

# Segmentation

## Principles and pitfalls

Elie Gurarie



17. - 28. JUNE 2024 IN GERMANY



# Behaviors are always changing!

It can be important and interesting to know **where / when / why**.

Lots of work has gone into finding where a movement track changes properties.  
This is, broadly, called *segmentation*.

## Journal of Animal Ecology

*Journal of Animal Ecology* 2016, **85**, 69–84



doi: 10.1111/1365-2656.12379

SPECIAL FEATURE: STUCK IN MOTION? RECONNECTING QUESTIONS AND TOOLS IN  
MOVEMENT ECOLOGY

### What is the animal doing? Tools for exploring behavioural structure in animal movements

Eliezer Gurarie<sup>1,2\*</sup>, Chloe Bracis<sup>3</sup>, Maria Delgado<sup>4,5</sup>, Trevor D. Meckley<sup>6</sup>, Ilpo Kojola<sup>7</sup> and  
C. Michael Wagner<sup>6</sup>

Edelhoff *et al.* *Movement Ecology* (2016) 4:21  
DOI 10.1186/s40462-016-0086-5

Movement Ecology

### REVIEW

Open Access



Path segmentation for beginners: an  
overview of current methods for detecting  
changes in animal movement patterns

Hendrik Edelhoff\*, Johannes Signer and Niko Balkenhol

# First Passage Time

## Spatial and simple

Asks, how long does it take an animal to leave a particular radius - **at every point?**

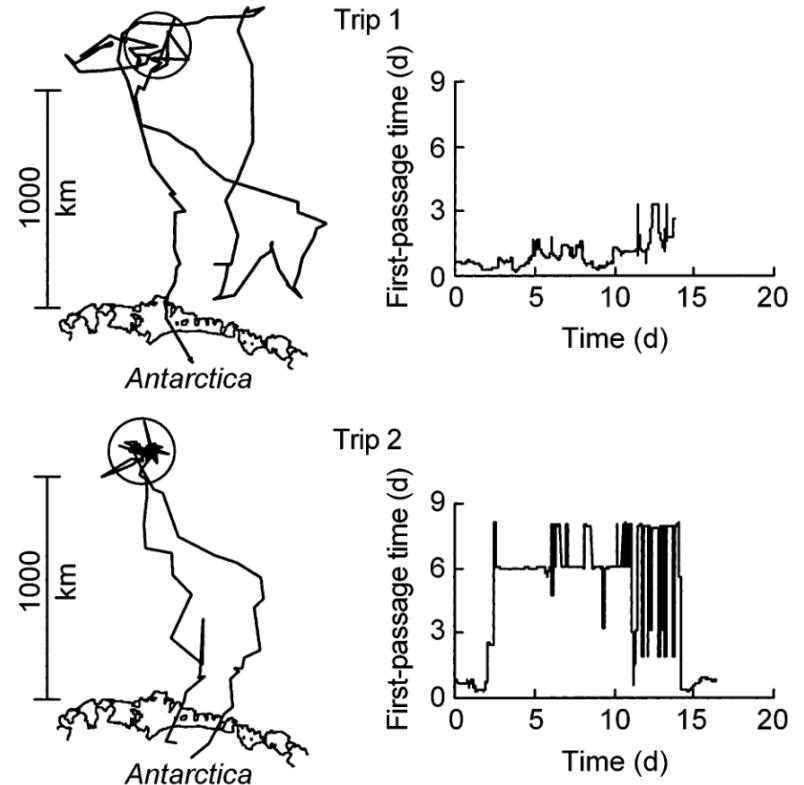
Ecology, 84(2), 2003, pp. 282–288  
© 2003 by the Ecological Society of America

### USING FIRST-PASSAGE TIME IN THE ANALYSIS OF AREA-RESTRICTED SEARCH AND HABITAT SELECTION

PER FAUCHALD<sup>1</sup> AND TORKILD TVERAA

Norwegian Institute for Nature Research, Division of Arctic Ecology, Polar Environmental Center,  
N-9296 Tromsø, Norway

In the adehabitat family of packages.



# Lavielle Segmentation

Statistically find the best division of a **single time-series** (e.g. speed).

Assumes that the time series is independent Normal with possible change in **mean** and **variance**

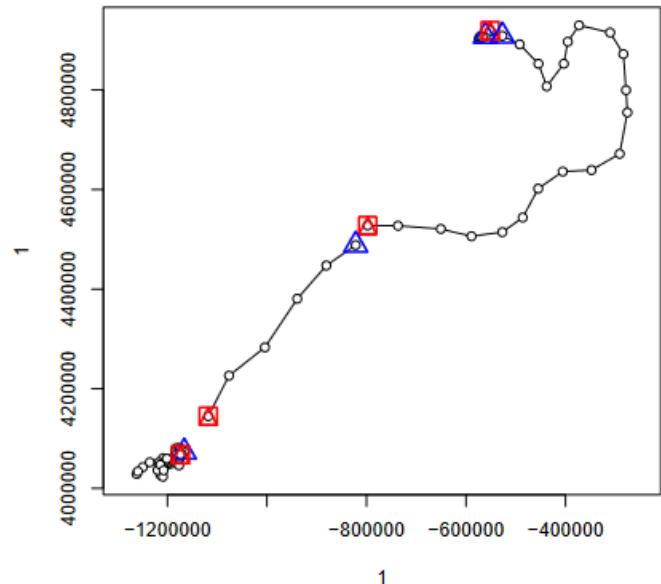
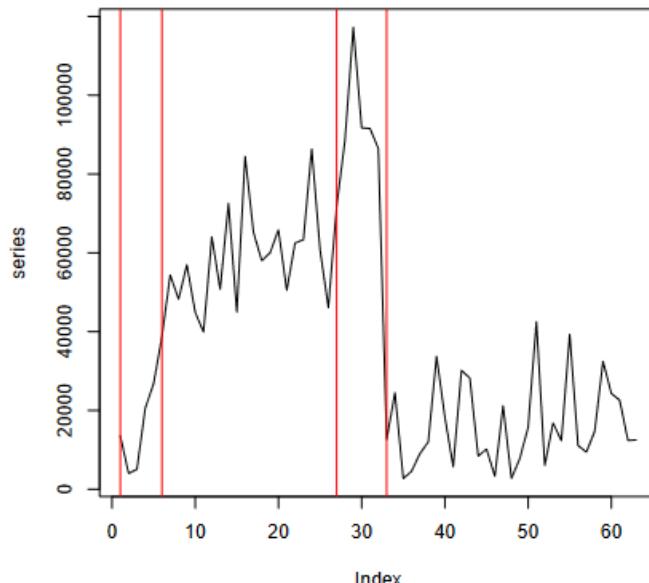
Very nicely implemented in adehabitatLT vignette:

Analysis of Animal Movements in R:  
the **adehabitatLT** Package

Clement Calenge,  
Office national de la chasse et de la faune sauvage  
Saint Benoit – 78610 Auffargis – France.

March 2019

This is a dolphin track.



IEEE TRANSACTIONS ON SIGNAL PROCESSING, VOL. 46, NO. 5, MAY 1998

1365

## Optimal Segmentation of Random Processes

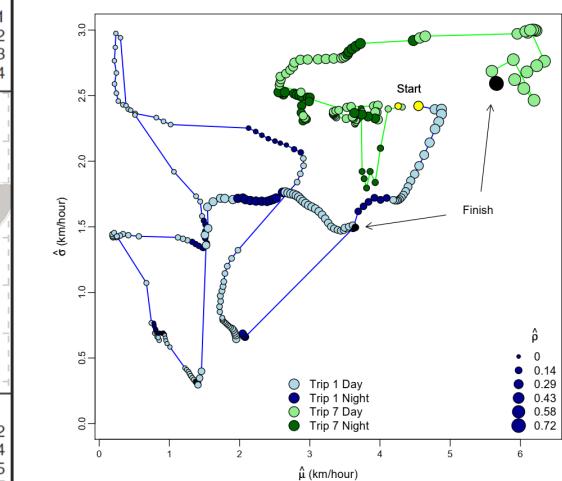
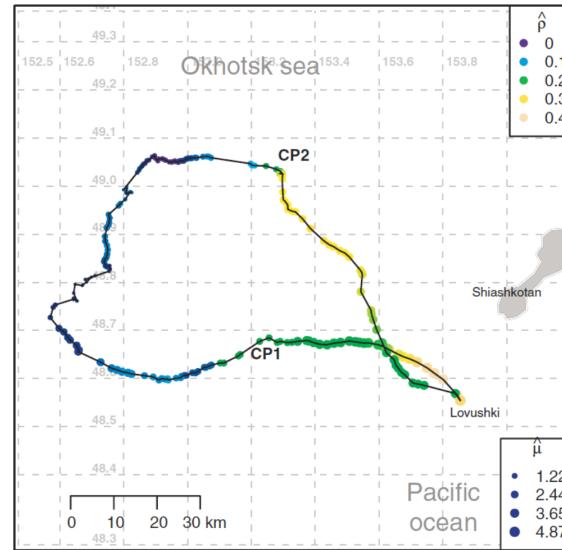
Marc Lavielle

