

Contents

1 Basic	1	8 Others	22
1.1 default code	1	8.1 SOS dp	22
1.2 .vimrc	1	8.2 De Bruijn sequence	22
1.3 Increase Stack Size (linux)	1	8.3 CDQ 分治	22
1.4 Misc	1	8.4 3D LIS	23
1.5 check	2	8.5 Ternary Search	23
1.6 python-related	2	8.6 Max Subrectangle	23
2 flow	2	8.7 Maximal Rectangle	23
2.1 ISAP $O(V^3)$	2	8.8 p-Median	24
2.2 MinCostFlow	2	8.9 Tree Knapsack	24
2.3 Dinic $O(V^2E)$	3	8.10 質數個數	24
2.4 Kuhn Munkres 最大完美二分匹配 $O(n^3)$	3	8.11 AC-Automaton	24
2.5 Flow Method	3		
3 Math	4	1 Basic	
3.1 FFT	4	1.1 default code	
3.2 Faulhaber $(\sum_{i=1}^n i^p)$	4	<code>#pragma GCC optimize("O3,unroll-loops")</code>	
3.3 Chinese Remainder	4	<code>#pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt")</code>	
3.4 Miller Rabin	4	<code>#include <bits/stdc++.h></code>	
3.5 Pollard Rho	5	<code>using namespace std;</code>	
3.6 Josephus Problem	5	<code>ios_base::sync_with_stdio(0); cin.tie(0); cout.tie(0);</code>	
3.7 Gaussian Elimination	5		
3.8 Inverse Matrix	5	1.2 .vimrc	
3.9 模反元素	6	<code>set nu rnu ts=4 sw=4 bs=2 ai hls cin mouse=a</code>	
3.10 $ax+by=gcd$	6	<code>color default</code>	
3.11 Discrete sqrt	6	<code>sy on</code>	
3.12 Prefix Inverse	6	<code>inoremap {<CR> {<CR><C-o>0</code>	
3.13 Roots of Polynomial 找多項式的根	6	<code>inoremap jk <Esc></code>	
3.14 Combination theorem	6	<code>nnoremap J 5j</code>	
3.15 Primes	6	<code>nnoremap K 5k</code>	
3.16 Phi	7	<code>nnoremap run :w!bar!g++ -std=c++14 -DLOCAL -Wfatal-</code>	
3.17 Int Sqrt	7	<code>errors -o test "%>done." && time ./test<</code>	
3.18 Result	7	<code>CR></code>	
4 Geometry	7	1.3 Increase Stack Size (linux)	
4.1 definition	7	<code>#include <sys/resource.h></code>	
4.2 Line definition	7	<code>void increase_stack_size() {</code>	
4.3 halfPlaneIntersection	8	<code>const rlim_t ks = 64*1024*1024;</code>	
4.4 Convex Hull	8	<code>struct rlimit rl;</code>	
4.5 Convex Hull trick	8	<code>int res=getrlimit(RLIMIT_STACK, &rl);</code>	
4.6 Intersection of 2 segments	9	<code>if(res==0){</code>	
4.7 Intersection of Polygon and Circle	9	<code>if(rl.rlim_cur<ks){</code>	
4.8 Circle cover	9	<code>rl.rlim_cur=ks;</code>	
4.9 Tangent line of two circles	10	<code>res=setrlimit(RLIMIT_STACK, &rl);</code>	
4.10 Poly Union	10	<code>} } }</code>	
4.11 Minkowski sum	10	1.4 Misc	
4.12 Area of Rectangles	10	編譯參數: <code>-std=c++14 -Wall -Wshadow (-fsanitize=</code>	
4.13 Min dist on Cuboid	11	<code>undefined)</code>	
4.14 Distance from Point to Line or Segment	11	<code>mt19937 gen(chrono::steady_clock::now().</code>	
4.15 Angle of two vector	11	<code>time_since_epoch().count());</code>	
4.16 極角排序	11	<code>int randint(int lb, int ub)</code>	
4.17 Heart of Triangle	11	<code>{ return uniform_int_distribution<int>(lb, ub)(gen); }</code>	
5 Graph	12	<code>#define SECs ((double)clock() / CLOCKS_PER_SEC)</code>	
5.1 Lowest Common Ancestor $O(lgn)$	12	<code>double startTime;</code>	
5.2 Hamiltonian path $O(n^22^n)$	12	<code>bool TIME() { // 比最大可執行時間小一點</code>	
5.3 Maximum Clique 最大團	12	<code>return SECs - startTime > 0.8;</code>	
5.4 Maximal Clique 極大團	12	<code>}</code>	
5.5 BCC based on vertex 點雙聯通分量	13	<code>int main() {</code>	
5.6 Strongly Connected Component 強連通分量	13	<code>startTime = SECs;</code>	
5.7 Manhattan MST	13	<code>}</code>	
5.8 Min Mean Cycle	14	<code>struct KeyHasher {</code>	
5.9 Directed Graph Min Cost Cycle	14	<code>size_t operator()(const Key& k) const {</code>	
5.10 Dominator Tree	15	<code>return k.first + k.second * 100000;</code>	
5.11 K-th Shortest Path	15	<code>} };</code>	
5.12 Floryd Warshall	16	<code>typedef unordered_map<Key,int,KeyHasher> map_t;</code>	
5.13 Minimum Steiner Tree	16	<code>// builtin function 可以代的值為int32</code>	
5.14 虛樹	16		
5.15 Tree Hash	16		
5.16 HeavyLight Decomposition	17		
5.17 Graph Theorem	17		
6 String	17		
6.1 PalTree $O(n)$	17		
6.2 Longest Increasing Subsequence	17		
6.3 Longest Common Subsequence $O(nlgn)$	17		
6.4 KMP	18		
6.5 SAIS $O(n)$	18		
6.6 Z Value $O(n)$	18		
6.7 Manacher Algorithm $O(n)$	19		
6.8 Smallest Rotation	19		
6.9 Cyclic LCS	19		
6.10 Hash	19		
7 Data Structure	19		
7.1 Segment tree	19		
7.2 持久化 SMT	20		
7.3 持久化並查集	21		
7.4 Trie	21		
7.5 Treap (interval reverse)	21		
7.6 BIT	22		
7.7 Black Magic	22		

```
__builtin_popcountll    // 二進位有幾個1
__builtin_clzll         // 左起第一個1之前0的個數
__builtin_parityll      // 1的個數的奇偶性
__builtin_mul_overflow(a,b,&h) // a*b是否溢位
```

1.5 check

```
for ((i=0;;i++))
do
    echo "$i"
    python3 gen.py > input
    ./ac < input > ac.out
    ./wa < input > wa.out
    diff ac.out wa.out || break
done
```

1.6 python-related

```
parser:
int(eval(num.replace("/", "///")))

from fractions import Fraction
from decimal import Decimal, getcontext, ROUND_HALF_UP,
    ROUND_CEILING, ROUND_FLOOR
getcontext().prec = 250 # set precision
getcontext().rounding = ROUND_HALF_UP

itwo = Decimal(0.5)
two = Decimal(2)

format(x, '0.10f') # set precision

N = 200
def angle(cosT):
    """given cos(theta) in decimal return theta"""
    for i in range(N):
        cosT = ((cosT + 1) / two) ** itwo
        sinT = (1 - cosT * cosT) ** itwo
        return sinT * (2 ** N)
pi = angle(Decimal(-1))

"""round to 2 decimal places"""
sum = Decimal(input())
sum.quantize(Decimal('.00'), ROUND_HALF_UP)

"""Fraction"""
x = Fraction(1, 3) # 1/3
x.as_integer_ratio() # (1, 3)

"""input list of integers"""
arr = list(map(int, input().split()))

"""把字元轉成ascii再轉回字串"""
chr(ord('a'))
```

2 flow

2.1 ISAP $O(V^3)$

```
struct Maxflow {
    static const int MAXV = 20010;
    static const int INF = 1000000;
    struct Edge {
        int v, c, r;
        Edge(int _v, int _c, int _r):
            v(_v), c(_c), r(_r) {}
    };
    int s, t;
    vector<Edge> G[MAXV*2];
    int iter[MAXV*2], d[MAXV*2], gap[MAXV*2], tot;
    void init(int x) {
        tot = x+2;
        s = x+1, t = x+2;
        for(int i = 0; i <= tot; i++) {
```

```
        G[i].clear();
        iter[i] = d[i] = gap[i] = 0;
    } }
    void addEdge(int u, int v, int c) {
        G[u].push_back(Edge(v, c, SZ(G[v])));
        G[v].push_back(Edge(u, 0, SZ(G[u]) - 1));
    }
    int dfs(int p, int flow) {
        if(p == t) return flow;
        for(int &i = iter[p]; i < SZ(G[p]); i++) {
            Edge &e = G[p][i];
            if(e.c > 0 && d[p] == d[e.v]+1) {
                int f = dfs(e.v, min(flow, e.c));
                if(f) {
                    e.c -= f;
                    G[e.v][e.r].c += f;
                    return f;
                }
            }
            if(--gap[d[p]] == 0) d[s] = tot;
            else {
                d[p]++;
                iter[p] = 0;
                ++gap[d[p]];
            }
        }
        return 0;
    }
    int solve() {
        int res = 0;
        gap[0] = tot;
        for(res = 0; d[s] < tot; res += dfs(s, INF));
        return res;
    }
    void reset() {
        for(int i=0;i<=tot;i++) {
            iter[i]=d[i]=gap[i]=0;
        } }
} } flow;
```

2.2 MinCostFlow

```
struct zkwflow{
    static const int maxN=10000;
    struct Edge{ int v,f,re; ll w;};
    int n,s,t,ptr[maxN]; bool vis[maxN]; ll dis[maxN];
    vector<Edge> E[maxN];
    void init(int _n,int _s,int _t){
        n=_n,s=_s,t=_t;
        for(int i=0;i<n;i++) E[i].clear();
    }
    void addEdge(int u,int v,int f,ll w){
        E[u].push_back({v,f,(int)E[v].size(),w});
        E[v].push_back({u,0,(int)E[u].size()-1,-w});
    }
    bool SPFA(){
        fill_n(dis,n,LLONG_MAX); fill_n(vis,n,false);
        queue<int> q; q.push(s); dis[s]=0;
        while (!q.empty()){
            int u=q.front(); q.pop(); vis[u]=false;
            for(auto &it:E[u]){
                if(it.f>0&&dis[it.v]>dis[u]+it.w){
                    dis[it.v]=dis[u]+it.w;
                    if(!vis[it.v]){
                        vis[it.v]=true; q.push(it.v);
                    }
                }
            }
        }
        return dis[t]!=LLONG_MAX;
    }
    int DFS(int u,int nf){
        if(u==t) return nf;
        int res=0; vis[u]=true;
        for(int &i=ptr[u];i<(int)E[u].size();i++){
            auto &it=E[u][i];
            if(it.f>0&&dis[it.v]==dis[u]+it.w&&!vis[it.v]){
                int tf=DFS(it.v,min(nf,it.f));
                res+=tf,nf-=tf,it.f-=tf;
                E[it.v][it.re].f+=tf;
                if(nf==0){ vis[u]=false; break; }
            }
        }
        return res;
    }
    pair<int,ll> flowC(){
```

```

int flow=0; ll cost=0;
while (SPFA()){
    fill_n(ptr,n,0);
    int f=DFS(s,INT_MAX);
    flow+=f; cost+=dis[t]*f;
}
return{ flow,cost };
} // reset: do nothing
} flow;

```

2.3 Dinic $O(V^2E)$

```

#define SZ(x) (int)x.size()
#define PB push_back
struct Dinic{
    struct Edge{ int v,f,re; };
    int n,s,t,level[MXN];
    vector<Edge> E[MXN];
    void init(int _n, int _s, int _t){
        n = _n; s = _s; t = _t;
        for (int i=0; i<n; i++) E[i].clear();
    }
    void add_edge(int u, int v, int f){
        E[u].PB({v,f,SZ(E[v])});
        E[v].PB({u,0,SZ(E[u])-1});
    }
    bool BFS(){
        for (int i=0; i<n; i++) level[i] = -1;
        queue<int> que;
        que.push(s);
        level[s] = 0;
        while (!que.empty()){
            int u = que.front(); que.pop();
            for (auto it : E[u]){
                if (it.f > 0 && level[it.v] == -1){
                    level[it.v] = level[u]+1;
                    que.push(it.v);
                }
            }
        }
        return level[t] != -1;
    }
    int DFS(int u, int nf){
        if (u == t) return nf;
        int res = 0;
        for (auto &it : E[u]){
            if (it.f > 0 && level[it.v] == level[u]+1){
                int tf = DFS(it.v, min(nf,it.f));
                res += tf; nf -= tf; it.f -= tf;
                E[it.v][it.re].f += tf;
                if (nf == 0) return res;
            }
        }
        if (!res) level[u] = -1;
        return res;
    }
    int flow(int res=0){
        while (BFS())
            res += DFS(s,2147483647);
        return res;
    }
} }flow;

