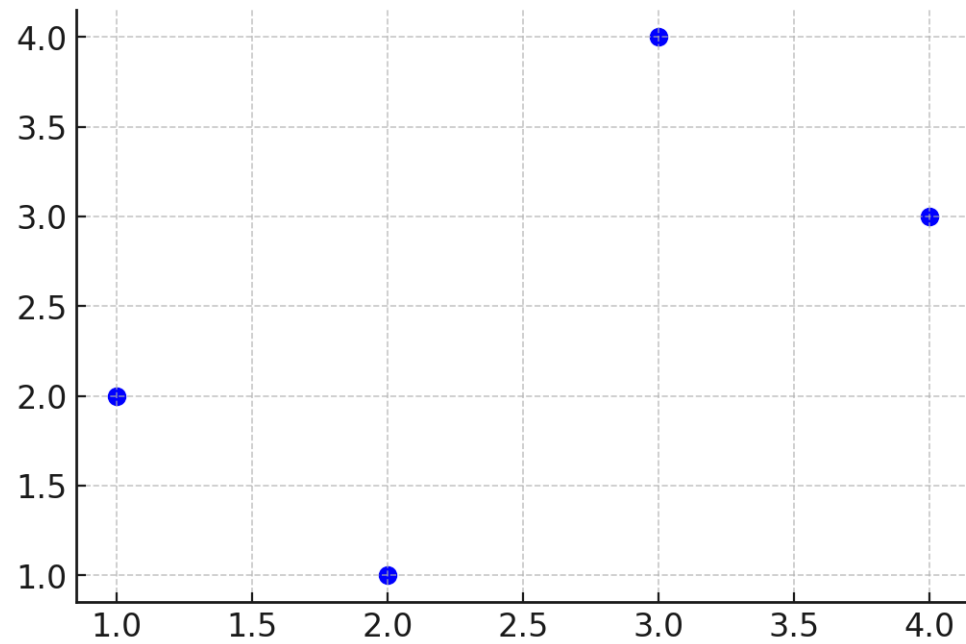


Take gradual steps towards
your goal

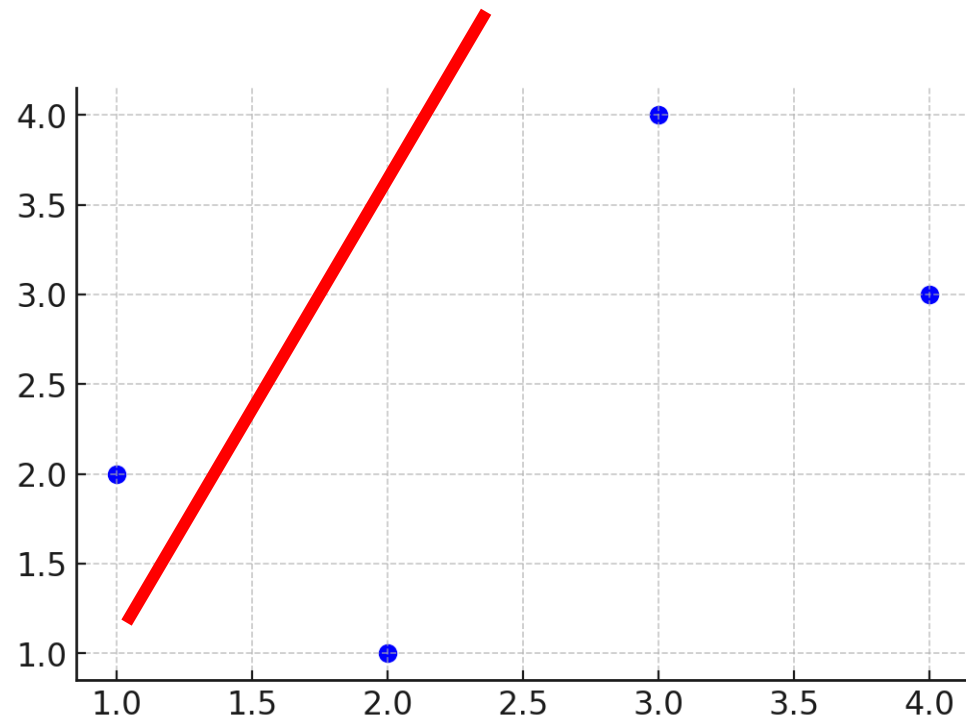


Not the best best answer but
a solution close to the best

Example

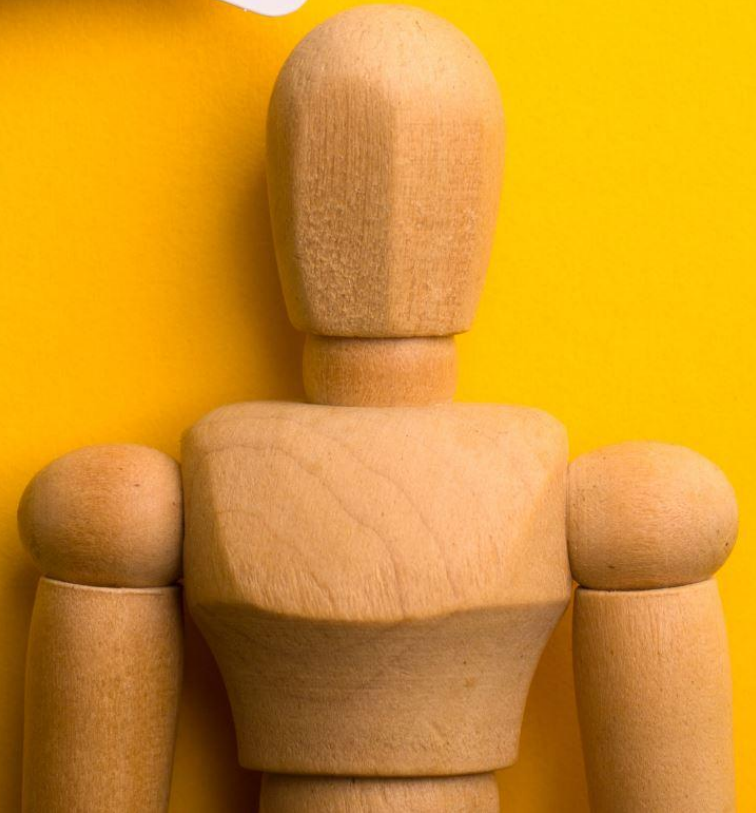


Example



—