# Behavioral Change Point Analysis

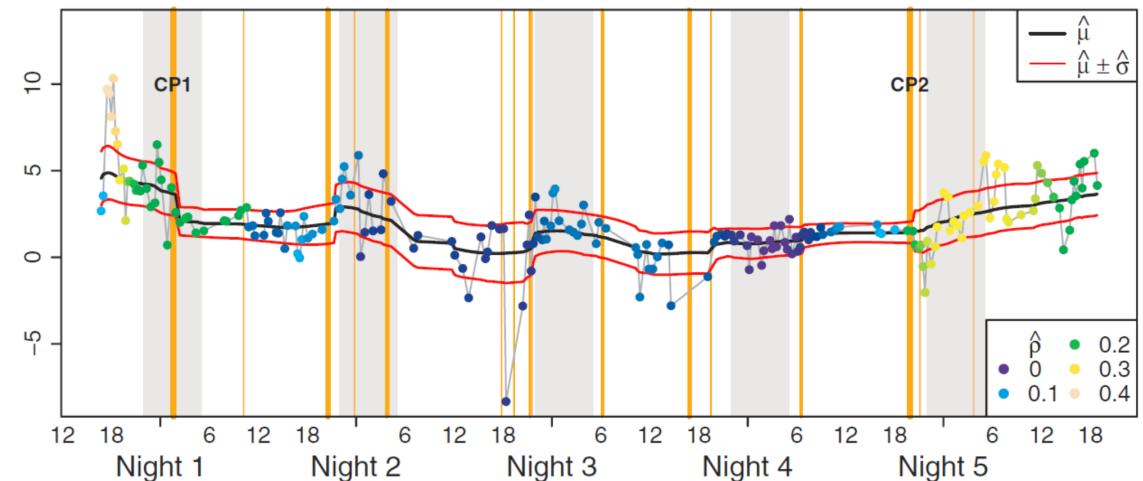
Gurarie et al. 2009

Expands on Lavielle by allowing for irregular data and auto-correlation.

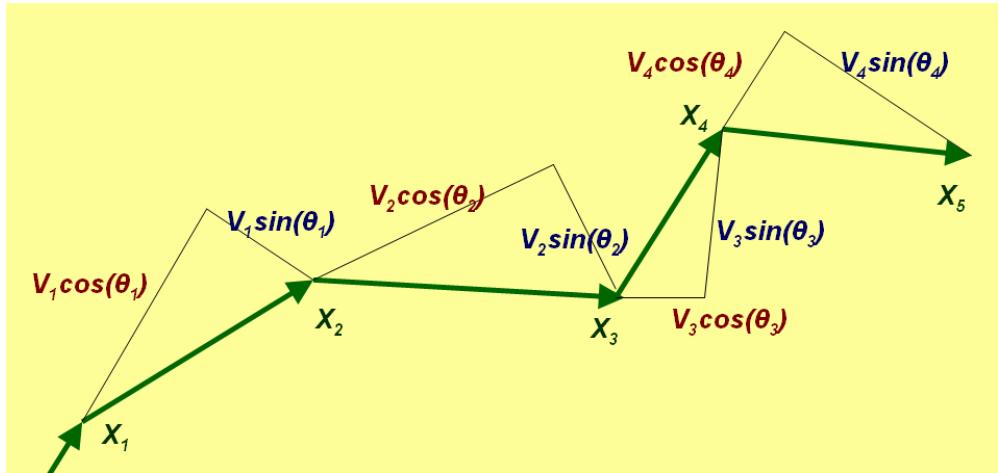
bcpapackage



(b)  $V\cos(\psi)$



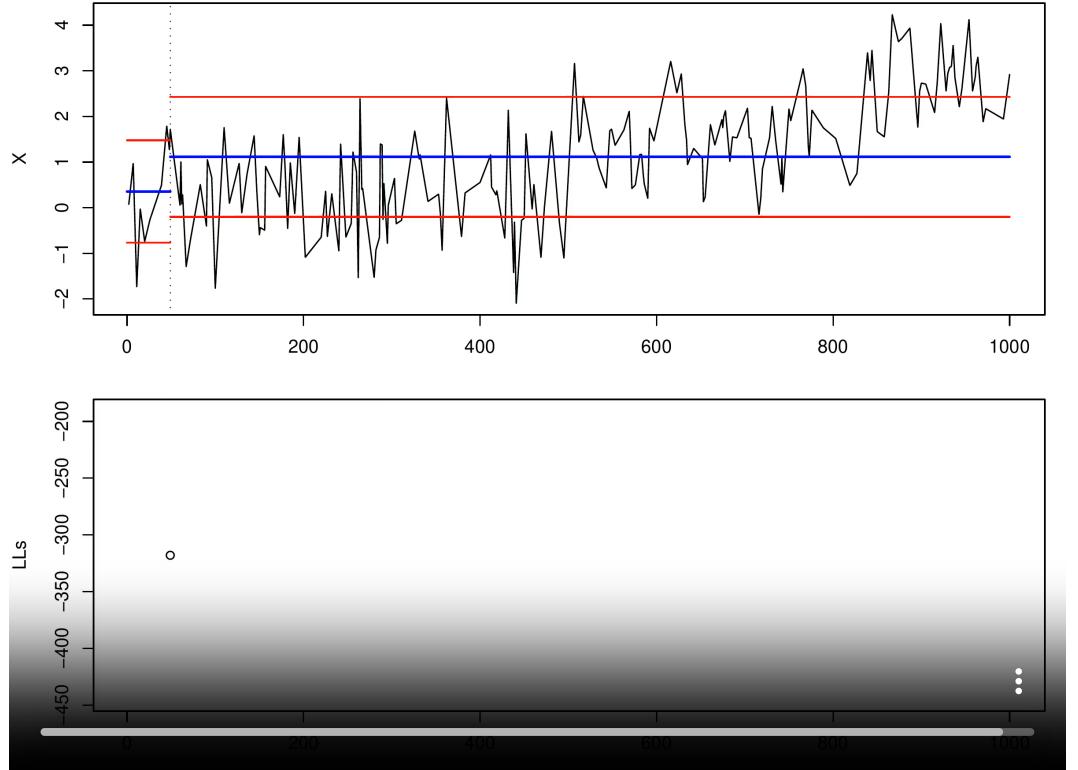
# Likelihood-based - single changepoint



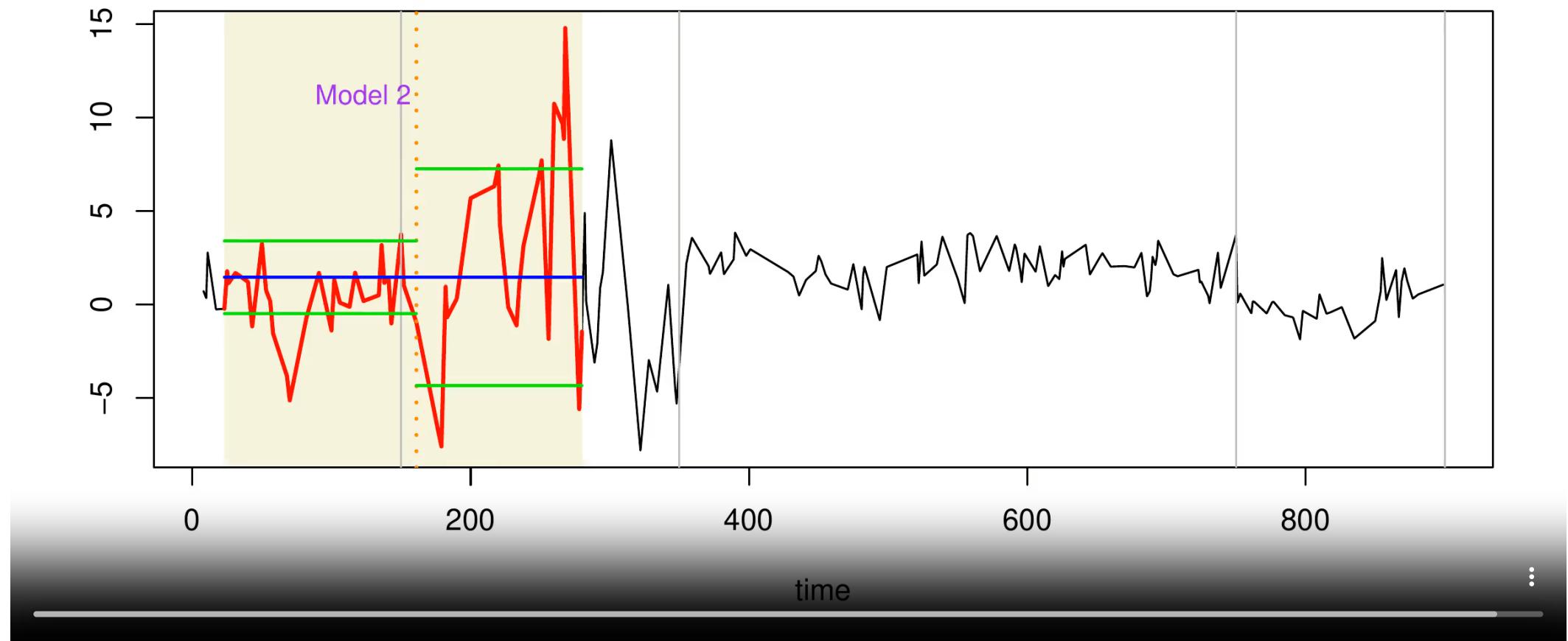
$$W(0) = W_0, \quad \text{Var}[W(t)] = \sigma^2,$$