```

2.4 Kuhn Munkres 最大完美二分匹配 $O(n^3)$

```

struct KM{ // max weight, for min negate the weights
    int n, mx[MXN], my[MXN], pa[MXN];
    ll g[MXN][MXN], lx[MXN], ly[MXN], sy[MXN];
    bool vx[MXN], vy[MXN];
    void init(int _n) { // 1-based
        n = _n;
        for(int i=1; i<=n; i++) fill(g[i], g[i]+n+1, 0);
    }
    void addEdge(int x, int y, ll w) {g[x][y] = w;}
    void augment(int y) {
        for(int x, z; y; y = z){
            x=pa[y], z=mx[x], my[y]=x, mx[x]=y;
        }
    }
    void bfs(int st) {
        for(int i=1; i<=n; ++i) sy[i]=INF, vx[i]=vy[i]=0;
        queue<int> q; q.push(st);
        for(;;) {

```

```

while(q.size()) {
    int x=q.front(); q.pop(); vx[x]=1;
    for(int y=1; y<=n; ++y) if(!vy[y]){
        ll t = lx[x]+ly[y]-g[x][y];
        if(t==0){
            pa[y]=x;
            if(!my[y]){augment(y);return;}
            vy[y]=1, q.push(my[y]);
        }else if(sy[y]>t) pa[y]=x,sy[y]=t;
    }
    ll cut = INF;
    for(int y=1; y<=n; ++y)
        if(!vy[y]&&cut>sy[y]) cut=sy[y];
    for(int j=1; j<=n; ++j){
        if(vx[j]) lx[j] -= cut;
        if(vy[j]) ly[j] += cut;
        else sy[j] -= cut;
    }
    for(int y=1; y<=n; ++y) if(!vy[y]&&sy[y]==0){
        if(!my[y]){augment(y);return;}
        vy[y]=1, q.push(my[y]);
    }
}
ll solve(){
    fill(mx, mx+n+1, 0); fill(my, my+n+1, 0);
    fill(ly, ly+n+1, 0); fill(lx, lx+n+1, -INF);
    for(int x=1; x<=n; ++x) for(int y=1; y<=n; ++y)
        lx[x] = max(lx[x], g[x][y]);
    for(int x=1; x<=n; ++x) bfs(x);
    ll ans = 0;
    for(int y=1; y<=n; ++y) ans += g[my[y]][y];
    return ans;
} }graph;

```

2.5 Flow Method

Maximize $c^T x$ subject to $Ax \leq b, x \geq 0$;
with the corresponding symmetric dual problem,
Minimize $b^T y$ subject to $A^T y \geq c, y \geq 0$.

Maximize $c^T x$ subject to $Ax \leq b$;
with the corresponding asymmetric dual problem,
Minimize $b^T y$ subject to $A^T y = c, y \geq 0$.

Minimum vertex cover on bipartite graph =
Maximum matching on bipartite graph

Minimum edge cover on bipartite graph =
vertex number - Minimum vertex cover(Maximum matching)

König Theorem

最小點覆蓋：選出最少的點，滿足每條邊至少有一個端點被選
二分圖中，最小點覆蓋 = 最大匹配

Independent set on bipartite graph =
vertex number - Minimum vertex cover(Maximum matching)

二分圖中，最大獨立集 = n - 最小點覆蓋

找出最小點覆蓋，做完dinic之後，
從源點dfs只走還有流量的邊，

左邊沒被走到的點跟右邊被走到的點就是答案，

其他點為最大獨立集

最大閉包(最大權閉合子圖)

源點連到所有正權點流量為點權

所有負權點連到匯點流量為點權(絕對值)

所有圖上的邊權重為 INF

路徑覆蓋數量

把每個點拆成 入點 和 出點，轉化為二分圖

原圖頂點數 - 二分圖最大匹配數

Maximum density subgraph $(\sum W_e + \sum W_v) / |V|$

Binary search on answer:

For a fixed D, construct a Max flow model as follow:

Let S be Sum of all weight(or inf)

1. from source to each node with cap = S

2. For each (u,v,w) in E, $(u \rightarrow v, \text{cap}=w)$, $(v \rightarrow u, \text{cap}=w)$

3. For each node v, from v to sink with cap = $S + 2 * D - \text{deg}[v] - 2 * (W \text{ of } v)$

where $\deg[v] = \sum \text{weight of edge associated with } v$
 If $\maxflow < S * |V|$, D is an answer.

Requiring subgraph: all vertex can be reached from
 source with
 edge whose cap > 0 .

3 Math

3.1 FFT

```
// const int MXN = 262144 (MXN must be 2^k)
// before any usage, run pre_fft() first
typedef long double ld;
typedef complex<ld> cplx; //real() ,imag()
const ld PI = acos(-1);
const cplx I(0, 1);

struct FFT{
    cplx omega[MXN+1];
    FFT(){ //pre_fft
        for(int i=0; i<=MXN; i++)
            omega[i] = exp(i * 2 * PI / MXN * I);
    }
    // n must be 2^k
    void fft(int n, cplx a[], bool inv=false){
        int basic = MXN / n;
        int theta = basic;
        for (int m = n; m >= 2; m >>= 1) {
            int mh = m >> 1;
            for (int i = 0; i < mh; i++) {
                cplx w = omega[inv ? MXN-(i*theta%MXN) : i*theta%MXN];
                for (int j = i; j < n; j += m) {
                    int k = j + mh;
                    cplx x = a[j] - a[k];
                    a[j] += a[k];
                    a[k] = w * x;
                }
            }
            theta = (theta * 2) % MXN;
        }
        int i = 0;
        for (int j = 1; j < n - 1; j++) {
            for (int k = n >> 1; k > (i ^ k); k >>= 1);
            if (j < i) swap(a[i], a[j]);
        }
        if(inv) for (i = 0; i < n; i++) a[i] /= n;
    }
    cplx arr[MXN+1];
    inline void mul(int _n, ll a[], int _m, ll b[], ll ans[])
    {
        int n=1, sum=_n+_m-1;
        while(n<sum)
            n<<=1;
        for(int i=0; i<n; i++) {
            double x=(i<n?a[i]:0), y=(i<m?b[i]:0);
            arr[i]=complex<double>(x+y, x-y);
        }
        fft(n, arr);
        for(int i=0; i<n; i++)
            arr[i]=arr[i]*arr[i];
        fft(n, arr, true);
        for(int i=0; i<sum; i++)
            ans[i]=(long long)(arr[i].real()/4+0.5);
    }
}fft;
```

3.2 Faulhaber ($\sum_{i=1}^n i^p$)

```
/* faulhaber' s formula -
 * cal power sum formula of all p=1~k in O(k^2) */
#define MAXK 2500
const int mod = 1000000007;
int b[MAXK]; // bernoulli number
int inv[MAXK+1]; // inverse
```

```
int cm[MAXK+1][MAXK+1]; // combinactories
int co[MAXK][MAXK+2]; // coeeficient of x^j when p=i
inline int getinv(int x) {
    int a=x, b=mod, a0=1, a1=0, b0=0, b1=1;
    while(b) {
        int q, t;
        q=a/b; t=b; b=a-b*q; a=t;
        t=b0; b0=a0-b0*q; a0=t;
        t=b1; b1=a1-b1*q; a1=t;
    }
    return a0<0?a0+mod:a0;
}
inline void pre() {
    /* combinational */
    for(int i=0; i<=MAXK; i++) {
        cm[i][0]=cm[i][i]=1;
        for(int j=1; j<i; j++)
            cm[i][j]=add(cm[i-1][j-1], cm[i-1][j]);
    }
    /* inverse */
    for(int i=1; i<=MAXK; i++) inv[i]=getinv(i);
    /* bernoulli */
    b[0]=1; b[1]=getinv(2); // with b[1] = 1/2
    for(int i=2; i<=MAXK; i++) {
        if(i&1) { b[i]=0; continue; }
        b[i]=1;
        for(int j=0; j<i; j++)
            b[i]=sub(b[i], mul(cm[i][j], mul(b[j], inv[i-j+1])));
    }
    /* faulhaber */
    // sigma_x=1~n {x^p} =
    // 1/(p+1) * sigma_j=0~p {C(p+1, j)*Bj*n^(p-j+1)}
    for(int i=1; i<=MAXK; i++) {
        co[i][0]=0;
        for(int j=0; j<=i; j++)
            co[i][i-j+1]=mul(inv[i+1], mul(cm[i+1][j], b[j]));
    }
}
/* sample usage: return f(n,p) = sigma_x=1~n (x^p) */
inline int solve(int n, int p) {
    int sol=0, m=n;
    for(int i=1; i<=p+1; i++) {
        sol=add(sol, mul(co[p][i], m));
        m = mul(m, n);
    }
    return sol;
}
```

3.3 Chinese Remainder

```
LL x[N], m[N];
LL CRT(LL x1, LL m1, LL x2, LL m2) {
    LL g = __gcd(m1, m2);
    if((x2 - x1) % g) return -1; // no sol
    m1 /= g; m2 /= g;
    pair<LL, LL> p = gcd(m1, m2);
    LL lcm = m1 * m2 * g;
    LL res = p.first * (x2 - x1) * m1 + x1;
    return (res % lcm + lcm) % lcm;
}
LL solve(int n) { // n>=2, be careful with no solution
    LL res=CRT(x[0], m[0], x[1], m[1]), p=m[0]/__gcd(m[0], m[1])*m[1];
    for(int i=2; i<n; i++){
        res=CRT(res, p, x[i], m[i]);
        p=p/__gcd(p, m[i])*m[i];
    }
    return res;
}
```

3.4 Miller Rabin

```
// n < 4,759,123,141          3 : 2, 7, 61
// n < 1,122,004,669,633      4 : 2, 13, 23, 1662803
// n < 3,474,749,660,383      6 : pirmses <= 13
// n < 2^64                    7 :
```

```
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
// Make sure testing integer is in range [2, n-2] if
// you want to use magic.
LL mul(LL x, LL y, LL mod){
    LL ret=x*y-(LL)((long double)x/mod*y)*mod;
    // LL ret=x*y-(LL)((long double)x*y/mod+0.5)*mod;
    return ret<0?ret+mod:ret;
}

LL magic[]={};
bool witness(LL a, LL n, LL u, int t){
    if(!a) return 0;
    LL x=myspow(a,u,n);
    for(int i=0; i<t; i++){
        LL nx=mul(x,x,n);
        if(nx==1&&x!=1&&x!=n-1) return 1;
        x=nx;
    }
    return x!=1;
}

bool miller_rabin(LL n){
    int s=(magic number size)
    // iterate s times of witness on n
    if(n<2) return 0;
    if(!(n&1)) return n == 2;
    ll u=n-1; int t=0;
    // n-1 = u*2^t
    while(!(u&1)) u>>=1, t++;
    while(s--){
        LL a=magic[s]%n;
        if(witness(a,n,u,t)) return 0;
    }
    return 1;
}
```

3.5 Pollard Rho

```
// does not work when n is prime  $O(n^{1/4})$ 
LL f(LL x, LL mod){ return add(mul(x,x,mod),1,mod); }
LL pollard_rho(LL n){
    if(!(n&1)) return 2;
    while(true){
        LL y=2, x=rand()%(n-1)+1, res=1;
        for(int sz=2; res==1; sz*=2){
            for(int i=0; i<sz && res<=1; i++){
                x = f(x, n);
                res = __gcd(abs(x-y), n);
            }
            y = x;
        }
        if (res!=0 && res!=n) return res;
    }
}
```

3.6 Josephus Problem

```
int josephus(int n, int m){ //n人每m次
    int ans = 0;
    for (int i=1; i<=n; ++i)
        ans = (ans + m) % i;
    return ans;
}
```

3.7 Gaussian Elimination

```
const int GAUSS_MOD = 100000007LL;
struct GAUSS{
    int n;
    vector<vector<int>>> v;
    int ppow(int a, int k){
        if(k == 0) return 1;
        if(k % 2 == 0) return ppow(a * a % GAUSS_MOD, k >> 1);
        if(k % 2 == 1) return ppow(a * a % GAUSS_MOD, k >> 1) * a % GAUSS_MOD;
    }
    vector<int> solve(){
```

```
vector<int> ans(n);
REP(now, 0, n){
    REP(i, now, n) if(v[now][now] == 0 && v[i][now] != 0)
        swap(v[i], v[now]); // det = -det;
    if(v[now][now] == 0) return ans;
    int inv = ppow(v[now][now], GAUSS_MOD - 2);
    REP(i, 0, n) if(i != now){
        int tmp = v[i][now] * inv % GAUSS_MOD;
        REP(j, now, n + 1) (v[i][j] += GAUSS_MOD - tmp * v[now][j] % GAUSS_MOD) %= GAUSS_MOD;
    }
}
REP(i, 0, n) ans[i] = v[i][n + 1] * ppow(v[i][i], GAUSS_MOD - 2) % GAUSS_MOD;
return ans;
}
// gs.v.clear(), gs.v.resize(n, vector<int>(n + 1, 0));
} gs;
```

