Reference Manual

Release 10.3

The Sage Development Team

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Here you find documentation for all of Sage's features, illustrated with lots of examples. A thematic index follows.

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