$$E[W(t)] = \mu, \quad \text{Corr}[W(t), W(t - \tau)] = \rho^\tau,$$

$$L(\boldsymbol{\Theta} | \mathbf{X}, \mathbf{T}) = \prod_{i=1}^n f(X_i | X_{i-1}, \boldsymbol{\Theta}_1) \prod_{j=n+1}^N f(X_j | X_{j-1}, \boldsymbol{\Theta}_2)$$



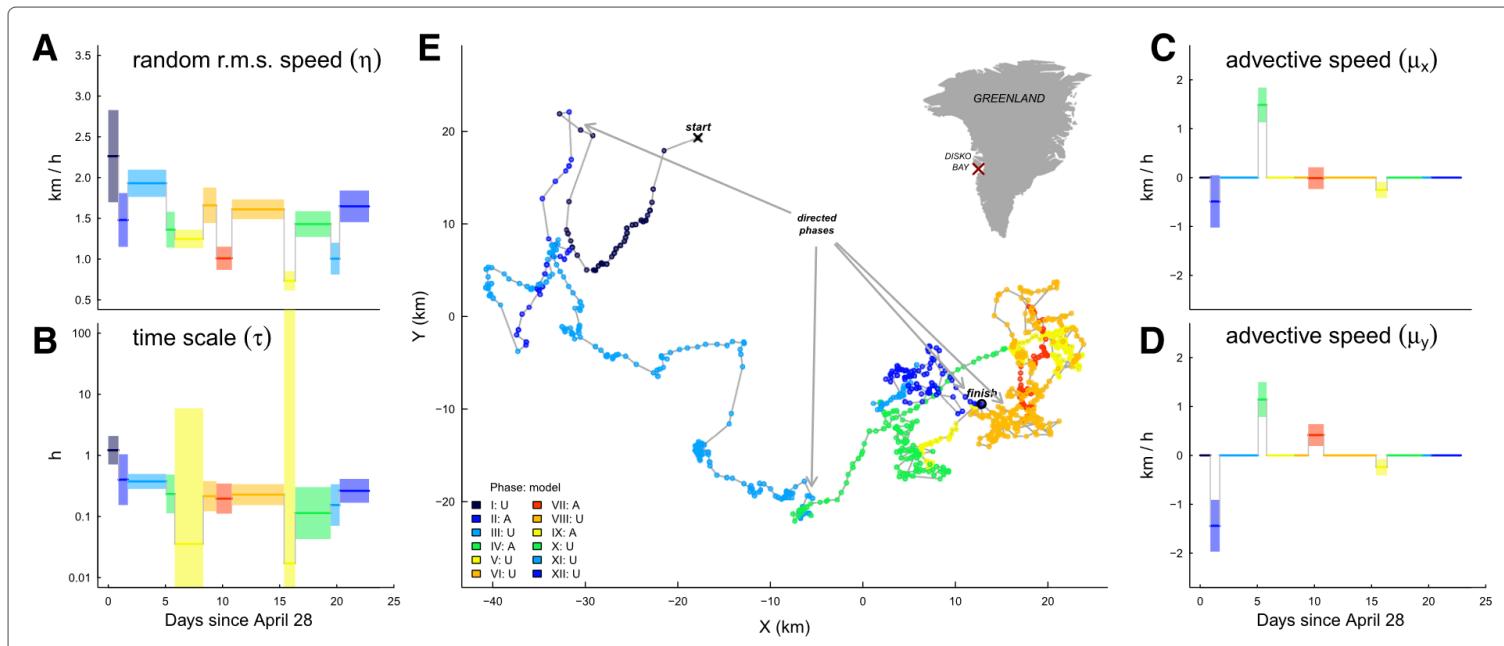
# Window-sweeping



# BCPA on Continuous Time Movement Models

Fits actual (continuous time) movement models and finds change points.

[smoove R package \(on GitHub\)](#)



Bowhead whale  
*Balaena mysticetus*

# BCPA on Continuous Time Movement Models

Can do fun things like rotation



Gurarie et al. *Movement Ecology* (2017) 5:13  
DOI 10.1186/s40462-017-0103-3

Movement Ecology

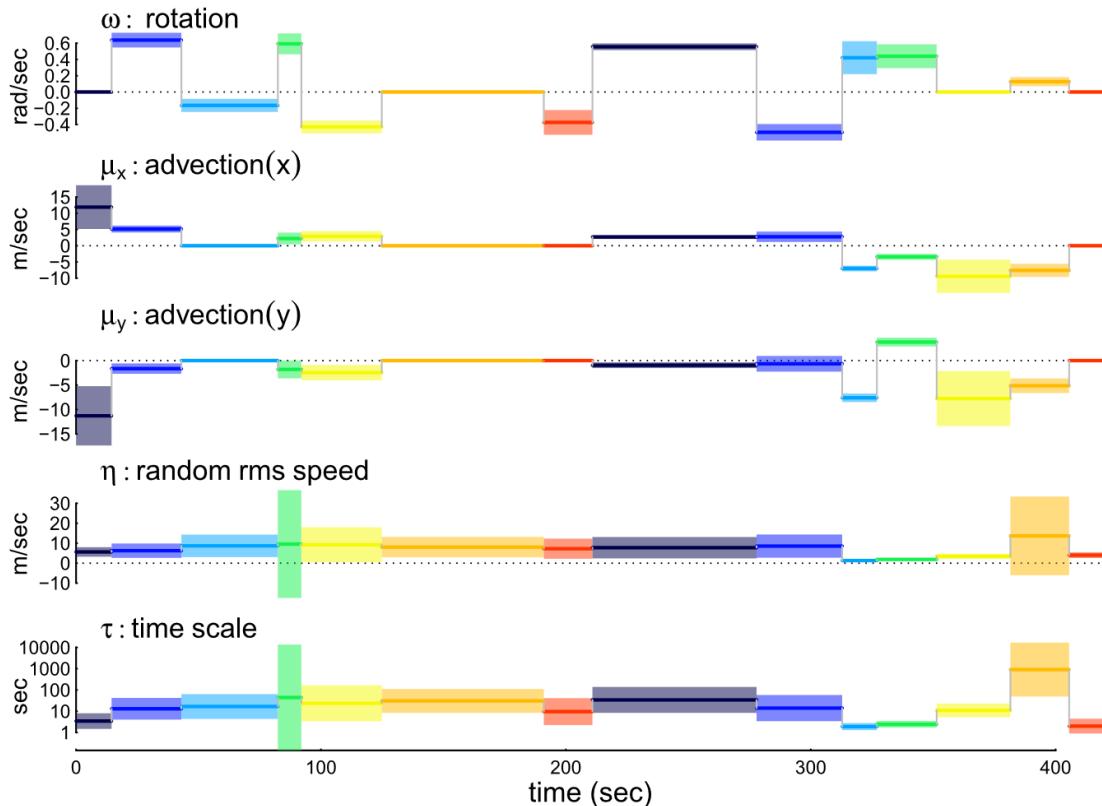
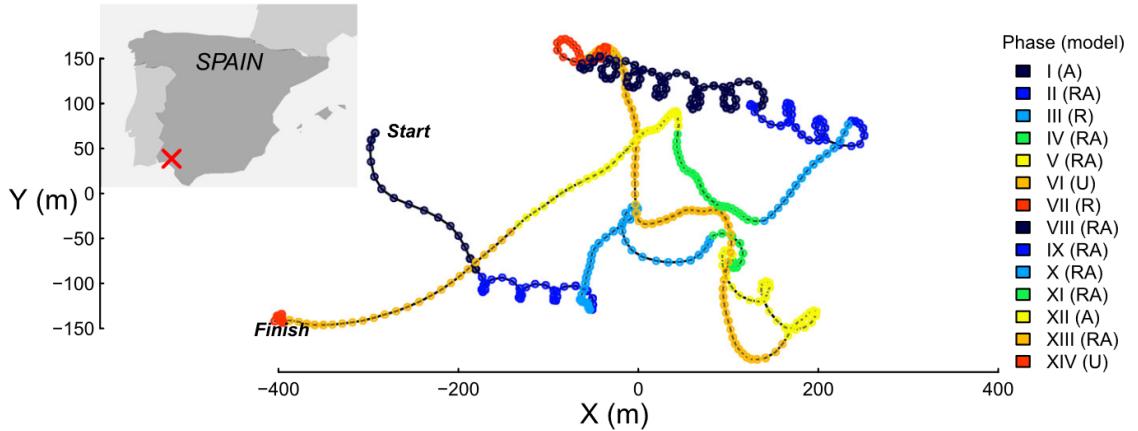
METHODOLOGY ARTICLE