3.8 Inverse Matrix

```
int GAUSS_MOD;
struct GAUSS{
    int n;
    vector<vector<int>>> v;
    vector<vector<int>>> rev;
    int mul(int x, int y, int mod){
        int ret=x*y-(int)((long double)x/mod*y)*mod;
        return ret<0?ret+mod:ret;
    }
    int ppow(int a, int b){//res=(a^b)%m
        int res=1, k=a;
        while(b){
            if((b&1)) res=mul(res,k,GAUSS_MOD)%GAUSS_MOD;
            k=mul(k,k,GAUSS_MOD)%GAUSS_MOD;
            b>>=1;
        }
        return res%GAUSS_MOD;
    }
    bool solve(){
        for(int now = 0; now < n; now++){
            int ch;
            for(ch = now; ch < n && !v[ch][now]; ch++);
            if(ch >= n) return 0;
            for(int i = now; i < n; i++) if(v[now][now] == 0 && v[i][now] != 0){
                swap(v[i], v[now]); // det = -det;
                swap(rev[i], rev[now]);
            }
            if(v[now][now] == 0) return 0;
            int inv = ppow(v[now][now], GAUSS_MOD - 2);
            for(int i = 0; i < n; i++) if(i != now){
                int tmp = v[i][now] * inv % GAUSS_MOD;
                for(int j = 0; j < n; j++){
                    (v[i][j] += GAUSS_MOD - tmp * v[now][j] % GAUSS_MOD) %= GAUSS_MOD;
                    (rev[i][j] += GAUSS_MOD - tmp * rev[now][j] % GAUSS_MOD) %= GAUSS_MOD;
                }
            }
        }
        return 1;
    }
} gs;
```

```
signed main(){
    int n, p; //n*n matrix, MOD=p
    cin>>n>>p; //if(!n && !p) return 0;
    GAUSS_MOD = p; gs.n = n;
    gs.v.clear(), gs.v.resize(n + 1, vector<int>(n + 2, 0));
    gs.rev.clear(), gs.rev.resize(n + 1, vector<int>(n + 2, 0));
    for(int i = 0; i < n; i++){
        for(int j = 0; j < n; j++){
            cin>>gs.v[i][j];
            if(i == j) gs.rev[i][j] = 1;
        }
    }
}
```



```

if(!gs.solve()) cout << "singular\n";
else{
    for(int i = 0; i < n; i++){
        int inv = gs.ppow(gs.v[i][i] , p - 2);
        for(int j = 0; j < n; j++){
            cout << (gs.rev[i][j] * inv % p) << " ";
            cout<<"\n";
        }
    }
    cout << "\n";
}

```

3.9 模反元素

```

long long inv(long long a,long long m){
    long long x,y;
    long long d=exgcd(a,m,x,y);
    if(d==1) return (x+m)%m;
    else return -1; //-1為無解
}

```

3.10 ax+by=gcd

```

PII gcd(int a, int b){
    if(b == 0) return {1, 0};
    PII q = gcd(b, a % b);
    return {q.second, q.first - q.second * (a / b)};
}

int exgcd(int a,int b,long long &x,long long &y) {
    if(b == 0){x=1,y=0;return a;}
    int now=exgcd(b,a%b,y,x);
    y-=a/b*x;
    return now;
}

```

3.11 Discrete sqrt

```

void calcH(LL &t, LL &h, const LL p) {
    LL tmp=p-1; for(t=0;(tmp&1)==0;tmp/=2) t++; h=tmp;
}
// solve equation x^2 mod p = a
bool solve(LL a, LL p, LL &x, LL &y) {
    if(p == 2) { x = y = 1; return true; }
    int p2 = p / 2, tmp = mypow(a, p2, p);
    if (tmp == p - 1) return false;
    if ((p + 1) % 4 == 0) {
        x=mypow(a,(p+1)/4,p); y=p-x; return true;
    } else {
        LL t, h, b, pb; calcH(t, h, p);
        if (t >= 2) {
            do {b = rand() % (p - 2) + 2;
                while (mypow(b, p / 2, p) != p - 1);
                pb = mypow(b, h, p);
            } int s = mypow(a, h / 2, p);
            for (int step = 2; step <= t; step++) {
                int ss = (((LL)(s * s) % p) * a) % p;
                for(int i=0;i<t-step;i++) ss=mul(ss,ss,p);
                if (ss + 1 == p) s = (s * pb) % p;
                pb = ((LL)pb * pb) % p;
            } x = ((LL)s * a) % p; y = p - x;
        } return true;
    }
}

```

3.12 Prefix Inverse

```

void solve( int m ){
    inv[ 1 ] = 1;
    for( int i = 2 ; i < m ; i ++ )
        inv[ i ] = ((LL)(m - m / i) * inv[m % i]) % m;
}

```

3.13 Roots of Polynomial 找多項式的根

```

const double eps = 1e-12;
const double inf = 1e+12;
double a[ 10 ], x[ 10 ]; // a[0..n](coef) must be
// filled
int n; // degree of polynomial must be filled
int sign( double x ){return (x < -eps)?(-1):(x>eps);}
double f(double a[], int n, double x){
    double tmp=1,sum=0;
    for(int i=0;i<=n;i++){
        { sum=sum+a[i]*tmp; tmp=tmp*x; }
    }
    return sum;
}
double binary(double l,double r,double a[],int n){
    int sl=sign(f(a,n,l)),sr=sign(f(a,n,r));
    if(sl==0) return l; if(sr==0) return r;
    if(sl*sr>0) return inf;
    while(r-l>eps){
        double mid=(l+r)/2;
        int ss=sign(f(a,n,mid));
        if(ss==0) return mid;
        if(ss*sl>0) l=mid; else r=mid;
    }
    return l;
}
void solve(int n,double a[],double x[],int &nx){
    if(n==1){ x[1]=-a[0]/a[1]; nx=1; return; }
    double da[10], dx[10]; int ndx;
    for(int i=n;i>=1;i--) da[i-1]=a[i]*i;
    solve(n-1,da,dx,ndx);
    nx=0;
    if(ndx==0){
        double tmp=binary(-inf,inf,a,n);
        if (tmp<inf) x[++nx]=tmp;
        return;
    }
    double tmp;
    tmp=binary(-inf,dx[1],a,n);
    if(tmp<inf) x[++nx]=tmp;
    for(int i=1;i<=ndx-1;i++){
        tmp=binary(dx[i],dx[i+1],a,n);
        if(tmp<inf) x[++nx]=tmp;
    }
    tmp=binary(dx[ndx],inf,a,n);
    if(tmp<inf) x[++nx]=tmp;
} // roots are stored in x[1..nx]

```

3.14 Combination thearom

```

const ll mod = 1e9 + 7;
ll fac[(int)2e6 + 1], inv[(int)2e6 + 1];
ll getinv(ll a){ return qpow(a, mod-2); }
void init(int n){
    fac[0] = 1;
    for(int i = 1; i <= n; i++){
        fac[i] = fac[i-1] * i % mod;
    }
    inv[n] = getinv(fac[n]);
    for(int i = n - 1; i >= 0; i--){
        inv[i] = inv[i + 1] * (i + 1) % mod;
    }
}
ll C(int n, int m){
    if(m > n) return 0;
    return fac[n] * inv[m] % mod * inv[n-m] % mod;
}

```

3.15 Primes

```

/* 12721, 13331, 14341, 75577, 123457, 222557, 556679
* 999983, 1097774749, 1076767633, 100102021, 999997771
* 1001010013, 1000512343, 987654361, 999991231
* 999888733, 98789101, 987777733, 999991921, 1010101333
* 1010102101, 1000000000039, 100000000000037
* 2305843009213693951, 4611686018427387847
* 9223372036854775783, 18446744073709551557 */

```

```

int mu[ N ], p_tbl[ N ];
vector<int> primes;
void sieve() {
    mu[ 1 ] = p_tbl[ 1 ] = 1;
    for( int i = 2 ; i < N ; i ++ ){
        if( !p_tbl[ i ] ){
            p_tbl[ i ] = i;
            primes.push_back( i );
            mu[ i ] = -1;
        }
        for( int p : primes ){
            int x = i * p;
            if( x >= M ) break;
            p_tbl[ x ] = p;
            mu[ x ] = -mu[ i ];
            if( i % p == 0 ){
                mu[ x ] = 0;
                break;
            }
        }
    }
}
vector<int> factor( int x ){
    vector<int> fac{ 1 };
    while( x > 1 ){
        int fn = SZ(fac), p = p_tbl[ x ], pos = 0;
        while( x % p == 0 ){
            x /= p;
            for( int i = 0 ; i < fn ; i ++ )
                fac.PB( fac[ pos ++ ] * p );
        }
    }
    return fac;
}

```

3.16 Phi

```

ll phi(ll n){ // 計算小於n的數中與n互質的有幾個
    ll res = n, a=n;
    for(ll i=2;i*i<=a;i++){ // O(sqrtN)
        if(a%i==0){
            res = res/i*(i-1);
            while(a%i==0) a/=i;
        }
    }
    if(a>1) res=res/a*(a-1);
    return res;
}

```

3.17 Int Sqrt

```

LL intSqrt(LL S) { //return origin val when S <= 0
    if (S <= 0) return S;
    LL x = S;
    for (LL nx;;x = nx){
        nx = (x+S/x)>>1LL;
        if(nx >= x) break;
    }
    return x;
}

```

3.18 Result

- Lucas' Theorem :
For $n, m \in \mathbb{Z}^*$ and prime P , $C(m, n) \bmod P = \prod(C(m_i, n_i))$ where m_i is the i -th digit of m in base P .
- Stirling approximation :
$$n! \approx \sqrt{2\pi n} \left(\frac{n}{e}\right)^n e^{\frac{1}{12n}}$$
- Stirling Numbers(permutation $|P| = n$ with k cycles):
 $S(n, k) = \text{coefficient of } x^k \text{ in } \prod_{i=0}^{n-1} (x + i)$
- Stirling Numbers(Partition n elements into k non-empty set):
$$S(n, k) = \frac{1}{k!} \sum_{j=0}^k (-1)^{k-j} \binom{k}{j} j^n$$
- Pick' s Theorem : $A = i + b/2 - 1$
在二維座標平面中畫上網格，對於任何簡單多邊形
 A : 面積、 i : 內部的格點數、 b : 邊上的格點數

- Catalan number : $C_n = \binom{2n}{n}/(n+1)$
 $C_n^{n+m} - C_{n+1}^{n+m} = (m+n)! \frac{n-m+1}{n+1}$ for $n \geq m$
 $C_n = \frac{1}{n+1} \binom{2n}{n} = \frac{(2n)!}{(n+1)n!}$
 $C_0 = 1$ and $C_{n+1} = 2 \binom{2n+1}{n+2} C_n$
 $C_0 = 1$ and $C_{n+1} = \sum_{i=0}^n C_i C_{n-i}$ for $n \geq 0$
- Euler Characteristic:
planar graph: $V - E + F - C = 1$
convex polyhedron: $V - E + F = 2$
 V, E, F, C : number of vertices, edges, faces(regions), and components
- Kirchhoff's theorem :
 $A_{ii} = \deg(i), A_{ij} = (i, j) \in E ? -1 : 0$, Deleting any one row, one column, and cal the $\det(A)$
- Polya' theorem (c is number of color, m is the number of cycle size):
 $(\sum_{i=1}^m c^{gcd(i, m)})/m$
- Burnside lemma:
 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$
- 錯排公式: (n 個人中，每個人皆不再原來位置的組合數):
 $dp[0] = 1; dp[1] = 0;$
 $dp[i] = (i-1) * (dp[i-1] + dp[i-2]);$
- Bell 數 (有 n 個人，把他們拆組的方法總數) :
 $B_0 = 1$
 $B_n = \sum_{k=0}^n s(n, k)$ (second - stirling)
 $B_{n+1} = \sum_{k=0}^n \binom{n}{k} B_k$
- Wilson's theorem :
 $(p-1)! \equiv -1 \pmod{p}$
- Fermat's little theorem :
 $a^p \equiv a \pmod{p}$
- Euler's totient function:
 $A^{B^C} \bmod p = \text{pow}(A, \text{pow}(B, C, p-1)) \bmod p$
- 歐拉函數降幕公式:
 $A^B \bmod C = A^{B \bmod \phi(C) + \phi(C)} \bmod C$
- 用歐拉函數求模反元素:
如果 a 和 n 互質，則 a 對 n 的模反元素
 $a^{-1} \equiv a^{\phi(n)-1} \pmod{n}$
- 6 的倍數:
 $(a-1)^3 + (a+1)^3 + (-a)^3 + (-a)^3 = 6a$
- 上高斯 (向上取整) :
 $\lceil \frac{a}{b} \rceil = \frac{a+b-1}{b}$
- 點到直線距離公式:
$$d = \frac{|ax_0 + by_0 + c|}{\sqrt{a^2 + b^2}}$$

4 Geometry

4.1 definition

```

#define all(a) a.begin(),a.end()
ostream& operator<<(ostream& os, const Pt& pt) {
    return os << "(" << pt.x << ", " << pt.y << ")";
}
typedef long double ld;
const ld eps = 1e-8;
const ld pi = acos(-1);
int dcmp(ld x) {
    if(abs(x) < eps) return 0;
    else return x < 0 ? -1 : 1;
}
struct Pt {
    ld x, y;
    Pt(ld _x=0, ld _y=0):x(_x), y(_y) {}
    Pt operator+(const Pt &a) const {
        return Pt(x+a.x, y+a.y);
    }
    Pt operator-(const Pt &a) const {
        return Pt(x-a.x, y-a.y);
    }
    Pt operator*(const ld &a) const {
        return Pt(x*a, y*a);
    }
    Pt operator/(const ld &a) const {
        return Pt(x/a, y/a);
    }
    ld operator*(const Pt &a) const {
        return x*a.x + y*a.y;
    }
}

