



# Detecting Bugs in Cars

finding needles in a haystack

*Automated Model-in-the-Loop Testing of Continuous Controllers Using Search*



Velocity



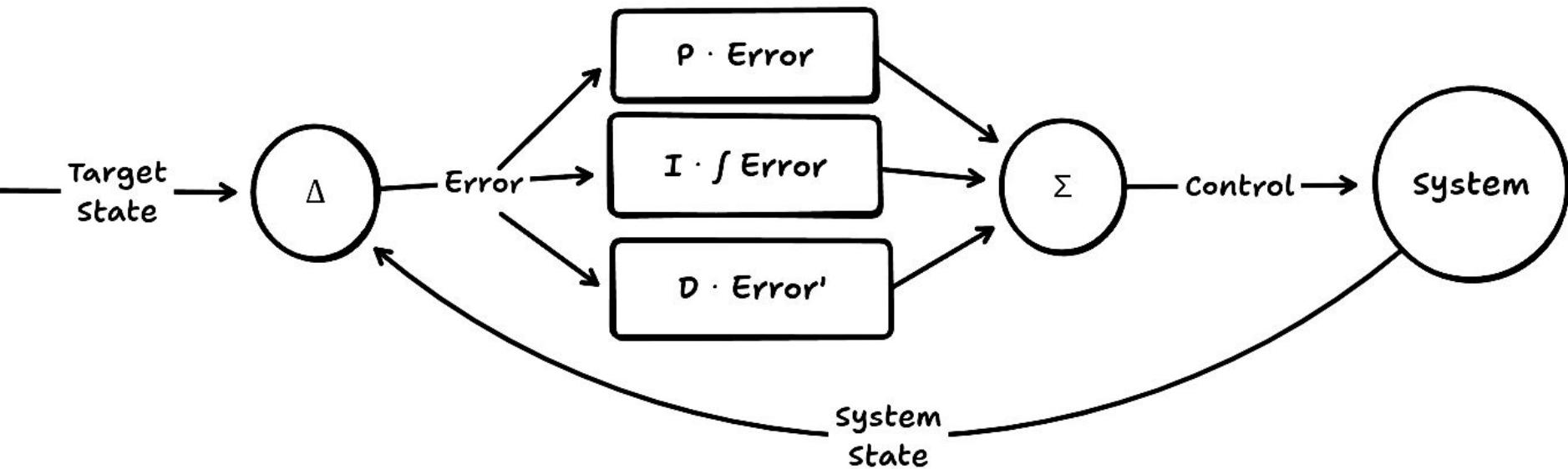
Orientation



Positioning

Error = Desired State - Actual State

# PID Controllers in a Nutshell



P, I, D are the tuning parameters of the controller.

# Model-in-the-Loop

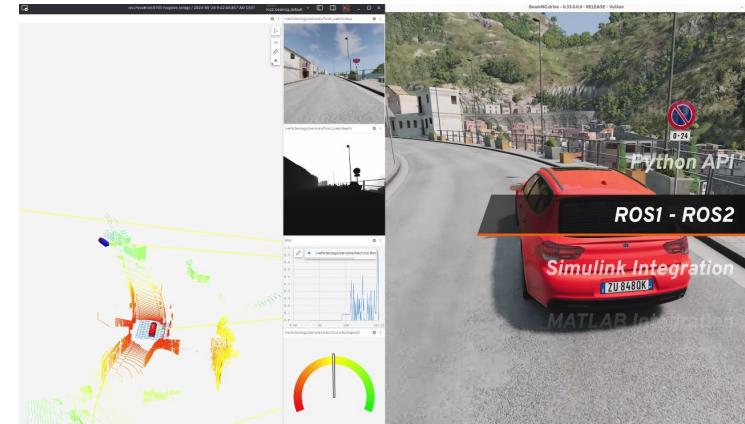
## On-Road

- Expensive - physical prototypes, facilities
- Time taking - setup, logistics, iterations
- Dangerous - real parts, real risks
- Non exhaustive - limited feasible tests

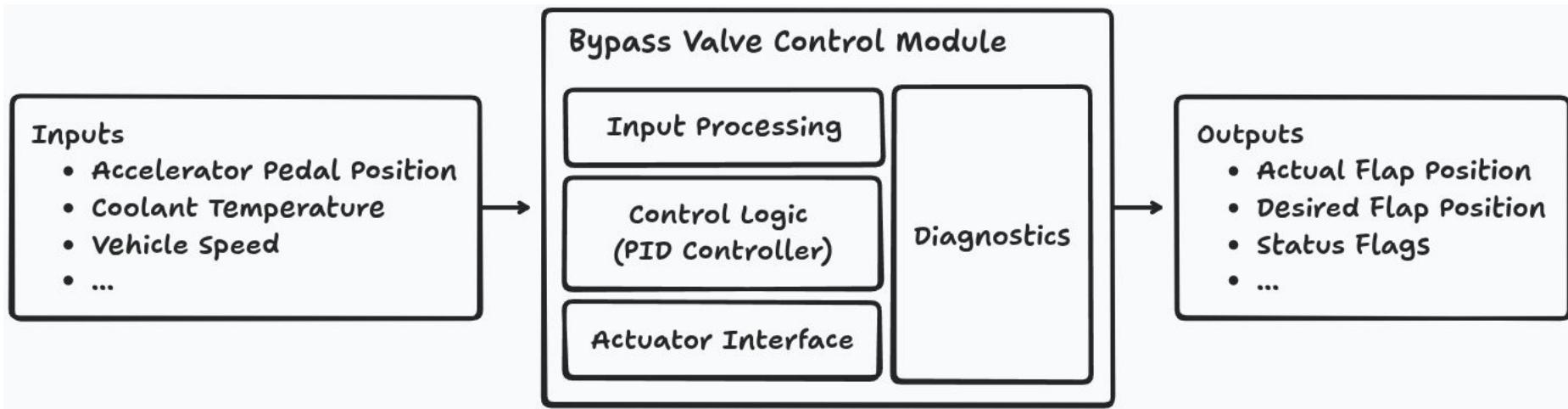


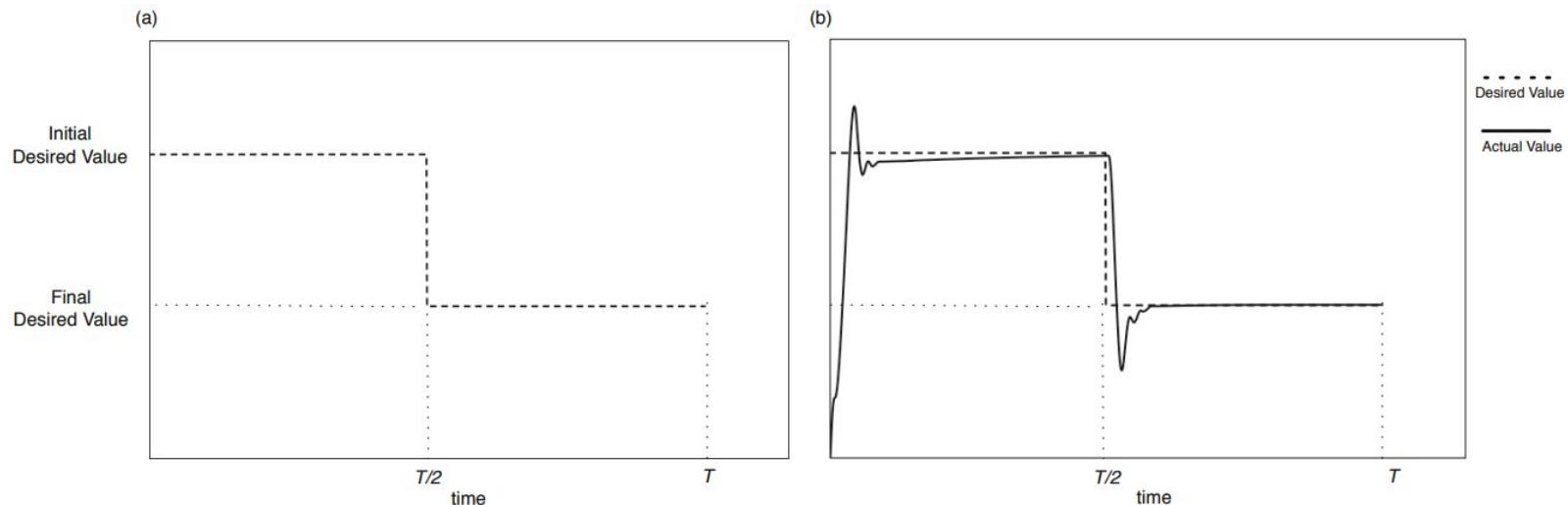
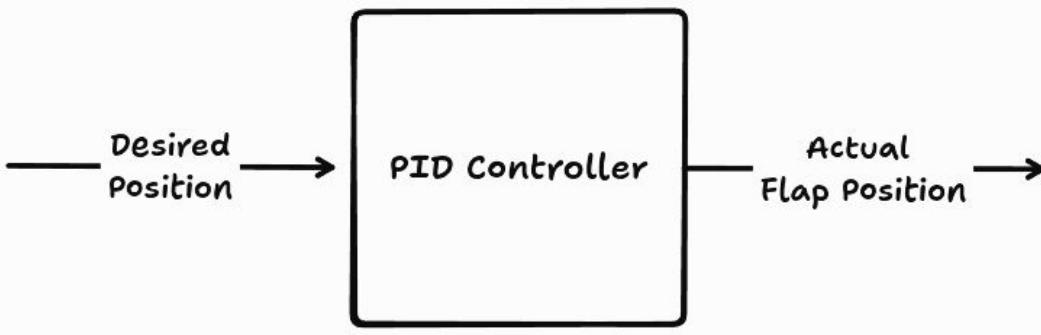
## Model-in-the-Loop (MiL)

- Cost-effective - no physical hardware
- Fast - rapid iteration and automation
- Safe - no physical risks
- Comprehensive - virtual edge case tests