Open Access



Correlated velocity models as a fundamental unit of animal movement: synthesis and applications

Eliezer Gurarie<sup>1\*</sup>, Christen H. Fleming<sup>1,2</sup>, William F. Fagan<sup>1</sup>, Kristin L. Laidre<sup>3</sup>, Jesús Hernández-Pliego<sup>4</sup> and Otso Ovaskainen<sup>5,6</sup>

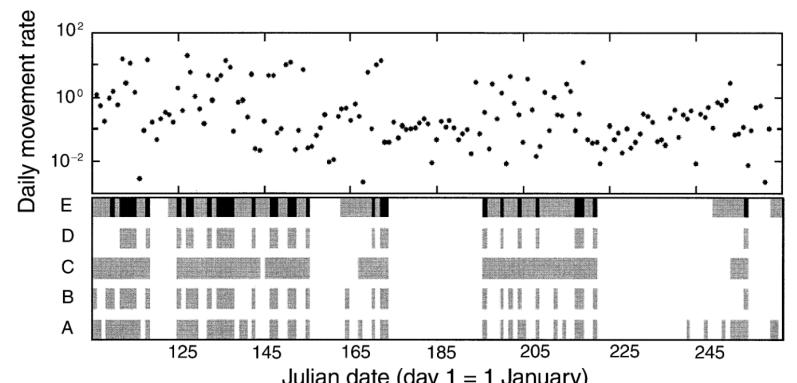
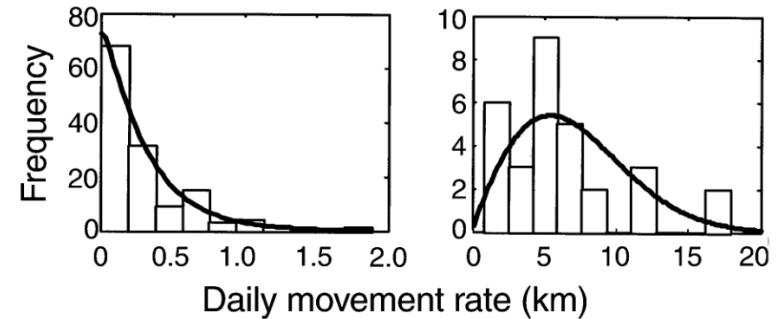
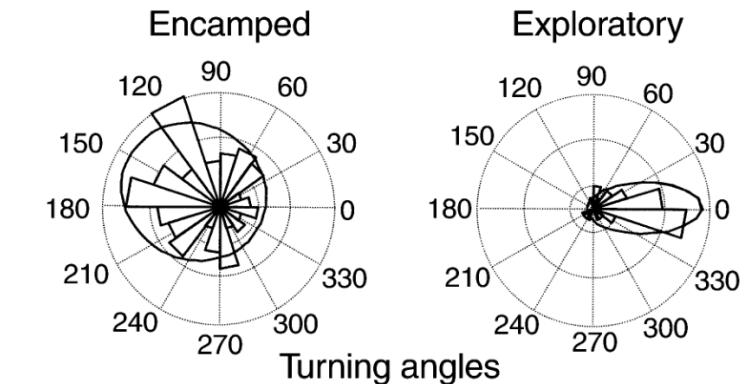


# Multi-state random walks

aka. **State-Space" modeling** or **Hidden Markov Movement Model**

1. Define pre-fixed number of states, with particular movement parameters for example:
  - persistence coefficient  $\rho$
  - and step-length distribution paramaters  $\alpha$  and  $\beta$
2. Estimate the **Markov transition probability matrix**
3. Make predictions from that probability matrix

Lots of examples! But they are all variations on **Morales et al. 2004**



# Sea Turtles! movement and diving

States include:

- **S1**, shallow dives, fast and directed horizontal movement;
- **S2**, mixture of dive depths, slower and less directed horizontal movement;
- **S3**, deep dives, intermediate speeds, and partially directed horizontal movement.

Parameter <sup>b</sup>	State 1 (SD)	State 2 (SD)	State 3 (SD)
$\mu$	30 (9.9)	2.0 (1.3)	21 (8.4)
$\sigma$	8.9 (3.0)	5.9 (4.6)	4.8 (3.2)
$P$	0.16 (0.048)	0.68 (0.096)	0.84 (0.048)
$\lambda$	8.1 (4.8)	8.1 (4.8)	8.1 (4.8)

Received: 14 October 2022 | Revised: 12 May 2023 | Accepted: 16 May 2023

DOI: 10.1111/cobi.14114

CONTRIBUTED PAPERS

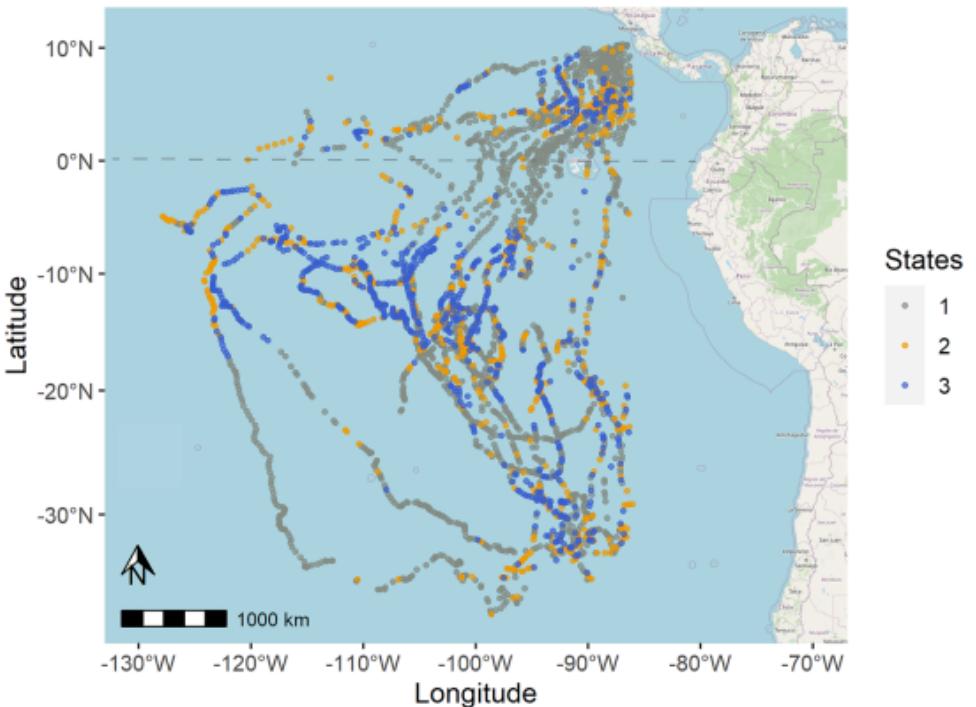
Conservation Biology

Incorporating multidimensional behavior into a risk management tool for a critically endangered and migratory species