```

```

ld operator^(const Pt &a) const {
    return x*a.y - y*a.x; }
bool operator<(const Pt &a) const {
    return x < a.x || (x == a.x && y < a.y); }
//return dcmp(x-a.x) < 0 || (dcmp(x-a.x) == 0 &&
    dcmp(y-a.y) < 0); }
bool operator==(const Pt &a) const {
    return dcmp(x-a.x) == 0 && dcmp(y-a.y) == 0; }
bool operator!=(const Pt &a) const {
    return !(*this == a); }
};
ld norm2(const Pt &a) {
    return a*a; }
ld norm(const Pt &a) {
    return sqrt(norm2(a)); }
Pt perp(const Pt &a) {
    return Pt(-a.y, a.x); }
Pt rotate(const Pt &a, ld ang) {
    return Pt(a.x*cos(ang)-a.y*sin(ang), a.x*sin(ang)+a.y*
        cos(ang)); }
bool collinear(Pt a, Pt b, Pt c) { return ((b - a) ^ (c
    - a)) == 0; }
struct Circle {
    Pt o; ld r;
    Circle(Pt _o=Pt(0, 0), ld _r=0):o(_o), r(_r) {}
};

```

4.2 Line definition

```

struct Line {
    Pt s, e, v; // start, end, end-start
    ld ang;
    Line(Pt _s=Pt(0, 0), Pt _e=Pt(0, 0)):s(_s), e(_e) { v
        = e-s; ang = atan2(v.y, v.x); }
    bool operator<(const Line &L) const {
        return ang < L.ang;
    } };

// NAN(parallel), INF(overlapping)
Pt LLIntersect(Line a, Line b) {
    Pt p1 = a.s, p2 = a.e, q1 = b.s, q2 = b.e;
    ld f1 = (p2-p1)^(q1-p1), f2 = (p2-p1)^(p1-q2), f;
    if(dcmp(f=f1+f2) == 0)
        return dcmp(f1)?Pt(NAN,NAN):Pt(INFINITY,INFINITY);
    return q1*(f2/f) + q2*(f1/f);
}

// p at L's left(1), right(-1), onLine(0)
int PtSide(Pt p, Line L) {
    return dcmp((L.e - L.s)^(p - L.s));
}

bool argcmp(const Pt &a, const Pt &b) { // arg(a) < arg
    (b)
    int f = (Pt{a.y, -a.x} > Pt{} ? 1 : -1) * (a != Pt
        {});
    int g = (Pt{b.y, -b.x} > Pt{} ? 1 : -1) * (b != Pt
        {});
    return f == g ? (a ^ b) > 0 : f < g;
}

```

4.3 halfPlaneIntersection

```

// 0(nlogn)
// 傳入 vector<Line>
// (半平面為點 st 往 ed 的逆時針方向)
// 回傳值為形成的凸多邊形的頂點 vector
// assume that Lines intersect
vector<Pt> HPI(vector<Line> P) {
    sort(P.begin(), P.end(), [&](Line l, Line m) {
        if (argcmp(l.v, m.v)) return true;
        if (argcmp(m.v, l.v)) return false;
        return PtSide(l.s, m) > 0;
    });
    int n = P.size(), l = 0, r = -1;
    for (int i = 0; i < n; i++) {
        if (i and !argcmp(P[i-1].v, P[i].v)) continue
        ;
    }
}

```

```

while (l < r and PtSide(LLIntersect(P[r-1], P[r]
    ), P[l]) <= 0) r--;
while (l < r and PtSide(LLIntersect(P[l], P[l
    +1]), P[r]) <= 0) l++;
P[+r] = P[l];
}
while (l < r and PtSide(LLIntersect(P[r-1], P[r]),
    P[l]) <= 0) r--;
while (l < r and PtSide(LLIntersect(P[l], P[l+1]),
    P[r]) <= 0) l++;
if (r - l <= 1 or !argcmp(P[l].v, P[r].v))
    return {}; // empty
if (PtSide(LLIntersect(P[l], P[r]), P[l+1]) <= 0) {
    assert(0);
    return {}; // infinity
}
vector<Line> lns = vector(P.begin() + l, P.begin()
    + r + 1);
lns.push_back(lns[0]);
vector<Pt> hpi;
for(int i = 1; i < lns.size(); i++) hpi.push_back(
    LLIntersect(lns[i-1], lns[i]));
return hpi;
}

```

4.4 Convex Hull

```

double cross(Pt o, Pt a, Pt b){
    return (a-o) ^ (b-o);
}
vector<Pt> convex_hull(vector<Pt> pt){ // O(N logN)
    sort(pt.begin(), pt.end());
    int top=0;
    vector<Pt> stk(2*pt.size());
    for (int i=0; i<(int)pt.size(); i++){
        while (top >= 2 && cross(stk[top-2], stk[top-1], pt[i]
            ]) <= 0) // 如果想要有點共線的點 · 把 <= 改成 <
            top--;
        stk[top++] = pt[i];
    }
    for (int i=pt.size()-2, t=top+1; i>=0; i--){
        while (top >= t && cross(stk[top-2], stk[top-1], pt[i]
            ]) <= 0)
            top--;
        stk[top++] = pt[i];
    }
    stk.resize(top-1);
    return stk;
}

```

4.5 Convex Hull trick

```

struct Convex { // O(logN) for each operation
    int n;
    vector<Pt> A, V, L, U;
    Convex(const vector<Pt> &A) : A(_A), n(_A.size()) {
        // n >= 3
        auto it = max_element(all(A));
        L.assign(A.begin(), it + 1);
        U.assign(it, A.end()), U.push_back(A[0]);
        for (int i = 0; i < n; i++) {
            V.push_back(A[(i + 1) % n] - A[i]);
        }
    }
    int inside(Pt p, const vector<Pt> &h, auto f) {
        auto it = lower_bound(all(h), p, f);
        if (it == h.end()) return 0;
        if (it == h.begin()) return p == *it;
        return 1 - dcmp((p - *prev(it))^( *it - *prev(it)))
            ;
    }
    // 1. whether a given point is inside the CH
    // ret 0: out, 1: on, 2: in
    int inside(Pt p) {
        return min(inside(p, L, less{}), inside(p, U,
            greater{}));
    }
}

```



```

static bool cmp(Pt a, Pt b) { return dcmp(a ^ b) > 0; }
// 2. Find tangent points of a given vector
// ret the idx of far/closer tangent point
int tangent(Pt v, bool close = true) {
    assert(v != Pt{});
    auto l = V.begin(), r = V.begin() + L.size() - 1;
    if (v < Pt{}) l = r, r = V.end();
    if (close) return (lower_bound(l, r, v, cmp) - V.begin()) % n;
    return (upper_bound(l, r, v, cmp) - V.begin()) % n;
}
// 3. Find 2 tang pts on CH of a given outside point
// return index of tangent points
// return {-1, -1} if inside CH
array<int, 2> tangent2(Pt p) {
    array<int, 2> t{-1, -1};
    if (inside(p) == 2) return t;
    if (auto it = lower_bound(all(L), p); it != L.end()
        and p == *it) {
        int s = it - L.begin();
        return {(s + 1) % n, (s - 1 + n) % n};
    }
    if (auto it = lower_bound(all(U), p, greater{}); it
        != U.end() and p == *it) {
        int s = it - U.begin() + L.size() - 1;
        return {(s + 1) % n, (s - 1 + n) % n};
    }
    for (int i = 0; i != t[0]; i = tangent((A[t[0] = i]
        - p), 0));
    for (int i = 0; i != t[1]; i = tangent((p - A[t[1]
        = i]), 1));
    return t;
}
int find(int l, int r, Line L) {
    if (r < l) r += n;
    int s = PtSide(A[l % n], L);
    return *ranges::partition_point(views::iota(l, r),
        [&](int m) {
            return PtSide(A[m % n], L) == s;
        }) - 1;
};
// 4. Find intersection point of a given line
// intersection is on edge (i, next(i))
vector<int> intersect(Line L) {
    int l = tangent(L.s - L.e), r = tangent(L.e - L.s);
    if (PtSide(A[l], L) == 0) return {l};
    if (PtSide(A[r], L) == 0) return {r};
    if (PtSide(A[l], L) * PtSide(A[r], L) > 0) return
        {};
    return {find(l, r, L) % n, find(r, l, L) % n};
}
};

```

4.6 Intersection of 2 segments

```

int ori( const Pt& o, const Pt& a, const Pt& b ){
    LL ret = ( a - o ) ^ ( b - o );
    return (ret > 0) - (ret < 0);
}
// p1 == p2 || q1 == q2 need to be handled
bool banana( const Pt& p1, const Pt& p2,
    const Pt& q1, const Pt& q2 ){
    if( ( ( p2 - p1 ) ^ ( q2 - q1 ) ) == 0 ){ // parallel
        if( ori( p1, p2, q1 ) ) return false;
        return ( ( p1 - q1 ) * ( p2 - q1 ) ) <= 0 ||
            ( ( p1 - q2 ) * ( p2 - q2 ) ) <= 0 ||
            ( ( q1 - p1 ) * ( q2 - p1 ) ) <= 0 ||
            ( ( q1 - p2 ) * ( q2 - p2 ) ) <= 0;
    }
    return (ori( p1, p2, q1 ) * ori( p1, p2, q2 ) <= 0) &&
        (ori( q1, q2, p1 ) * ori( q1, q2, p2 ) <= 0);
}

```

4.7 Intersection of Polygon and Circle

```
ld PCIntersect(vector<Pt> v, Circle cir) {
```

```

for(int i = 0 ; i < (int)v.size() ; ++i) v[i] = v[i]
    - cir.o;
ld ans = 0, r = cir.r;
int n = v.size();
for(int i = 0 ; i < n ; ++i) {
    Pt pa = v[i], pb = v[(i+1)%n];
    if(norm(pa) < norm(pb)) swap(pa, pb);
    if(dcmp(norm(pb)) == 0) continue;
    ld s, h, theta;
    ld a = norm(pb), b = norm(pa), c = norm(pb-pa);
    ld cosB = (pb*(pb-pa))/a/c, B = acos(cosB);
    if(cosB > 1) B = 0;
    else if(cosB < -1) B = PI;
    ld cosC = (pa*pb)/a/b, C = acos(cosC);
    if(cosC > 1) C = 0;
    else if(cosC < -1) C = PI;
    if(a > r) {
        s = (C/2)*r*r;
        h = a*b*sin(C)/c;
        if(h < r && B < PI/2) s -= (acos(h/r)*r*r - h*
            sqrt(r*r-h*h));
    }
    else if(b > r) {
        theta = PI - B - asin(sin(B)/r*a);
        s = 0.5*a*r*sin(theta) + (C-theta)/2*r*r;
    }
    else s = 0.5*sin(C)*a*b;
    ans += abs(s)*dcmp(v[i]^v[(i+1)%n]);
}
return abs(ans);
}

```

4.8 Circle cover

```

#define N 1021
#define ld long double
struct CircleCover{ // O(N^2 logN)
    int C; Circle c[ N ]; //填入C(圓數量),c(圓陣列)
    bool g[ N ][ N ], overlap[ N ][ N ];
    // Area[i] : area covered by at least i circles
    ld Area[ N ];
    void init( int _C ){ C = _C; }
    bool CCinter( Circle& a, Circle& b, Pt& p1, Pt& p2
        ){
        Pt o1 = a.o, o2 = b.o;
        ld r1 = a.r, r2 = b.r;
        if( norm( o1 - o2 ) > r1 + r2 ) return {};
        if( norm( o1 - o2 ) < max(r1, r2) - min(r1, r2) )
            return {};
        ld d2 = ( o1 - o2 ) * ( o1 - o2 );
        ld d = sqrt(d2);
        if( d > r1 + r2 ) return false;
        Pt u=(o1+o2)*0.5 + (o1-o2)*((r2*r2-r1*r1)/(2*d2));
        ld A=sqrt((r1+r2+d)*(r1-r2+d)*(r1+r2-d)*(-r1+r2+d));
        Pt v=Pt( o1.y-o2.y, -o1.x + o2.x ) * A / (2*d2);
        p1 = u + v; p2 = u - v;
        return true;
    }
    struct Teve {
        Pt p; ld ang; int add;
        Teve() {}
        Teve(Pt _a, ld _b, int _c):p(_a), ang(_b), add(_c)
            {}
        bool operator<(const Teve &a)const
            {return ang < a.ang;}
    }eve[ N * 2 ];
    // strict: x = 0, otherwise x = -1
    bool disjunct( Circle& a, Circle& b, int x )
    {return dcmp( norm( a.o - b.o ) - a.r - b.r ) > x;}
    bool contain( Circle& a, Circle &b, int x )
    {return dcmp( a.r - b.r - norm( a.o - b.o ) ) > x;}
    bool contain(int i, int j){
        /* c[j] is non-strictly in c[i]. */
        return (dcmp(c[i].r - c[j].r) > 0 ||
            (dcmp(c[i].r - c[j].r) == 0 && i < j) ) &&
            contain(c[i], c[j], -1);
    }
    void solve(){
        for( int i = 0 ; i <= C + 1 ; i ++ )

