

Recursion

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① Sub-Sequence

void subsequence(string in, string out)

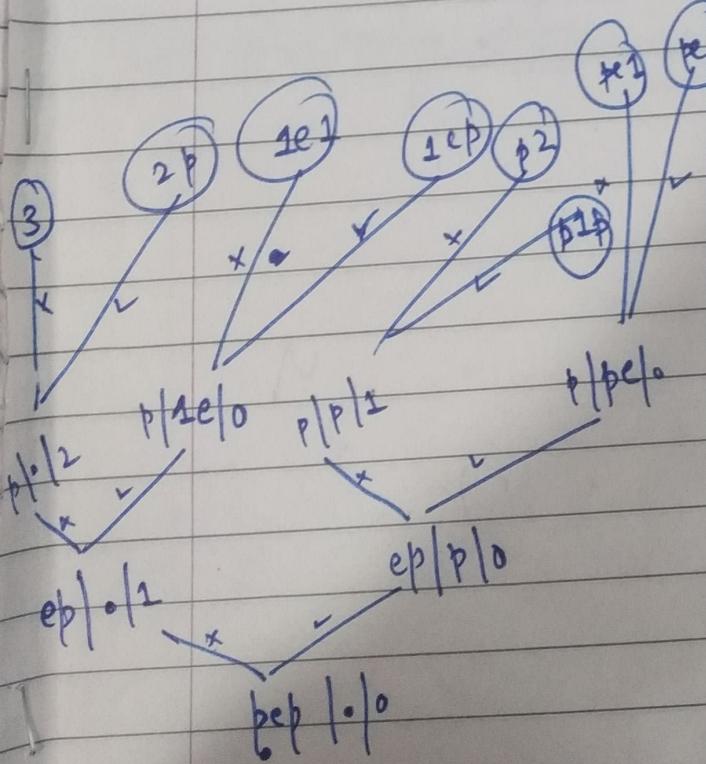
```
{
    if (in.length() == 0)
        cout << out; return;
```

```
subsequence(in.substr(1), out + in[0]);
subsequence(in.substr(1), out);
```

{}

bench UP
1.1

pep	0 000 pep
②	0 01 pep
③	0 10 p1p
④	0 10 p2p
⑤	1 01 1ep
⑥	1 10 2p
⑦	1 11 3



```
void solve (string in, out, count)
{
    if (str.length() == 0)
        cout << out + count;
    else
        cout << out;
    return;
}
```

```
if (count == 0)
    solve (in.substr(1), out + in[0]);
```

```
else
    solve (in, out + in[0], count + 1);
```

```
solve (-, count + 1, out);
```

↓

⑧ → count + 1
⑨ → 0

(2)

Phone Key pad

`vector<string> keypad = { "", "", "abc", "def", "ghi", "jkl",
 "mno", "pqrs", "tuv", "wxyz" };`

`void phonkeypad (vector<int> in, stringout, int i){`

`if (i == in.size())`

`cout << out; return;`

`if (in[i] == 0 || in[i] == 1)`

`phonkeypad (in, out, i + 1);`

`for (int k = 0; k < keypad[in[i]].length(); k++)`

`phonkeypad (in, out + keypad[in[i]][k], i + 1);`

3 4

③

Pn C

arr(4,0)

↑

```
void permute (vector<int> arr, tq, q, psf, string ans)
{
    if (tq == q)
        cout << ans; return;
```

```
for (int box = 0; i < arr.size(); i++)
{
    if (arr[box] != 1) arr[box] = 1;
    permute (arr, tq - 1, q, psf + 1, ans + "q, " + box + " ");
    arr[box] = 0;
}
```

void combination

-1

int box = index + 1

(box)

→ coin change \leftarrow can use same coin multiple time

(int)

o

(4) Board Ladder

```

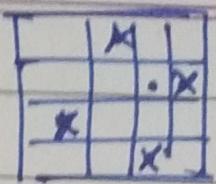
void BoardGame ( int src, int dest, ladder, string ans )
{
    if (src == dest) cout << ans; return;
    if (src > dest) return;

    // 1, 6 opening
    if (src == 0)
    {
        boardGame (1, dest, ladder, ans + "1");
        boardGame (1, dest, ladder, ans + "6");
    }

    // Ladder
    if (ladder[src] != 0)
        boardGame (ladder[src], dest, ladder, ans + (ladder[src] + "L"));
    else
        for (dice = 1; dice <= 6; dice++)
        {
            int inter = src + dice;
            boardGame (inter, dest, ladder, ans + "dice");
        }
    }
}