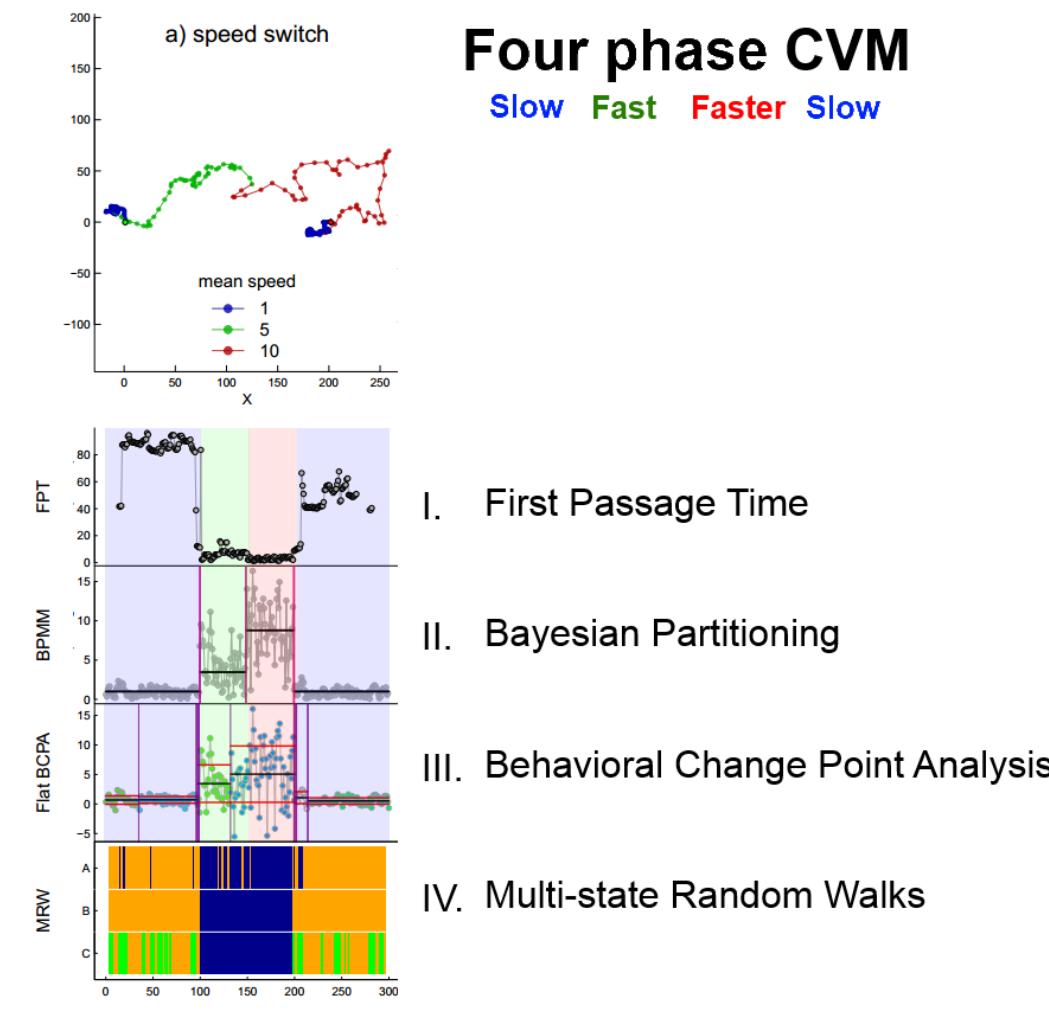
Nicole Barbour<sup>1,2,3,6</sup> | George L. Shillinger<sup>3,4,5</sup> | Eliezer Gurarie<sup>2,6</sup> | Aimee L. Hoover<sup>3</sup> | Philippe Gaspar<sup>7</sup> | Julien Temple-Boyer<sup>7</sup> | Tony Candela<sup>3,7</sup> | William F. Fagan<sup>2</sup> | Helen Bailey<sup>1</sup>



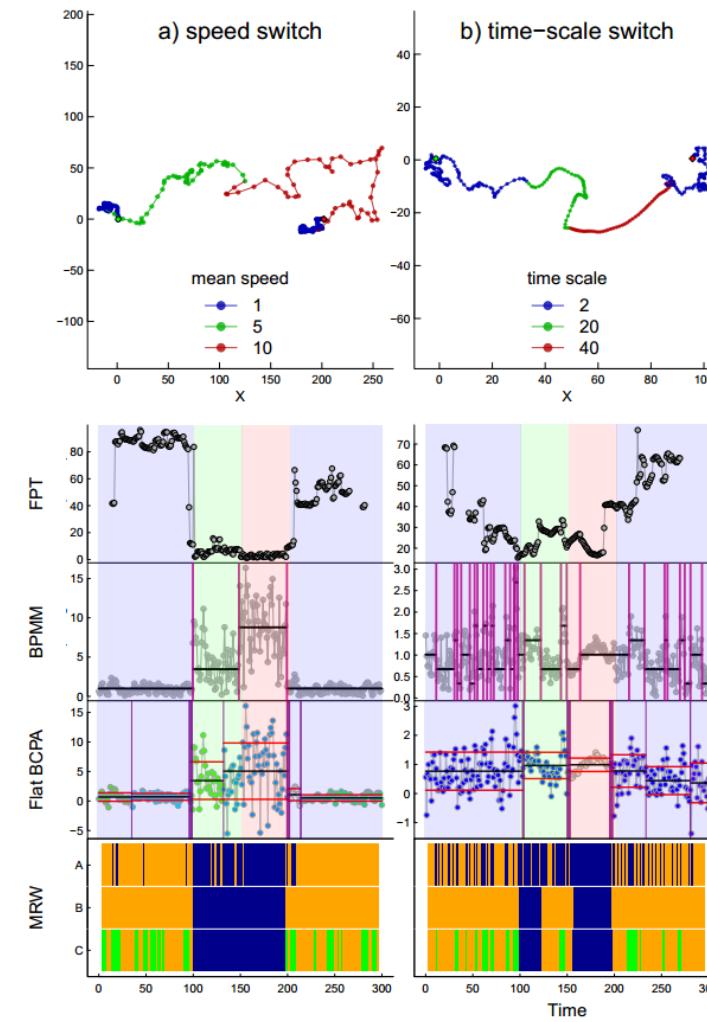
(a)



# Comparing tools



# Comparing tools

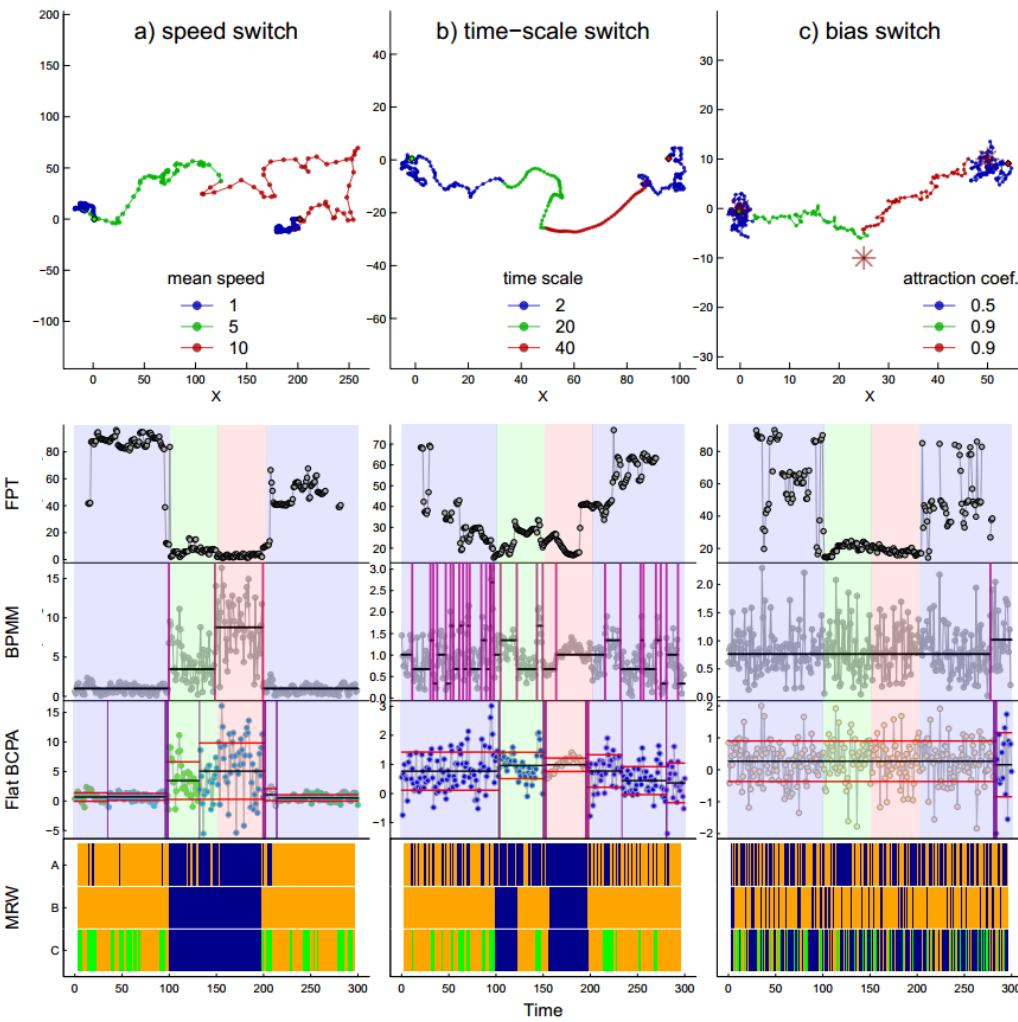


**Four phase CVM**  
tortuous less tortuous  
linear tortuous

# Comparing tools

A tool **must** know what it is modeling!