```

4.9 Tangent line of two circles

4.10 Poly Union

```

if (argcmp(v, u)) return false;
return PtSide(l.s, r) < 0;
};
sort(all(Ls), cmp);
for (int l = 0, r = 0; l < Ls.size(); l = r) {
    while (r < Ls.size() and !cmp(Ls[l], Ls[r])) r
        ++;
    Line L = Ls[l];
    vector<pair<Pt, int>> event;
    for (auto &LLL : Ls) {
        Pt& c = LLL.s, d = LLL.e;
        if (dcmp((L.s - L.e) ^ (c - d)) != 0) {
            int s1 = PtSide(c, L) == 1;
            int s2 = PtSide(d, L) == 1;
            if (s1 ^ s2) event.emplace_back(
                LLIntersect(L, Line(c, d)), s1 ? 1
                : -1);
        } else if (PtSide(c, L) == 0 and dcmp((L.s
            - L.e) * (c - d)) > 0) {
            event.emplace_back(c, 2);
            event.emplace_back(d, -2);
        }
    }
    sort(all(event), [&](auto i, auto j) {
        return (L.s - i.first) * (L.s - L.e) < (L.s
            - j.first) * (L.s - L.e);
    });
    int cov = 0, tag = 0;
    Pt lst{0, 0};
    for (auto [p, s] : event) {
        if (cov >= tag) {
            Area[cov] += lst ^ p;
            Area[cov - tag] -= lst ^ p;
        }
        if (abs(s) == 1) cov += s;
        else tag += s / 2;
        lst = p;
    }
}
for (int i = n - 1; i >= 0; i--) Area[i] += Area[i
    + 1];
for (int i = 1; i <= n; i++) Area[i] /= 2;
return Area;
};

```

4.11 Minkowski sum

4.12 Area of Rectangles

```
struct AreaofRectangles{
#define cl(x) (x<<1)
```

```

#define cr(x) (x<<11)
ll n, id, sid;
pair<ll,ll> tree[MXN<<3]; // count, area
vector<ll> ind;
tuple<ll,ll,ll> scan[MXN<<1];
void pull(int i, int l, int r){
    if(tree[i].first) tree[i].second = ind[r+1] -
        ind[l];
    else if(l != r){
        int mid = (l+r)>>1;
        tree[i].second = tree[cl(i)].second + tree[
            cr(i)].second;
    }
    else tree[i].second = 0;
}
void upd(int i, int l, int r, int ql, int qr, int v
){
    if(ql <= l && r <= qr){
        tree[i].first += v;
        pull(i, l, r); return;
    }
    int mid = (l+r) >> 1;
    if(ql <= mid) upd(cl(i), l, mid, ql, qr, v);
    if(qr > mid) upd(cr(i), mid+1, r, ql, qr, v);
    pull(i, l, r);
}
void init(int _n){
    n = _n; id = sid = 0;
    ind.clear(); ind.resize(n<<1);
    fill(tree, tree+(n<<2), make_pair(0, 0));
}
void addRectangle(int lx, int ly, int rx, int ry){
    ind[id++] = lx; ind[id++] = rx;
    scan[sid++] = make_tuple(ly, 1, lx, rx);
    scan[sid++] = make_tuple(ry, -1, lx, rx);
}
ll solve(){
    sort(ind.begin(), ind.end());
    ind.resize(unique(ind.begin(), ind.end()) - ind
        .begin());
    sort(scan, scan + sid);
    ll area = 0, pre = get<0>(scan[0]);
    for(int i = 0; i < sid; i++){
        auto [x, v, l, r] = scan[i];
        area += tree[l].second * (x-pre);
        upd(1, 0, ind.size()-1, lower_bound(ind.
            begin(), ind.end(), l)-ind.begin(),
            lower_bound(ind.begin(), ind.end(), r)-
            ind.begin()-1, v);
        pre = x;
    }
    return area;
}
} rect;

```

4.13 Min dist on Cuboid

```

typedef LL T;
T r;
void turn(T i, T j, T x, T y, T z,
    T x0, T y0, T L, T W, T H) {
    if (z==0) { T R = x*y; if (R<r) r=R; return; }
    if(i>=0 && i<2) turn(i+1, j, x0+L+z, y, x0+L-x,
        x0+L, y0, H, W, L);
    if(j>=0 && j<2) turn(i, j+1, x, y0+W+z, y0+W-y,
        x0, y0+W, L, H, W);
    if(i<=0 && i>-2) turn(i-1, j, x0-z, y, x-x0,
        x0-H, y0, H, W, L);
    if(j<=0 && j>-2) turn(i, j-1, x, y0-z, y-y0,
        x0, y0-H, L, H, W);
}
T solve(T L, T W, T H,
    T x1, T y1, T z1, T x2, T y2, T z2){
    if( z1!=0 && z1!=H ){
        if( y1==0 || y1==W )
            swap(y1,z1), swap(y2,z2), swap(W,H);
        else swap(x1,z1), swap(x2,z2), swap(L,H);
    }
    if (z1==H) z1=0, z2=H-z2;
    r=INF; turn(0,0,x2-x1,y2-y1,z2,-x1,-y1,L,W,H);
    return r;
}

```

4.14 Distance from Point to Line or Segment

```

ld Dis_of_Line_and_Point(Line l, Pt p) {
    ld cross_product = abs((p - l.s) ^ l.v);
    ld line_length = sqrtl(l.v * l.v);
    return cross_product / line_length;
}

ld Dis_of_Segment_and_Point(Pt a, Pt b, Pt o) {
    Pt v = b - a;
    if(v * (o - a) <= 0) return norm(o - a);
    if(v * (o - b) >= 0) return norm(o - b);
    ld cross_product = abs((o - a) ^ v);
    ld line_length = sqrtl(v * v);
    return cross_product / line_length;
}

```

4.15 Angle of two vector

```

// radian of OA and OB (directed angle)
ld Angle_of_two_vector(Pt A, Pt B, Pt O) {
    ld a = (A - O) * (B - O);
    ld b = (A - O) ^ (B - O);
    ld theta = atan2(b, a);
    return theta;
}

```

4.16 極角排序

```

//極角排序
//atan2(y, x) version
// p is reference point
// 180 度開始，逆時針排序，剛好在 180 度會排最後
bool cmp(Pt &lhs, Pt rhs) {
    return atan2((lhs - p).y, (lhs - p).x) < atan2((rhs
        - p).y, (rhs - p).x);
}

//cross product version
// p is reference point
// 270 度開始，逆時針排序，剛好在 270 度會排最後
bool cmp(const Pt& lhs, const Pt& rhs) {
    if ((lhs < p) ^ (rhs < p)) return (lhs < p) < (rhs
        < p);
    return ((lhs - p) ^ (rhs - p)) > 0;
}

```

4.17 Heart of Triangle

```

Pt inCenter( Pt &A, Pt &B, Pt &C) { // 內心
    double a = norm(B-C), b = norm(C-A), c = norm(A-B);
    return (A * a + B * b + C * c) / (a + b + c);
}

Pt circumCenter( Pt &a, Pt &b, Pt &c) { // 外心
    Pt bb = b - a, cc = c - a;
    double db=norm2(bb), dc=norm2(cc), d=2*(bb ^ cc);
    return a-Pt(bb.Y*dc-cc.Y*db, cc.X*db-bb.X*dc) / d;
}

Pt othroCenter( Pt &a, Pt &b, Pt &c) { // 垂心
    Pt ba = b - a, ca = c - a, bc = b - c;
    double Y = ba.Y * ca.Y * bc.Y,
        A = ca.X * ba.Y - ba.X * ca.Y,
        x0= (Y+ca.X*ba.Y*b.X-ba.X*ca.Y*c.X) / A,
        y0= -ba.X * (x0 - c.X) / ba.Y + ca.Y;
    return Pt(x0, y0);
}

```

5 Graph

5.1 Lowest Common Ancestor $O(\lg n)$

```

struct LCA {
    int n, ti, lgN;
    int anc[MXN + 5][__lg(MXN) + 1] = {0};
    int MaxLength[MXN][__lg(MXN) + 1] = {0};
    int time_in[MXN] = {0};
    int time_out[MXN] = {0};
    LCA(int _n, int f):n(_n), ti(0), lgN(__lg(n)) {
        dfs(f, f, 0);
        build();
    }
    void dfs(int now, int f, int len_to_father) { // dfs
        for (auto i : graph[now]) {
            ti++;
            anc[now][0] = f;
            time_in[now] = ti;
            MaxLength[now][0] = len_to_father;
            if (i.first == f) continue;
            dfs(i.first, now, i.second);
        }
        time_out[now] = ti;
    }
    void build() { // build anc[], MaxLength[]
        for (int i = 1; i <= lgN; ++i) {
            for (int u = 1; u <= n; ++u) {
                anc[u][i] = anc[anc[u][i - 1]][i - 1];
                MaxLength[u][i] = max(MaxLength[u][i - 1],
                                     MaxLength[anc[u][i - 1]][i - 1]);
                // dis[u][i] += dis[anc[u][i - 1]][i - 1];
                // + dis[u][i - 1];
            }
        }
    }
    bool isAncestor(int x, int y) {
        return time_in[x] <= time_in[y] && time_out[x] >=
            time_out[y];
    }
    int getLCA(int u, int v) {
        if (isAncestor(u, v)) return u;
        if (isAncestor(v, u)) return v;
        for (int i = lgN; i >= 0; --i) {
            if (!isAncestor(anc[u][i], v)) {
                u = anc[u][i];
            }
        }
        return anc[u][0];
    }
    int getMAX(int u, int v) { //獲得路徑上最大邊權
        int lca = getLCA(u, v);
        int maxx = -1;
        for (int i = lgN; i >= 0; --i) {
            // u to lca
            if (!isAncestor(anc[u][i], lca)) {
                maxx = max(maxx, MaxLength[u][i]);
                u = anc[u][i];
            }
            // v to lca
            if (!isAncestor(anc[v][i], lca)) {
                maxx = max(maxx, MaxLength[v][i]);
                v = anc[v][i];
            }
        }
        if (u != lca) maxx = max(maxx, MaxLength[u][0]);
        if (v != lca) maxx = max(maxx, MaxLength[v][0]);
        return maxx;
    }
};

```

5.2 Hamiltonian path $O(n^2 2^n)$

//dp[i][j] = 目前在j節點走過{i}節點的最短路徑

```

for(int i=1; i < (1 << n); i++) {
    for(int j = 1; j < n; j++) {

```

```

        if(!((1 << j) & i)&&(i&1)) {
            for(int k = 0; k < n; k++) {
                if(j == k) continue;
                if((1 << k) & i) dp[j][i|(1 << j)] =
                    min(dp[j][i|(1 << j)], dp[k][i]+dis[k][j]);
            }
        }
    }
}

```

5.3 MaximumClique 最大團

```

#define N 111
struct MaxClique { // 0-base
    typedef bitset<N> Int;
    Int linkto[N], v[N];
    int n;
    void init(int _n) {
        n = _n;
        for(int i = 0; i < n; i++) {
            linkto[i].reset(); v[i].reset();
        }
    }
    void addEdge(int a, int b) {
        v[a][b] = v[b][a] = 1;
    }
    int popcount(const Int& val) {
        return val.count();
    }
    int lowbit(const Int& val) {
        return val._Find_first();
    }
    int ans, stk[N];
    int id[N], di[N], deg[N];
    Int cans;
    void maxclique(int elem_num, Int candi) {
        if(elem_num > ans) {
            ans = elem_num; cans.reset();
            for(int i = 0; i < elem_num; i++)
                cans[id[stk[i]]] = 1;
        }
        int potential = elem_num + popcount(candi);
        if(potential <= ans) return;
        int pivot = lowbit(candi);
        Int smaller_candi = candi & (~linkto[pivot]);
        while(smaller_candi.count() && potential > ans) {
            int next = lowbit(smaller_candi);
            candi[next] = !candi[next];
            smaller_candi[next] = !smaller_candi[next];
            potential--;
            if(next == pivot || (smaller_candi & linkto[next]).count()) {
                stk[elem_num] = next;
                maxclique(elem_num + 1, candi & linkto[next]);
            }
        }
    }
    int solve() {
        for(int i = 0; i < n; i++) {
            id[i] = i; deg[i] = v[i].count();
        }
        sort(id, id + n, [&](int id1, int id2) {
            return deg[id1] > deg[id2];
        });
        for(int i = 0; i < n; i++) di[id[i]] = i;
        for(int i = 0; i < n; i++) {
            for(int j = 0; j < n; j++) {
                if(v[i][j]) linkto[di[i]][di[j]] = 1;
            }
            Int cand; cand.reset();
            for(int i = 0; i < n; i++) cand[i] = 1;
            ans = 1;
            cans.reset(); cans[0] = 1;
            maxclique(0, cand);
            return ans;
        }
    }
};

```

5.4 MaximalClique 極大團

```

#define N 80
struct MaxClique { // 0-base
    typedef bitset<N> Int;
    Int lnk[N], v[N];
    int n;
    void init(int _n) {
        n = _n;