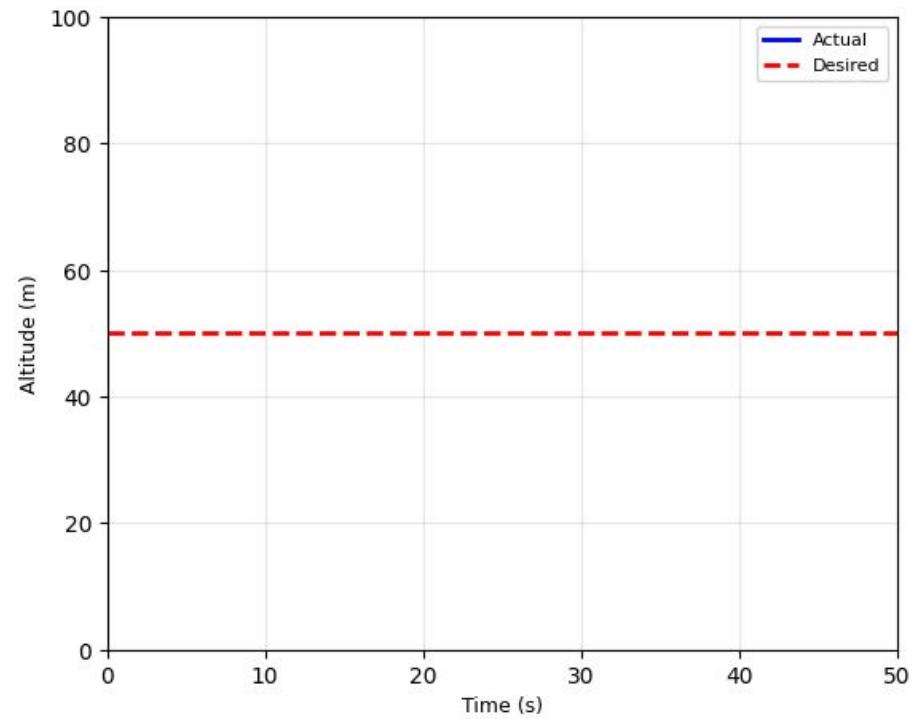
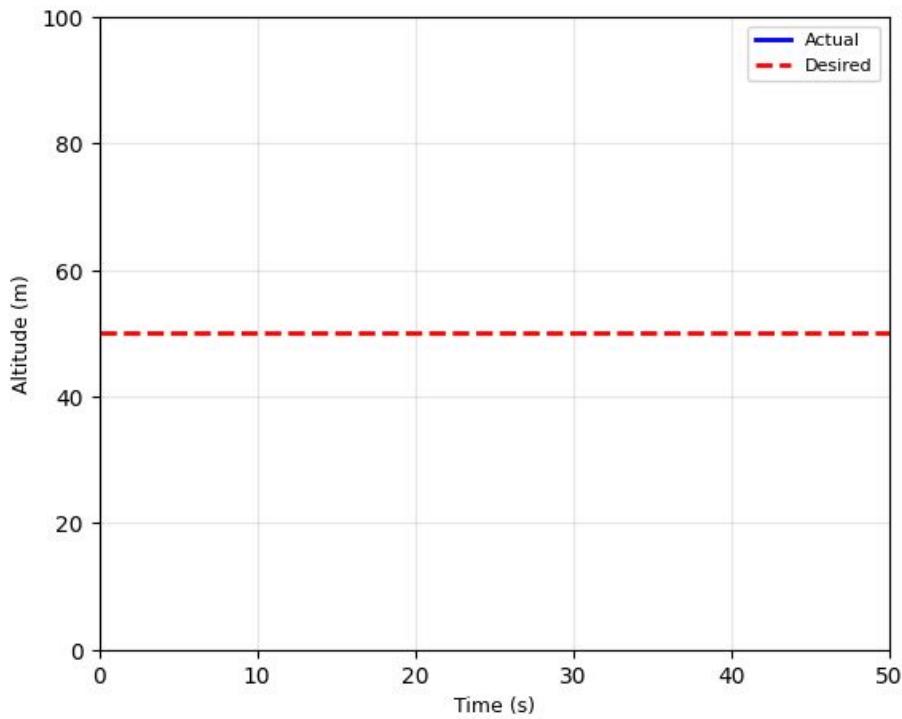
# Delphi



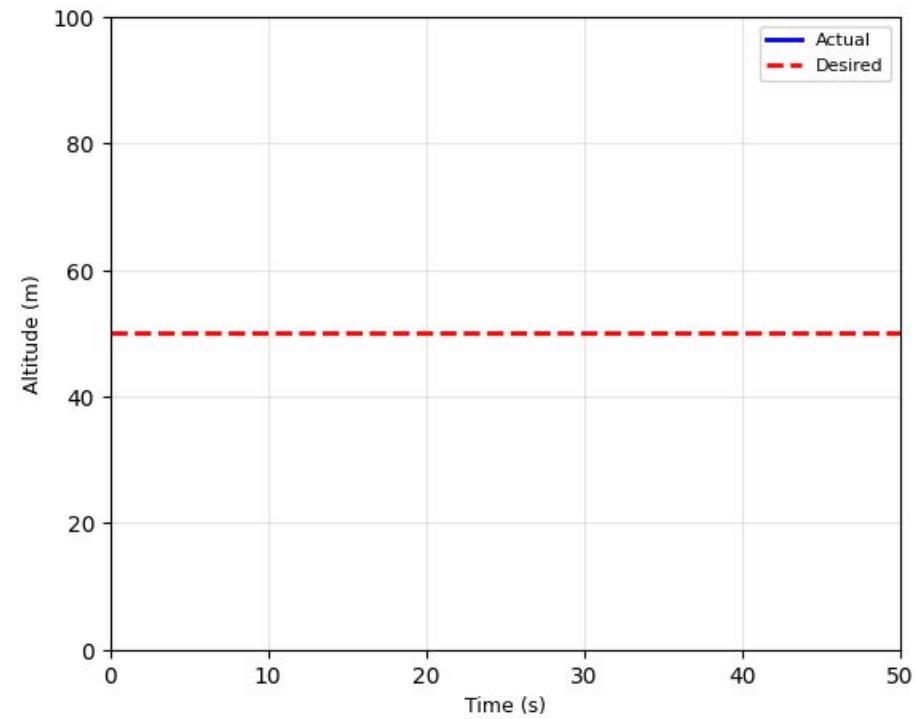
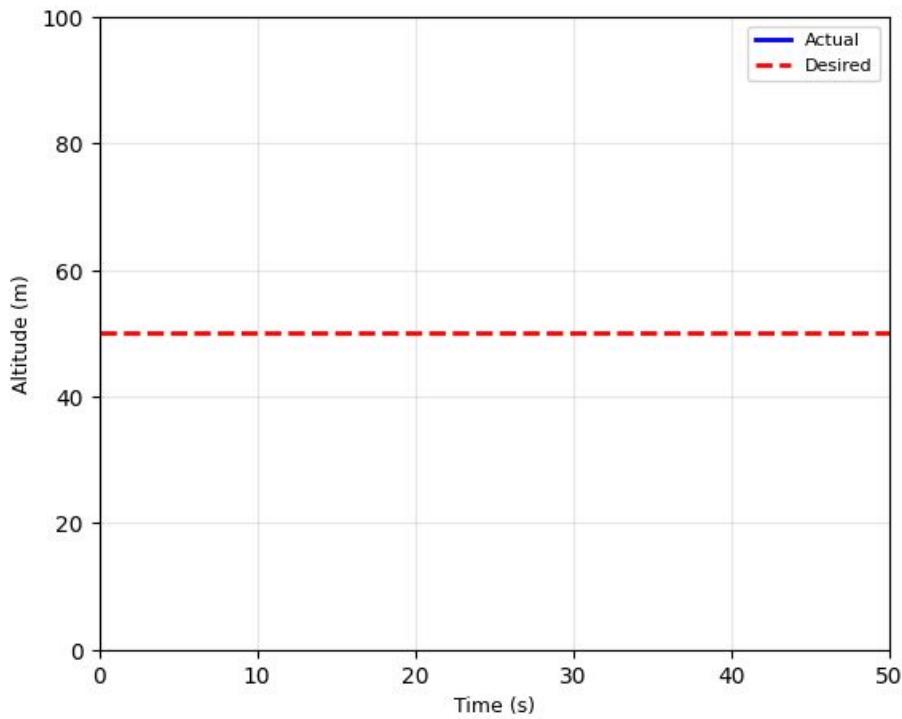


**Fig. 3.** Controller input step functions: (a) Step function. (b) Output of the controller (actual) given the input step function (desired).

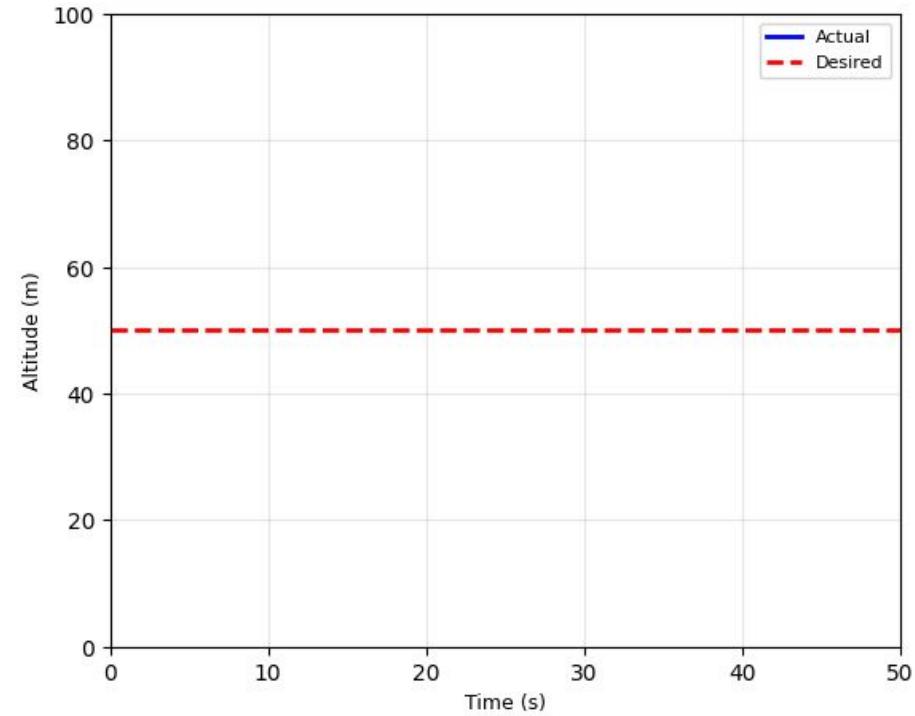
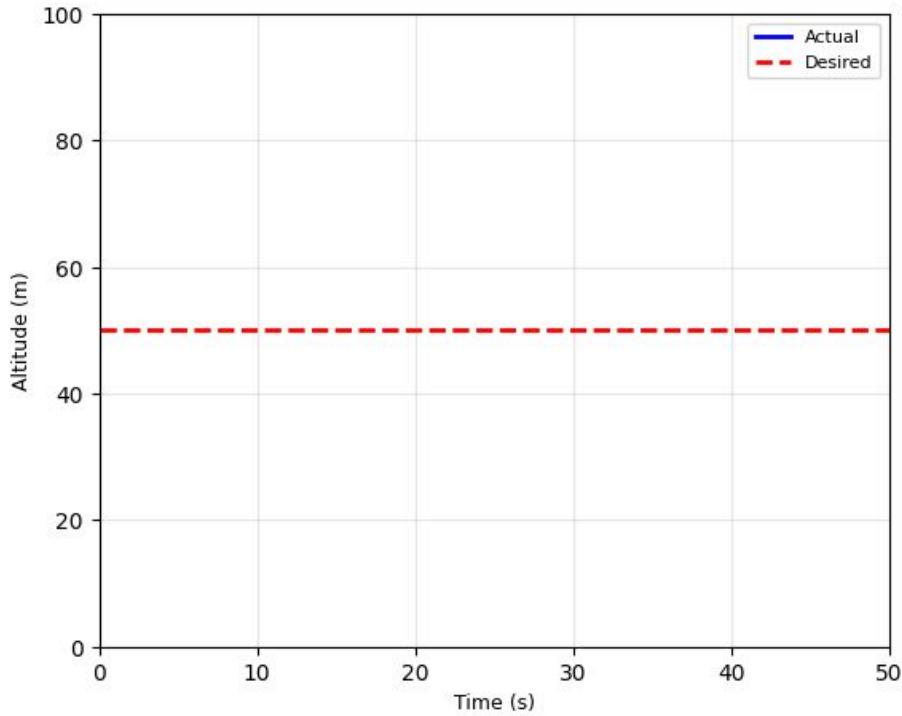
Error = Desired Position - Actual Position



\*disregard label names

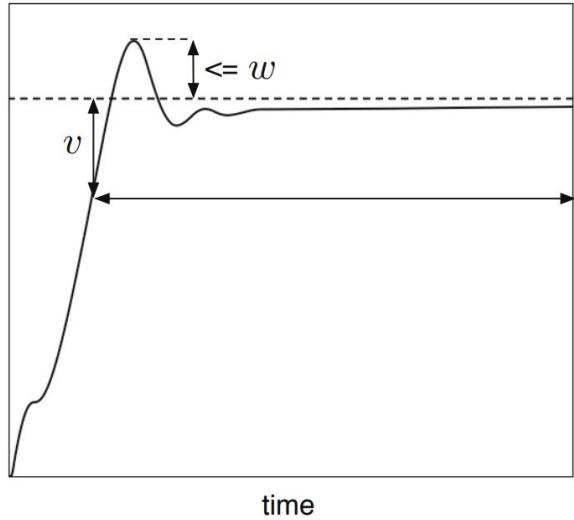


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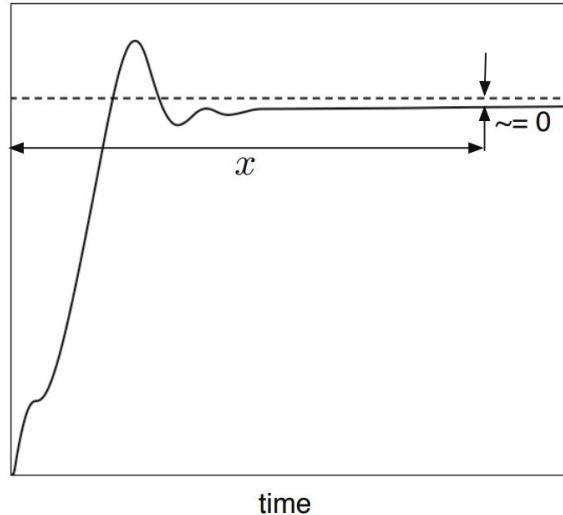