And the "best" tool depends on the process you are capturing



## Biased CRW

three points of attraction

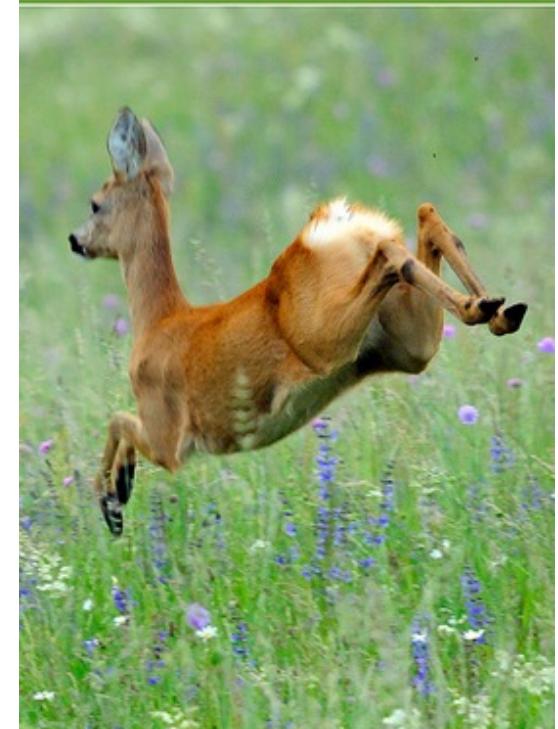
uniform speed and tortuosity

# **Targeted segmentation**

Looking for a **specific** behavior.

- Migration or range-shift timing
- Calving / Parturition events
- Dispersal events

**Model-based estimation of behavioral changepoints**



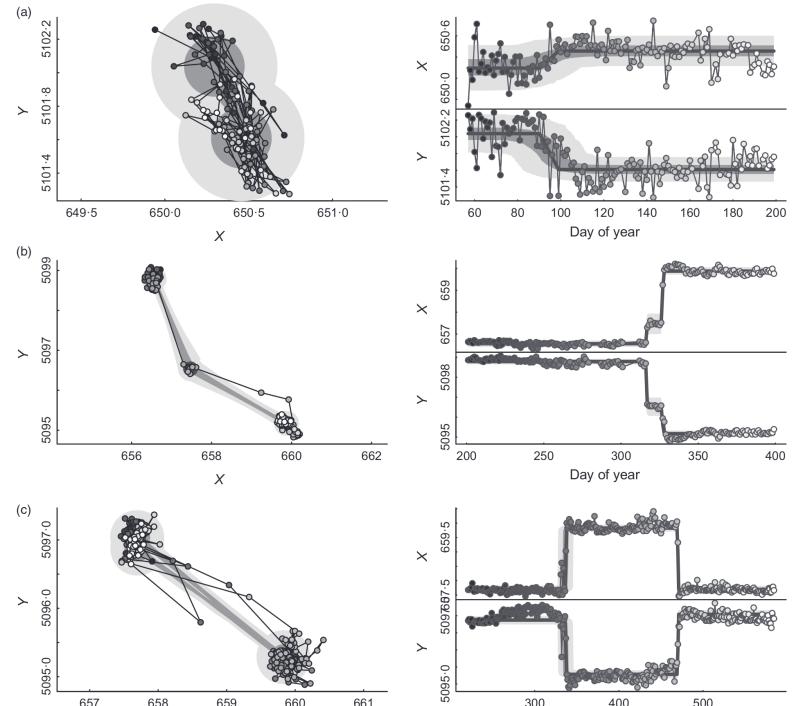
# Migration and range-change estimation

WN or OU or OUF in each range ... then

$$\mathbf{m}(t) = \begin{cases} \mathbf{m}_1 & \text{where } t < t_1 \\ \mathbf{m}_1 + (m_2 - m_1) \times (t - t_1) / \Delta t & \text{where } t_1 < t < t_1 + \Delta t . \\ \mathbf{m}_2 & \text{where } t > t_1 + \Delta t \end{cases}$$

- Identification of "subtle" shifts (hard for NSD)
- Estimation of parameters with confidence intervals
- Various hypothesis tests: **was the shift significant? did it return? was there a stopover?**

**WARNING:** as always some **strong assumptions!**



Journal of Animal Ecology

Journal of Animal Ecology 2017, 86, 943–959



doi: 10.1111/1365-2656.12674

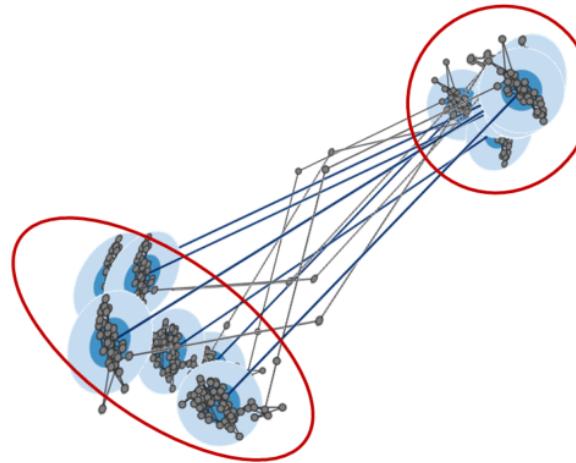
A framework for modelling range shifts and migrations: asking when, whither, whether and will it return

Eliezer Gurarie<sup>\*1</sup>, Francesca Cagnacci<sup>2,3</sup>, Wibke Peters<sup>2,4</sup>, Christen H. Fleming<sup>1,5</sup>, Justin M. Calabrese<sup>1,5</sup>, Thomas Mueller<sup>6,7</sup> and William F. Fagan<sup>1</sup>

marcher R package

# Hierarchical Migration Modeling

What if you have too many individuals!?



Each individual:

**Migration**( $A, m_1, m_2, t_1, dt$ )

Lots of individuals!

**Herd Range:**

winter:  $M_1 \sim \text{Range}(\text{location}_1, \text{shape}_1)$   
calving  $M_2 \sim \text{Range}(\text{location}_2, \text{shape}_2)$

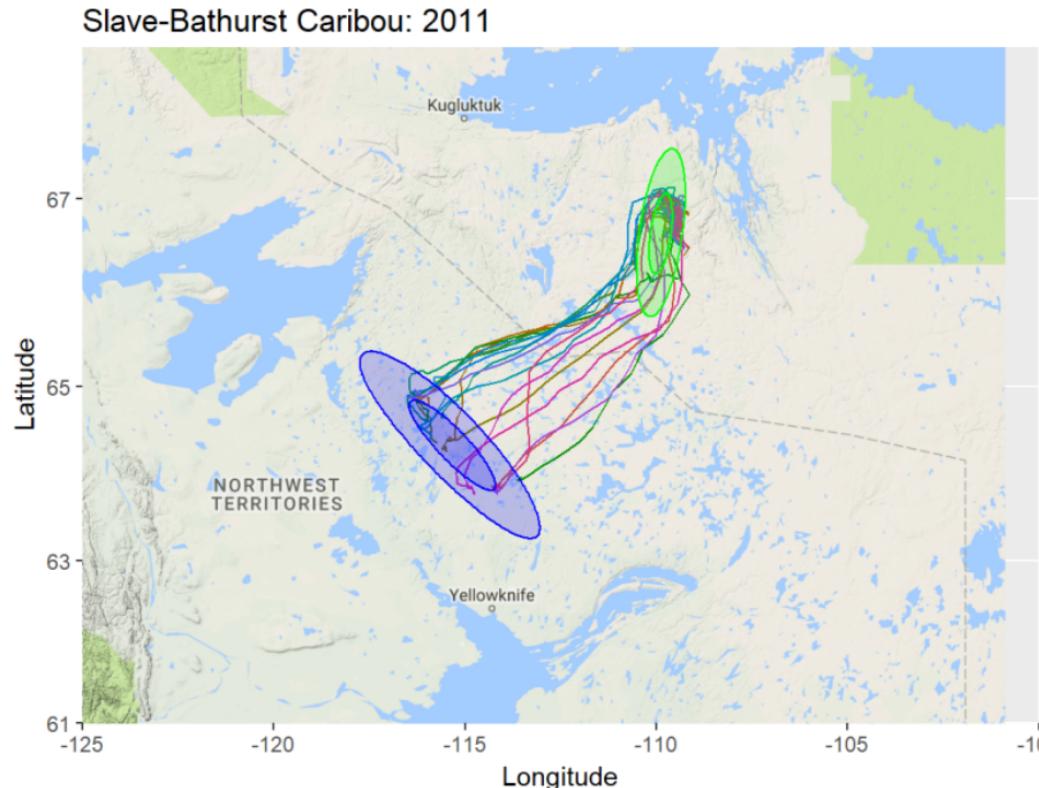
**Migration Timing:**

start: Mean and standard deviation of  
**departure times**  
duration: Mean and standard deviation of  
**migration duration**