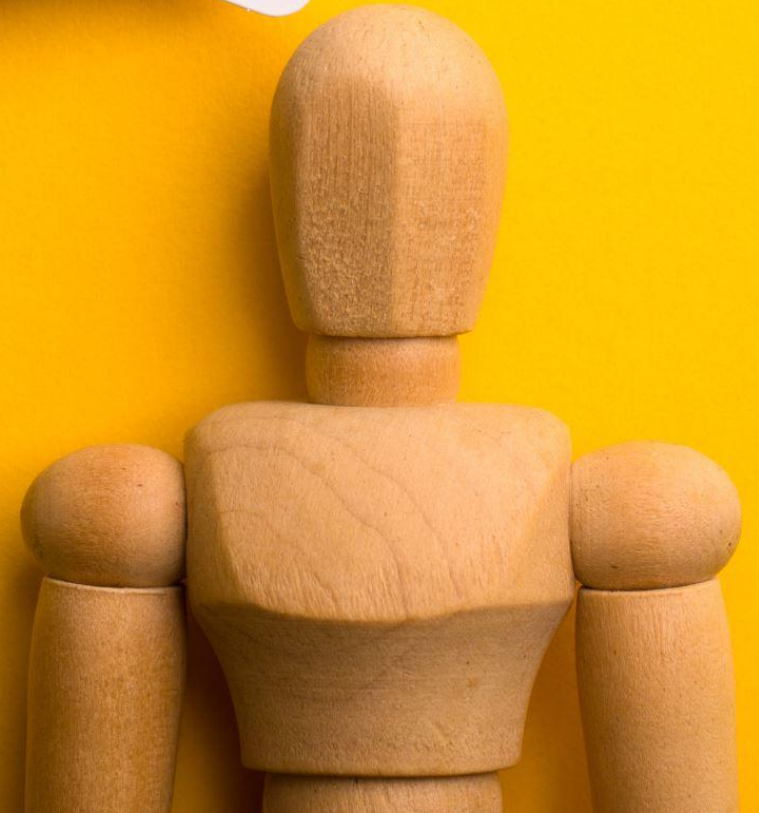
What is our goal?



What is our goal?

Minimize loss

Gain parameter values

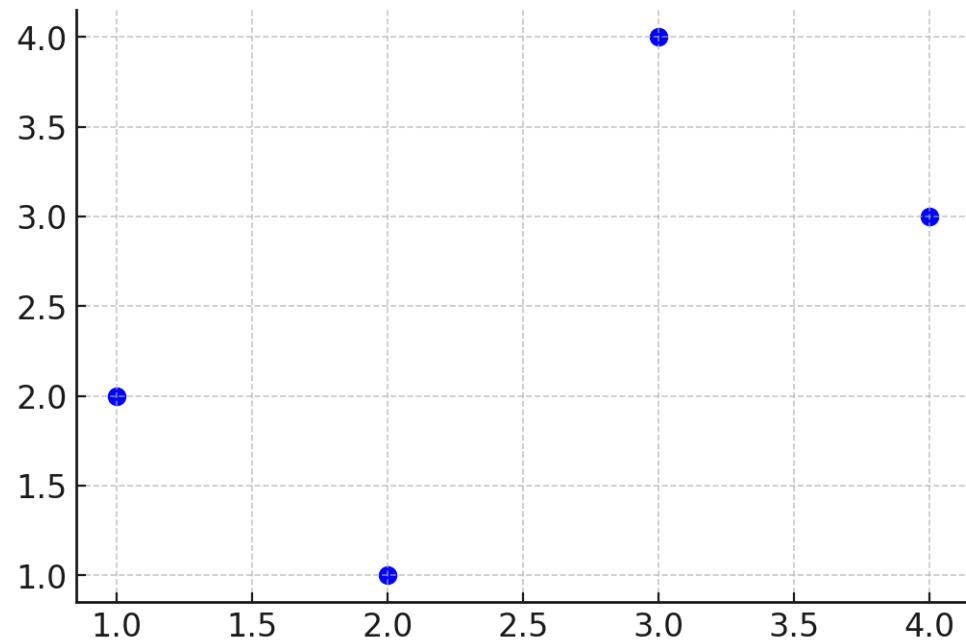


What Was Loss?

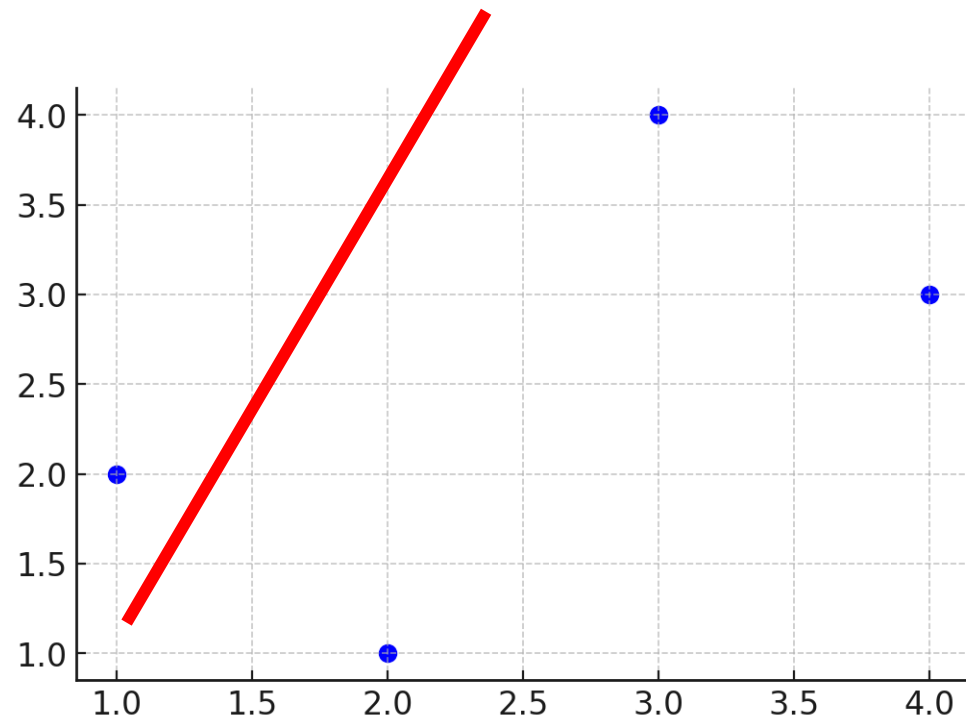
- MSE (mean squared error)