```

```

    for(int i = 0 ; i < n ; i ++){
        lnk[i].reset(); v[i].reset();
    }
}
void addEdge(int a , int b)
{ v[a][b] = v[b][a] = 1; }
int ans , stk[N], id[N] , di[N] , deg[N];
Int cans;
void dfs(int elem_num, Int candi, Int ex){
    if(candi.none() && ex.none()){
        cans.reset();
        for(int i = 0 ; i < elem_num ; i ++){
            cans[id[stk[i]]] = 1;
            ans = elem_num; // cans is a maximal clique
            return;
        }
    }
    int pivot = (candi.ex).Find_first();
    Int smaller_candi = candi & (~lnk[pivot]);
    while(smaller_candi.count()){
        int nxt = smaller_candi.Find_first();
        candi[nxt] = smaller_candi[nxt] = 0;
        ex[nxt] = 1;
        stk[elem_num] = nxt;
        dfs(elem_num+1, candi & lnk[nxt], ex & lnk[nxt]);
    }
}
int solve(){
    for(int i = 0 ; i < n ; i ++){
        id[i] = i; deg[i] = v[i].count();
    }
    sort(id , id + n , [&](int id1, int id2){
        return deg[id1] > deg[id2]; });
    for(int i = 0 ; i < n ; i ++){ di[id[i]] = i; }
    for(int i = 0 ; i < n ; i ++){
        for(int j = 0 ; j < n ; j ++){
            if(v[i][j]) lnk[di[i]][di[j]] = 1;
        }
    }
    ans = 1; cans.reset(); cans[0] = 1;
    dfs(0, Int(string(n, '1')), 0);
    return ans;
}
} solver;

```

5.5 BCC based on vertex 點雙聯通分量

```

#define PB push_back
#define REP(i, n) for(int i = 0; i < n; i++)
struct BccVertex {
    int n, nScc, step, dfn[MXN], low[MXN];
    vector<int> E[MXN], sccv[MXN];
    int top, stk[MXN];
    void init(int _n) { // 初始化n點
        n = _n; nScc = step = 0;
        for (int i=0; i<n; i++) E[i].clear();
    }
    void addEdge(int u, int v) // 無向邊
    { E[u].PB(v); E[v].PB(u); }
    void DFS(int u, int f) {
        dfn[u] = low[u] = step++;
        stk[top++] = u;
        for (auto v:E[u]) {
            if (v == f) continue;
            if (dfn[v] == -1) {
                DFS(v, u);
                low[u] = min(low[u], low[v]);
                if (low[v] >= dfn[u]) {
                    int z;
                    sccv[nScc].clear();
                    do {
                        z = stk[--top];
                        sccv[nScc].PB(z);
                    } while (z != v);
                    sccv[nScc++].PB(u);
                }
            } else {
                low[u] = min(low[u], dfn[v]);
            }
        }
    }
    vector<vector<int>> solve() { // 回傳(size=2 橋, size
        >2 點雙連通分量)
        vector<vector<int>> res;
        for (int i=0; i<n; i++)
            dfn[i] = low[i] = -1;
        for (int i=0; i<n; i++)
            if (dfn[i] == -1) {

```

```

                top = 0;
                DFS(i, i);
            }
            REP(i, nScc) res.PB(sccv[i]);
            return res;
        }
    } graph;
}

```

5.6 Strongly Connected Component 強連通分量

```

#define PB push_back
#define FZ(x) memset(x, 0, sizeof(x)) //fill zero
struct Scc{
    int n, nScc, vst[MXN], bln[MXN];
    vector<int> E[MXN], rE[MXN], vec;
    void init(int _n){
        n = _n;
        for (int i=0; i<MXN; i++)
            E[i].clear(), rE[i].clear();
    }
    void addEdge(int u, int v){
        E[u].PB(v); rE[v].PB(u);
    }
    void DFS(int u){
        vst[u]=1;
        for (auto v : E[u]) if (!vst[v]) DFS(v);
        vec.PB(u);
    }
    void rDFS(int u){
        vst[u] = 1; bln[u] = nScc;
        for (auto v : rE[u]) if (!vst[v]) rDFS(v);
    }
    void solve(){
        nScc = 0;
        vec.clear();
        FZ(vst);
        for (int i=0; i<n; i++){
            if (!vst[i]) DFS(i);
            reverse(vec.begin(), vec.end());
            FZ(vst);
            for (auto v : vec)
                if (!vst[v]){
                    rDFS(v); nScc++;
                }
        }
    }
};

```

5.7 ManhattanMST

```

//return {{u,v},w}: u <-> v (w), 需要再手動去重
//need Point definition
vector<pair<pair<int,int>, int>> ManhattanMST(vector<Pt
> P) {
    vector<int> id(P.size());
    iota(id.begin(), id.end(), 0);
    vector<pair<pair<int,int>, int>> edg;
    for (int k = 0; k < 4; k++) {
        sort(id.begin(), id.end(), [&](int i, int j) {
            return (P[i] - P[j]).x < (P[j] - P[i]).y;
        });
        map<int, int> sweep;
        for (int i : id) {
            auto it = sweep.lower_bound(-P[i].y);
            while (it != sweep.end()) {
                int j = it->second;
                Pt d = P[i] - P[j];
                if (d.y > d.x) break;
                edg.push_back({i, j}, d.x + d.y);
                it = sweep.erase(it);
            }
            sweep[-P[i].y] = i;
        }
        for (Pt &p : P) {
            if (k % 2) p.x = -p.x;
            else swap(p.x, p.y);
        }
    }
}

```



```

    } } }
    for(int j=0; j<(int)grev[i].size(); j++) if(grev[
        i][j].to > i)
        mldc=min(mldc,d[grev[i][j].to] + grev[i][j].w);
    }
    return mldc / bunbo;
} }graph;

```

5.10 DominatorTree

```

struct DominatorTree{ // O(N)
#define REP(i,s,e) for(int i=(s);i<=(e);i++)
#define REPD(i,s,e) for(int i=(s);i>=(e);i--)
    int n , m , s;
    vector< int > g[ MAXN ] , pred[ MAXN ];
    vector< int > cov[ MAXN ];
    int dfn[ MAXN ] , nfd[ MAXN ] , ts;
    int par[ MAXN ]; //idom[u] s到u的最後一個必經點
    int sdom[ MAXN ] , idom[ MAXN ];
    int mom[ MAXN ] , mn[ MAXN ];
    inline bool cmp( int u , int v )
    { return dfn[ u ] < dfn[ v ]; }
    int eval( int u ){
        if( mom[ u ] == u ) return u;
        int res = eval( mom[ u ] );
        if(cmp( sdom[ mn[ mom[ u ] ] ] , sdom[ mn[ u ] ] ))
            mn[ u ] = mn[ mom[ u ] ];
        return mom[ u ] = res;
    }
    void init( int _n , int _m , int _s ){
        ts = 0; n = _n; m = _m; s = _s;
        REP( i , 1 , n ) g[ i ].clear(), pred[ i ].clear();
    }
    void addEdge( int u , int v ){
        g[ u ].push_back( v );
        pred[ v ].push_back( u );
    }
    void dfs( int u ){
        ts++;
        dfn[ u ] = ts;
        nfd[ ts ] = u;
        for( int v : g[ u ] ) if( dfn[ v ] == 0 ){
            par[ v ] = u;
            dfs( v );
        }
    }
    void build(){
        REP( i , 1 , n ){
            dfn[ i ] = nfd[ i ] = 0;
            cov[ i ].clear();
            mom[ i ] = mn[ i ] = sdom[ i ] = i;
        }
        dfs( s );
        REPD( i , n , 2 ){
            int u = nfd[ i ];
            if( u == 0 ) continue;
            for( int v : pred[ u ] ) if( dfn[ v ] ){
                eval( v );
                if( cmp( sdom[ mn[ v ] ] , sdom[ u ] ) )
                    sdom[ u ] = sdom[ mn[ v ] ];
            }
            cov[ sdom[ u ] ].push_back( u );
            mom[ u ] = par[ u ];
            for( int w : cov[ par[ u ] ] ){
                eval( w );
                if( cmp( sdom[ mn[ w ] ] , par[ u ] ) )
                    idom[ w ] = mn[ w ];
                else idom[ w ] = par[ u ];
            }
            cov[ par[ u ] ].clear();
        }
        REP( i , 2 , n ){
            int u = nfd[ i ];
            if( u == 0 ) continue;
            if( idom[ u ] != sdom[ u ] )
                idom[ u ] = idom[ idom[ u ] ];
        }
    } }domT;

```

5.11 K-th Shortest Path

```

// time: O(|E| \lg |E| + |V| \lg |V| + K)
// memory: O(|E| \lg |E| + |V|)
struct KSP{ // 1-base
    struct nd{
        int u, v; ll d;
        nd(int ui = 0, int vi = 0, ll di = INF)
            { u = ui; v = vi; d = di; }
    };
    struct heap{
        nd* edge; int dep; heap* chd[4];
    };
    static int cmp(heap* a, heap* b)
    { return a->edge->d > b->edge->d; }
    struct node{
        int v; ll d; heap* H; nd* E;
        node(){
            node(ll _d, int _v, nd* _E)
                { d = _d; v = _v; E = _E; }
            node(heap* _H, ll _d)
                { H = _H; d = _d; }
            friend bool operator<(node a, node b)
                { return a.d > b.d; }
        };
        int n, k, s, t;
        ll dst[ N ];
        nd *nxt[ N ];
        vector<nd*> g[ N ], rg[ N ];
        heap *nullNd, *head[ N ];
        void init( int _n , int _k , int _s , int _t ){
            n = _n; k = _k; s = _s; t = _t;
            for( int i = 1 ; i <= n ; i ++ ){
                g[ i ].clear(); rg[ i ].clear();
                nxt[ i ] = NULL; head[ i ] = NULL;
                dst[ i ] = -1;
            }
        }
        void addEdge( int ui , int vi , ll di ){
            nd* e = new nd(ui, vi, di);
            g[ ui ].push_back( e );
            rg[ vi ].push_back( e );
        }
        queue<int> dfsQ;
        void dijkstra(){
            while(dfsQ.size()) dfsQ.pop();
            priority_queue<node> Q;
            Q.push(node(0, t, NULL));
            while (!Q.empty()){
                node p = Q.top(); Q.pop();
                if(dst[p.v] != -1) continue;
                dst[ p.v ] = p.d;
                nxt[ p.v ] = p.E;
                dfsQ.push( p.v );
                for(auto e: rg[ p.v ] )
                    Q.push(node(p.d + e->d, e->u, e));
            }
        }
        heap* merge(heap* curNd, heap* newNd){
            if(curNd == nullNd) return newNd;
            heap* root = new heap;
            memcpy(root, curNd, sizeof(heap));
            if(newNd->edge->d < curNd->edge->d){
                root->edge = newNd->edge;
                root->chd[2] = newNd->chd[2];
                root->chd[3] = newNd->chd[3];
                newNd->edge = curNd->edge;
                newNd->chd[2] = curNd->chd[2];
                newNd->chd[3] = curNd->chd[3];
            }
            if(root->chd[0]->dep < root->chd[1]->dep)
                root->chd[0] = merge(root->chd[0],newNd);
            else
                root->chd[1] = merge(root->chd[1],newNd);
            root->dep = max(root->chd[0]->dep, root->chd[1]->
                dep) + 1;
            return root;
        }
        vector<heap*> V;
        void build(){
            nullNd = new heap;
            nullNd->dep = 0;
            nullNd->edge = new nd;
            fill(nullNd->chd, nullNd->chd+4, nullNd);
            while(not dfsQ.empty()){
                int u = dfsQ.front(); dfsQ.pop();

```

```

if(!nxt[ u ]) head[ u ] = nullNd;
else head[ u ] = head[nxt[ u ]->v];
V.clear();
for( auto& e : g[ u ] ){
    int v = e->v;
    if( dst[ v ] == -1 ) continue;
    e->d += dst[ v ] - dst[ u ];
    if( nxt[ u ] != e ){
        heap* p = new heap;
        fill(p->chd, p->chd+4, nullNd);
        p->dep = 1;
        p->edge = e;
        V.push_back(p);
    }
}
if(V.empty()) continue;
make_heap(V.begin(), V.end(), cmp);
#define L(X) ((X<<1)+1)
#define R(X) ((X<<1)+2)
for( size_t i = 0 ; i < V.size() ; i ++ ){
    if(L(i) < V.size()) V[i]->chd[2] = V[L(i)];
    else V[i]->chd[2]=nullNd;
    if(R(i) < V.size()) V[i]->chd[3] = V[R(i)];
    else V[i]->chd[3]=nullNd;
}
head[u] = merge(head[u], V.front());
} }
vector<ll> ans;
void first_K(){
    ans.clear();
    priority_queue<node> Q;
    if( dst[ s ] == -1 ) return;
    ans.push_back( dst[ s ] );
    if( head[s] != nullNd )
        Q.push(node(head[s], dst[s]+head[s]->edge->d));
    for( int _ = 1 ; _ < k and not Q.empty() ; _ ++ ){
        node p = Q.top(), q; Q.pop();
        ans.push_back( p.d );
        if(head[ p.H->edge->v ] != nullNd){
            q.H = head[ p.H->edge->v ];
            q.d = p.d + q.H->edge->d;
            Q.push(q);
        }
        for( int i = 0 ; i < 4 ; i ++ )
            if( p.H->chd[ i ] != nullNd ){
                q.H = p.H->chd[ i ];
                q.d = p.d - p.H->edge->d + p.H->chd[ i ]->
                    edge->d;
                Q.push( q );
            }
    }
}
void solve(){ // ans[i] stores the i-th shortest path
    dijkstra();
    build();
    first_K(); // ans.size() might less than k
} }solver;