# Hierarchical Migration Modeling

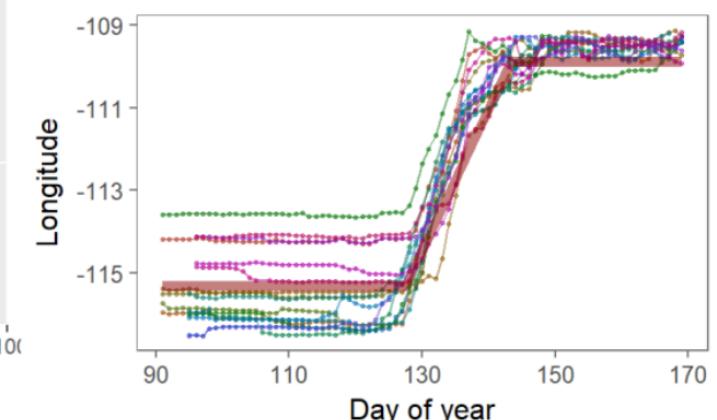
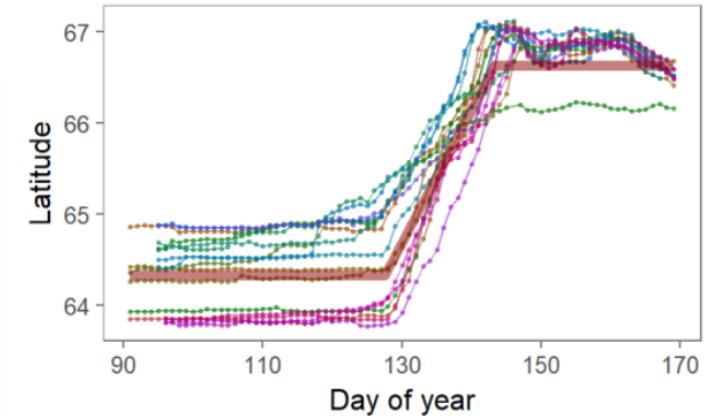
Herd Ranges:

$$\mathbf{M}_1 \sim \text{BivarNormal}(\mu_1, \Sigma_1) \quad \mathbf{M}_2 \sim \text{BivarNormal}(\mu_2, \Sigma_2)$$



Migration Timing:

$$t^* \sim \mathcal{N}(\mu_t, \sigma_t) \quad \Delta t^* \sim \mathcal{N}(\mu_{\Delta t}, \sigma_{\Delta t})$$



# marcher in 3D?

mit Wibke Peters und Johannes Singer



## Model

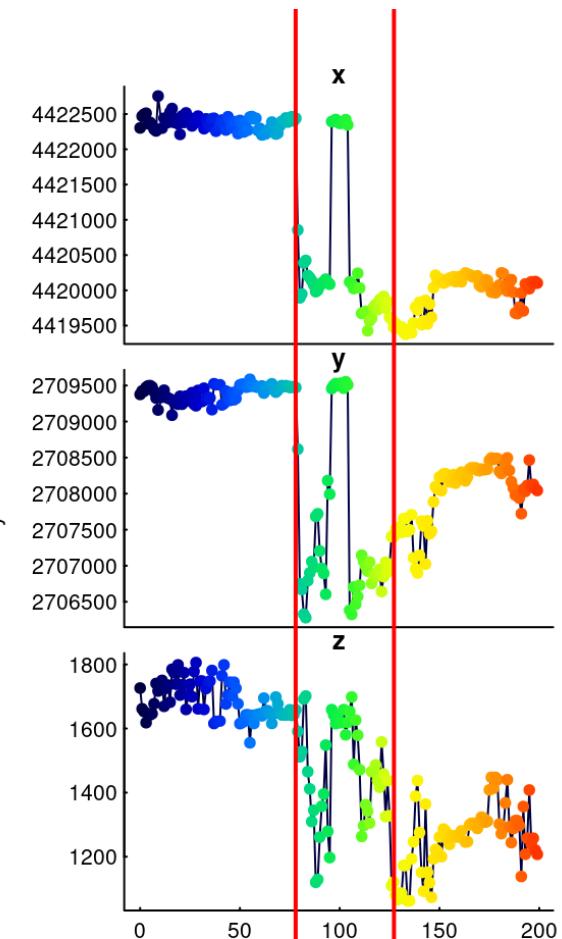
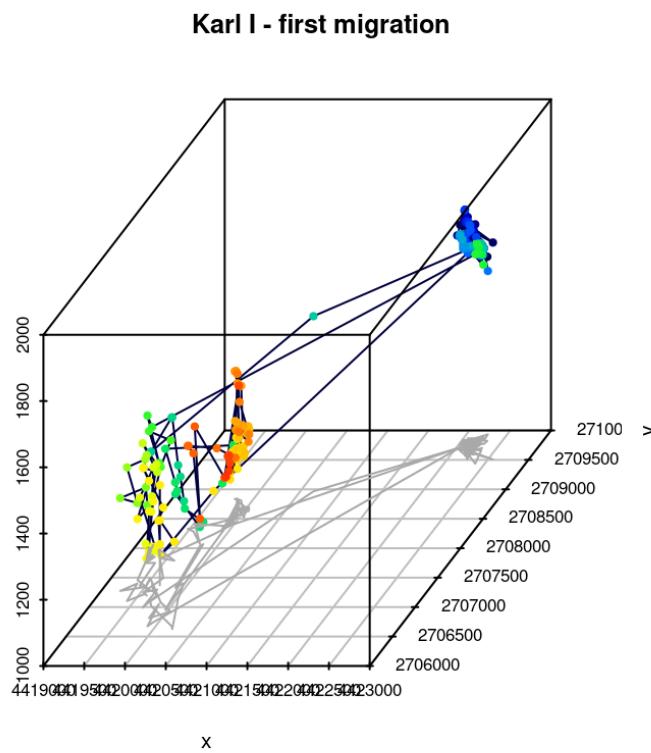
$$X_p \sim AR1(\mu_{x,p}, \sigma_{x,p}, \phi_{x,p})$$

$$Y_p \sim AR1(\mu_{y,p}, \sigma_{y,p}, \phi_{y,p})$$

$$Z_p \sim AR1(\mu_{z,p}, \sigma_{z,p}, \phi_{z,p})$$

## Likelihood

$$\begin{aligned} \mathcal{L}(\theta|V_d) = & \prod_{d=1}^D \prod_{i=1}^{t_1} \mathcal{L}_{\mathcal{AR}}(\mu_{d,1}, \sigma_{d,1}, \phi_{d,1} | V_{d,i \leq t_1}) \times \\ & \prod_{d=1}^D \prod_{i=t_1+1}^{t_2} \mathcal{L}_{\mathcal{AR}}(\mu_{d,2}, \sigma_{d,2}, \phi_{d,2} | V_{d,t_1 < i \leq t_2}) \times \\ & \prod_{d=1}^D \prod_{i=t_2}^n \mathcal{L}_{\mathcal{AR}}(\mu_{d,3}, \sigma_{d,3}, \phi_{d,3} | V_{d,i > t_2}) \end{aligned}$$



# Detecting parturition times

When [mammals / birds] [give birth / lay eggs] they (generally) stops moving for a while to [nurse / incubate].

Several model-based methods to identify those locations / times.

