

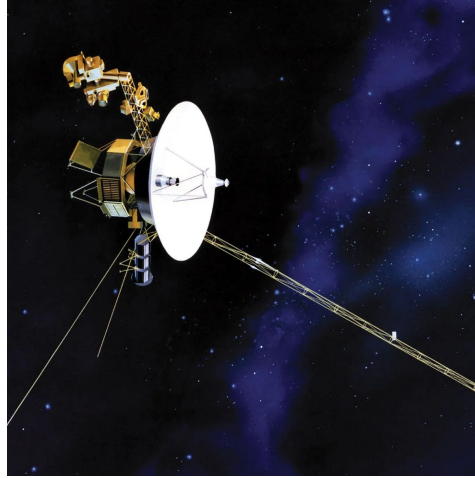
# Detecting Bugs in Cars

finding needles in a haystack

*Automated Model-in-the-Loop Testing of Continuous Controllers Using Search*



Velocity



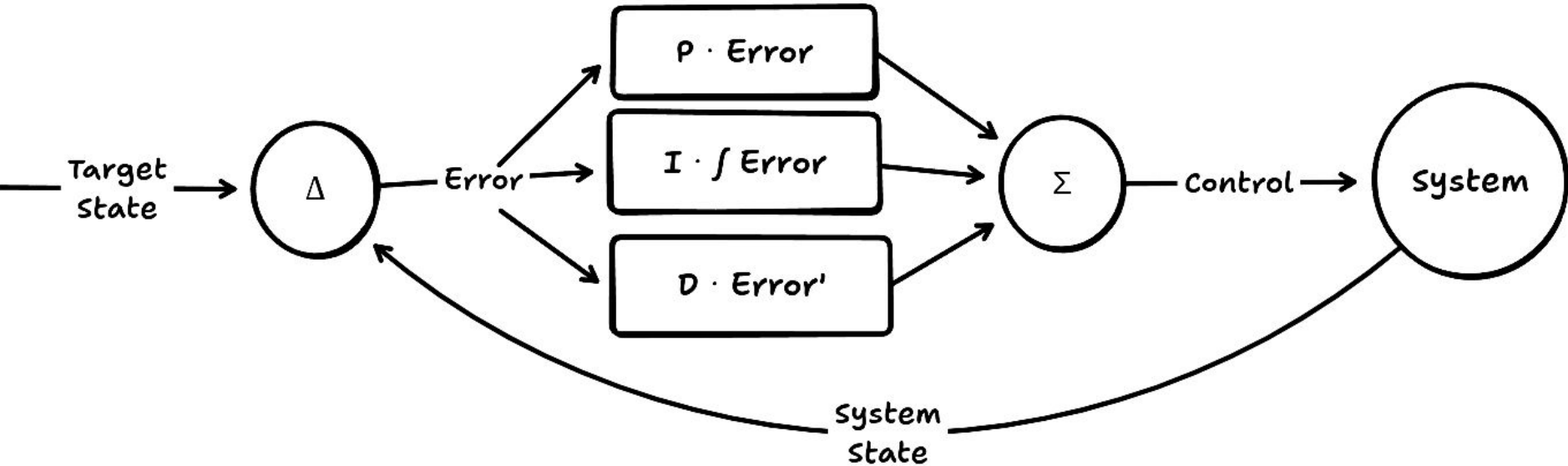
Orientation



Positioning

$$\text{Error} = \text{Desired State} - \text{Actual State}$$

# PID Controllers in a Nutshell



P, I, D are the tuning parameters of the controller.

# Model-in-the-Loop

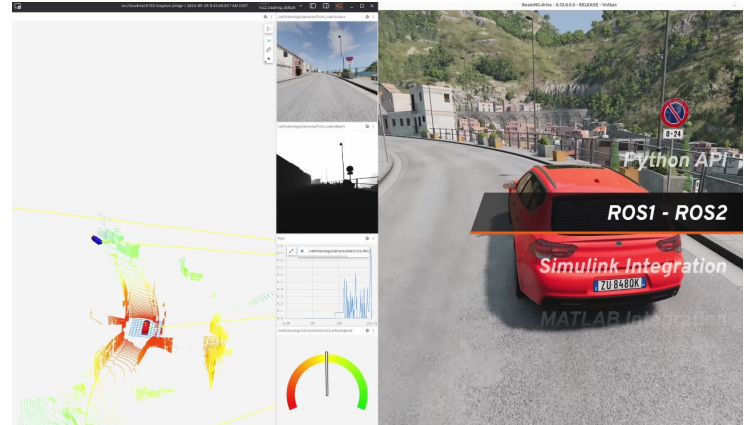
## On-Road

- Expensive - physical prototypes, facilities
- Time taking - setup, logistics, iterations
- Dangerous - real parts, real risks
- Non exhaustive - limited feasible tests

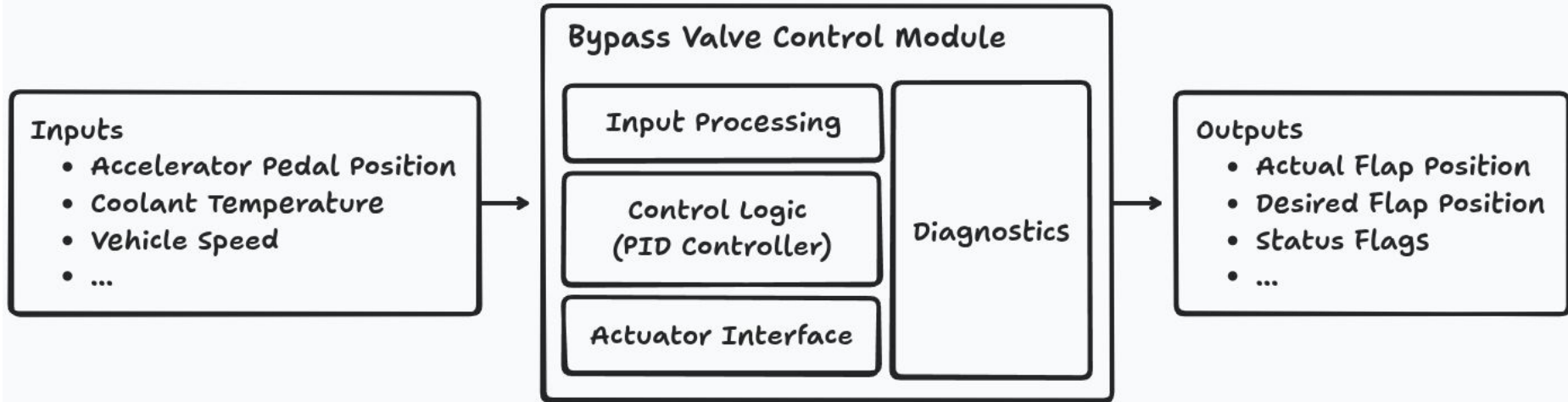


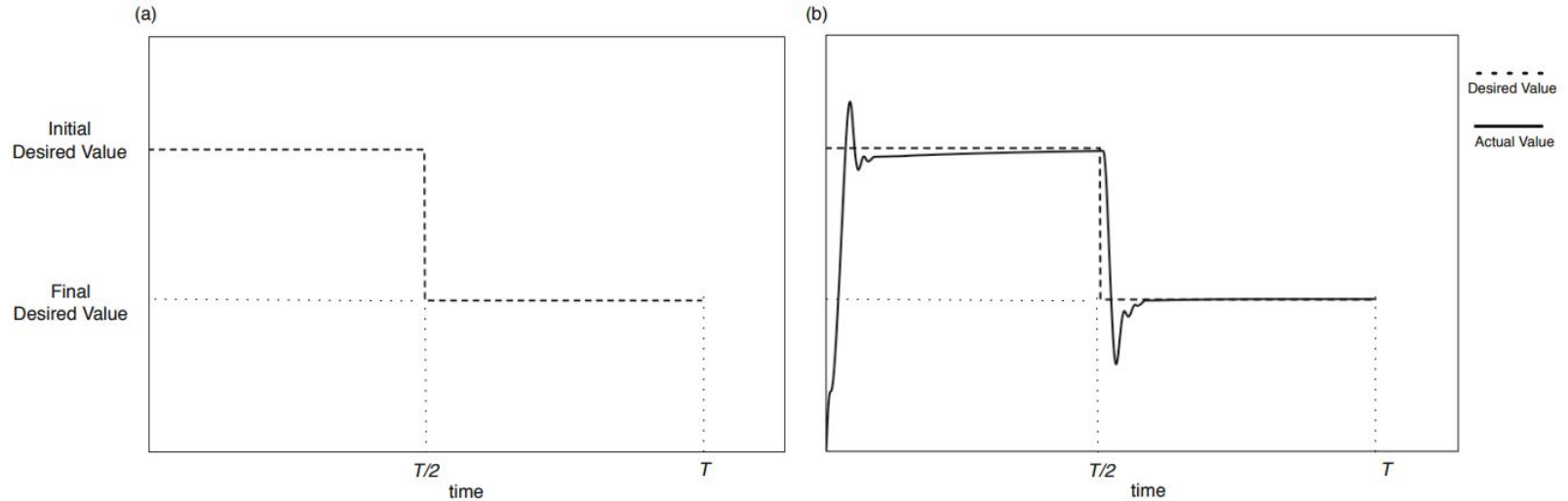
## Model-in-the-Loop (MiL)

- Cost-effective - no physical hardware
- Fast - rapid iteration and automation
- Safe - no physical risks
- Comprehensive - virtual edge case tests



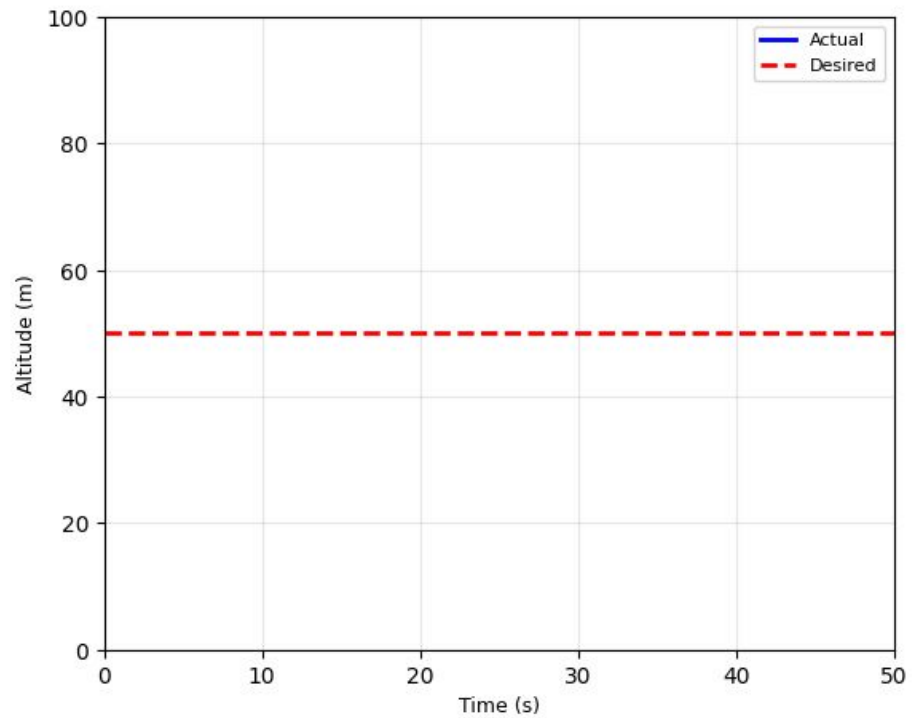
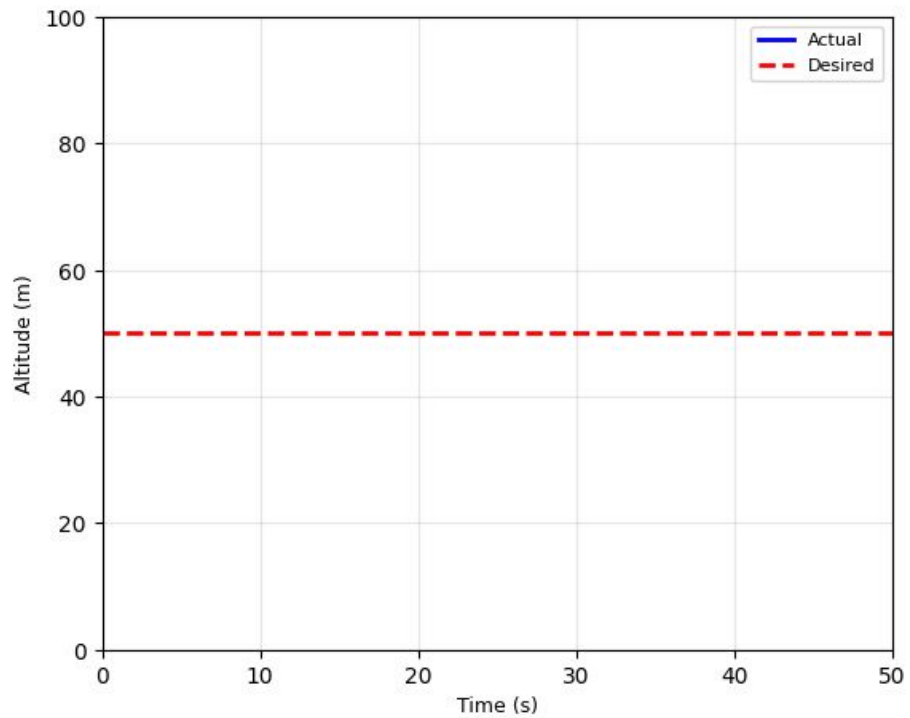
# Delphi