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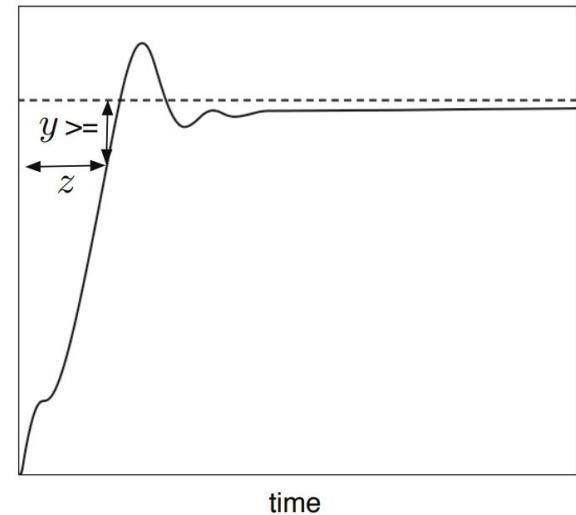
## Overshoot (Smoothness)



## Convergence (Liveness)

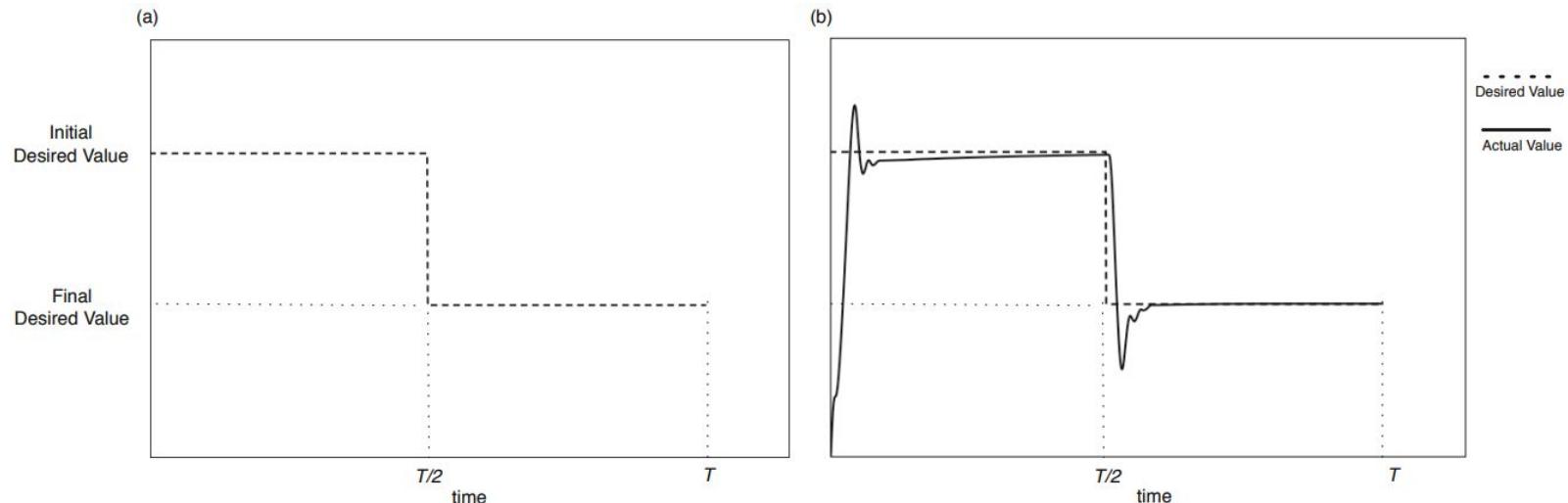
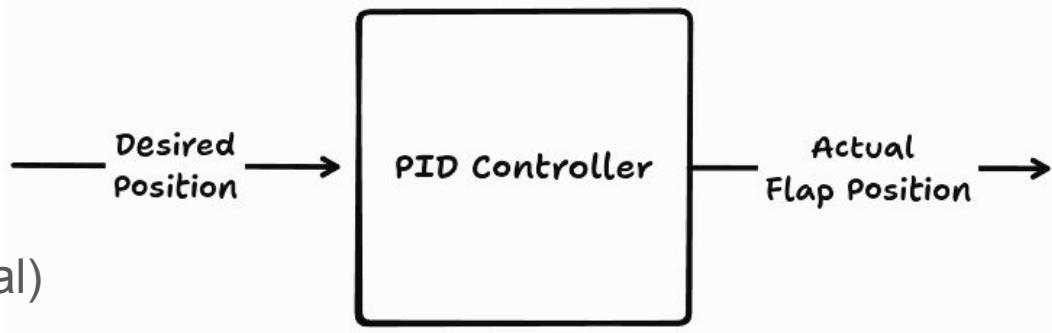


## Responsiveness



# Representation

(Desired, Actual)



**Fig. 3.** Controller input step functions: (a) Step function. (b) Output of the controller (actual) given the input step function (desired).

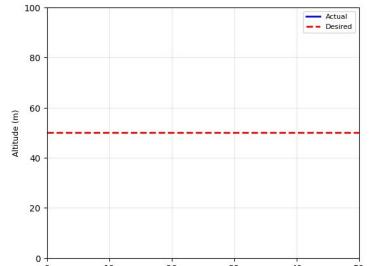
# Fitness O(Desired, Actual)

Overshoot  
(Smoothness)

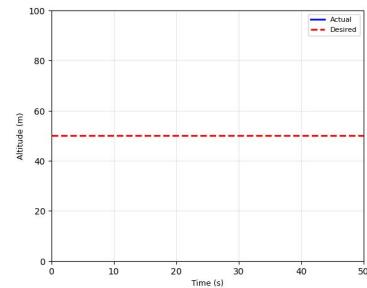
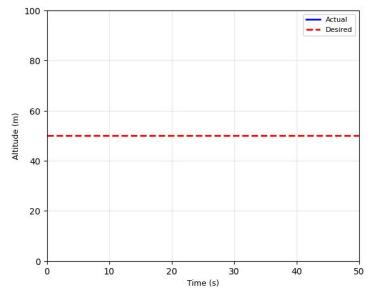
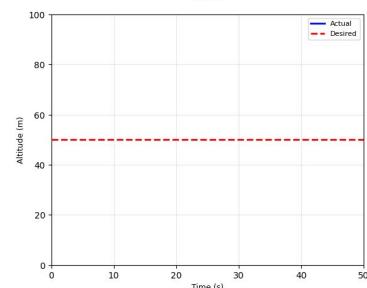
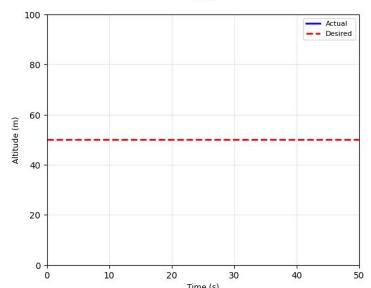
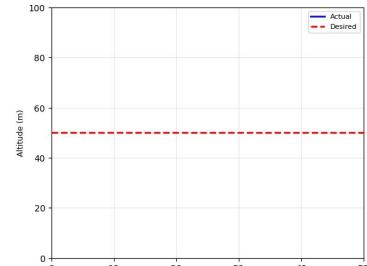
Convergence  
(Liveness)