## Ecology and Evolution

Open Access

### Inferring parturition and neonate survival from movement patterns of female ungulates: a case study using woodland caribou

Craig A. DeMars<sup>1</sup>, Marie Auger-Méthé<sup>1</sup>, Ulrike E. Schlägel<sup>2</sup> & Stan Boutin<sup>1</sup>

<sup>1</sup>Department of Biological Sciences, University of Alberta, Edmonton, AB T6G 2E9, Canada

<sup>2</sup>Department of Mathematical and Statistical Sciences, University of Alberta, Edmonton, AB T6G 2G1, Canada

ARTICLE  
Macrosystems Ecology

ECOSPHERE  
AN ESA OPEN ACCESS JOURNAL

### Continental synchrony and local responses: Climatic effects on spatiotemporal patterns of calving in a social ungulate

Ophélie H. Couriot<sup>1,2,3</sup> | Matthew D. Cameron<sup>4</sup> | Kyle Joly<sup>4</sup> |  
Jan Adamczewski<sup>5</sup> | Mitch W. Campbell<sup>6</sup> | Tracy Davison<sup>7</sup> |  
Anne Gunn<sup>2,8</sup> | Alicia P. Kelly<sup>9</sup> | Mathieu Leblond<sup>10</sup> | Judy Williams<sup>5</sup> |  
William F. Fagan<sup>1,2</sup> | Anna Brose<sup>2</sup> | Eliezer Gurarie<sup>1,2</sup>



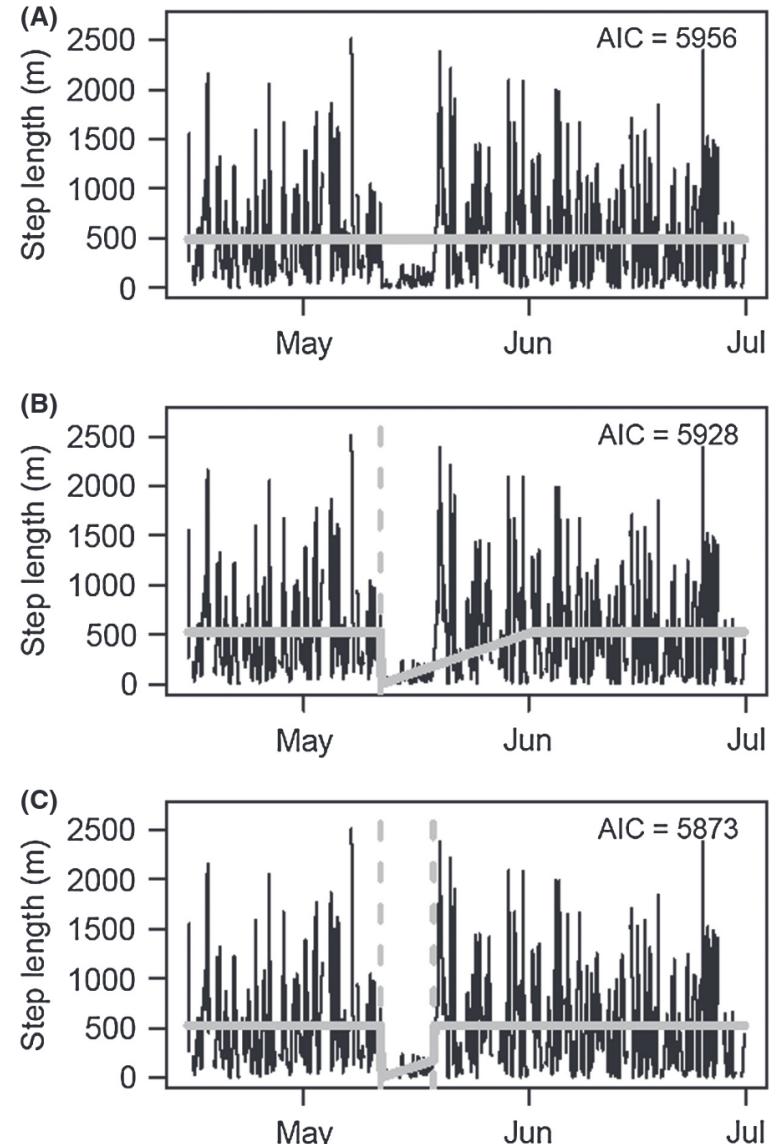
# Parturition model for caribou

- Focus on "speed" (displacements / time intervals)
- Modeled as Gamma distribution (shape / scale parameters)
- The parameters shift:
  - no change - **no birth**
  - fall to (near) zero and recover slowly: **calf survival**
  - fall to (near) zero and recover suddenly: **calf died**

$$R(t) = \begin{cases} \alpha_m \times \beta_m & \text{when } t < \tau_c \\ \left( \alpha_c + \frac{\alpha_m - \alpha_c}{\kappa} t \right) \left( \beta_c + \frac{\beta_m - \beta_c}{\kappa} t \right) & \text{when } \tau_c \leq t \leq \tau_c + \kappa, \\ \alpha_m \times \beta_m & \text{when } t > \tau_c + \kappa \end{cases}$$

- can be identified & compared with maximum likelihood

TuktuTools R package



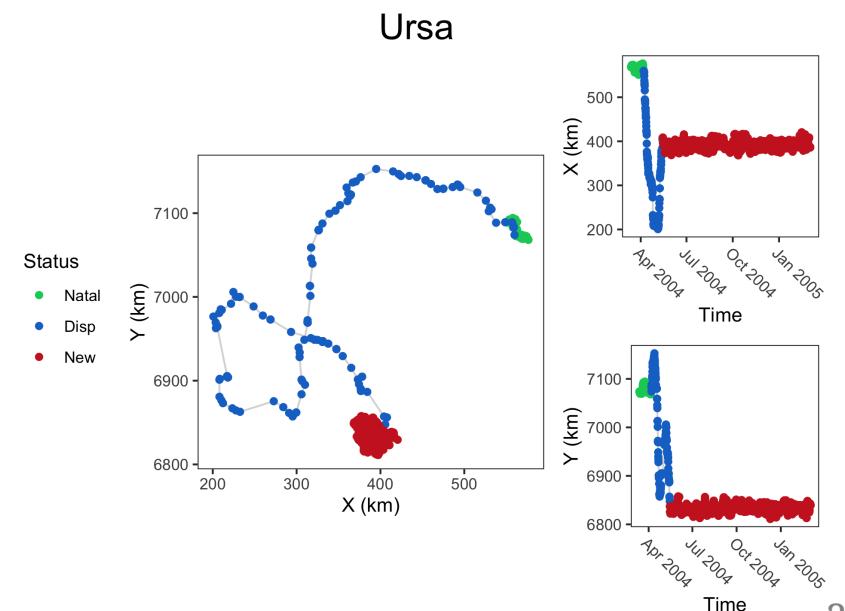
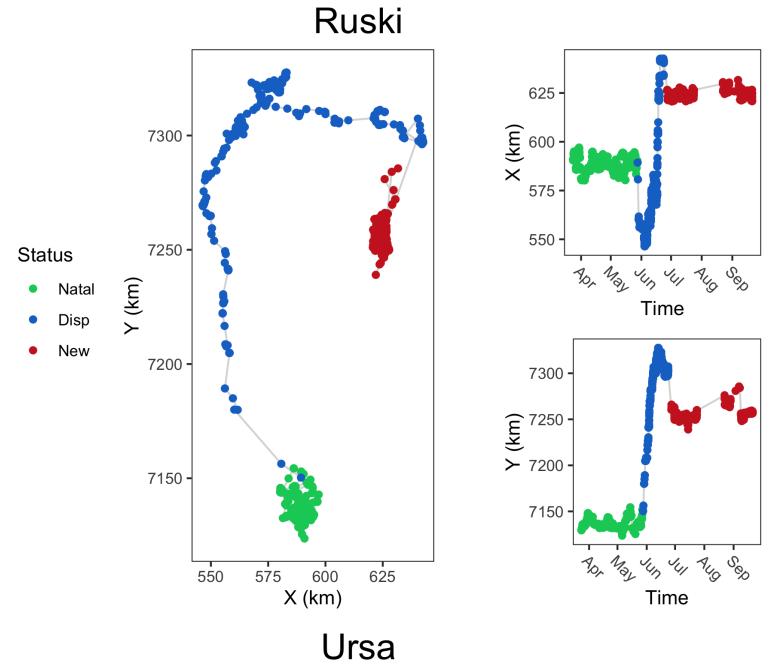
# Dispersal events

Fundamental ecological process, important general question

Model:

$$\mathbf{Z}(t) = \begin{cases} \text{OUF}(\tau_{v1}, \tau_{z1}, A) & t < t_d \\ \text{CVM}(\tau_v, \nu) & t_d \leq t < t_s \\ \text{OUF}(\tau_{v3}, \tau_{z2}, A) & t \geq t_s \end{cases}$$

R package `disperser` (not ready for prime time)



# You Choose!

- Multi-state Random Walk with `momentuhmm`
- Behavioral Change-points of Continuous-time Movement Models with `smoove`
- Migration / range-shift estimation with `marcher`
- Hierarchical migration model with `TuktuMigration`