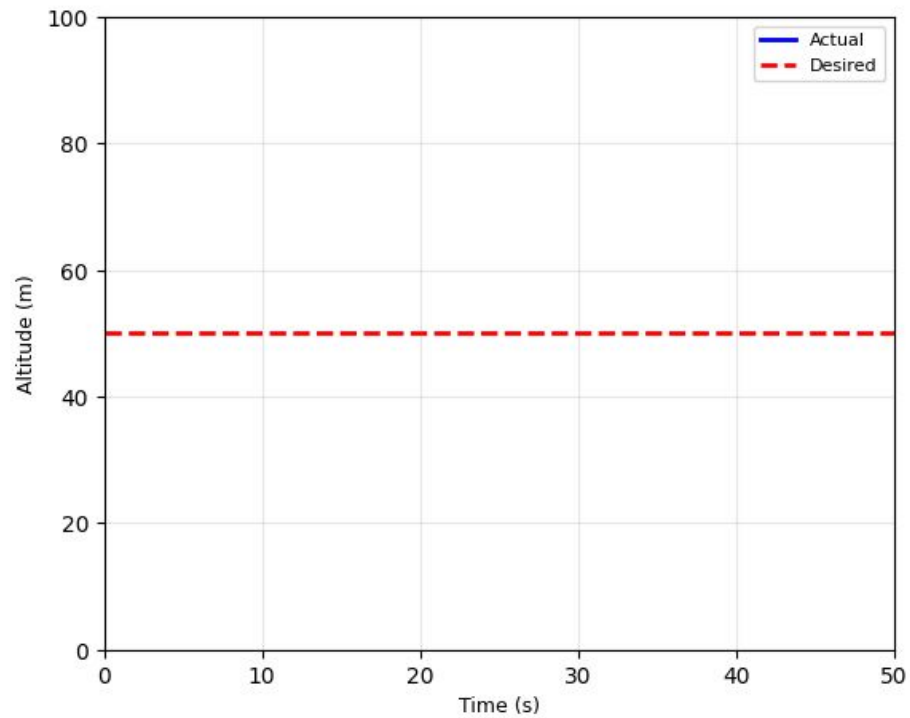
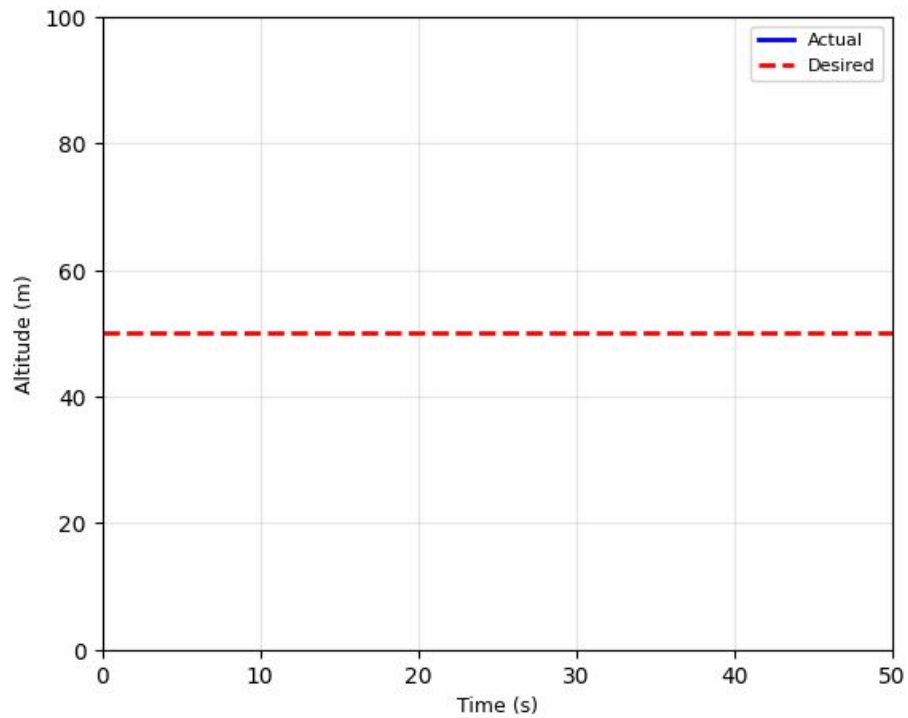
**Fig. 3.** Controller input step functions: (a) Step function. (b) Output of the controller (actual) given the input step function (desired).

$$\text{Error} = \text{Desired Position} - \text{Actual Position}$$

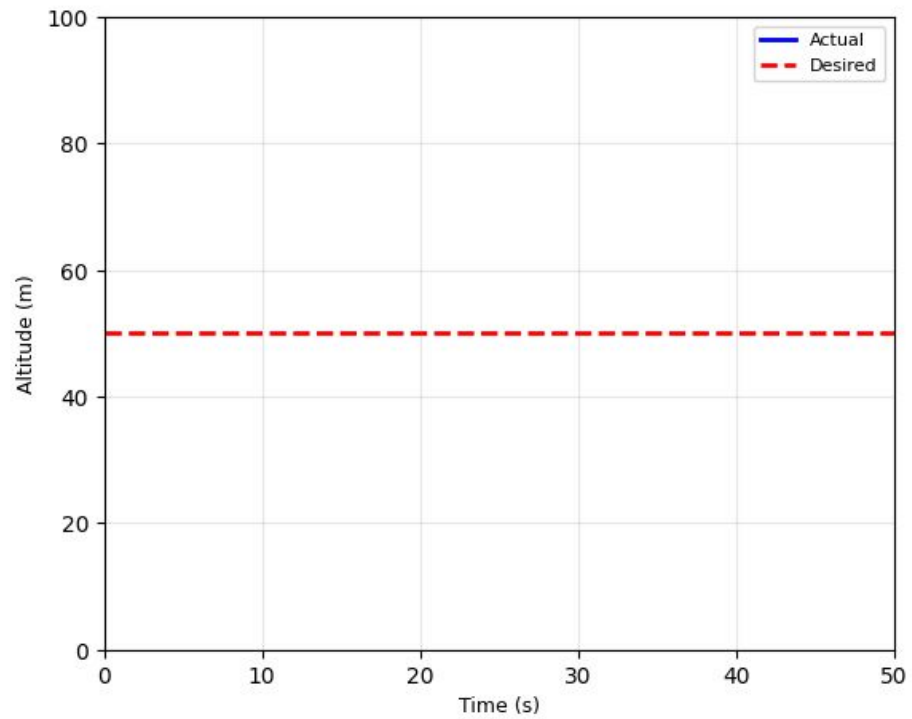
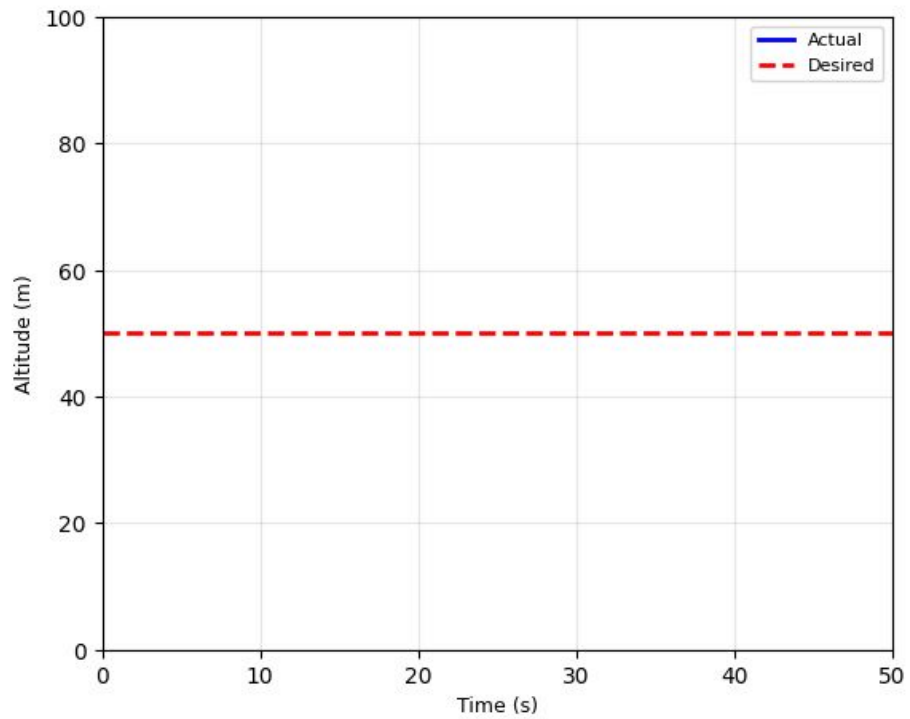