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$

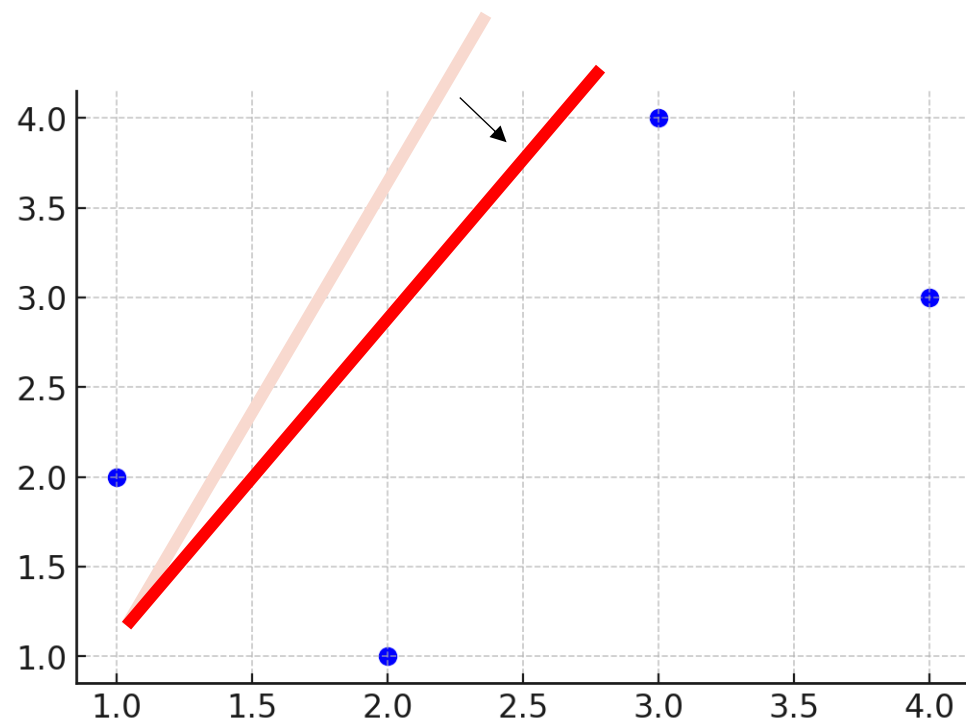
Example



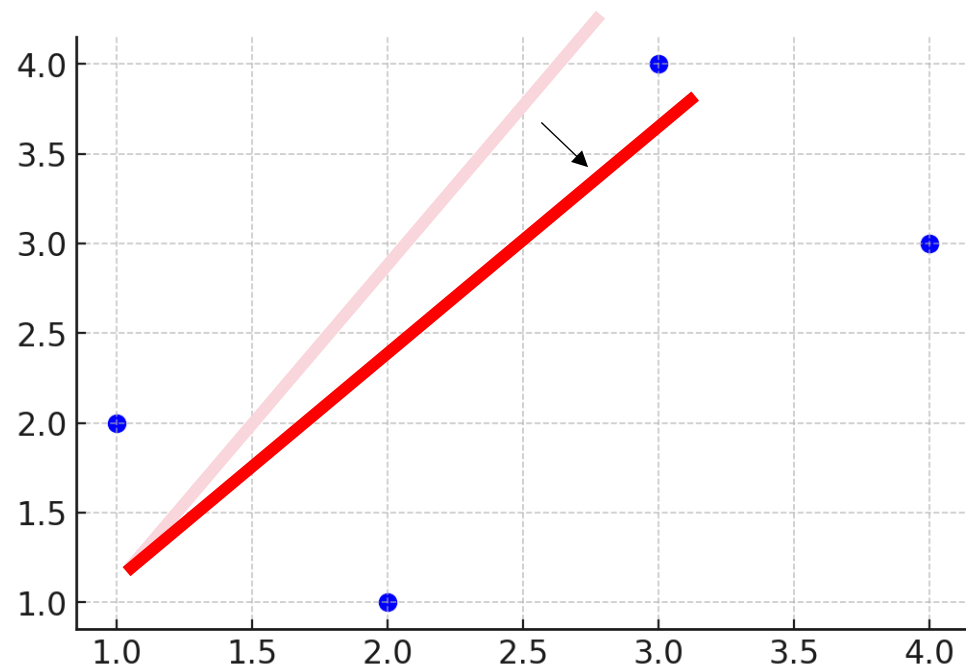
Example



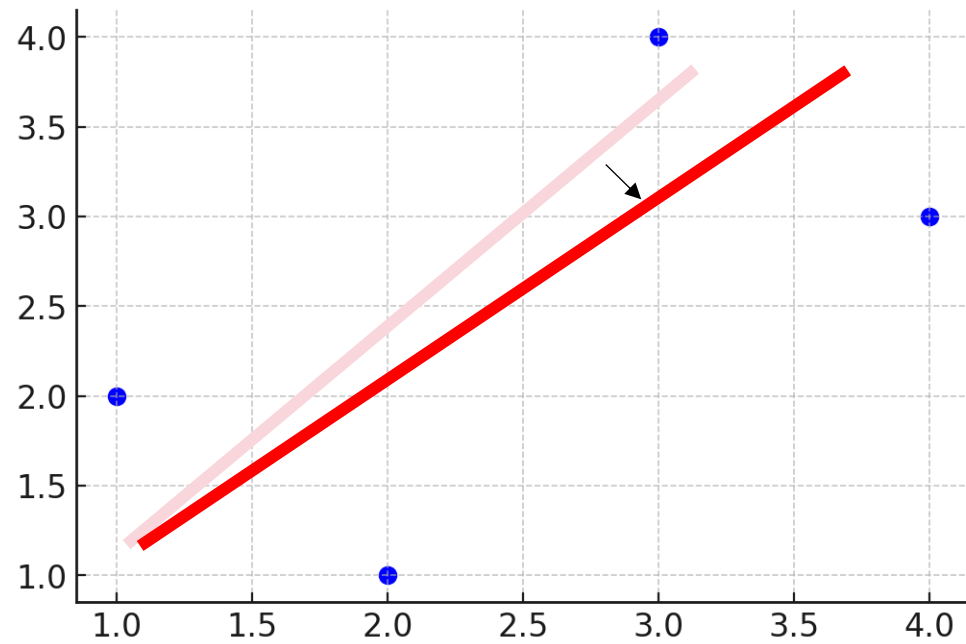
Example



Example



Example

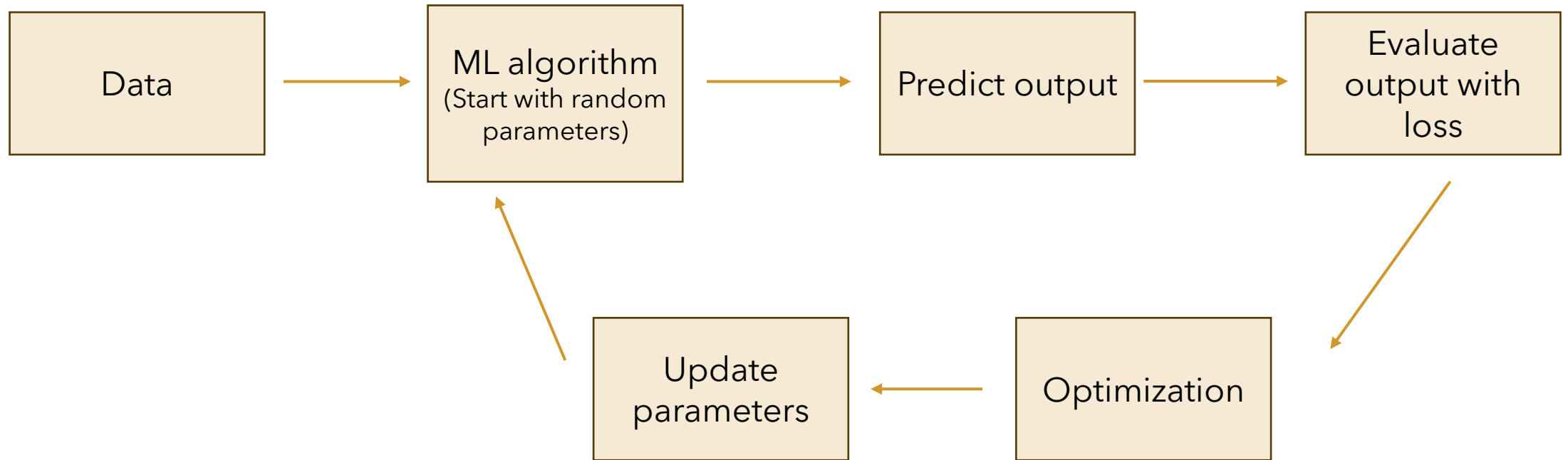




Mathematically How?

- We should solve this mathematically
- But how?

Framework



Optimization Algorithms

- Gradient Descend
