

Contents

1	Util	2
1.1	GCD	2
1.2	LCM	2
1.3	Bezout's identity	2
1.4	Digit sum	2
1.5	Musical chairs	3
2	Primality	4
2.1	Primality testing : simple	4
2.2	Prime factors	4
3	Congruences	5
3.1	Linear congruence	5

1 Util

1.1 GCD

GCD by Euclid's algorithm.

Requires math.

```
1 //If you need it for long values, remember to change abs to labs
2 int gcd(int x, int y){return y ? gcd(y, x % y) : abs(x);}
```

1.2 LCM

Requires 1.1 gcd.

```
1 typedef long long ll;
2 ll lcm(int x, int y){
3     if(x && y) return abs(x) / gcd(x,y) * ll(y);
4 }
```

1.3 Bezout's identity

Find some a and b such that $ax + by = \gcd(x, y)$

Requires utility

```
1 typedef pair<int, int> bezout;
2
3 bezout find_bezout(int x, int y){
4     if(y == 0) return bezout(1,0);
5     bezout u = find_bezout(y, x % y);
6     return bezout(u.second, u.first - (x/y) * u.second);
7 }
```

1.4 Digit sum

Find the sum of all decimal digits present in some interval $a < b < 10^9$.

```
1 #include <cstdio>
2
3 int c[2][10], pow10[10];
4 void count(int x, int *cnt){
5     int d, dcnt = 0, r = 0, rem0 = 0, v;
6     while(x){
7         d = x % 10; x /= 10;
```

```

8         if(dcnt){
9             v = d * pow10[dcnt - 1] * dcnt;
10            for(int i = 0; i < 10; ++i) cnt[i] += v;
11            if(!d) rem0 += (pow10[dcnt] - 1) - r;
12        }
13        v = pow10[dcnt];
14        for(int i = 1; i < d; ++i) cnt[i] += v;
15        if(d) cnt[d] += r + 1;
16        r = pow10[dcnt++] * d + r;
17    }
18    cnt[0] -= rem0;
19 }
20
21 int main(void){
22     pow10[0] = 1;
23     for(int i = 1; i < 10; ++i)
24         pow10[i] = 10 * pow10[i - 1];
25     for(int a, b; scanf("%d %d", &a, &b) == 2 && a && b;){
26         long long ans = 0;
27         for(int i = 0; i < 10; ++i)
28             c[0][i] = c[1][i] = 0;
29         count(b, c[1]);
30         count(a - 1, c[0]);
31         for(int i = 1; i < 10; ++i)
32             ans += (long long)i * (c[1][i] - c[0][i]);
33         printf("%lld\n", ans);
34     }
35     return 0;
36 }

```

1.5 Musical chairs

N children are seated on N chairs arranged around a circle. The chairs are numbered from 1 to N . Your program pre-selects a positive number D . The program starts going in circles counting the children starting with the first chair. Once the count reaches D , that child leaves the game, removing his/her chair. The program starts counting again, beginning with the next chair in the circle. The last child remaining in the circle is the winner. Given N and D determine the winner.

```

1 // :3
2
3 #include <stdio>
4

```

```

5 | int dp[1048576];
6 | int main(void){
7 |     dp[1] = 0;
8 |     for(int d, i, n; scanf("%d %d", &n, &d) == 2 && (n || d); ){
9 |         for(i = 2; i <= n; ++i) dp[i] = (dp[i - 1] + d) % i;
10 |        printf("%d %d %d\n", n, d, dp[n] + 1);
11 |    }
12 |    return 0;
13 | }

```

2 Primality

2.1 Primality testing : simple

Requires math.

```

1 | bool is_prime(int n){
2 |     if(n < 0) return is_prime(-n);
3 |     if(n < 5 || n % 2 == 0 || n % 3 == 0) return (n == 2 || n == 3);
4 |     int maxP = sqrt(n) + 2;
5 |     for(int p = 5; p < maxP; p += 6)
6 |         if(n % p == 0 || n % (p+2) == 0 ) return false;
7 |     return true;
8 | }

```

2.2 Prime factors

Squeeze the prime factors out of n .

Requires math.

```

1 | typedef map<int,int> prime_map;
2 |
3 | void squeeze(prime_map &M, int &n, int p) {for(; n % p == 0; n /= p)M[p]++;}
4 | prime_map factor(int n){
5 |     prime_map M;
6 |     if(n < 0)
7 |         return factor(-n);
8 |     if(n < 2)
9 |         return M;
10 |    squeeze(M, n, 2); squeeze(M, n, 3);
11 |    int maxP = sqrt(n) + 2;
12 |    for(int p = 5; p < maxP; p += 6){

```

```
13     squeeze(M, n, p); squeeze(M, n, p+2);
14 }
15 if(n > 1)M[n]++;
16 return M;
17 }
```

3 Congruences

3.1 Linear congruence

Find the lowest non-negative solution to $ax \equiv b \pmod{m}$

Requires 1.3 find_bezout

```
1  /*
2   *   Find the lowest non-negative solution to  $a*x = b \pmod{m}$ 
3   *   Return -1 if the congruence is not possible.
4   */
5  int mod(int x, int m){return x % m + (x < 0) ? m : 0;}
6
7  int solve_mod(int a, int b, int m){
8      if(m < 0) return solve_mod(a, b, -m);
9      if(a < 0 || a >= m || b < 0 || b >= m)
10         return solve_mod(mod(a, m), mod(b, m), m);
11      bezout t = find_bezout(a, m);
12      int d = t.first * a + t.second * m;
13      if(b % d) return -1;
14      else return mod(t.first * (b / d), m);
15 }
```