\*disregard label names



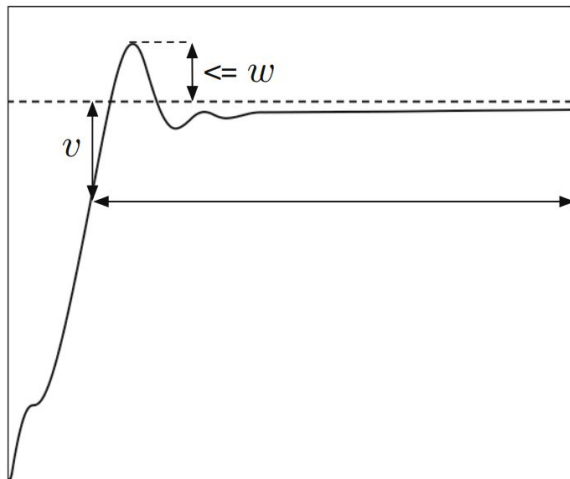


\*disregard label names



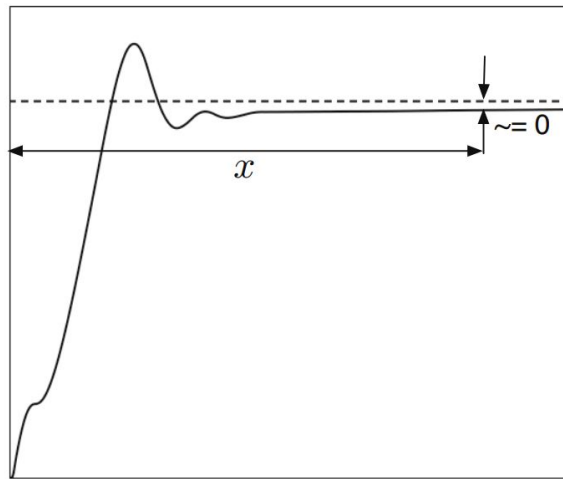
\*disregard label names

### Overshoot (Smoothness)



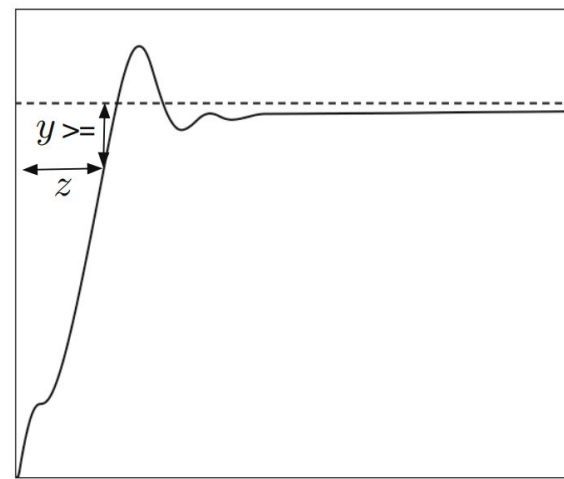
time

### Convergence (Liveness)



time

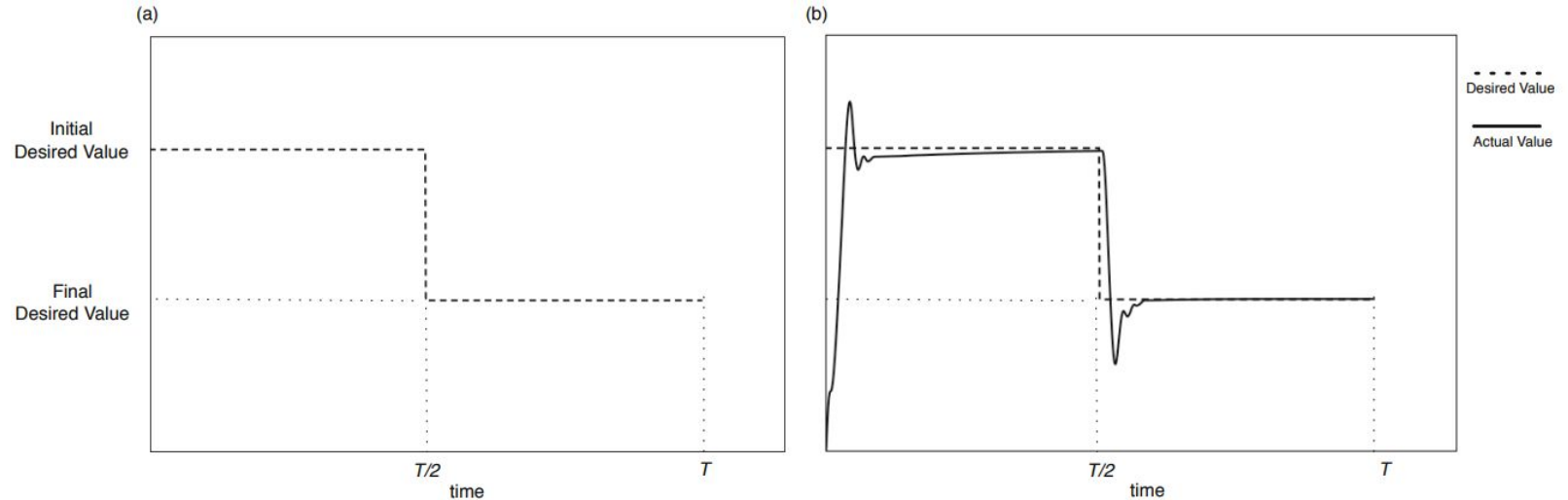
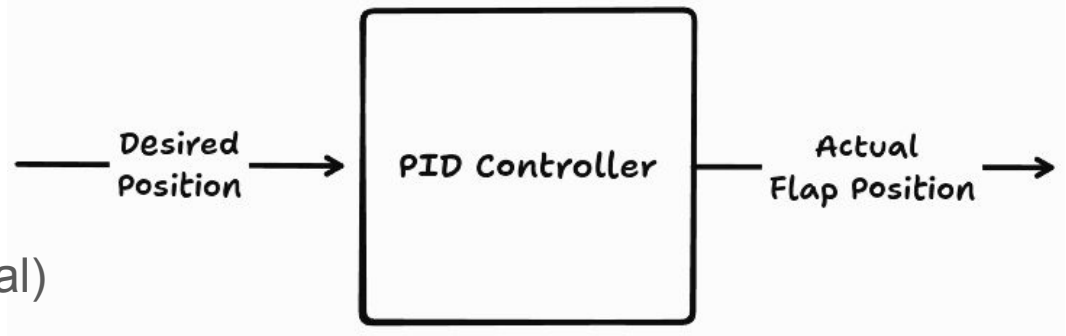
### Responsiveness



time

# Representation

(Desired, Actual)



**Fig. 3.** Controller input step functions: (a) Step function. (b) Output of the controller (actual) given the input step function (desired).

Fitness  $O(\text{Desired}, \text{Actual})$

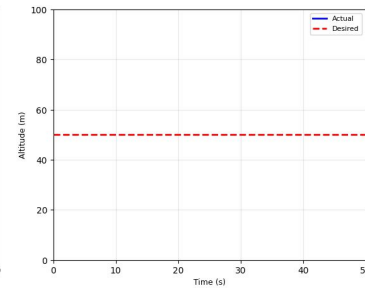
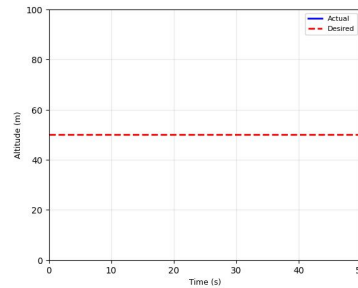
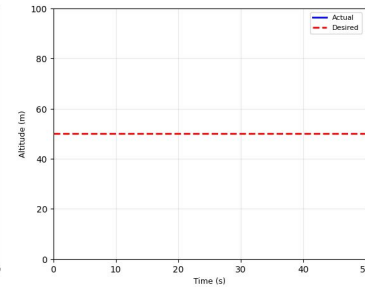
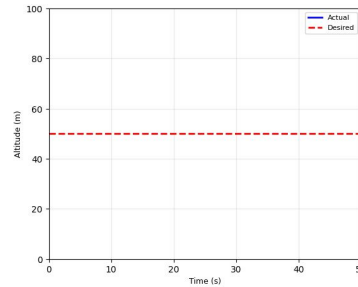
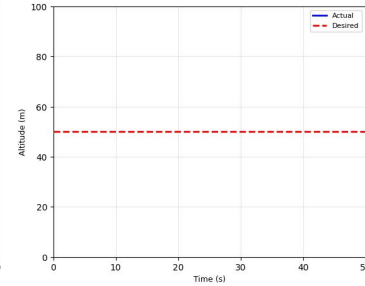
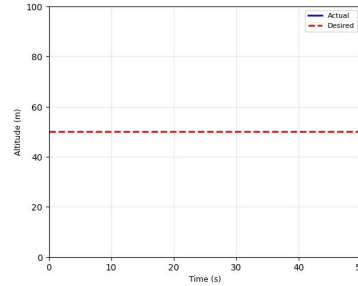
Overshoot  
(Smoothness)

Convergence  
(Liveness)