- Stochastic Gradient Descend
- Adam
- AdamW
- RMSProp
- Newton's Method

Gradient Descend

- The problem was how we get to update the line in LR

Gradient Descend

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- Gradient descend does this with calculating derivatives again!

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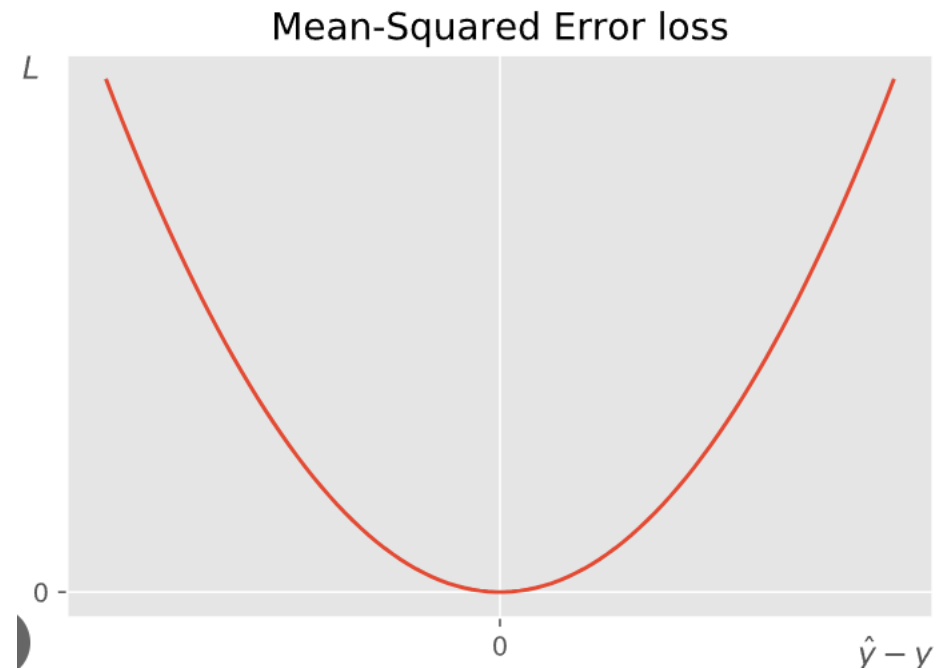
Gradient Descend