Responsiveness

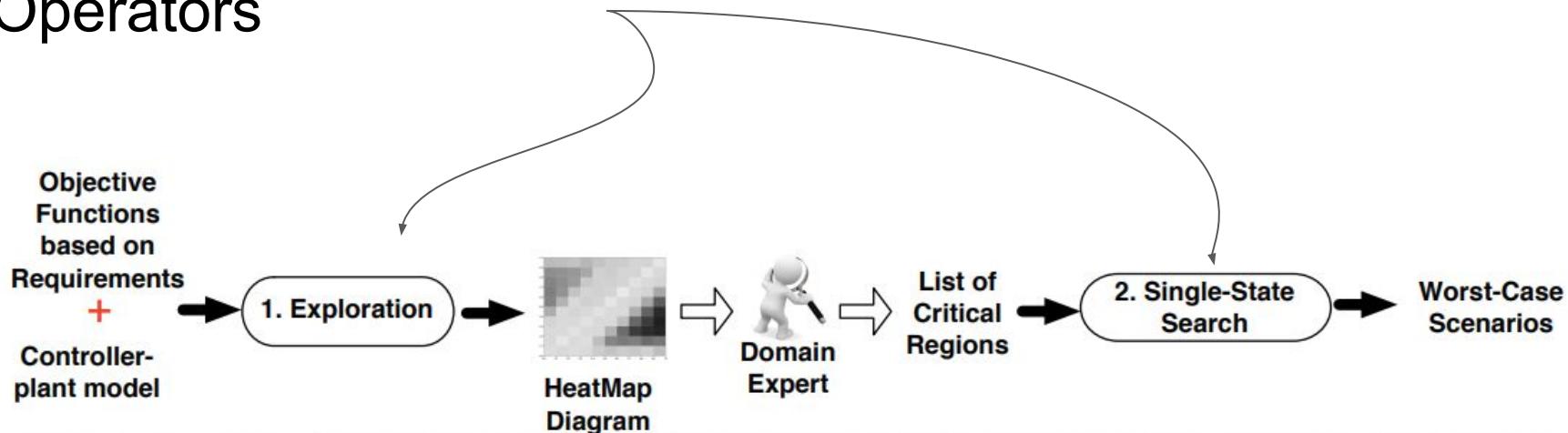
## Abnormal



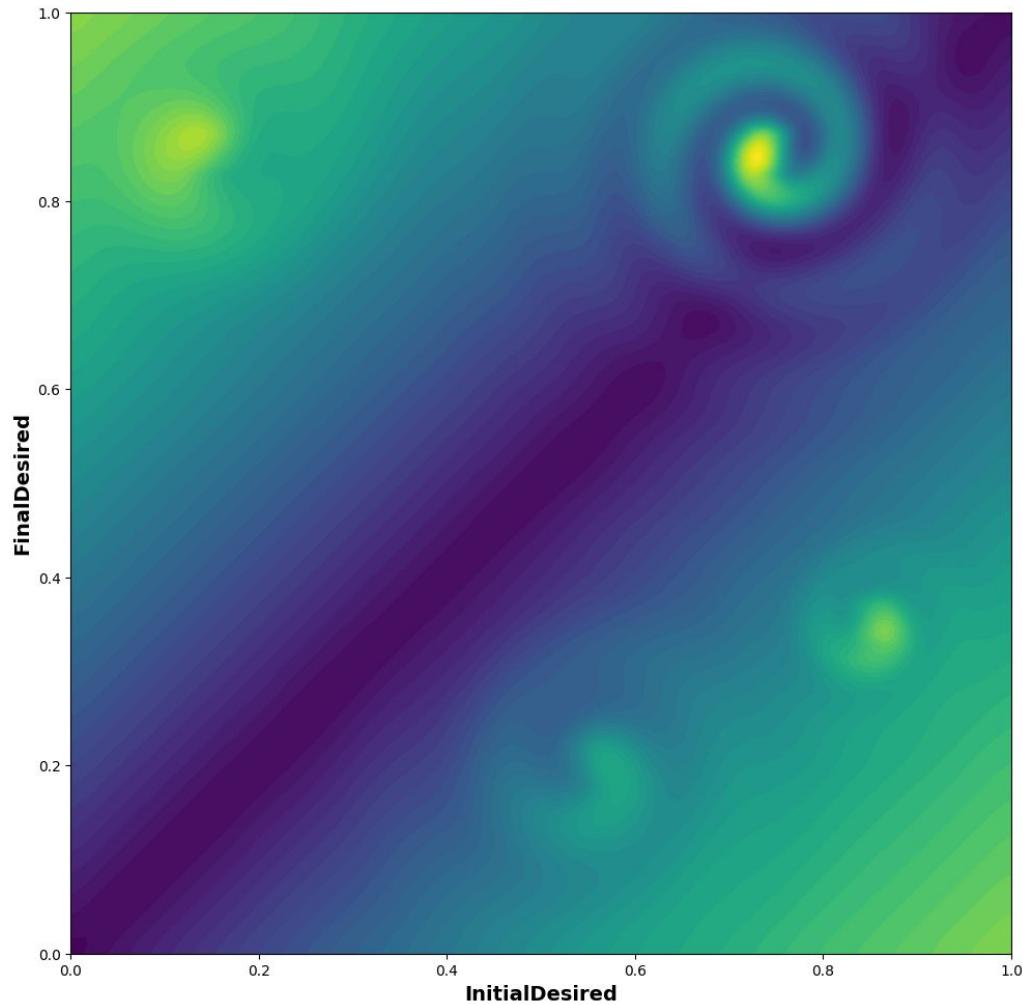
## Normal



# Operators



**Fig. 4.** An overview of our automated approach to MiL testing of continuous controllers.

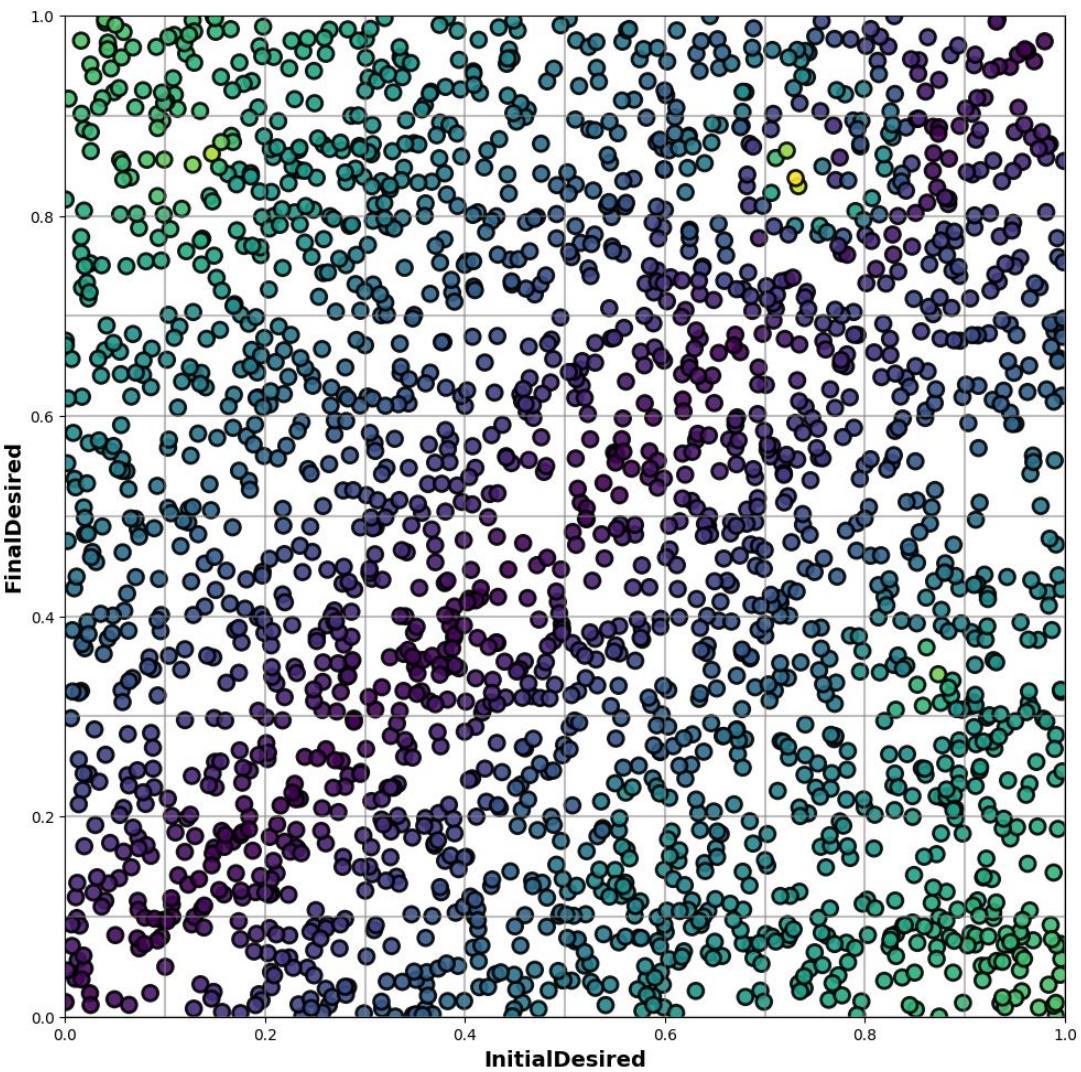


**Algorithm.** RANDOMEXPLORATION

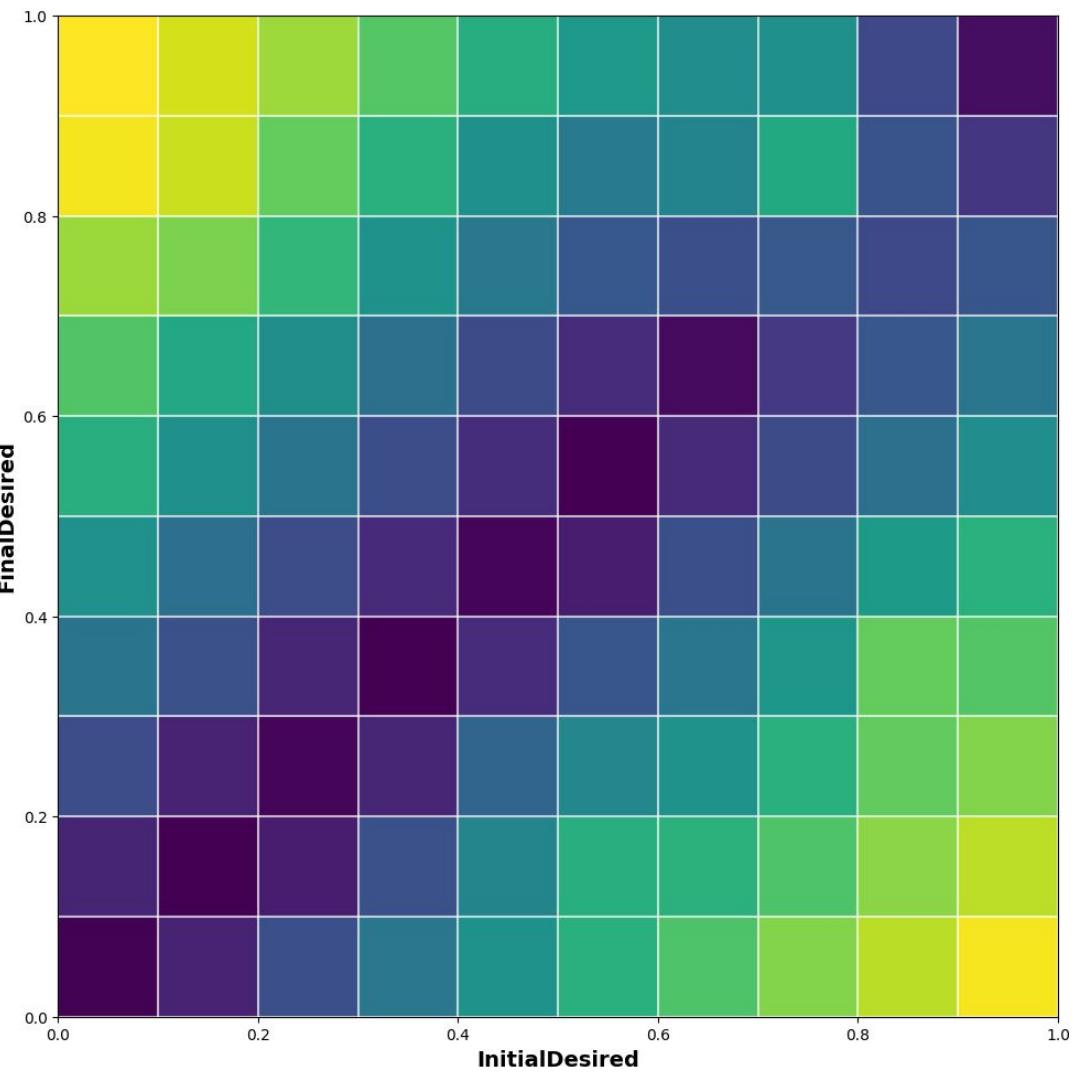
**Input:** A controller-plant model  $M$  with input search space  $S$ .  
An objective function  $O$ . An observation time  $T$ .

**Output:** An overview diagram (HeatMap).

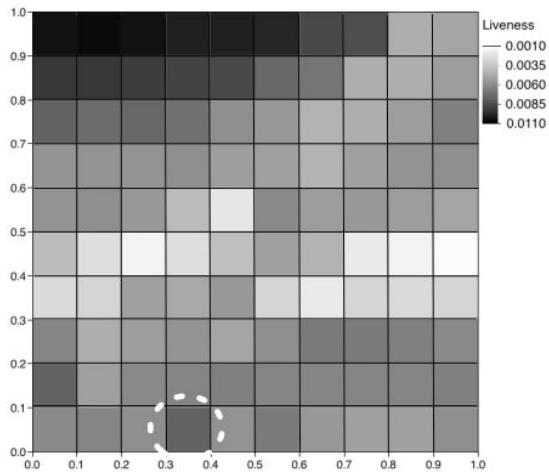
1. Partition  $S$  into equal sub-regions
2. Let  $P = \{\}$
3. **repeat**
4.   Let  $p = (\text{Initial Desired}, \text{Final Desired})$  be  
     a random point in  $S$
5.   Let Desired be a step function generated based on  $p$  and  $T$
6.   Run  $M$  with the Desired input to obtain the Actual output
7.    $o = O(\text{Desired}, \text{Actual})$
8.    $P = \{(p, o)\} \cup P$
9. **until** there are at least  $N$  points in each region of  $S$  **do**
10. Create a HeatMap diagram based on  $P$



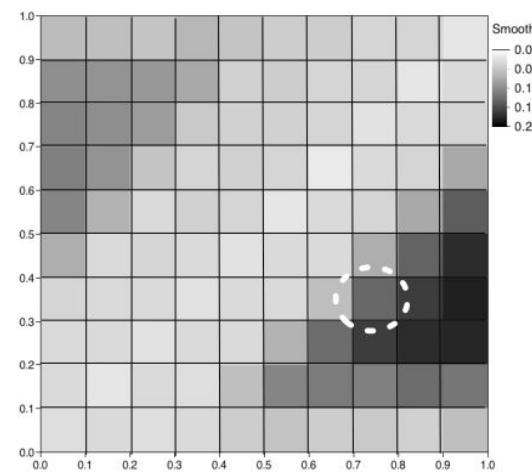
- (1) Confidence about the behaviors over the dark shaded regions.
- (2) The diagrams facilitate discovery of anomalies
- (3) A sharp contrast may indicate abnormal behavior