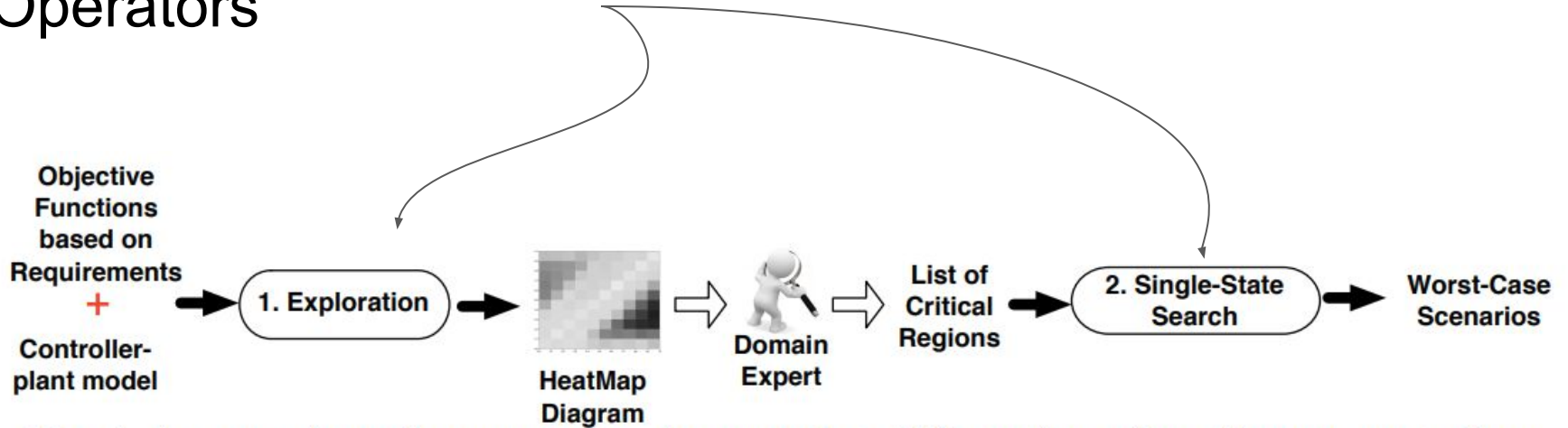
Responsiveness

Abnormal

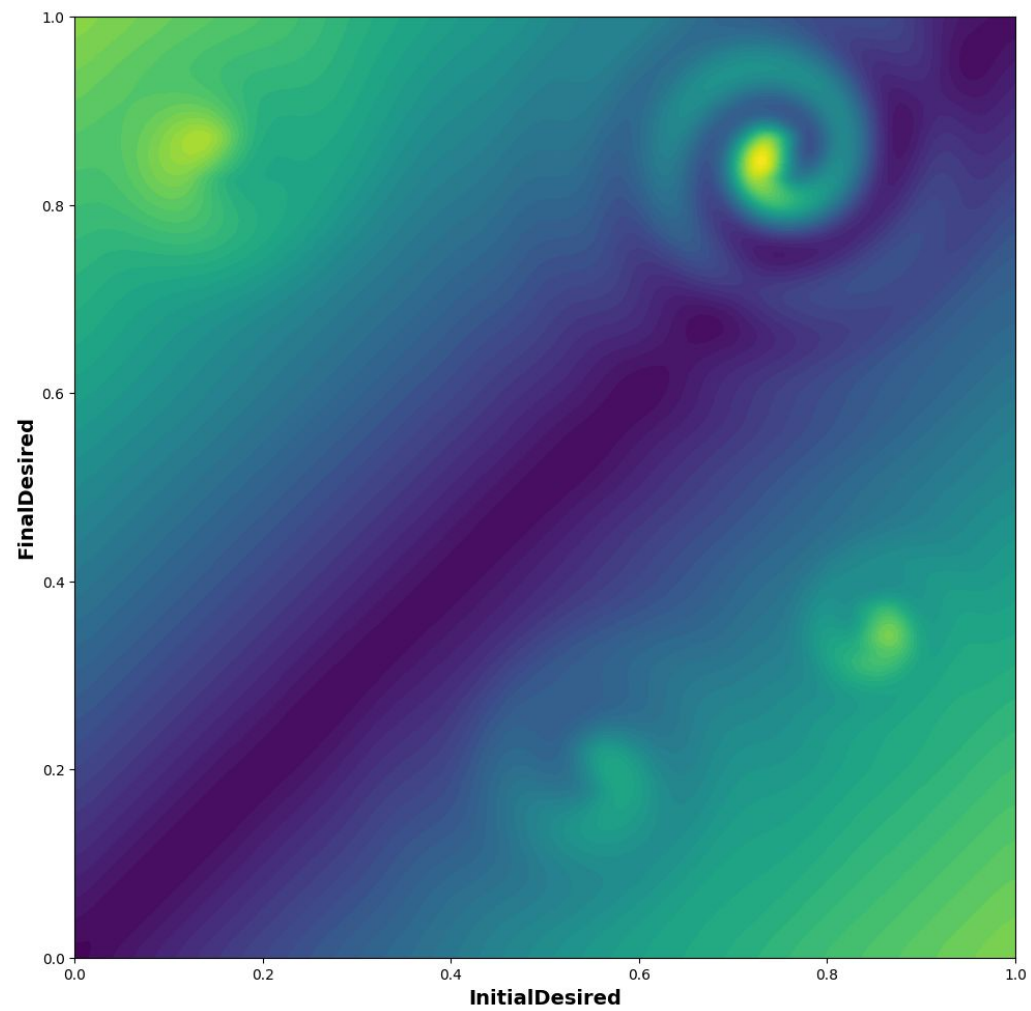
Normal



# Operators



**Fig. 4.** An overview of our automated approach to MiL testing of continuous controllers.



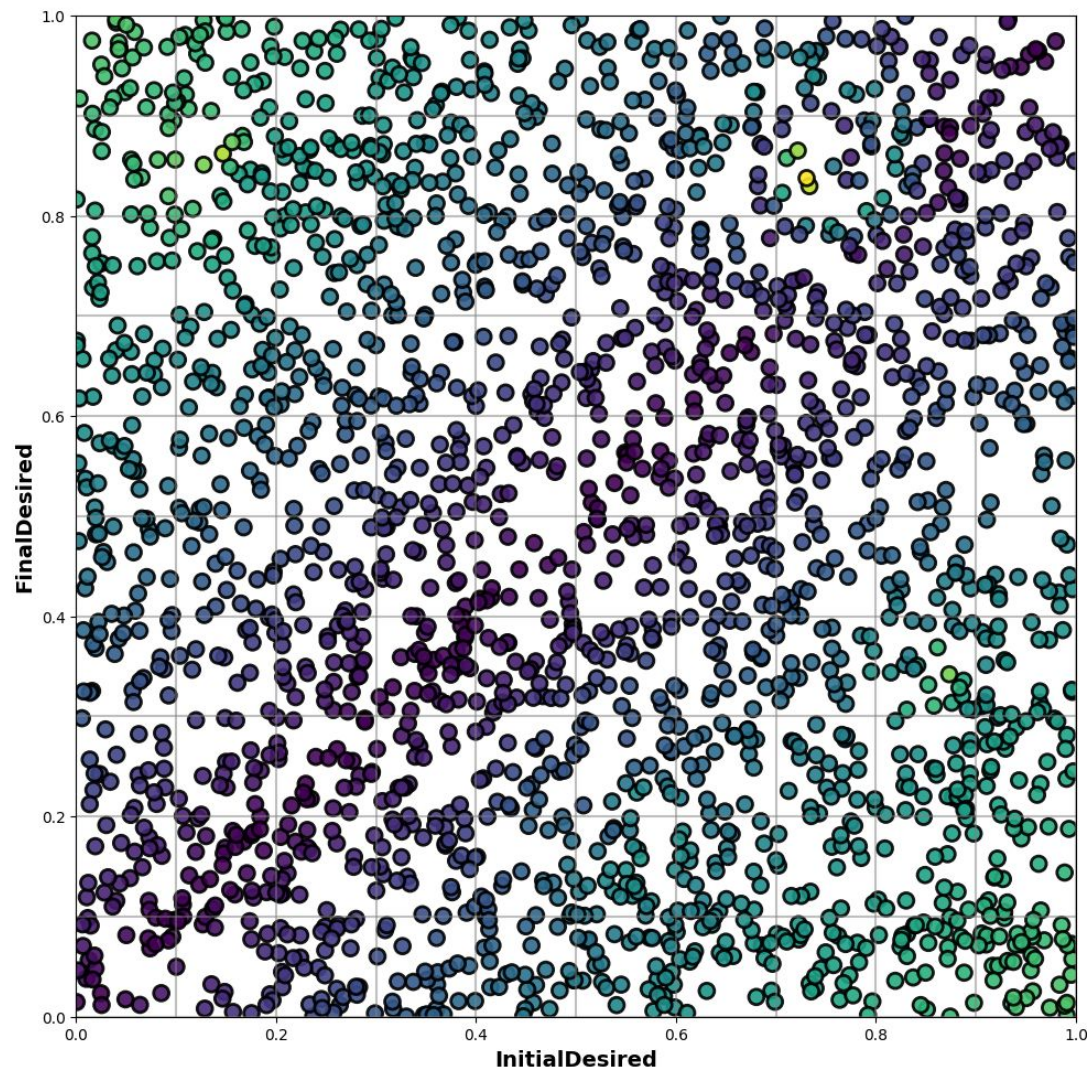


**Algorithm.** RANDOMEXPLORATION

**Input:** A controller-plant model  $M$  with input search space  $S$ .  
An objective function  $O$ . An observation time  $T$ .

**Output:** An overview diagram (HeatMap).

1. Partition  $S$  into equal sub-regions
2. Let  $P = \{\}$
3. **repeat**
4.   Let  $p = (\text{Initial Desired}, \text{Final Desired})$  be a random point in  $S$
5.   Let  $\text{Desired}$  be a step function generated based on  $p$  and  $T$
6.   Run  $M$  with the  $\text{Desired}$  input to obtain the  $\text{Actual}$  output
7.    $o = O(\text{Desired}, \text{Actual})$
8.    $P = \{(p, o)\} \cup P$
9. **until** there are at least  $N$  points in each region of  $S$  **do**
10. Create a HeatMap diagram based on  $P$

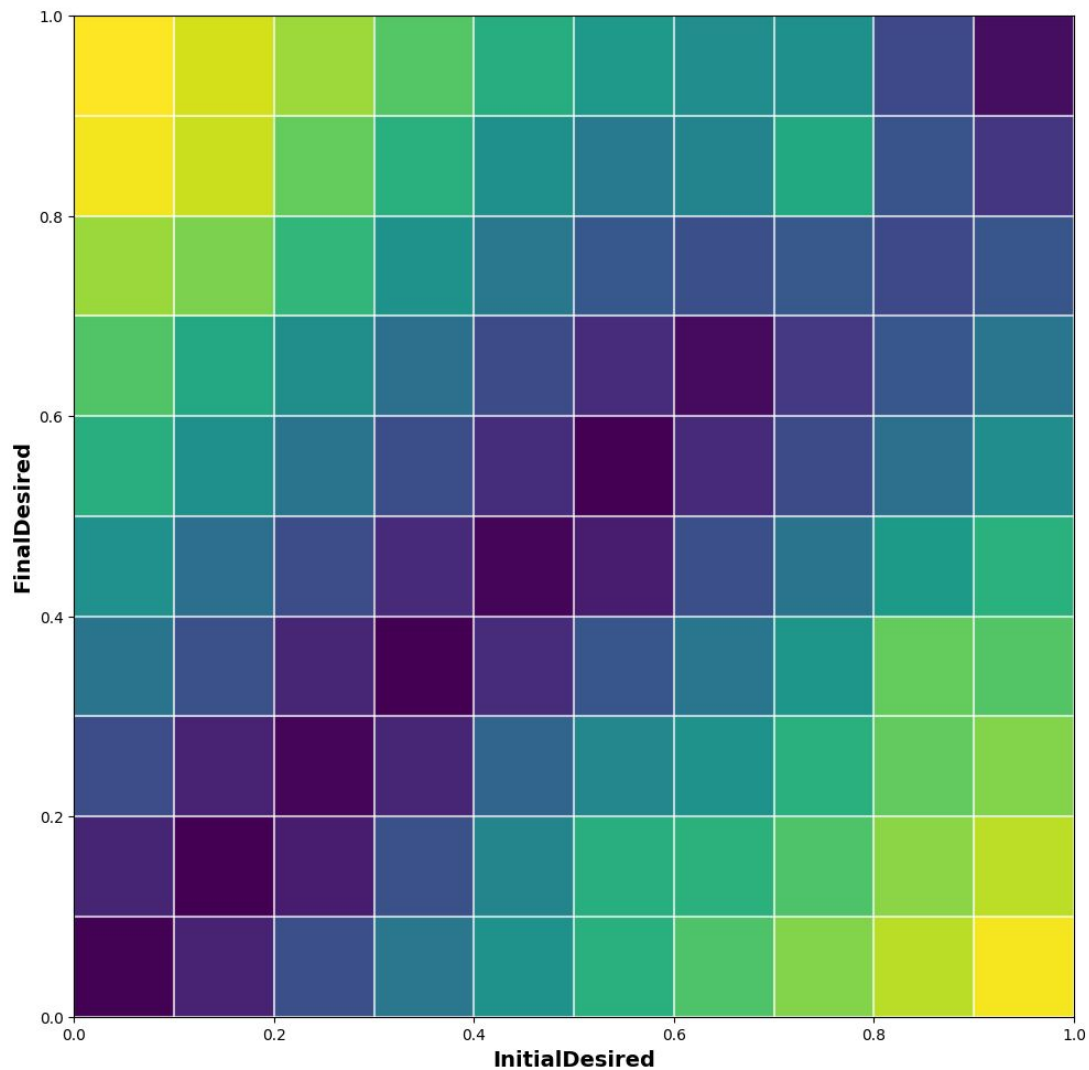




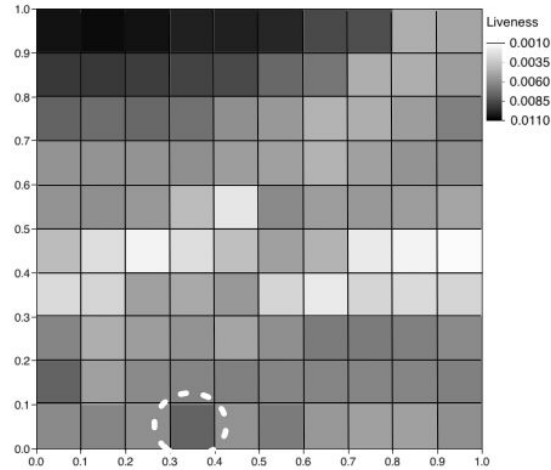
(1) Confidence about the behaviors over the dark shaded regions.