- The problem was how we get to update the line in LR
- Gradient descend does this with calculating derivatives again!
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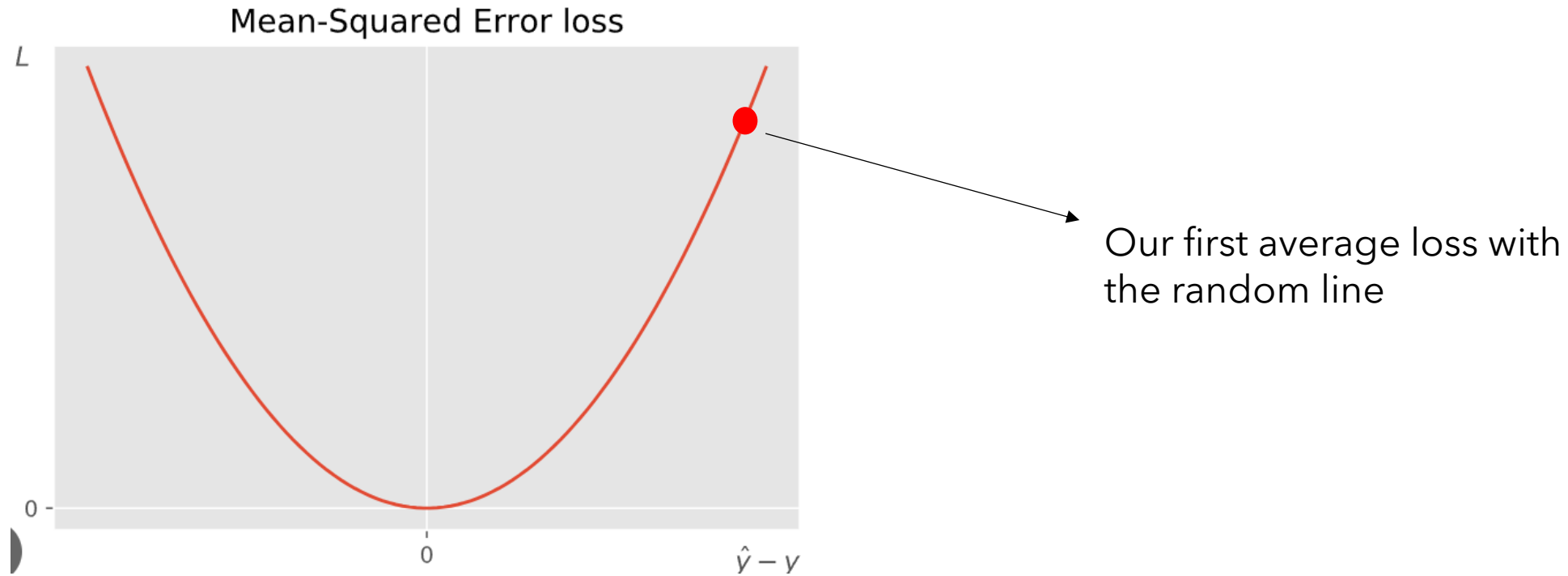
But what do we mean?

opposite direction of parameter derivatives
with respect to loss!

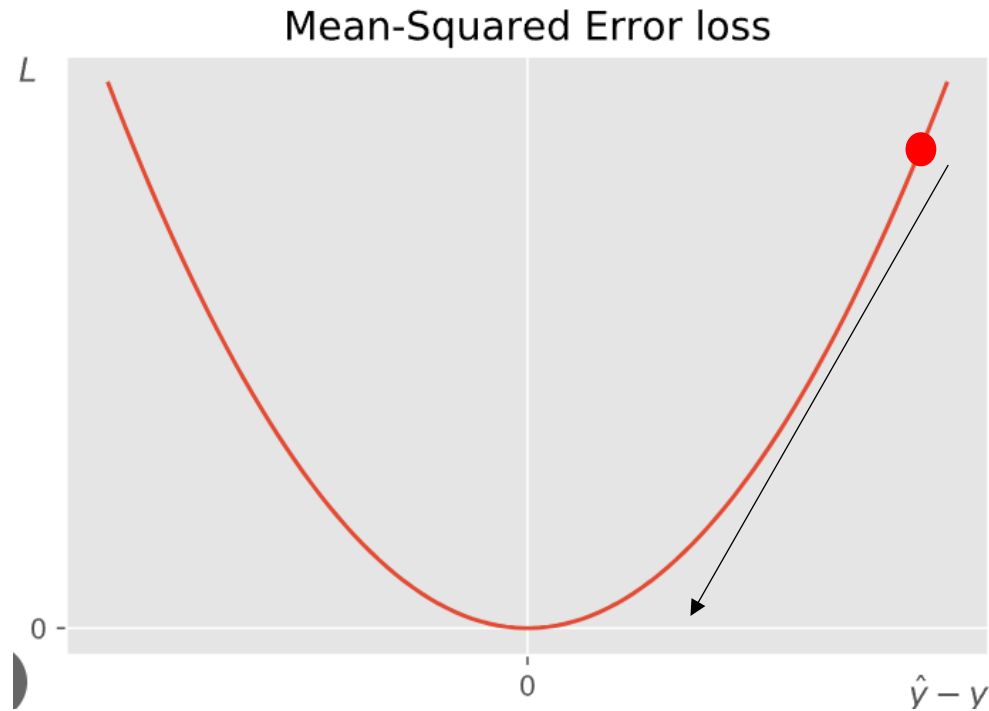
$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$



opposite direction of parameter derivatives with respect to loss!

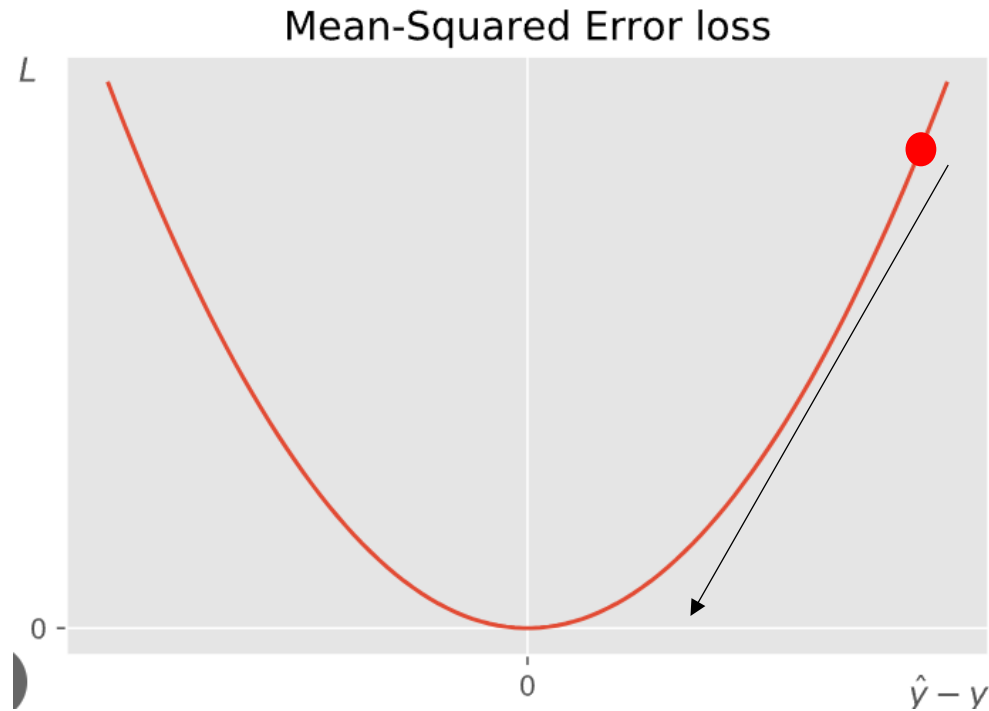


opposite direction of parameter derivatives with respect to loss!