```

```

#define INF 1023456789
int n , dst[V][V] , dp[1 << T][V] , tdst[V];
void init( int _n ){
    n = _n;
    for( int i = 0 ; i < n ; i ++ ){
        for( int j = 0 ; j < n ; j ++ )
            dst[ i ][ j ] = INF;
        dst[ i ][ i ] = 0;
    }
}
void add_edge( int ui , int vi , int wi ){
    dst[ ui ][ vi ] = min( dst[ ui ][ vi ] , wi );
    dst[ vi ][ ui ] = min( dst[ vi ][ ui ] , wi );
}
void shortest_path(){ // using spfa may faster
    for( int k = 0 ; k < n ; k ++ )
        for( int i = 0 ; i < n ; i ++ )
            for( int j = 0 ; j < n ; j ++ )
                dst[ i ][ j ] = min( dst[ i ][ j ] ,
                    dst[ i ][ k ] + dst[ k ][ j ] );
} // call shorest_path before solve
int solve( const vector<int>& ter ){
    int t = (int)ter.size();
    for( int i = 0 ; i < ( 1 << t ) ; i ++ )
        for( int j = 0 ; j < n ; j ++ )
            dp[ i ][ j ] = INF;
    for( int i = 0 ; i < n ; i ++ )
        dp[ 0 ][ i ] = 0;
    for( int msk = 1 ; msk < ( 1 << t ) ; msk ++ ){
        if( msk == ( msk & (-msk) ) ){
            int who = __lg( msk );
            for( int i = 0 ; i < n ; i ++ )
                dp[ msk ][ i ] = dst[ ter[ who ] ][ i ];
            continue;
        }
        for( int i = 0 ; i < n ; i ++ )
            for( int submsk = ( msk - 1 ) & msk ; submsk ;
                submsk = ( submsk - 1 ) & msk )
                dp[ msk ][ i ] = min( dp[ msk ][ i ] ,
                    dp[ submsk ][ i ] +
                    dp[ msk ^ submsk ][ i ] );
        for( int i = 0 ; i < n ; i ++ ){
            tdst[ i ] = INF;
            for( int j = 0 ; j < n ; j ++ )
                tdst[ i ] = min( tdst[ i ] ,
                    dp[ msk ][ j ] + dst[ j ][ i ] );
        }
        for( int i = 0 ; i < n ; i ++ )
            dp[ msk ][ i ] = tdst[ i ];
    }
    int ans = INF;
    for( int i = 0 ; i < n ; i ++ )
        ans = min( ans , dp[ ( 1 << t ) - 1 ][ i ] );
    return ans;
} }solver;

```

5.12 Floryd Warshall

```

for( int k=0 ; k < n ; k++ )
    for( int i=0 ; i < n ; i++ )
        for( int j=0 ; j < n ; j++ )
            if( dis[i][j] > dis[i][k]+dis[k][j] && dis[i][k]
                < INF && dis[k][j] < INF )
                dis[i][j]=dis[i][k]+dis[k][j];
for( int i=0 ; i < n ; i++ )
    for( int j=0 ; j < n ; j++ )
        for( int k=0 ; k < n && dis[i][j] != negINF ; k++ )
            if( dis[k][k] < 0 && dis[i][k] != INF && dis[k]
                [j] != INF )
                dis[i][j]=negINF;

```

5.13 Minimum Steiner Tree

```

// Minimum Steiner Tree 重要點的mst
// O(V 3AT + V^2 2AT)
struct SteinerTree{
#define V 33
#define T 8

```

5.14 虛樹

```

vector<int> virTree(vector<int> ver, LCA &lca) {
    auto cmp = [&](int u, int v){return time_in[u] <
        time_in[v];};
    sort(ver.begin(),ver.end(),cmp); //用dfn排序
    vector<int>res(ver.begin(),ver.end());
    for(int i = 1; i < ver.size(); i++){
        res.push_back(lca.getLCA(ver[i-1],ver[i])); //把
        LCA丟進虛樹內
    }
    sort(res.begin(),res.end(),cmp); //再用dfn排序
    res.erase(unique(res.begin(),res.end()), res.end());
    ; //去掉重複的點
    return res;
}

```

5.15 Tree Hash

```

map<vector<int>, int> id;
int dfs(int x, int f){
    vector<int> sub;
    for (int v : edge[x]){

```

```

    if (v != f)
        sub.push_back(dfs(v, x));
}
sort(sub.begin(), sub.end());
if (!id.count(sub))
    id[sub] = id.size();
return id[sub];
}

```

5.16 HeavyLightDecomposition

```

// 詢問,修改複雜度  $O(\log^2 n)$ 
// 1-base

int sz[MXN], dep[MXN], son[MXN], fa[MXN];

// 第一次 dfs
// 找重兒子 需要紀錄當前節點的子樹大小(sz)、深度(dep)、
// 重兒子(son)、父節點(fa)
// 沒有子節點 son[x] = 0
void dfs_sz(int x, int f, int d) { //當前節點 x · 父節點 f · 深度 d
    sz[x] = 1; dep[x] = d; fa[x] = f;
    for(int i : edge[x]) {
        if(i == f) continue;
        dfs_sz(i, x, d+1);
        sz[x] += sz[i];
        if(sz[son[x]] < sz[i]) son[x] = i;
    }
}

// 第二次 dfs
int top[MXN]; // 每個節點所在的鏈的頂端節點
int dfn[MXN]; // 節點編號,編號為在線段樹上的位置
int rnk[MXN]; // 編號為哪個節點
int bottom[MXN]; // 維護每個節點的子樹中最大 dfn 編號
int cnt = 0;
int dfs_hld(int x, int f){
    top[x] = (son[fa[x]] == x ? top[fa[x]] : x);
    rnk[cnt] = x;
    bottom[x] = dfn[x] = cnt++;
    if(son[x]) bottom[x] = max(bottom[x], dfs_hld(son[x], x)); // 更新子樹最大編號
    for(int i : edge[x]){
        if(i == f || i == son[x]) continue;
        bottom[x] = max(bottom[x], dfs_hld(i, x)); // 更新子樹最大編號
    }
    return bottom[x];
}

// 求出 lca
// 不斷跳鏈 · 直到 u,v 跳到同一條鏈上為止
// 每次跳鏈選所在的鏈頂端深度較深的一端往上跳
int getLca(int u, int v) {
    while(top[u] != top[v]){
        if(dep[top[u]] > dep[top[v]])
            u = fa[top[u]];
        else
            v = fa[top[v]];
    }
    return dep[u] > dep[v] ? v : u;
}

// 路徑權重總和
int query(int u, int v) {
    int ret = 0;
    while(top[u] != top[v]){
        if(dep[top[u]] > dep[top[v]]){
            ret += segtree.query(dfn[top[u]], dfn[u]);
            u = fa[top[u]];
        }
        else{
            ret += segtree.query(dfn[top[v]], dfn[v]);
            v = fa[top[v]];
        }
    }
    // 最後到同一條鏈上

```

```

    ret += segtree.query(min(dfn[u], dfn[v]), max(dfn[u], dfn[v]));
    return ret;
}

```

5.17 Graph Thearom

- 差分約束條件:
約束條件 $V_j - V_i \leq W$ addEdge(V_i, V_j, W) and run bellman-ford or spfa
- 龜兔賽跑演算法:
開始賽跑, 兔子一次走兩格、烏龜一次走一格直到他們相遇停止
此時讓兔子返回起始點, 兩者以相同走一格的速度繼續前進, 他們就會在環入口會合
- 2-SAT 條件:
滿足 $(x_1 \text{ or } y_1) \text{ and } (x_2 \text{ or } y_2) \text{ and } \dots$ 對於一個限制 $(x \text{ or } y)$ · 則加兩條邊 $x \rightarrow y, y \rightarrow \neg x$

6 String

6.1 PalTree $O(n)$

```

// state[i]代表第i個字元為結尾的最長回文編號
// len[s]是對應的回文長度
// num[s]是有幾個回文後綴
// cnt[s]是這個回文子字串在整個字串中的出現次數
// fail[s]是他長度次長的回文後綴 · aba的fail是a
const int MXN = 1000010;
struct PalT{
    int nxt[MXN][26], fail[MXN], len[MXN];
    int tot, lst, n, state[MXN], cnt[MXN], num[MXN];
    int diff[MXN], sfail[MXN], fac[MXN], dp[MXN];
    char s[MXN] = {-1};
    int newNode(int l, int f){
        len[tot] = l, fail[tot] = f, cnt[tot] = num[tot] = 0;
        memset(nxt[tot], 0, sizeof(nxt[tot]));
        diff[tot] = (l > 0 ? l - len[f] : 0);
        sfail[tot] = (l > 0 && diff[tot] == diff[f] ? sfail[f] : f);
        return tot++;
    }
    int getfail(int x){
        while(s[n - len[x] - 1] != s[n]) x = fail[x];
        return x;
    }
    int getmin(int v){
        dp[v] = fac[n - len[sfail[v]] - diff[v]];
        if(diff[v] == diff[fail[v]])
            dp[v] = min(dp[v], dp[fail[v]]);
        return dp[v] + 1;
    }
    int pushC(){
        int c = s[n] - 'a', np = getfail(lst);
        if(!lst || np[c] == -1){
            lst = newNode(len[np] + 2, np[getfail(fail[np])][c]);
            nxt[np][c] = lst; num[lst] = num[fail[lst]] + 1;
        }
        fac[n] = n;
        for(int v = lst; len[v] > 0; v = sfail[v])
            fac[n] = min(fac[n], getmin(v));
        return ++cnt[lst], lst;
    }
    void init(const char *_s){
        tot = lst = n = 0;
        newNode(0, 1), newNode(-1, 1);
        for(; s[n];) s[n+1] = s[n], ++n, state[n-1] = pushC();
        for(int i = tot - 1; i > 1; i--) cnt[fail[i]] += cnt[i];
    }
}palt;

```

6.2 Longest Increasing Subsequence

```

vector<int> getLIS(vector<int> a){
    vector<int> lis;
    for(int i : a){

```

```

    if(lis.empty() || lis.back() < i)    lis.push_Back(
        i);
    else    *lower_bound(lis.begin(), lis.end(), i) =
        i;
}
return lis;
}

```

6.3 Longest Common Subsequence $O(nlgn)$

```

int LCS(string& s1, string& s2) {
    vector<int> p[128]; // 假設字元範圍為 0 ~ 127
    for (int i = 0; i < s2.size(); ++i) p[s2[i]].
        push_back(i);
    vector<int> v;
    v.push_back(-1);

    for (int i = 0; i < s1.size(); ++i)
        for (int j = p[s1[i]].size() - 1; j >= 0; --j) {
            int n = p[s1[i]][j];

            if (n > v.back())
                v.push_back(n);
            else
                *lower_bound(v.begin(), v.end(), n) = n;
        }
    return v.size() - 1;
};

```

6.4 KMP

/* len-failure[k]:
在k結尾的情況下，這個子字串可以由開頭
長度為(len-failure[k])的部分重複出現來表達

failure[k]為次長相同前綴後綴

如果我們不只想求最多，而且以0-base做為考量
，那可能的長度由大到小會是

failuer[k]、failure[failuer[k]-1]
、failure[failure[failuer[k]-1]-1]..
直到有值為0為止 */

```

int failure[MXN];
vector<int> KMP(string& t, string& p) {
    vector<int> ret;
    if(p.size() > t.size()) return ret;
    for(int i = 1, j = failure[0] = -1; i < p.size(); i
        ++){
        while(j >= 0 && p[j + 1] != p[i]) j = failure[j
        ];
        if(p[j + 1] == p[i]) j++;
        failure[i] = j;
    }
    for(int i = 0, j = -1; i < t.size(); i++) {
        while (j >= 0 && p[j + 1] != t[i]) j = failure[
        j];
        if(p[j + 1] == t[i]) j++;
        if(j == p.size() - 1) {
            ret.push_back(i - p.size() + 1);
            j = failure[j];
        }
    }
    return ret;
}