(2) The diagrams facilitate discovery of anomalies

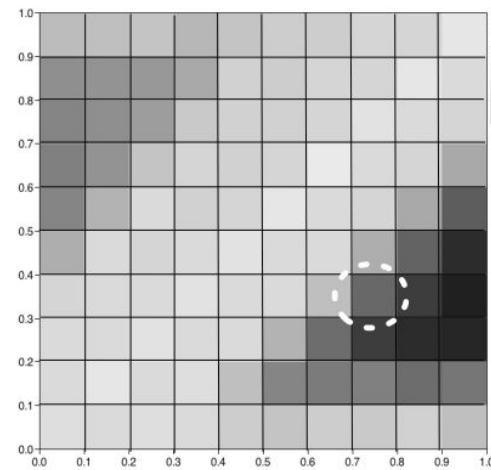
(3) A sharp contrast may indicate abnormal behavior



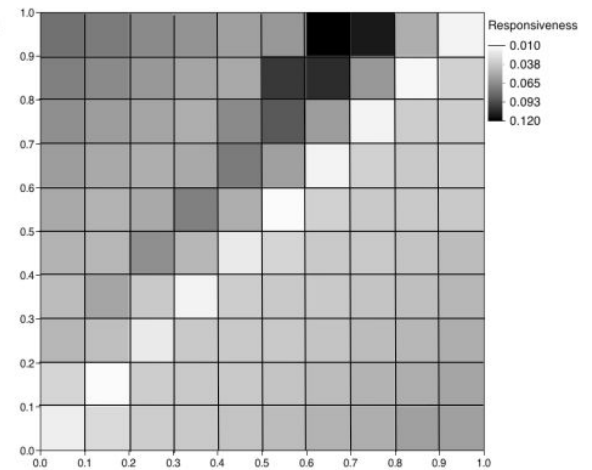
(a) Liveness



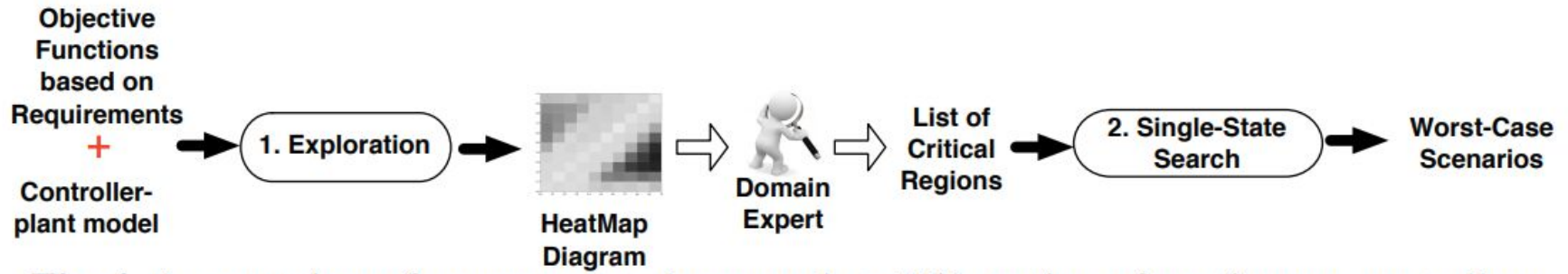
(b) Smoothness



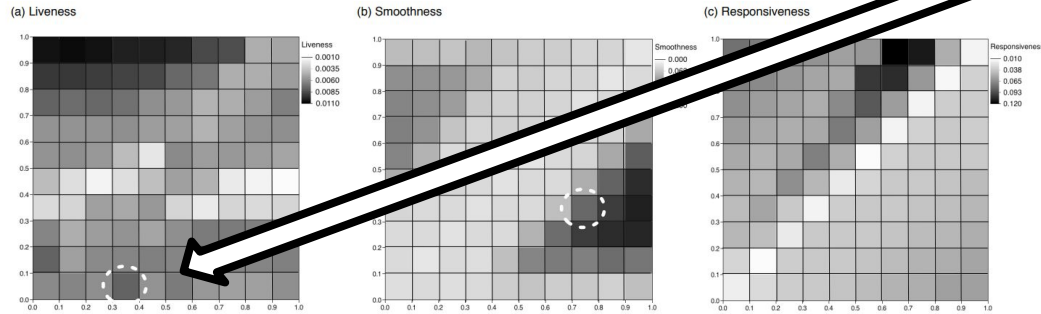
(c) Responsiveness



**Fig. 7.** HeatMap diagrams generated for our case study for the Liveness (a), Smoothness (b) and Responsiveness (c) requirements.



**Fig. 4.** An overview of our automated approach to MiL testing of continuous controllers.



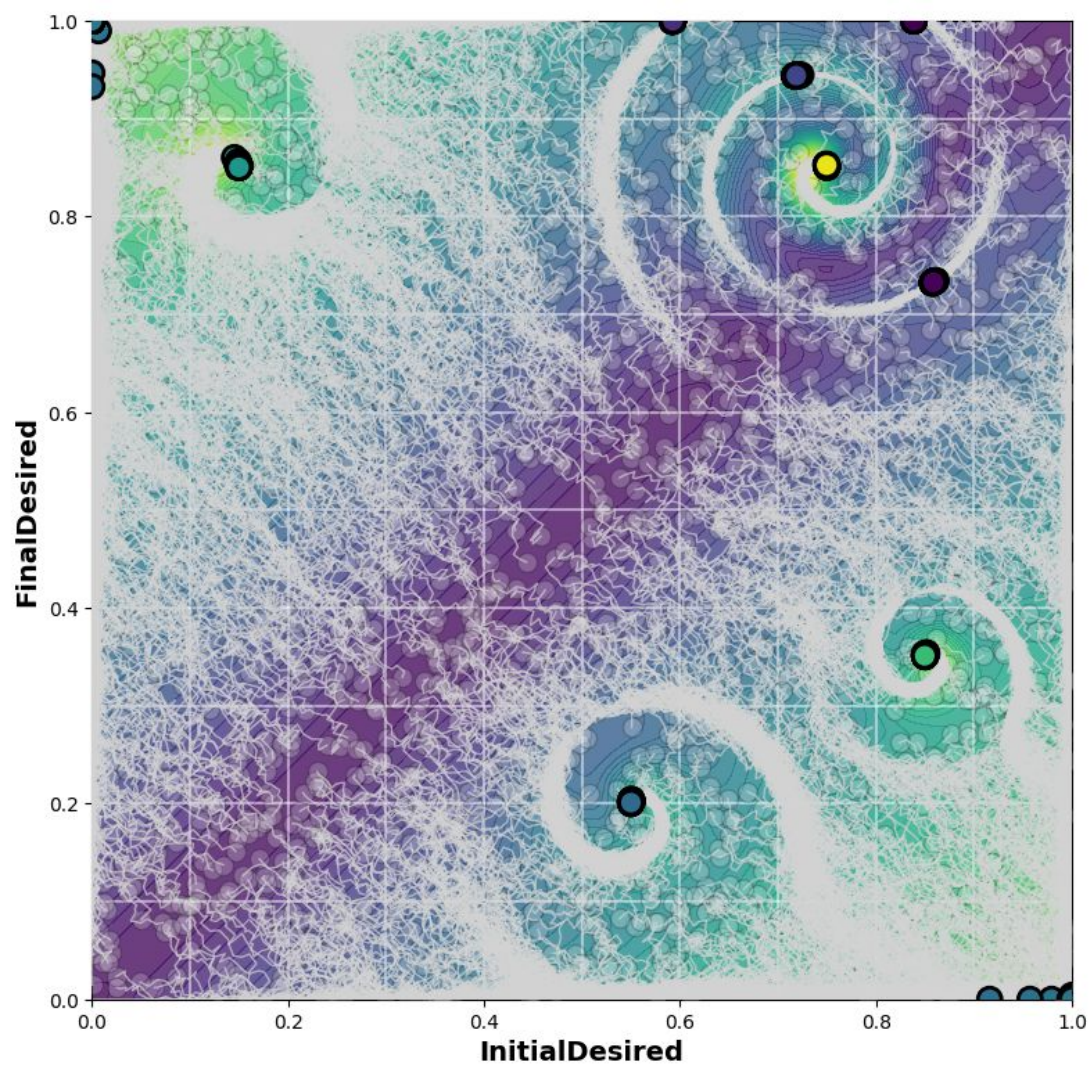
**Fig. 7.** HeatMap diagrams generated for our case study for the Liveness (a), Smoothness (b) and Responsiveness (c) requirements.

**Algorithm.** SINGLESTATESEARCH

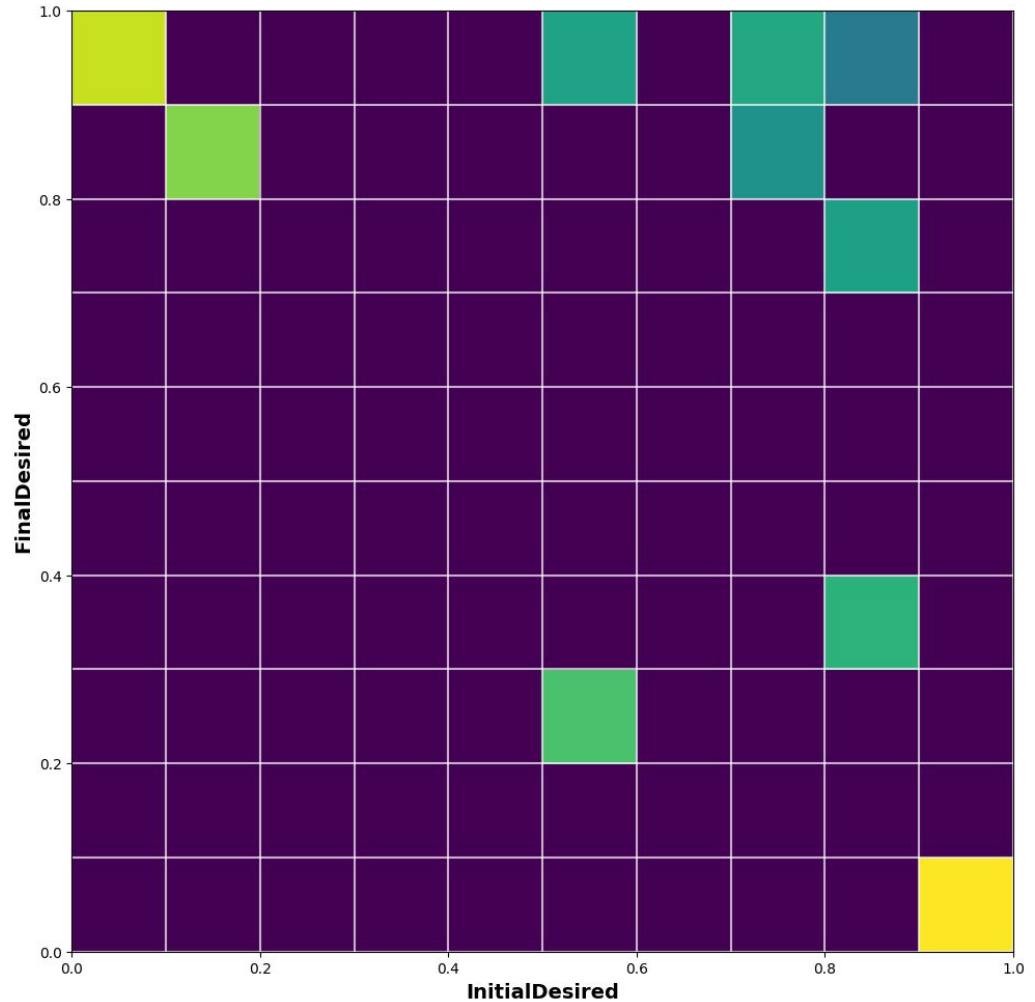
**Input:** A controller-plant model  $M$ . A region  $r$ .  
The set  $P$  computed by the algorithm in Figure 5(a).  
An objective function  $O$ .