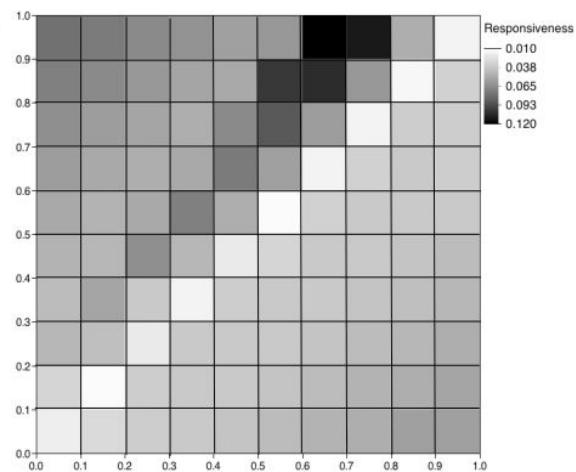
(a) Liveness



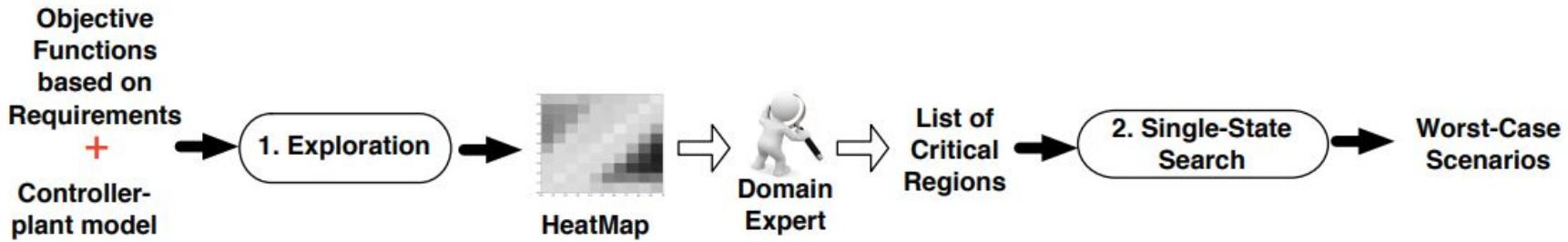
(b) Smoothness



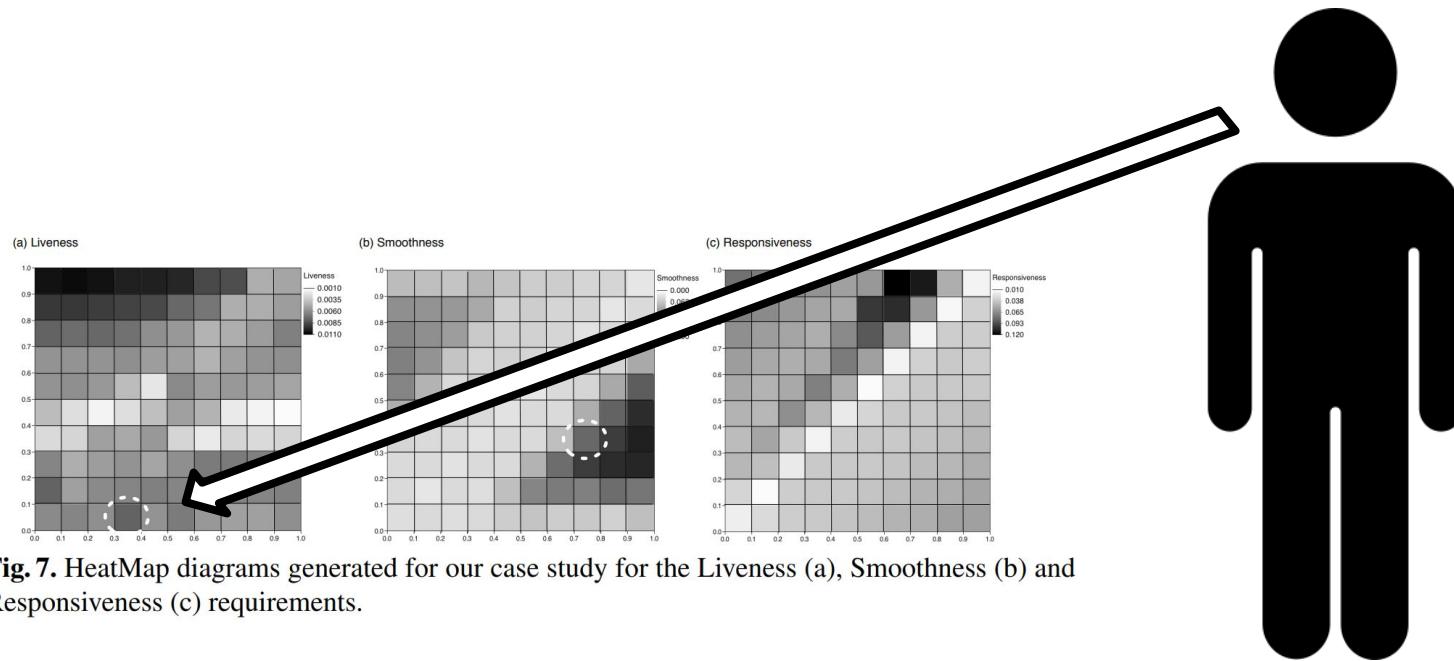
(c) Responsiveness



**Fig. 7.** HeatMap diagrams generated for our case study for the Liveness (a), Smoothness (b) and Responsiveness (c) requirements.



**Fig. 4.** An overview of our automated approach to MiL testing of continuous controllers.



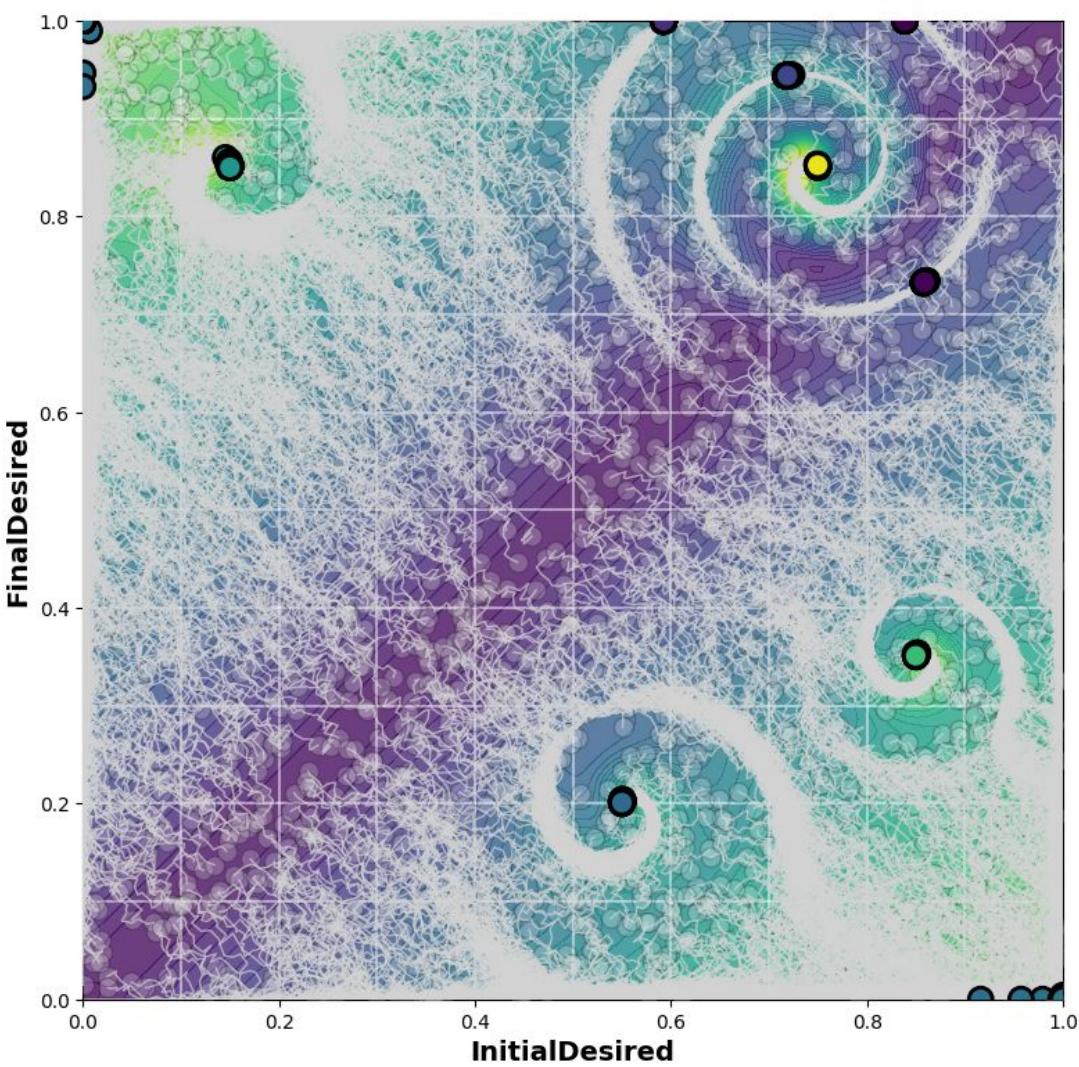
**Fig. 7.** HeatMap diagrams generated for our case study for the Liveness (a), Smoothness (b) and Responsiveness (c) requirements.

**Algorithm.** SINGLESTATESEARCH

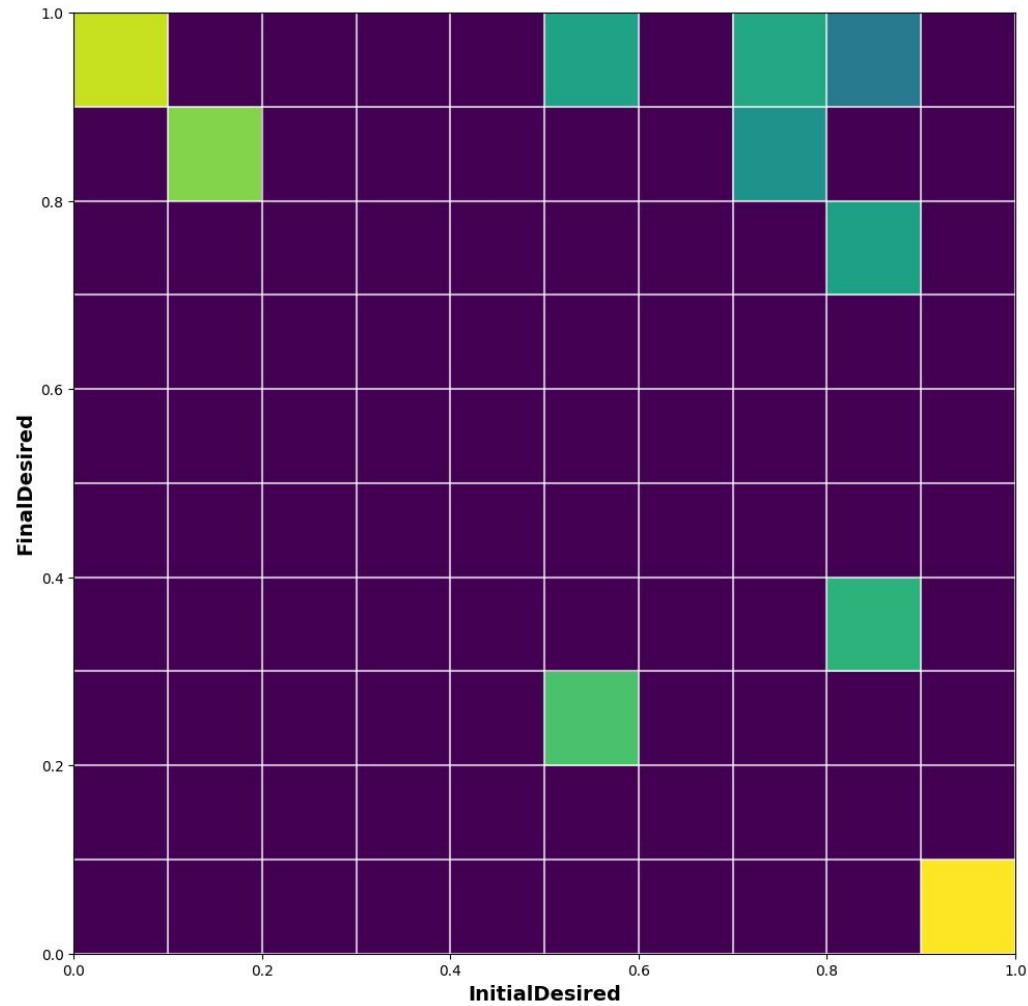
**Input:** A controller-plant model  $M$ . A region  $r$ .  
The set  $P$  computed by the algorithm in Figure 5(a).  
An objective function  $O$ .