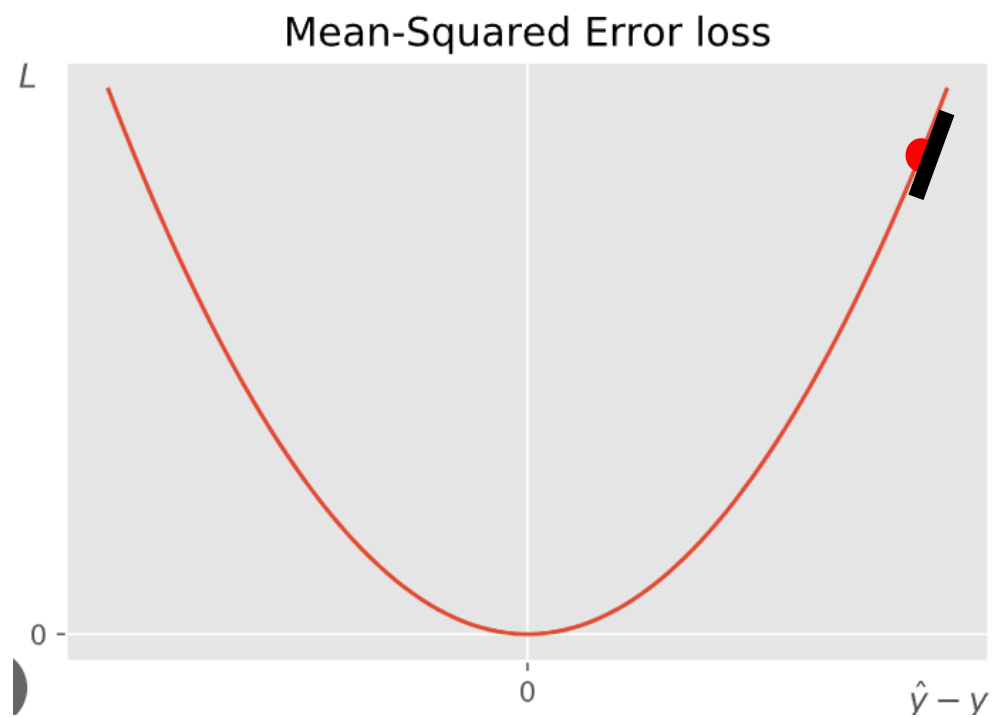
We want this loss to be as
close as to 0

opposite direction of parameter derivatives with respect to loss!

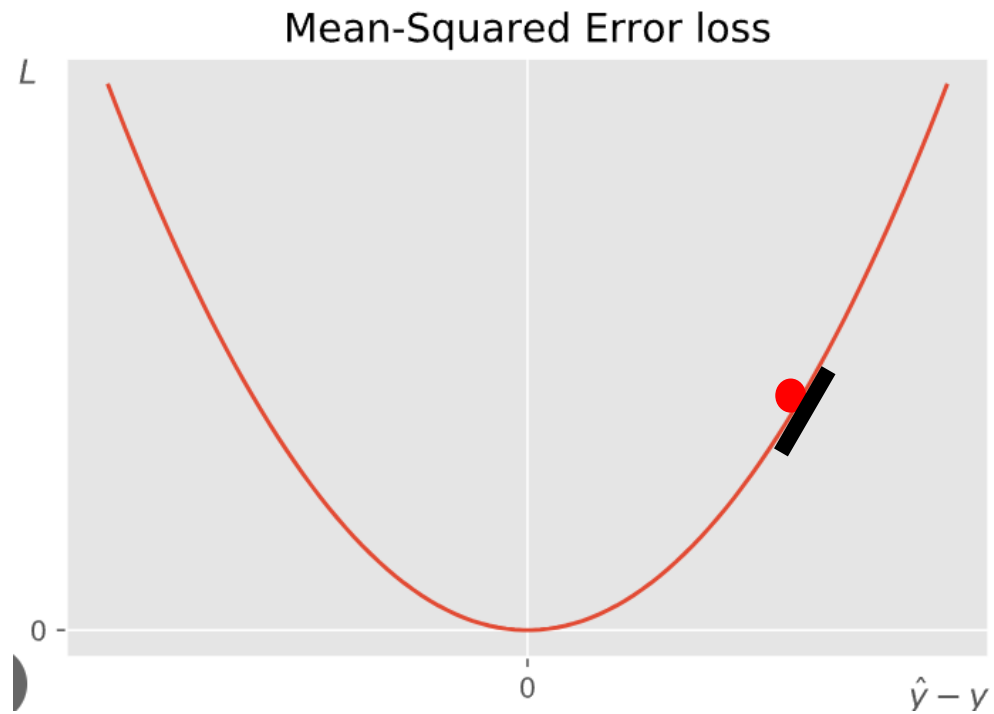


In order to move towards that direction, we have to move in the opposite direction of slope (derivate)