```

(5)

N-Queen

```
void nqueen(vector<vector<int>> chess, int tq, string ans, int index) {
    if (tq == chess.size())
        cout << ans; return;
```

```
for (int i = index + 1; i < chess.size() * chess.size();)
    { int row = i / chess.size();
      int col = i % chess.size();
```

Permutation

& not
Combination

```
if (chess[row][col] == 0)
    { if (isqueenSafe(chess, row, col))
```

```
        { chess[row][col] = 1;
```

```
        nqueen(chess, tq + 1, ans + (i), i)
```

```
        chess[row][col] = 0;
```

```
} }
```

```
}
```

→ bool isQueenSafe (chess, row, col)

{

vector <vector < int >> dir =

{ { -1, 0 }, { 1, 0 }, { 2, 1 }, { -1, -1 }, { 0, 1 }, { 0, -1 }
 { -1, 1 }, { 1, -1 } },

for (int i=0 ; dir.size() ; i++)

{ for (int dist=1, true ; dist++)

{ int equal = col + dist * dir[i][1];
 int equalRow = row + dist * dir[i][0];

, if (equal < 0 || equal >= chess.size() - 1
 break;

if (chess[equal][equal] == 1)

return false;

 }

return true;

}

→ bool isKnightSafe

{ { -1, 2 }, { 1, -2 }, { -2, 1 }, { 2, 1 }, { -1, -2 }, { 1, 2 }
 { -2, -1 }, { 2, -1 } }

for (int i=0 ; i < dir.size() ; i++)

int equal = col + dir[i][1];

int equalRow = row + dir[i][0];

⑥ Permutation

abc cat
acb cab
bac acb
bca bac

⑦ Ge

```
void permutation(string in, string ans)
{
    if (in.length() == 0)
        cout << ans << endl;
}
```

```
for (int i = 0; i < in.length(); i++)
{
    char ch = in[i];
    string left = in.substr(0, i);
    string right = in.substr(i + 1);
    permutation(left + right, ans + ch);
}
```

① Generate Brackets

```
void generateBrackets( int i, int n, int closing,  
                      just opening  
                      string ans )  
{ if ( i == 2 * n )  
    cout << ans; return;  
  
if ( opening < n )  
    generate( i+1, n, closing, opening+1, ans + "{" );  
  
if ( closing < opening )  
    generate( i+1, n, closing+1, opening, ans + "}" );  
}
```

⑧ 0/1 Knapsack

2^n

$(n+m)$

problem No.

Date

DP

int knapsack (vector<int> weight, vector<int> pri, ^(w))

int ⁱ, int cap,

{ if (i == w.size || cap == 0)
return 0;

int ans = 0;

int inc, exc = 0;

if (cap >= w[i])

{ inc = p[i] + knapsack (w, p, i+1, ^{cap})
exc = knapsack (w, p, i+1, cap);

ans = max (inc, exc)

return ans;

dP[i][~~cap~~]

]

→ Fractional Knapsack

Pri

280 ¹
²

weight

40

100 ¹
²

10

20 ³

120

ratio

7

10

6

5

cap = 60

50-10-50-40
5-10

sort

10

7

6 5

⑩ Solve Sudoku - Backtracking

```
bool solve (int mat[9][9], int i, int j, int n)
{
    if (i == n) pointMat. return true;
```

// next line if (j == n)

```
return solve (mat, i + 1, 0, n);
```

// prefilled if (mat[i][j] != 0)

```
return solve (mat, i, j + 1, n);
```

```
for (int num = 1; num <= 9; num++)
```

```
{ if (canPlace (mat, i, j, num))
```

```
{ mat[i][j] = num;
```

```
bool canWeSolve = solve (mat, i, j + 1, n);
```

```
if (canWeSolve)
```

```
return true;
```

```
}
```

```
}
```

```
mat[i][j] = 0;
```

```
return false;
```

```
}
```

bool canPlace (int mat [] [], int i, int j, int num)

{

// row & col

for (int x = 0; x < n ; x++)