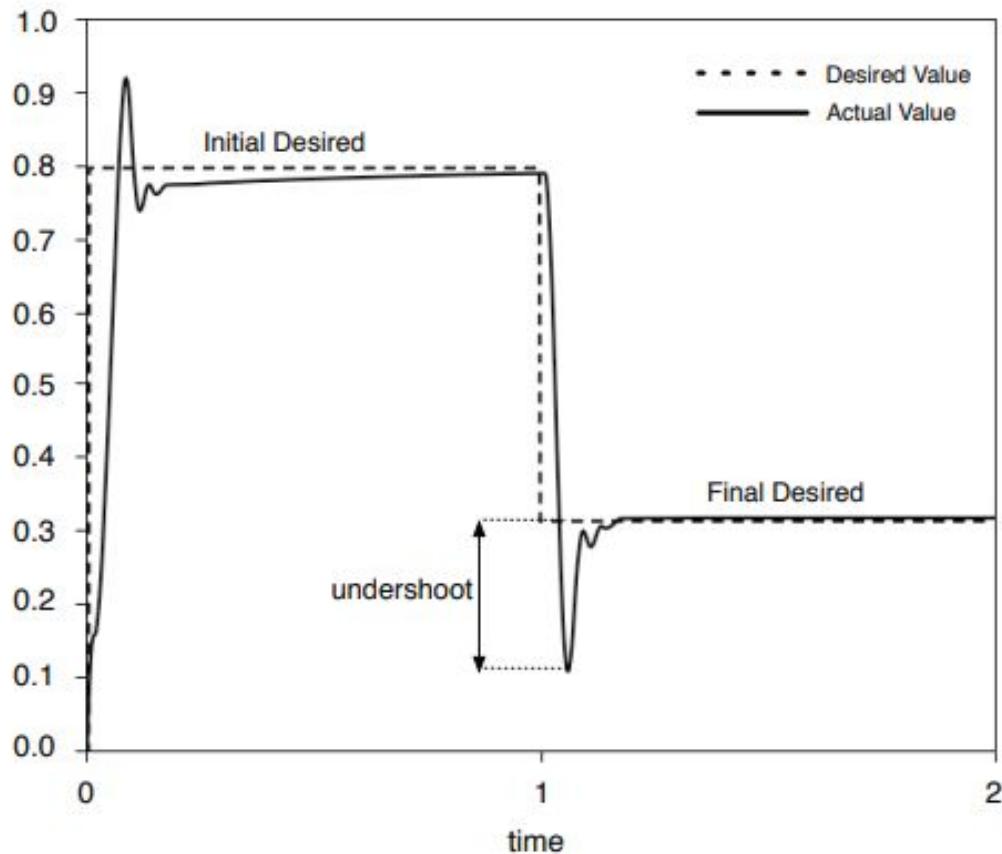
**Output:** The worst case scenario  $testCase$ .

1.  $P' = \{(p, o) \in P \mid p \in r\}$
2. Let  $(p, o) \in P'$  s.t. for all  $(p', o') \in P'$ , we have  $o \geq o'$
3.  $worstFound = o$
4. **for** K iterations :
5.   Let Desired be a step function generated by  $p$
6.   Run  $M$  with the Desired input to obtain the Actual output
7.    $v = O(\text{Desired}, \text{Actual})$
8.   **if**  $v > worstFound$  :
9.      $worstFound = v$
10.     $testCase = p$
11. **return**  $testCase$

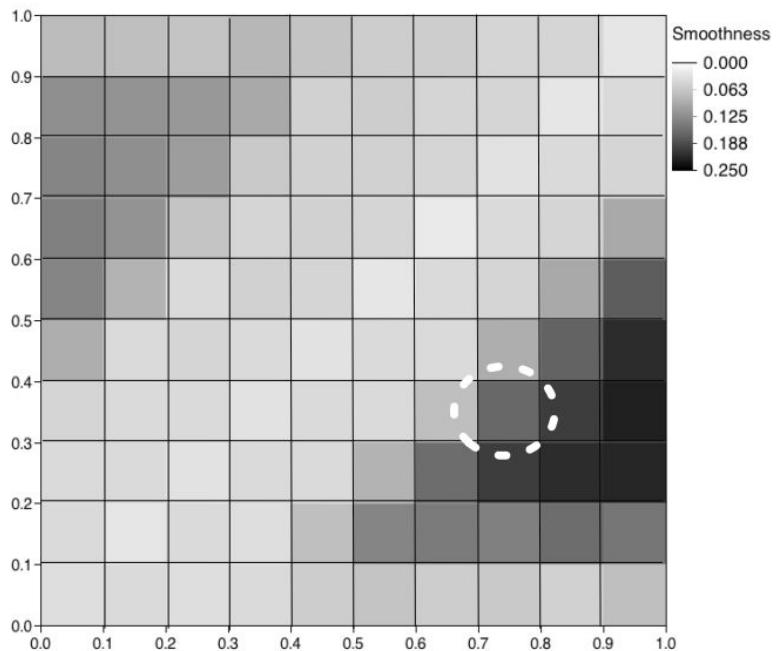


- 11 worst case scenarios
- Requirements violations
- Controller model error
- Plant model error

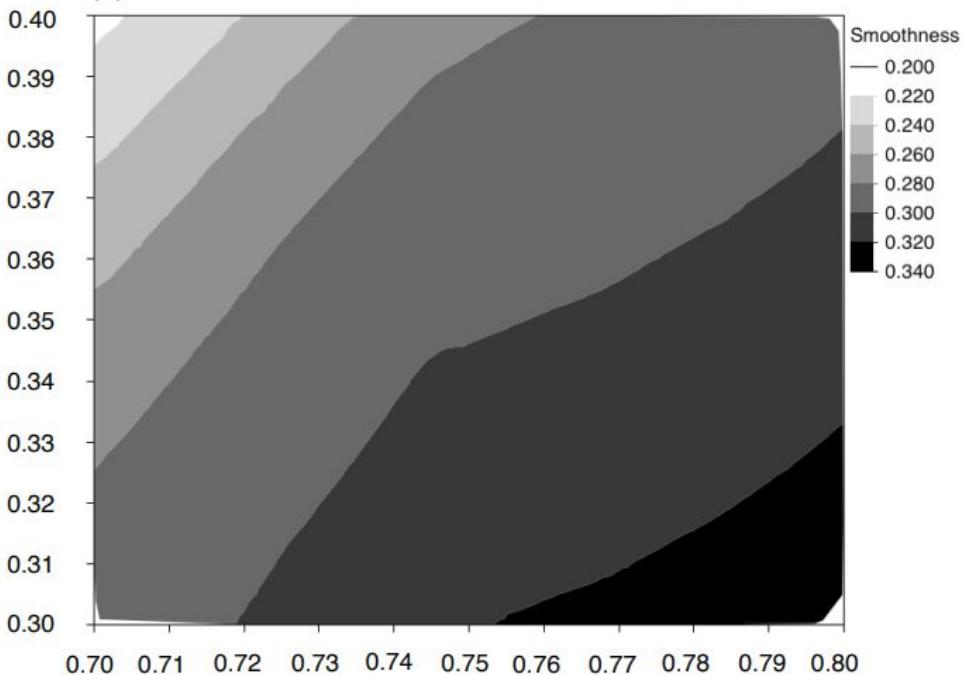




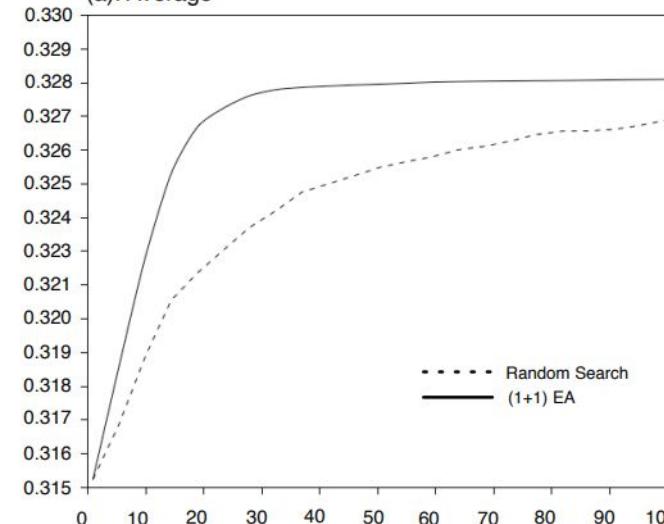
(b) Smoothness



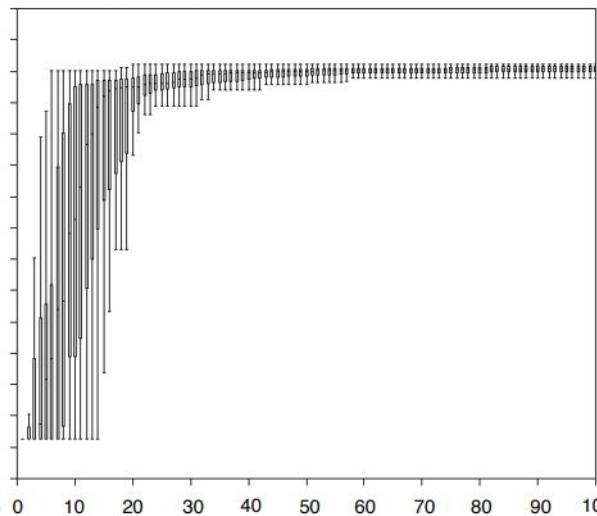
(a)