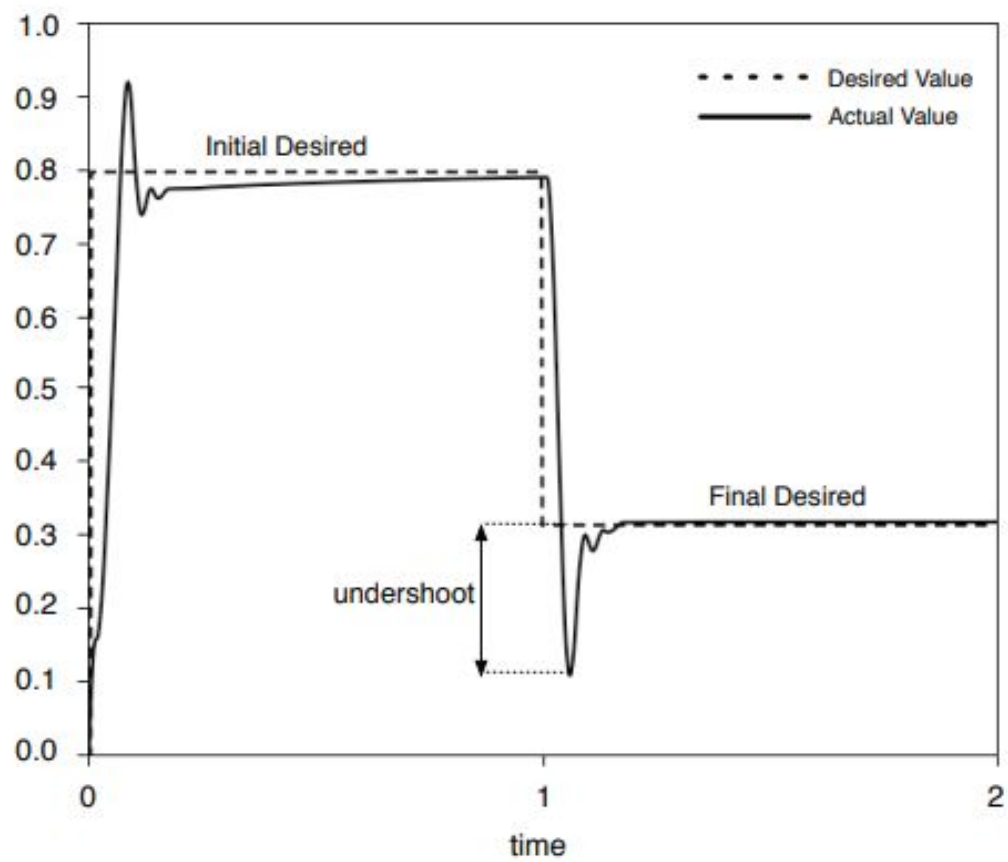
**Output:** The worst case scenario  $testCase$ .

1.  $P' = \{(p, o) \in P \mid p \in r\}$
2. Let  $(p, o) \in P'$  s.t. for all  $(p', o') \in P'$ , we have  $o \geq o'$
3.  $worstFound = o$
4. **for** K iterations :
5.   Let Desired be a step function generated by  $p$
6.   Run  $M$  with the Desired input to obtain the Actual output
7.    $v = O(Desired, Actual)$
8.   **if**  $v > worstFound$  :
9.      $worstFound = v$   
       $testCase = p$
10.    $p = Tweak(p)$
11. **return**  $testCase$



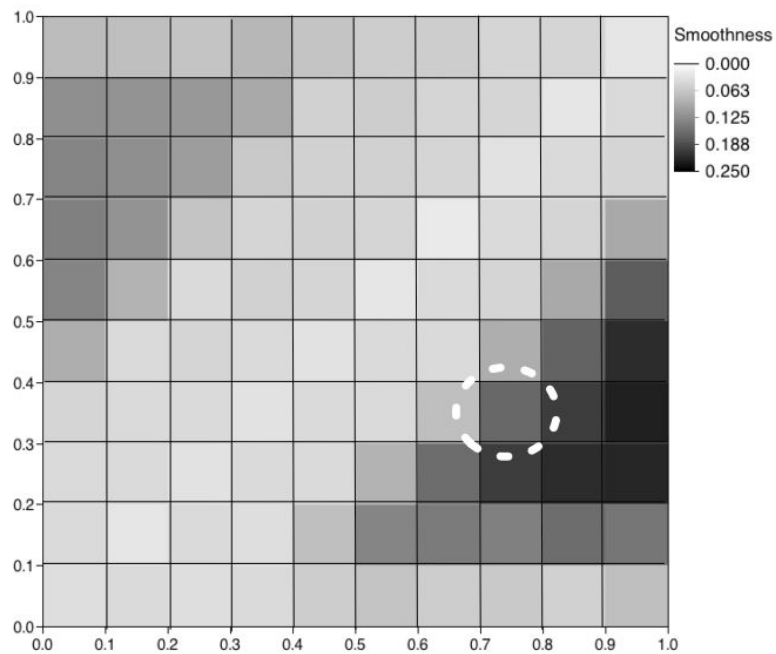
- 11 worst case scenarios
- Requirements violations
- Controller model error
- Plant model error



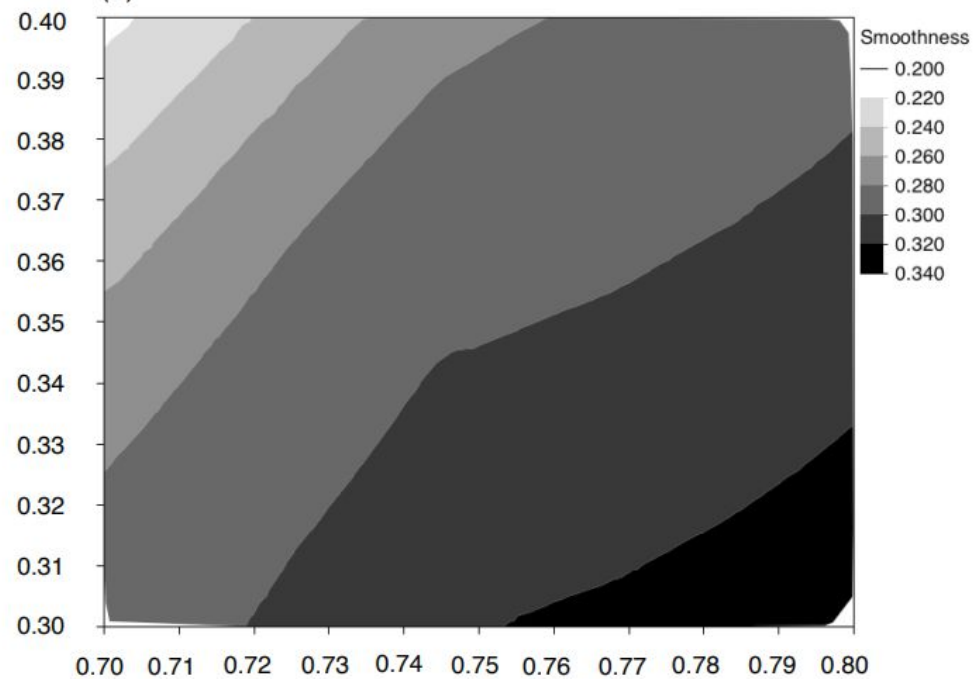




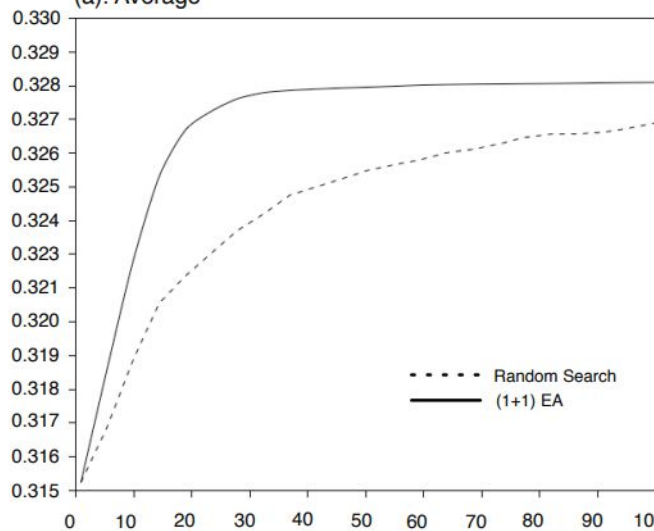
(b) Smoothness



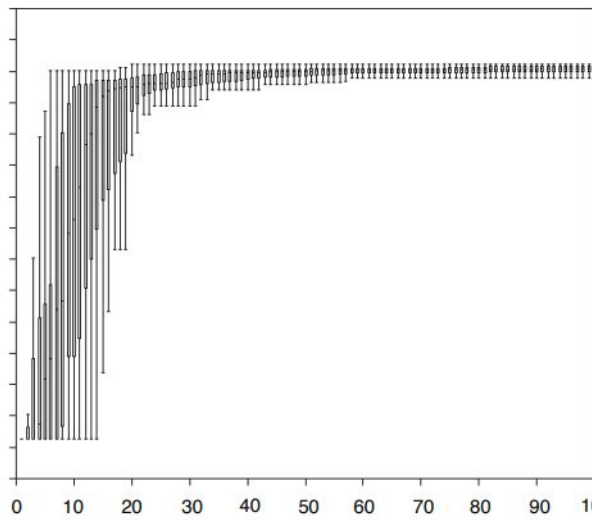
(a)