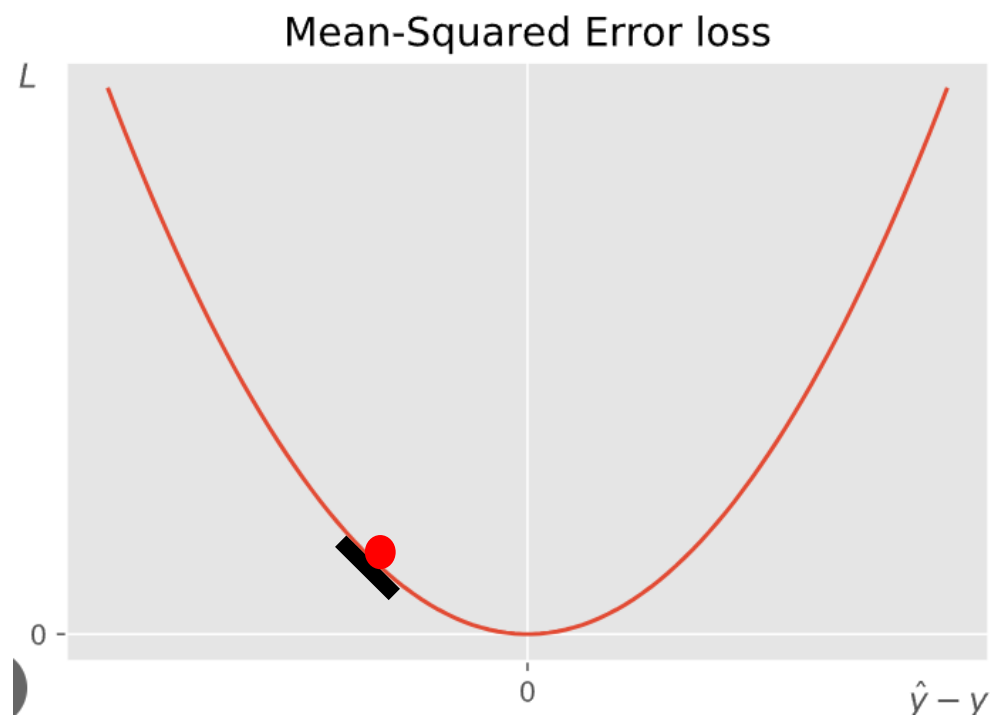
opposite direction of parameter derivatives
with respect to loss!



opposite direction of parameter derivatives
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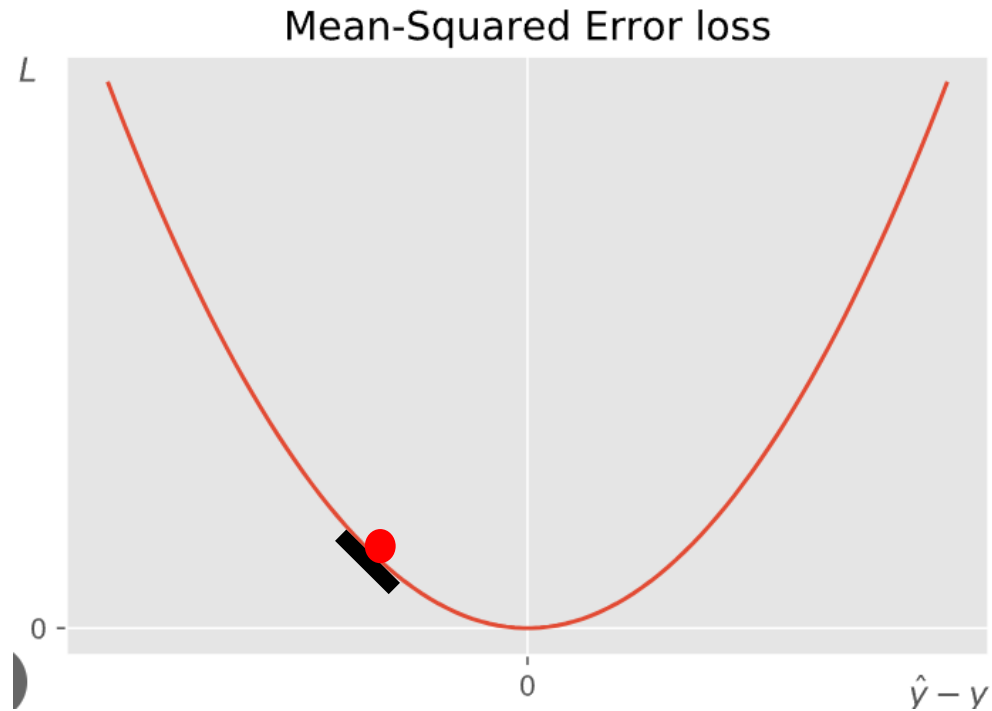


opposite direction of parameter derivatives
with respect to loss!



$$w^+ = w^- - \frac{\partial L}{\partial w}$$

opposite direction of parameter derivatives
with respect to loss!



$$w^+ = w^- - \alpha \frac{\partial L}{\partial w}$$

Now let's see mathematically!

- opposite direction of **parameter derivatives** with respect to loss!
- Loss is calculated:

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$

Now let's see mathematically!

- opposite direction of **parameter derivatives** with respect to loss!
- Loss is calculated:

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$

Given in data

$2x+4$

Now let's see mathematically!

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$

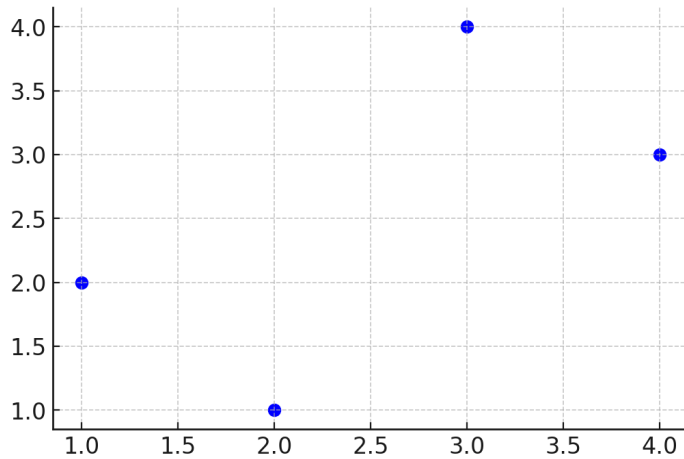
Given in data

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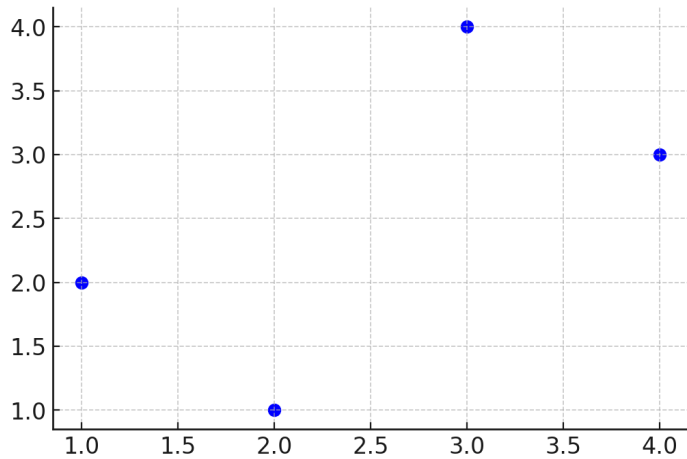
Data = (1,2), (2,1), (3,4), (4,3)
 $y' = 2x + 4$