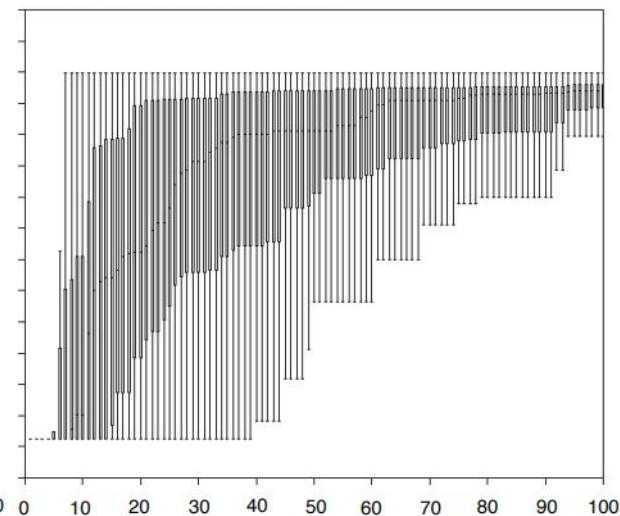
(a). Average



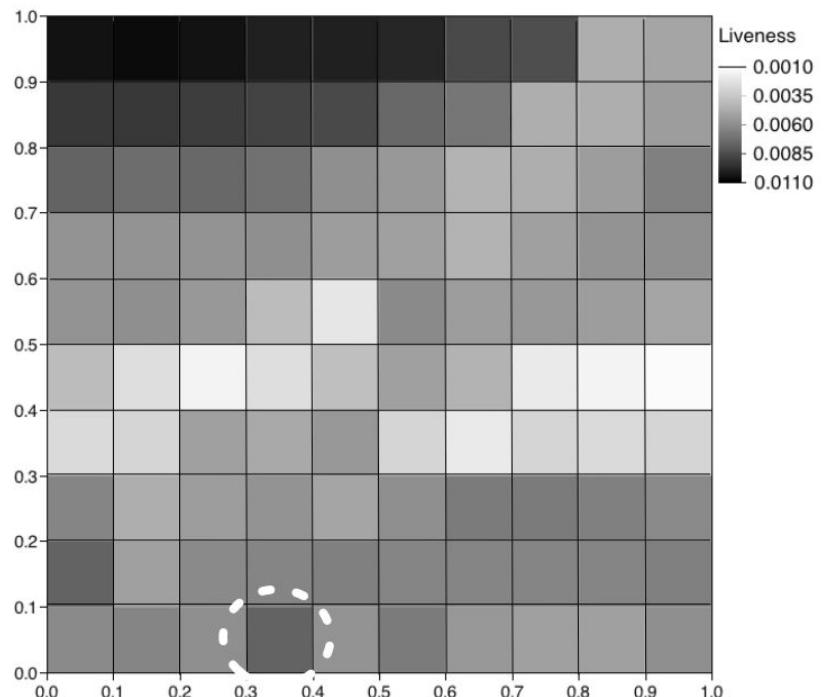
(b). (1+1) EA Distribution



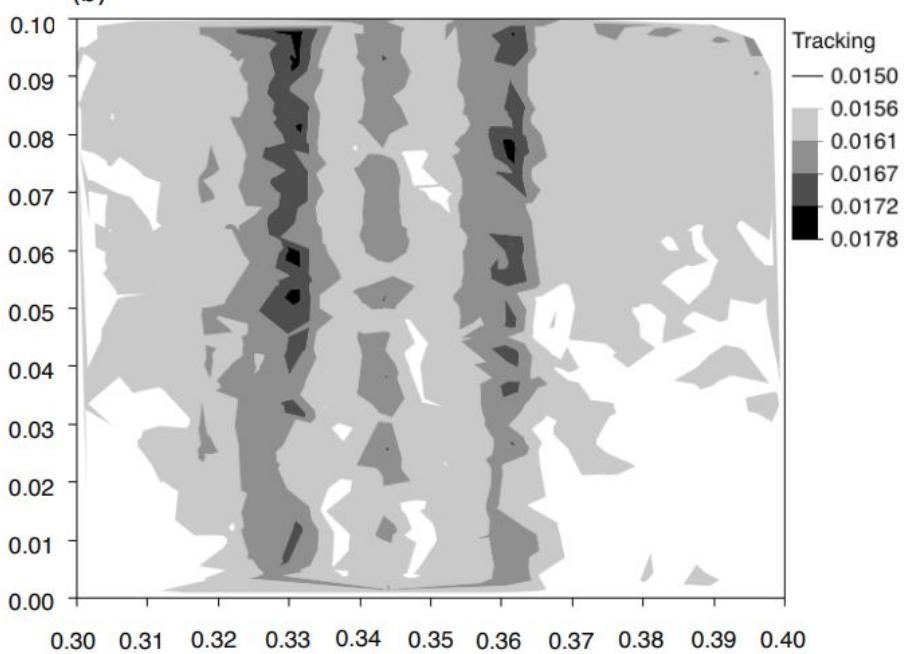
(c). Random Search Distribution



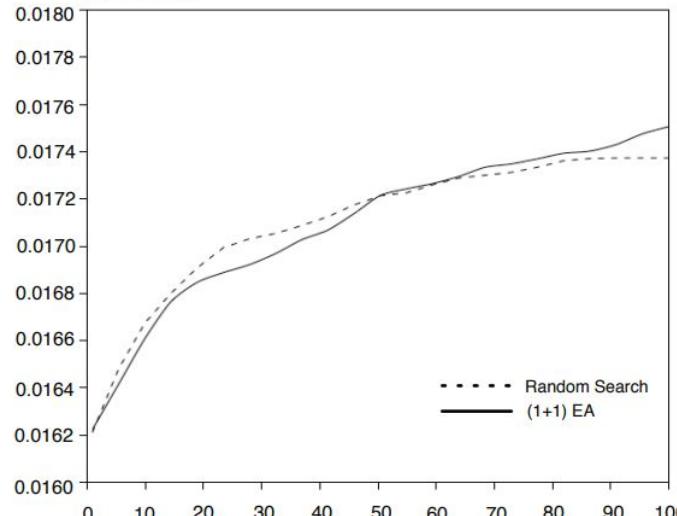
(a) Liveness



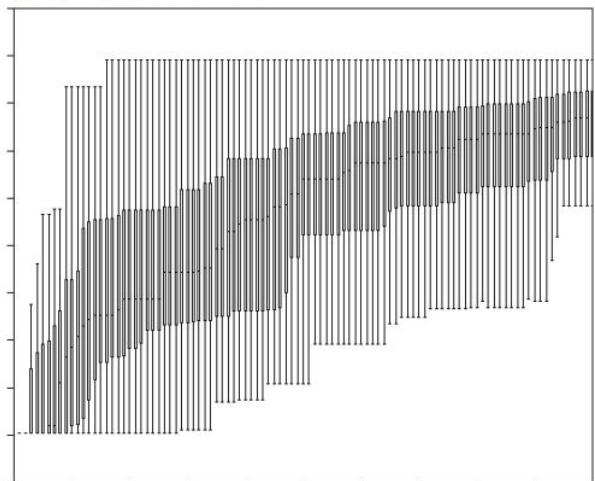
(b)



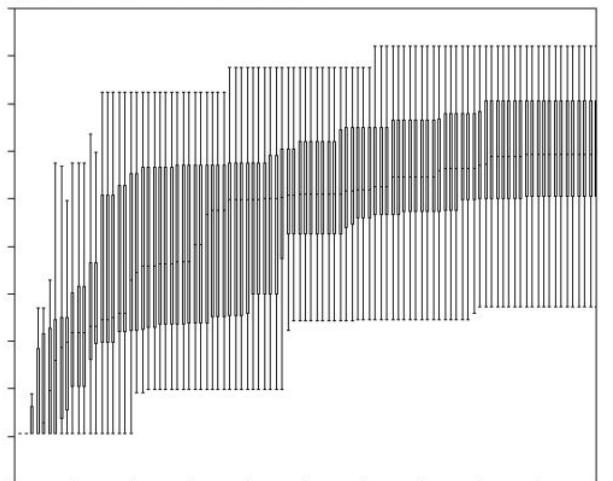
(d). Average

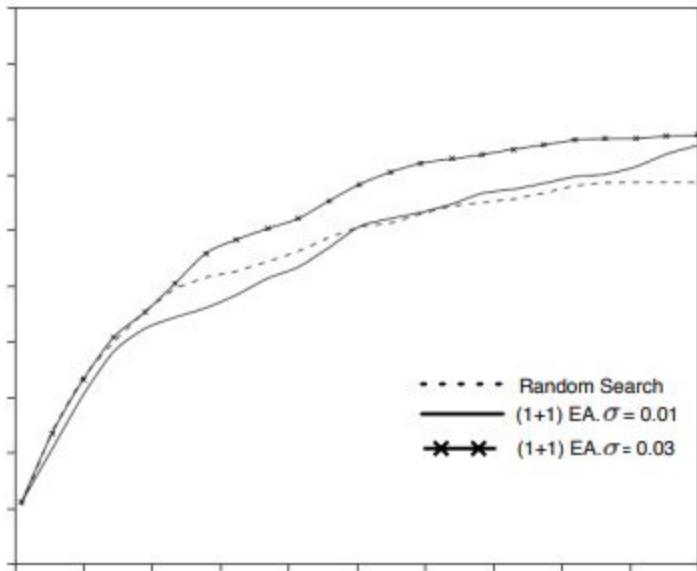


(e). (1+1) EA Distribution



(f). Random Search Distribution

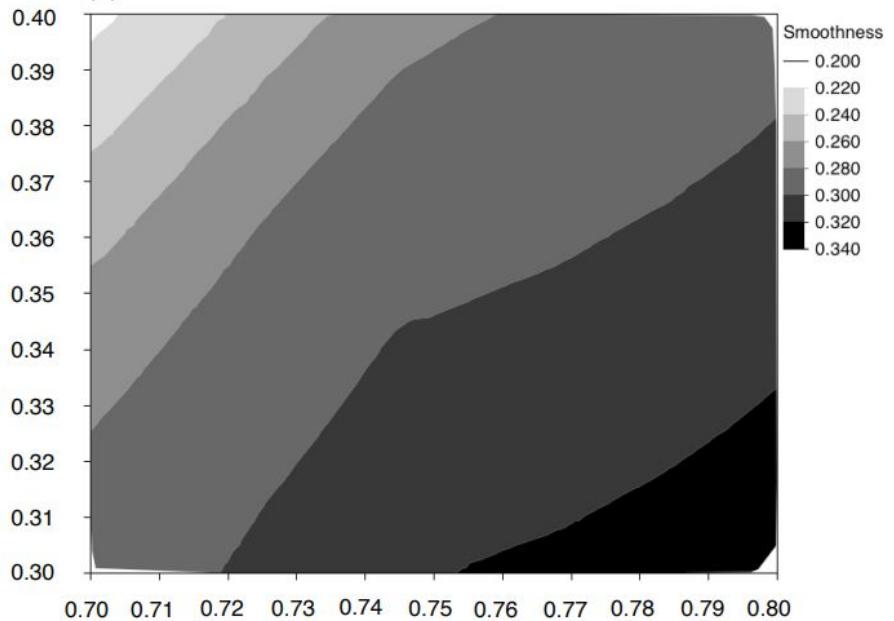




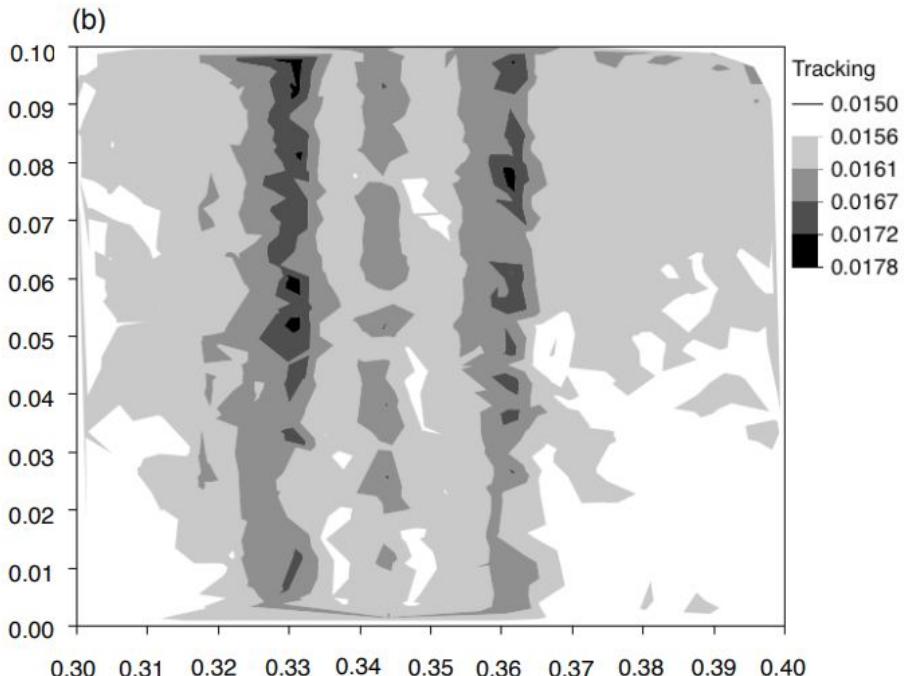
**Fig. 10.** Comparing average values for (1+1) EA with  $\sigma = 0.01$ , (1+1) EA with  $\sigma = 0.03$ , and random search for the region in Figure 7(a)

# TAKEAWAYS

(a)



(b)



# No one tool for the job

## Random Search:

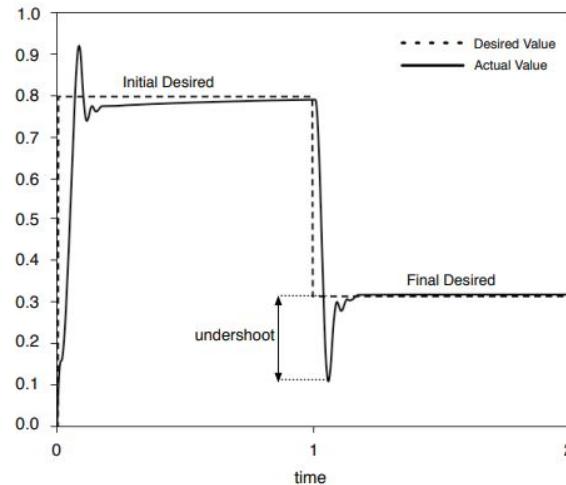
- Terrible for finding exact peaks
- Effective at finding which hills are worth climbing

## Local Search:

- Terrible for global search (stuck in local peaks)
- Effective at finding the precise peak in a specific area

# Turn requirements into numbers

- Translate qualitative into quantitative
- Frame as an optimization problem



Did it overshoot?