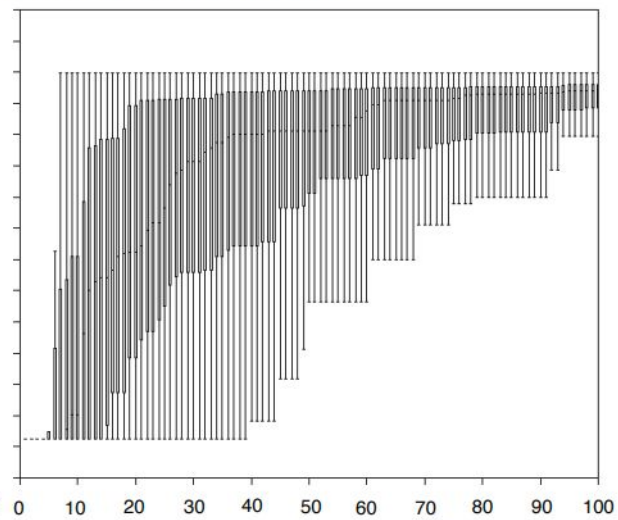
(a). Average



(b). (1+1) EA Distribution

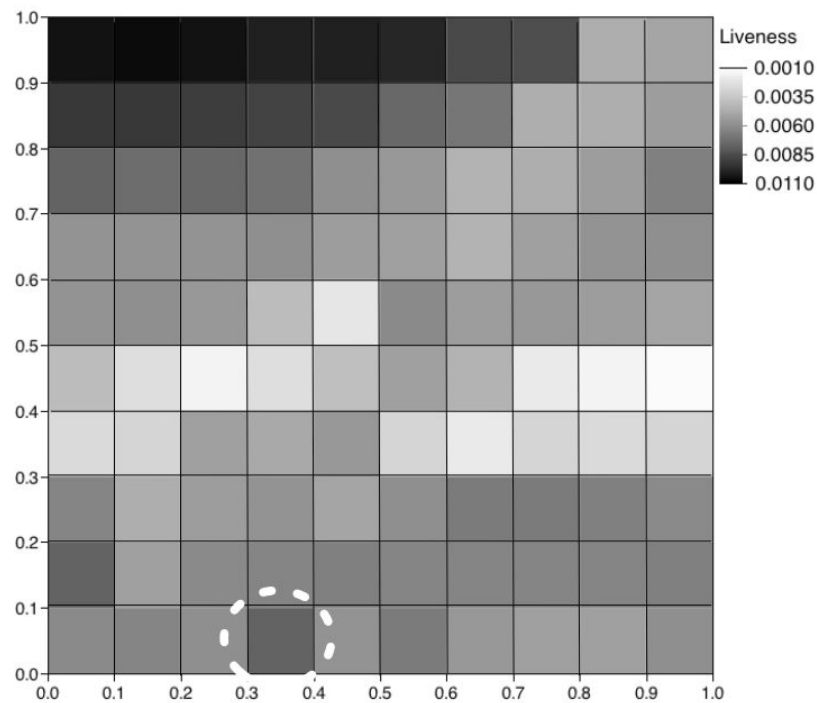


(c). Random Search Distribution

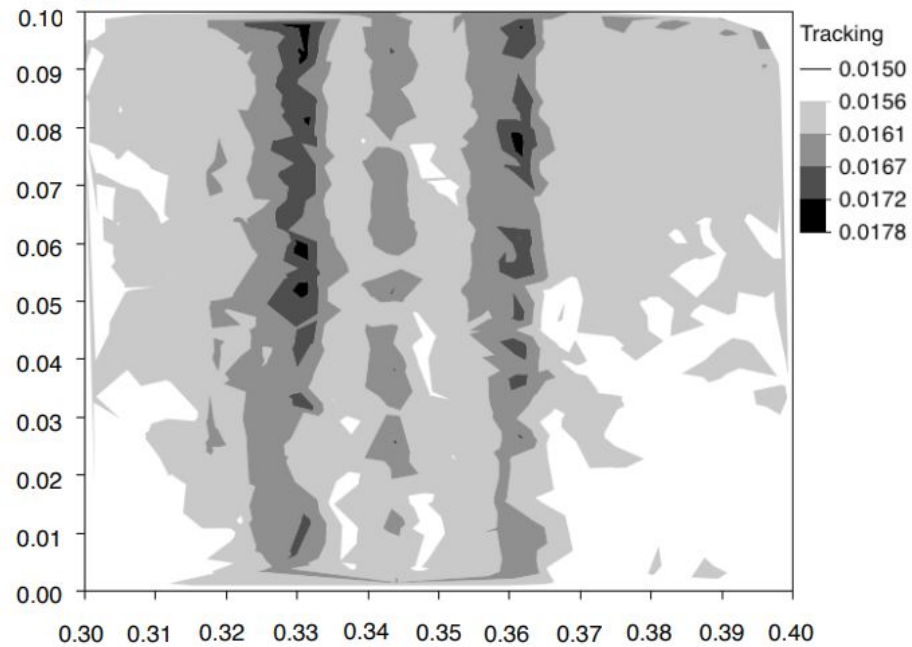




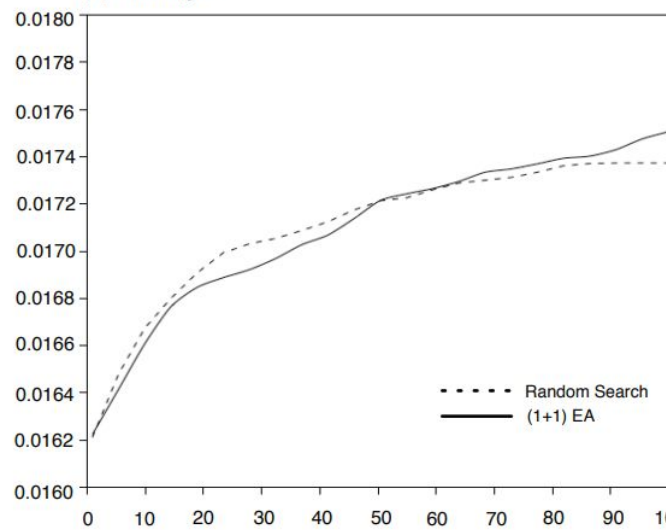
(a) Liveness



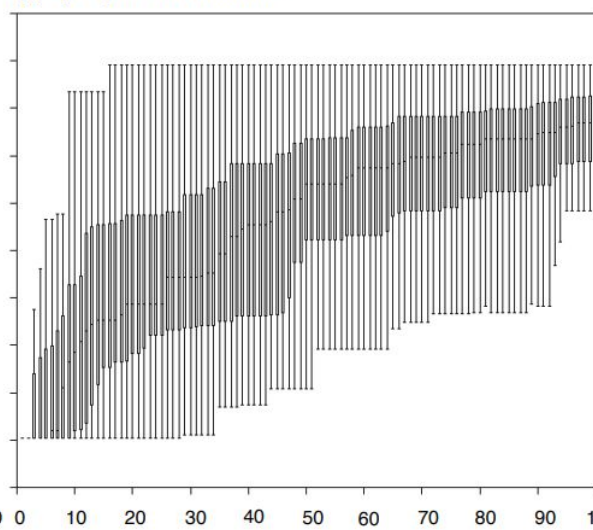
(b)



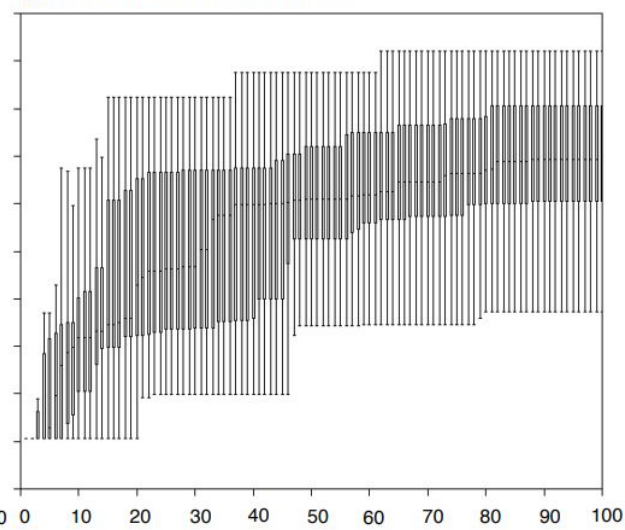
(d). Average

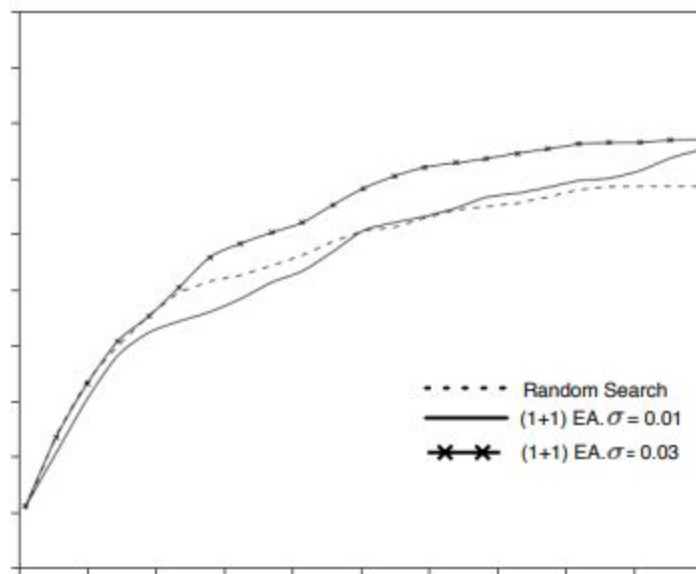


(e). (1+1) EA Distribution



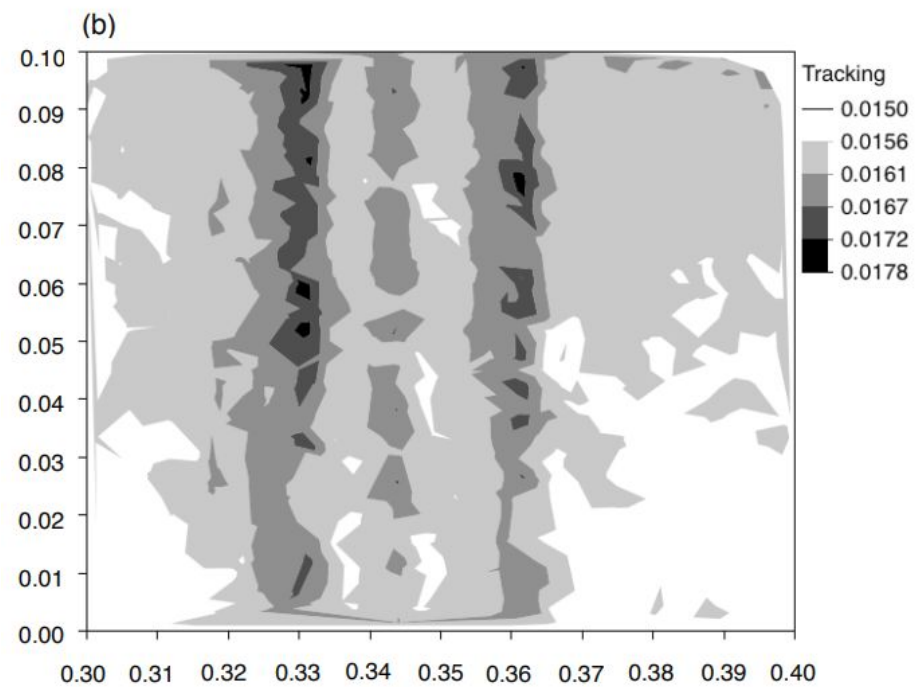
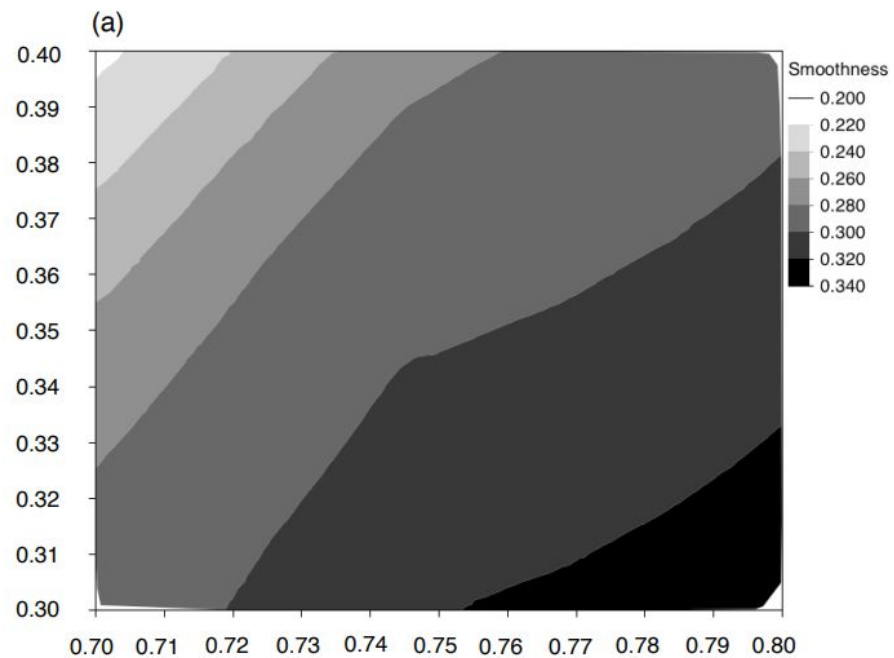
(f). Random Search Distribution





**Fig. 10.** Comparing average values for (1+1) EA with  $\sigma = 0.01$ , (1+1) EA with  $\sigma = 0.03$ , and random search for the region in Figure 7(a)

# TAKEAWAYS



# No one tool for the job

## Random Search:

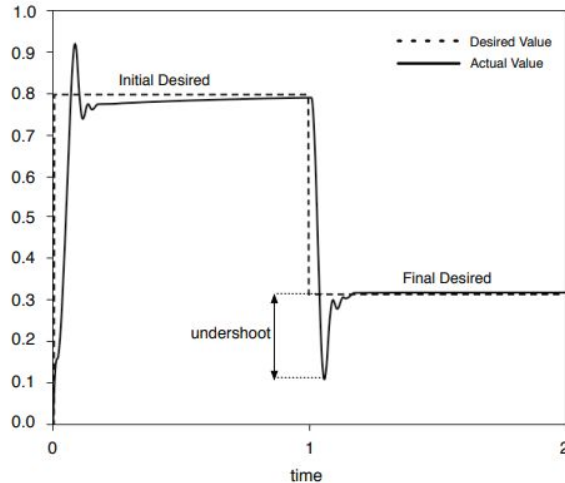
- Terrible for finding exact peaks
- Effective at finding which hills are worth climbing

## Local Search:

- Terrible for global search (stuck in local peaks)
- Effective at finding the precise peak in a specific area

# Turn requirements into numbers

- Translate qualitative into quantitative
- Frame as an optimization problem



Did it overshoot?