{ if (mat [i] [x] == num || mat [x] [j] == num)

return false;

}

// small box

int &n = sqrt (n);

int sx = (i / &n) * &n ;

int sy = (j / m) * &n ;

for (int x = sx ; x < sy + &n ; x++)

for (y = sy ; y < sy + &n ; y++)

if (mat [x] [y] == num)

return false;

return true;

}

⑪ Reverse Stack

```
void reverse ( stack<int> s )
{
    if ( s.empty() ) return;
    int top = s.top();
    s.pop();
    reverse ( s );
    insertAtBottom ( s, x );
}
```

```
void insertAtBottom ( stack<int> s, int x )
{
    if ( s.empty() )
    {
        s.push ( x );
        return;
    }
    int top = s.top();
    insertAtBottom ( s, x );
    s.push ( top );
}
```

"123" → ABC
A W
L C

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(12)

Num To Char

```
void numToChar(string in, string out, int i)
{
    if(i >= in.length())
        cout << out << endl;
}
```

```
int fdigit = in[i] - '0';
char ch = fdigit + 'A' - 1;
```

```
numToChar(in, out + ch, i+1);
```

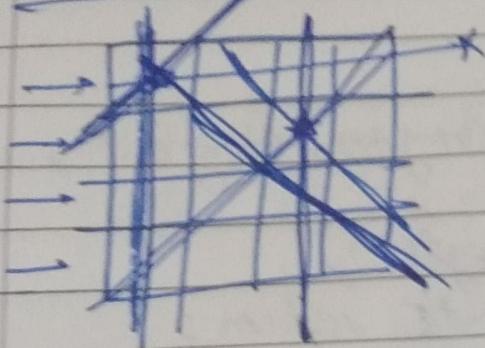
```
if(i+1 != in.length())
{
    int sdigit = in[i+1] - '0';
    int no = fdigit * 10 + sdigit;
    if(no <= 26)
        char ch = no + 'A' - 1;
    numToChar(in, out + ch, i+2);
}
```

}

(5.2)

N-Queen

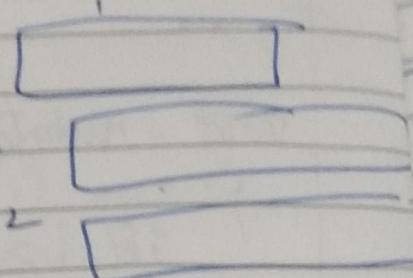
(13)



col

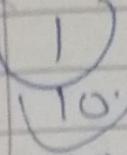
ds

diagonal



lexi

(14)



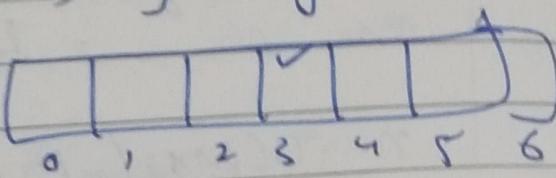
10

10

1

~~8-C~~

	0	1	2	3
0	0	1	2	3
1	1	2	3	4
2	2	3	4	5
3	3	4	5	6

 $(2 \times n) - 1$ diagonals~~8-C~~

	0	1	2	3
0	0	-1	-2	-3
1	-1	0	-1	-2
2	-2	1	0	-1
3	-3	2	1	0

(4-1)

(4-3)

```
void solve (row, n, diag1, diag2, col, ans)
```

```
{ if (row == n)
```

```
    cout << ans; return;
```

```
    for (c = 0; c < n; c++)
```

```
{ if (col[c] == false && diag[r+c] ==
```

```
&& diag[r+c+n-1] == false)
```

```
{
```

```
     = true.
```

```
solve (row+1, n, diag1, diag2, col,
```

```
ans + "row" + "
```

diag1[]

diag2[2n-1]

col[n]

solve(0, diag1, diag2, ans);

```
 = false
```

Lexical Order

Dictionary type

1000.

(14)

(1)

100

1000

(11)

+

1

1

1

1

101

111

102

112

1

1

1

1

109

119

int n = 1000;

```
for (int i=1; i<=9; i++)
    dfs(i, n);
```

```
void dfs(int i, int n)
{
    if (i > n) return;
    cout << i;
    for (int j=0; j<10; j++)
    {
        dfs(i*10 + j, n);
    }
}
```