

-  $E(Y) = \mu_Y$       SUMPRODUCT()

-  $Var(Y) = \sigma_Y^2 = E[(Y - \mu_Y)^2] = E[(Y - E(Y))^2]$



	H	T	$f(y) \leftarrow$ marg. distr.
H	1/4	1/4	1/2
T	1/4	1/4	1/2
$f(x)$	1/2	1/2	1

marginal distr.

Conditional

$f(x|y)$

$$f(x|y=H) = \frac{1/4}{1/2} = \begin{cases} 1/2 \\ 1/2 \end{cases}$$

independence: marginal = conditional i.e.  $f(x) = f(x|y)$

-  $COV(X, Y) = E[(X - \mu_X)(Y - \mu_Y)]$

- Correlation =  $\frac{COV(X, Y)}{\sigma_X \sigma_Y}$

### Sampling

- i.i.d

-  $\bar{Y}$  - simple (equal weighted) avg.      mean      var.

-  $Y \sim (\mu_Y, \sigma_Y^2) \Rightarrow \bar{Y} \sim N(\mu_Y, \frac{\sigma_Y^2}{n})$

$$- \frac{\bar{Y} - \mu_Y}{\sqrt{\frac{\sigma_Y^2}{n}}} \sim N(0, 1) \quad \text{aka std. normal} \\ \text{aka } z \text{ score}$$

$$- \text{when } n \text{ small } (n < 30) \quad \frac{\bar{Y} - \mu_Y}{\sqrt{\frac{\sigma_Y^2}{n}}} \sim t_{n-1}$$

-  $z$  - 95% obs. are between -1.96  $\sigma$ 's and 1.96  $\sigma$ 's

-  $t$  - 95% obs are between -C.V. and C.V.

$$|C.V.| > 1.96$$

see statistical table for exact C.V.