$$\text{Loss} = [(2-6)^2 + (1-8)^2 + (4-10)^2 + (3-12)^2] / 4 = [16 + 49 + 36 + 81] / 4 = 45.5$$

Now let's see mathematically!

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$



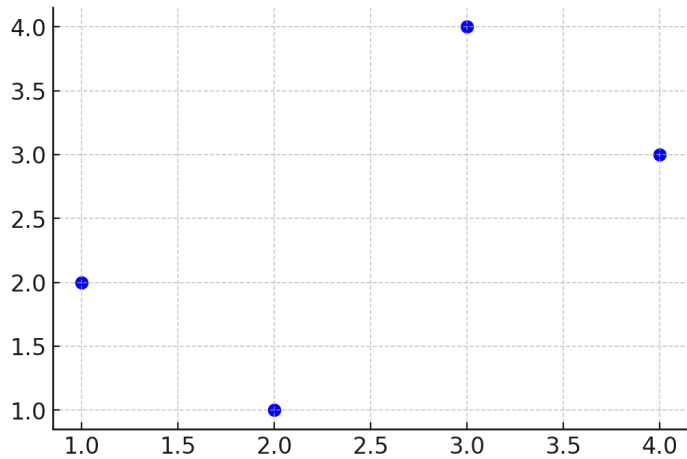
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$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (y - (ax + b))^2$$

Now let's see mathematically!

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$



Data = (1,2), (2,1), (3,4), (4,3)
 $y' = 2x + 4$

$$\text{Loss} = [(2-6)^2 + (1-8)^2 + (4-10)^2 + (3-12)^2] / 4 = [16 + 49 + 36 + 81] / 4 = 45.5$$

$$E = \frac{1}{n} \sum_{i=0}^n (y_i - (mx_i + c))^2$$

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$$D_m = \frac{1}{n} \sum_{i=0}^n 2(y_i - (mx_i + c))(-x_i)$$

$$D_m = \frac{-2}{n} \sum_{i=0}^n x_i(y_i - \bar{y}_i)$$

$$m = m - \alpha \times D_m$$

$$D_c = \frac{-2}{n} \sum_{i=0}^n (y_i - \bar{y}_i)$$

$$c = c - \alpha \times D_c$$

$$E = \frac{1}{n} \sum_{i=0}^n (y_i - (mx_i + c))^2$$

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$$D_m = \frac{-2}{n} \sum_{i=0}^n x_i(y_i - \bar{y}_i)$$

$$m = m - \alpha \times D_m$$

$$\text{new } m = 2 - 0.01 \times 2 = 0.02$$

$$D_c = \frac{-2}{n} \sum_{i=0}^n (y_i - \bar{y}_i)$$

$$c = c - \alpha \times D_c$$

$$\text{new } c = 4 - 0.01 \times 2 = 2.02$$

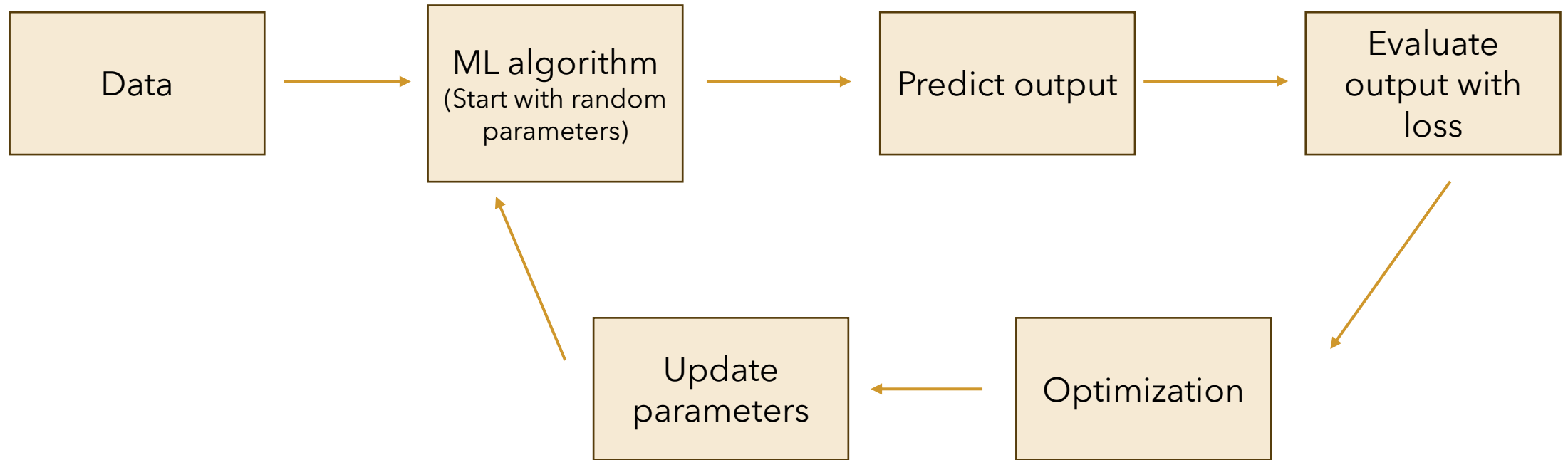
$$y = 0.02x + 2.02$$

New line: $y = 0.02x + 2.02$

Previous line: $y = 2x + 4$

Best fitted line: $y = x + 0.6$

Framework





Code