Qualitative	Quantitative
Yes	$O_s = \max error(t)  = 0.2$

*Oracle problem:* automatically determining if a program's output is correct for a given input

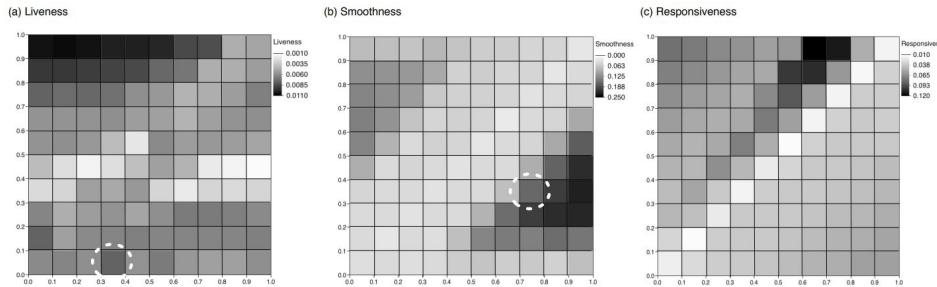
# **CRITICISMS**

# Novelty and Significance

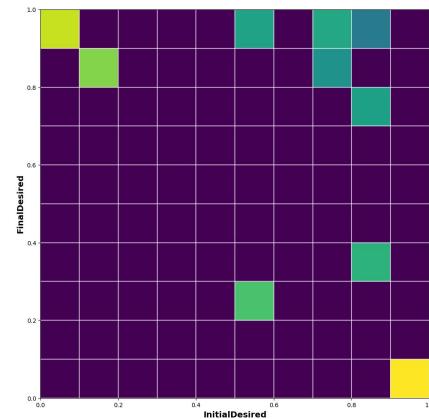
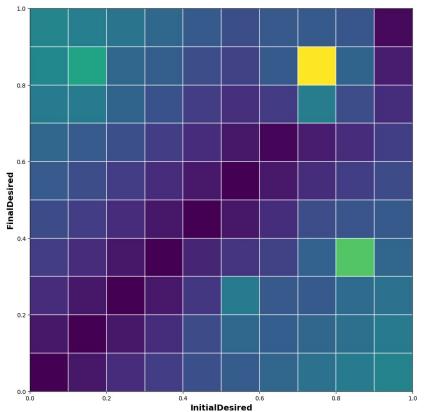
- The general concept had been already established by prior work  
(eg, Lindlar et al., 2009)
- Automated and more effective alternative to manual testing.
- Demonstration of requirements into objective functions.
- Two-phase workflow
- Heatmap to convey the information
- Three generic controller metrics  
(reusable for this class of problem)

# Soundness and Verifiability

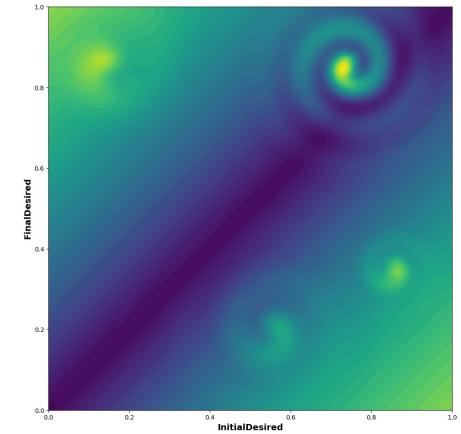
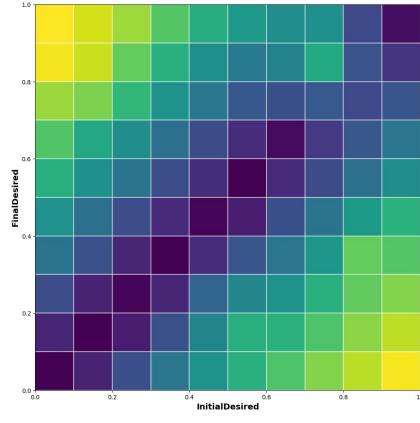
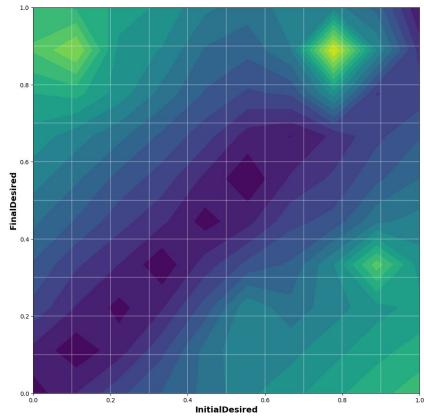
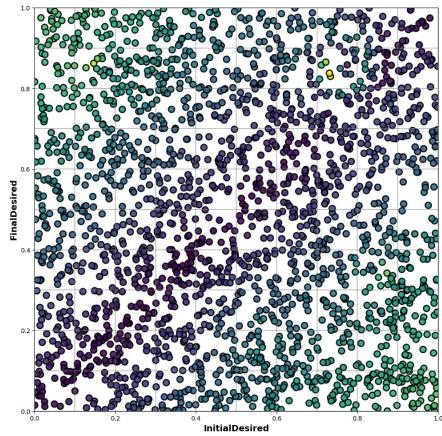
- Simplified 2D search space (fixed all other system inputs).
  - How well would the methodology scale as more parameters are added?
- Reliability of humans in the loop



**Fig. 7.** HeatMap diagrams generated for our case study for the Liveness (a), Smoothness (b) and Responsiveness (c) requirements.



# Soundness and Verifiability



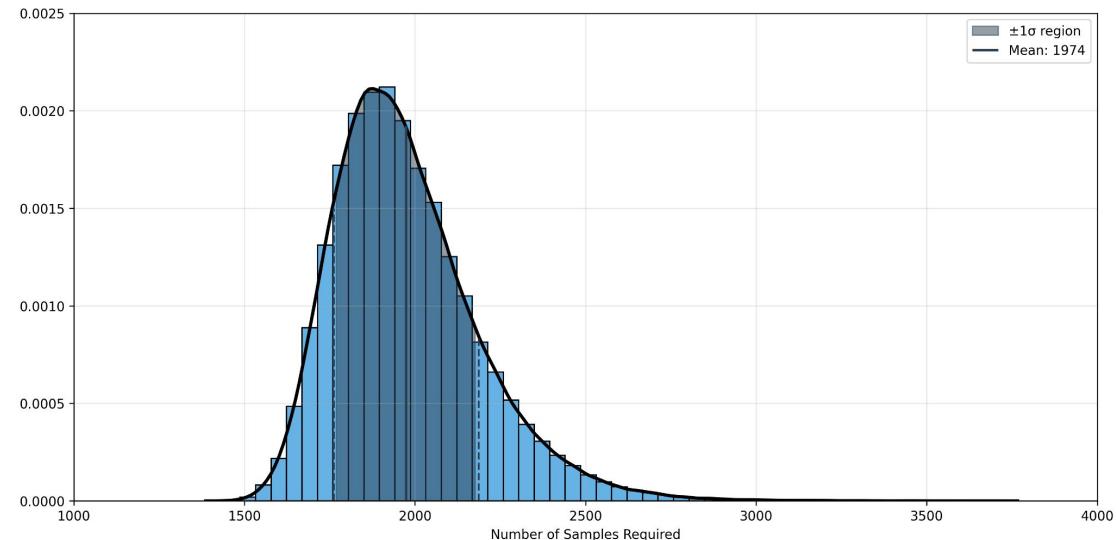
# Soundness and Verifiability

## Algorithm. RANDOMEXPLORATION

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An objective function  $O$ . An observation time  $T$ .
- Output:** An overview diagram (HeatMap).
1. Partition  $S$  into equal sub-regions
  2. Let  $P = \{\}$
  3. **repeat**
  4.   Let  $p = (\text{Initial Desired}, \text{Final Desired})$  be a random point in  $S$
  5.   Let Desired be a step function generated based on  $p$  and  $T$
  6.   Run  $M$  with the Desired input to obtain the Actual output
  7.    $o = O(\text{Desired}, \text{Actual})$
  8.    $P = \{(p, o)\} \cup P$
  9. **until** there are at least  $N$  points in each region of  $S$  **do**
  10. Create a HeatMap diagram based on  $P$

200k Monte Carlo Runs  
 $E[N]: 1974$   
 $\sigma(N): 212$

Min: 1442  
Max: 3711



*"We decided to generate around 1000 points in  $S$  during the exploration step."*

# Soundness and Verifiability

## Algorithm. RANDOMEXPLORATION

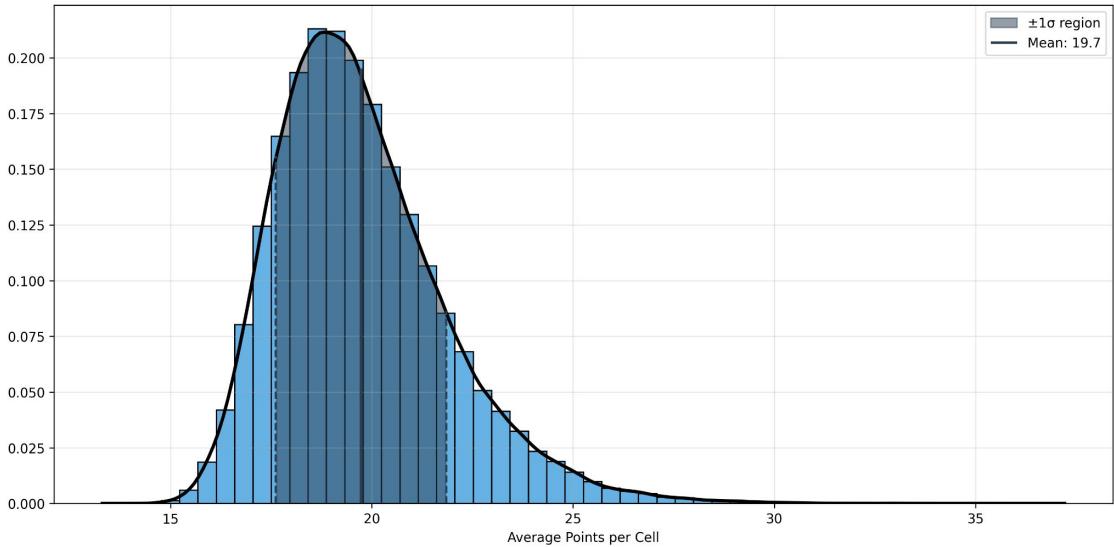
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200k Monte Carlo Runs  
 $E[N]: 1974$   
 $\sigma(N): 212$

Min: 1442  
Max: 3711



*“We divided up  $S$  into 100 equal squares [...] at least 10 points are simulated in each region during exploration”*

# Final Assessment

- Well written, structured and motivated
- Good figures
- Implementation details and rationale could have been a bit more clear
- Demonstrates the search-based approach outperformed humans and random search
- Critical regions are not always trivial to identify by eye
- Rationale for sampling strategy could have been explained in more detail

# THANK YOU!

+ Q&A