Qualitative	Quantitative
Yes	$O_s = \max \text{error}(t)  = 0.2$

**Oracle problem:** automatically determining if a program's output is correct for a given input

# CRITICISMS

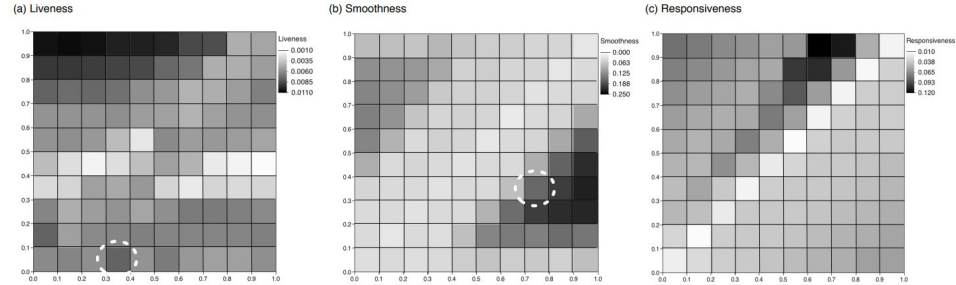


# Novelty and Significance

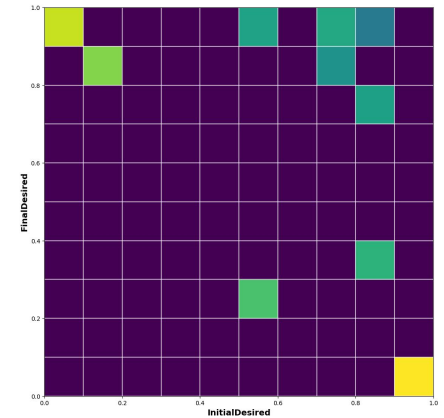
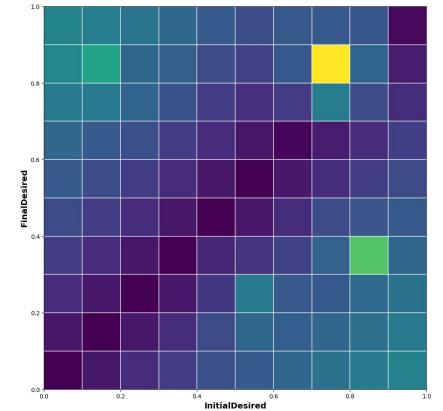
- The general concept had been already established by prior work (eg, Lindlar et al., 2009)
- Two-phase workflow
- Heatmap to convey the information
- Three generic controller metrics (reusable for this class of problem)
- Automated and more effective alternative to manual testing.
- Demonstration of requirements into objective functions.

# Soundness and Verifiability

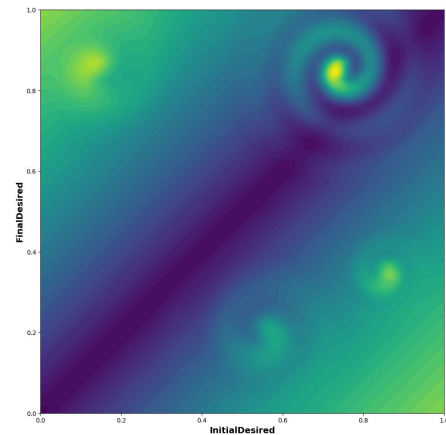
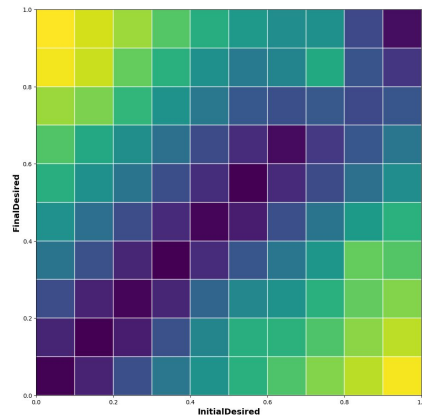
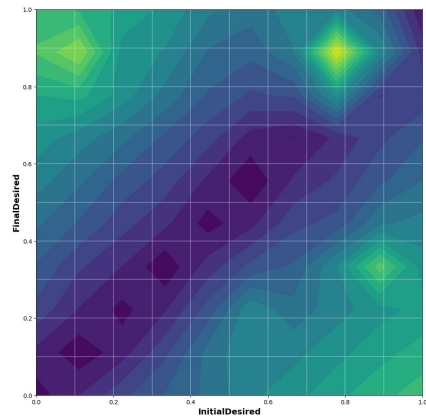
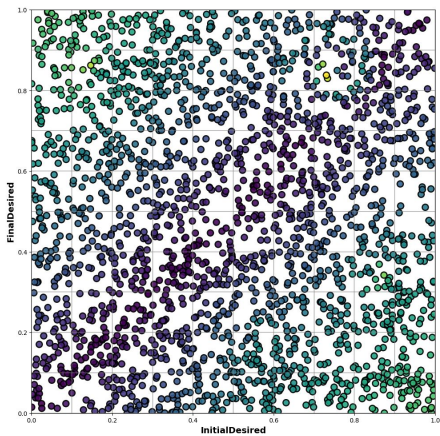
- Simplified 2D search space (fixed all other system inputs).
  - How well would the methodology scale as more parameters are added?
- Reliability of humans in the loop



**Fig. 7.** HeatMap diagrams generated for our case study for the Liveness (a), Smoothness (b) and Responsiveness (c) requirements.



# Soundness and Verifiability



# Soundness and Verifiability

**Algorithm.** RANDOMEXPLORATION

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An objective function  $O$ . An observation time  $T$ .

**Output:** An overview diagram (HeatMap).

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2. Let  $P = \{\}$
3. **repeat**
4.   Let  $p = (\text{Initial Desired}, \text{Final Desired})$  be a random point in  $S$
5.   Let  $\text{Desired}$  be a step function generated based on  $p$  and  $T$
6.   Run  $M$  with the  $\text{Desired}$  input to obtain the  $\text{Actual}$  output
7.    $o = O(\text{Desired}, \text{Actual})$
8.    $P = \{(p, o)\} \cup P$
9. **until** there are at least  $N$  points in each region of  $S$  **do**
10. Create a HeatMap diagram based on  $P$

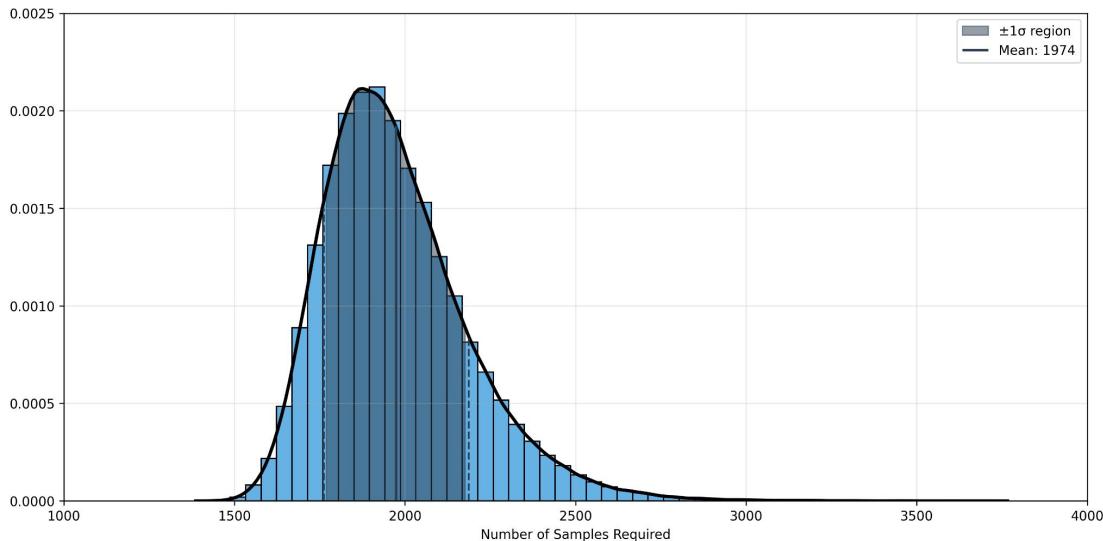
200k Monte Carlo Runs

$E[N]$ : 1974

$\sigma(N)$ : 212

Min: 1442

Max: 3711



*“We decided to generate around 1000 points in  $S$  during the exploration step.”*

# Soundness and Verifiability

**Algorithm.** RANDOMEXPLORATION

**Input:** A controller-plant model  $M$  with input search space  $S$ .

An objective function  $O$ . An observation time  $T$ .

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9. **until** there are at least  $N$  points in each region of  $S$  **do**
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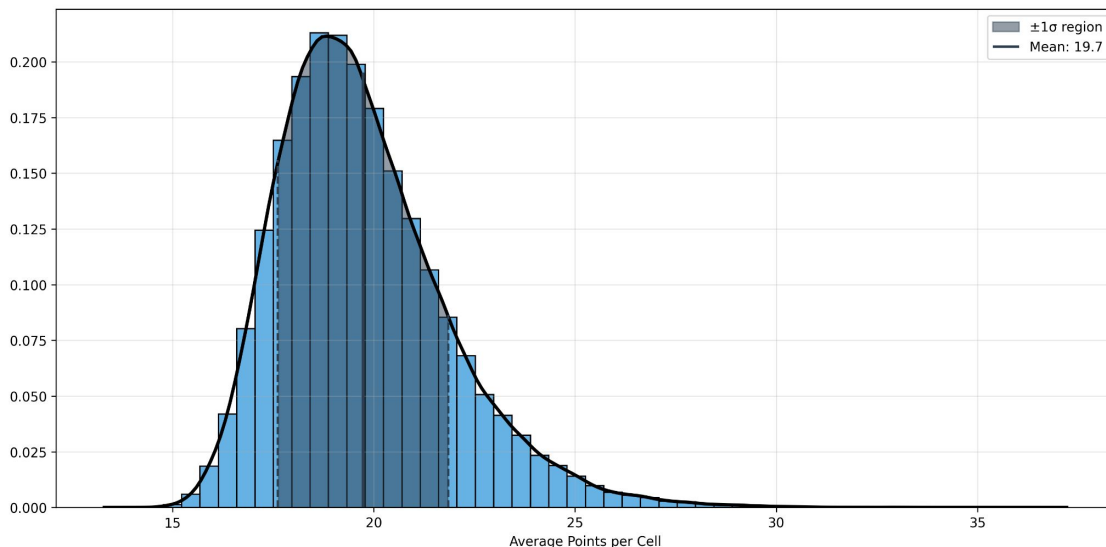
200k Monte Carlo Runs

$E[N]$ : 1974

$\sigma(N)$ : 212

Min: 1442

Max: 3711



*“We divided up  $S$  into 100 equal squares [...] at least 10 points are simulated in each region during exploration”*

# Final Assessment

- Well written, structured and motivated
- Good figures
- Implementation details and rationale could have been a bit more clear
- Demonstrates the search-based approach outperformed humans and random search
- Critical regions are not always trivial to identify by eye
- Rationale for sampling strategy could have been explained in more detail

# THANK YOU!

+ Q&A