```

6.5 SAIS $O(n)$

/* ** SA · 將字串的所有後綴排序後的數組 ** */
/* SA[i]儲存排序後第i小的後綴從哪裡開始 */
/* ** H[i]為第i小的字串跟第i-1小的LCP ** */
/* ** 註：LCP(Longest Common Prefix) ** */
/* ** ex:S = "babd", SA[0] = 1("abd") ** */
/* ** SA[1] = 0("babd"), SA[2] = 2("bd") ** */
/* ** H[0] = 0, H[1] = 0, H[2] = 1("b") ** */
/* 傳入參數:ip 陣列放字串，len為字串長度 */
/* 需保證ip[len]為0，且字串裡的元素不為0 */

```

const int N = 300010;
struct SA{
#define REP(i,n) for ( int i=0; i<int(n); i++ )
#define REP1(i,a,b) for ( int i=(a); i<=int(b); i++ )
    bool _t[N*2];
    int _s[N*2], _sa[N*2], _c[N*2], x[N], _p[N], _q[N*2],
        hei[N], r[N];
    int operator [] (int i){ return _sa[i]; }
    void build(int *s, int n, int m){
        memcpy(_s, s, sizeof(int) * n);
        sais(_s, _sa, _p, _q, _t, _c, n, m);
        mkhei(n);
    }
    void mkhei(int n){
        REP(i,n) r[_sa[i]] = i;
        hei[0] = 0;
        REP(i,n) if(r[i]) {
            int ans = i>0 ? max(hei[r[i-1]] - 1, 0) : 0;
            while(_s[i+ans] == _s[_sa[r[i]-1]+ans]) ans++;
            hei[r[i]] = ans;
        }
    }
    void sais(int *s, int *sa, int *p, int *q, bool *t,
        int *c, int n, int z){
        bool uniq = t[n-1] = true, neq;
        int nn = 0, nmzx = -1, *nsa = sa + n, *ns = s + n,
            lst = -1;
#define MS0(x,n) memset((x),0,n*sizeof(*(x)))
#define MAGIC(XD) MS0(sa, n); \
        memcpy(x, c, sizeof(int) * z); \
        XD; \
        memcpy(x + 1, c, sizeof(int) * (z - 1)); \
        REP(i,n) if(sa[i] && !t[sa[i]-1]) sa[x[s[sa[i
            ]-1]]++] = sa[i]-1; \
        memcpy(x, c, sizeof(int) * z); \
        for(int i = n - 1; i >= 0; i--) if(sa[i] && t[sa[i
            ]-1]) sa[--x[s[sa[i]-1]]] = sa[i]-1;
        MS0(c, z);
        REP(i,n) uniq &= ++c[s[i]] < 2;
        REP(i,z-1) c[i+1] += c[i];
        if (uniq) { REP(i,n) sa[--c[s[i]]] = i; return; }
        for(int i = n - 2; i >= 0; i--) t[i] = (s[i]==s[i
            +1] ? t[i+1] : s[i]<s[i+1]);
        MAGIC(REP1(i,1,n-1) if(t[i] && !t[i-1]) sa[--x[s[i
            ]]] = p[q[i]=nn++] = i);
        REP(i, n) if (sa[i] && t[sa[i]] && !t[sa[i]-1]) {
            neq=lst<0 || memcmp(s+sa[i],s+lst,(p[q[sa[i]]+1]-sa
                [i])*sizeof(int));
            ns[q[lst=sa[i]]]=nmzx+=neq;
        }
        sais(ns, nsa, p + nn, q + n, t + n, c + z, nn, nmzx
            + 1);
        MAGIC(for(int i = nn - 1; i >= 0; i--) sa[--x[s[p[
            nsa[i]]]]] = p[nsa[i]]);
    }
}sa;
int H[ N ], SA[ N ];
void suffix_array(int* ip, int len) {
    // should padding a zero in the back
    // ip is int array, len is array length
    // ip[0..n-1] != 0, and ip[len] = 0
    ip[len++] = 0;
    sa.build(ip, len, 128);
    for (int i=0; i<len; i++) {
        H[i] = sa.hei[i + 1];
        SA[i] = sa._sa[i + 1];
    }
    // resulting height, sa array \in [0,len)
}

```

6.6 Z Value $O(n)$

```

//z[i] = lcp(s[1...n-1],s[i...n-1])
int z[MAXN];
void Z_value(const string& s) {
    int i, j, left, right, len = s.size();
    left=right=0; z[0]=len;
    for(i=1;i<len;i++) {
        j=max(min(z[i-left],right-i),0);
        for(;i+j<len&&s[i+j]==s[j];j++);
    }
}

```



```

    z[i]=j;
    if(i+z[i]>right) {
        right=i+z[i];
        left=i;
    }
}

```

6.7 Manacher Algorithm $O(n)$

```

// 求以每個字元為中心的最長回文半徑
// 頭尾以及每個字元間都加入一個
// 沒出現過的字元 · 這邊以'@'為例
// s為傳入的字串 · len為字串長度
// z為儲存答案的陣列 (有包含'@'要小心)
// ex: s = "abaac" -> "@a@b@a@a@c@"
// z = [12141232121]
void z_value_pal(char *s,int len,int *z){
    len=(len<<1)+1;
    for(int i=len-1;i>=0;i--){
        s[i]=i&1?s[i>>1]:'@';
        z[0]=1;
        for(int i=1,l=0,r=0;i<len;i++){
            z[i]=i<r?min(z[l+l-i],r-i):1;
            while(i-z[i]>=0&&i+z[i]<len&&s[i-z[i]]==s[i+z[i]])
                ++z[i];
            if(i+z[i]>r) l=i,r=i+z[i];
        }
    }
}

```

6.8 Smallest Rotation

```

//rotate(begin(s),begin(s)+minRotation(s),end(s))
int minRotation(string s) {
    int a = 0, N = s.size(); s += s;
    rep(b,0,N) rep(k,0,N) {
        if(a+k == b || s[a+k] < s[b+k])
            {b += max(0, k-1); break;}
        if(s[a+k] > s[b+k]) {a = b; break;}
    }
    return a;
}

```

6.9 Cyclic LCS

```

#define L 0
#define LU 1
#define U 2
const int mov[3][2]={0,-1, -1,-1, -1,0};
int al,bl;
char a[MAXL*2],b[MAXL*2]; // 0-indexed
int dp[MAXL*2][MAXL];
char pred[MAXL*2][MAXL];
inline int lcs_length(int r) {
    int i=r+al,j=bl,l=0;
    while(i>r) {
        char dir=pred[i][j];
        if(dir==LU) l++;
        i+=mov[dir][0];
        j+=mov[dir][1];
    }
    return l;
}
inline void reroot(int r) { // r = new base row
    int i=r,j=1;
    while(j<=bl&&pred[i][j]!=LU) j++;
    if(j>bl) return;
    pred[i][j]=L;
    while(i<2*al&&j<=bl) {
        if(pred[i+1][j]==U) {
            i++;
            pred[i][j]=L;
        } else if(j<bl&&pred[i+1][j+1]==LU) {
            i++;
            j++;
            pred[i][j]=L;
        } else {
            j++;
        }
    }
}

```

```

int cyclic_lcs() {
    // a, b, al, bl should be properly filled
    // note: a WILL be altered in process
    // -- concatenated after itself
    char tmp[MAXL];
    if(al>bl) {
        swap(al,bl);
        strcpy(tmp,a);
        strcpy(a,b);
        strcpy(b,tmp);
    }
    strcpy(tmp,a);
    strcat(a,tmp);
    // basic lcs
    for(int i=0;i<=2*al;i++) {
        dp[i][0]=0;
        pred[i][0]=U;
    }
    for(int j=0;j<=bl;j++) {
        dp[0][j]=0;
        pred[0][j]=L;
    }
    for(int i=1;i<=2*al;i++) {
        for(int j=1;j<=bl;j++) {
            if(a[i-1]==b[j-1]) dp[i][j]=dp[i-1][j-1]+1;
            else dp[i][j]=max(dp[i-1][j],dp[i][j-1]);
            if(dp[i][j-1]==dp[i][j]) pred[i][j]=L;
            else if(a[i-1]==b[j-1]) pred[i][j]=LU;
            else pred[i][j]=U;
        }
    }
    // do cyclic lcs
    int clcs=0;
    for(int i=0;i<al;i++) {
        clcs=max(clcs,lcs_length(i));
        reroot(i+1);
    }
    // recover a
    a[al]='\0';
    return clcs;
}

```

6.10 Hash

```

//字串雜湊前的idx是0-base · 雜湊後為1-base
//即區間為 [0,n-1] -> [1,n]
//若要取得區間[L,R]的值得
//H[R] - H[L-1] * p^(R-L+1)
//cmp為比較從i開始長度為len的字串和
//((h[i+len-1] - h[i-1] * qpow(p, len) % modl + modl)
//從j開始長度為len的字串是否相同
#define x first
#define y second
pair<int,int> Hash[MXN];
void build(const string& s){
    pair<int,int> val = make_pair(0,0);
    Hash[0]=val;
    for(int i=1; i<=s.size(); i++){
        val.x = (val.x * P1 + s[i-1]) % MOD;
        val.y = (val.y * P2 + s[i-1]) % MOD;
        Hash[i] = val;
    }
}
bool cmp( int i, int j, int len ) {
    return ((Hash[i+len-1].x-Hash[i-1].x*qpow(P1,len)%
        MOD+MOD)%MOD == (Hash[j+len-1].x-Hash[j-1].x*
        qpow(P1,len)%MOD+MOD)%MOD)
        && ((Hash[i+len-1].y-Hash[i-1].y*qpow(P2,len)%MOD+
        MOD)%MOD == (Hash[j+len-1].y-Hash[j-1].y*qpow(
        P2,len)%MOD+MOD)%MOD);
}

```

7 Data Structure

7.1 Segment tree

```
// !!!注意build()時初始化用的陣列也是1-base
// !!!query(0, 0) 會報錯
#define cl(x) (x*2)
#define cr(x) (x*2+1)

struct segmentTree {
    int n;
    vector<int> seg, tag, cov;
    segmentTree(int _n): n(_n) {
        seg = tag = cov = vector<int>(n * 4, 0);
    }
    void push(int i, int L, int R) {
        if(cov[i]) {
            seg[i] = cov[i] * (R - L + 1);
            if(L < R) {
                cov[cl(i)] = cov[cr(i)] = cov[i];
                tag[cl(i)] = tag[cr(i)] = 0;
            }
            cov[i] = 0;
        }
        if(tag[i]) {
            seg[i] += tag[i] * (R - L + 1);
            if(L < R) {
                tag[cl(i)] += tag[i];
                tag[cr(i)] += tag[i];
            }
            tag[i] = 0;
        }
    }
    void pull(int i, int L, int R) {
        if(L >= R) return;
        int mid = L + R >> 1;
        push(cl(i), L, mid);
        push(cr(i), mid + 1, R);
        seg[i] = seg[cl(i)] + seg[cr(i)];
    }
    void build(vector<int>& arr, int i = 1, int L = 1,
        int R = -1) {
        if(R == -1) R = n;
        if(L == R) return void(seg[i] = arr[L]);
        int mid = L + R >> 1;
        build(arr, cl(i), L, mid);
        build(arr, cr(i), mid + 1, R);
        pull(i, L, R);
    }
    int query(int rL, int rR, int i = 1, int L = 1, int
        R = -1) {
        if(R == -1) R = n;
        push(i, L, R);
        if(rL <= L && R <= rR) return seg[i];
        int mid = L + R >> 1, ret = 0;
        if(rL <= mid) ret += query(rL, rR, cl(i), L,
            mid);
        if(mid < rR) ret += query(rL, rR, cr(i), mid +
            1, R);
        return ret;
    }
    void update(int rL, int rR, int val, int i = 1, int
        L = 1, int R = -1) {
        if(R == -1) R = n;
        push(i, L, R);
        if(rL <= L && R <= rR) return void(tag[i] = val
            );
        int mid = L + R >> 1;
        if(rL <= mid) update(rL, rR, val, cl(i), L, mid
            );
        if(mid < rR) update(rL, rR, val, cr(i), mid +
            1, R);
        pull(i, L, R);
    }
    void cover(int rL, int rR, int val, int i = 1, int
        L = 1, int R = -1) {
        if(R == -1) R = n;
        push(i, L, R);
        if(rL <= L && R <= rR) return void(cov[i] = val
            );
        int mid = L + R >> 1;
        if(rL <= mid) cover(rL, rR, val, cl(i), L, mid
            );
        if(mid < rR) cover(rL, rR, val, cr(i), mid +
            1, R);
        pull(i, L, R);
    }
};
```

```
};
/* Test Case:
4
1 2 3 4
5
2 1 3
1 1 3 1
2 1 3
1 1 4 1
2 1 4
*/
```

7.2 持久化 SMT

```
struct node{
    node *l, *r;
    int val;
};

vector<node*> ver;
int arr[MXN] = {0};

//0-base
struct SegmentTree{
    int n;
    node *root;
    void build(int _n){
        n = _n;
        root = build(0, n-1);
    }
    node* build(int L, int R){
        node *x = new node();
        if(L == R){ x->val = arr[L]; return x;}
        int mid = (L+R)/2;
        x->l = build(L, mid);
        x->r = build(mid + 1, R);
        x->val = x->l->val + x->r->val;
        return x;
    }
    int query(node *ro, int L, int R){return query(ro, 0,
        n-1, L, R);}
    int query(int L, int R){return query(root, 0, n-1, L,
        R);}
    int query(node *x, int L, int R, int recL, int recR){
        if(recL <= L && R <= recR) return x->val;
        int mid = (L+R)/2, res = 0;
        if(recL <= mid) res += query(x->l, L, mid, recL,
            recR);
        if(mid < recR) res += query(x->r, mid+1, R, recL,
            recR);
        return res;
    }
    void update(int pos, int v){update(root, 0, n-1, pos,
        v);}
    void update(node *x, int L, int R, int pos, int v){
        if(L == R){ x->val = v; arr[L] = v; return;}
        int mid = (L+R)/2;
        if(pos <= mid) update(x->l, L, mid, pos, v);
        else update(x->r, mid+1, R, pos, v);
        x->val = x->l->val + x->r->val;
    }
    node *update_ver(node *pre, int l, int r, int pos,
        int v){
        node *x = new node(); //當前位置建立新節點
        if(l == r){
            x->val = v;
            return x;
        }
        int mid = (l+r)>>1;
        if(pos <= mid){ //更新左邊
            x->l = update_ver(pre->l, l, mid, pos, v); //左邊
            節點連向新節點
            x->r = pre->r; //右邊連到原本的右邊
        }
        else{ //更新右邊
            x->l = pre->l; //左邊連到原本的左邊
            x->r = update_ver(pre->r, mid+1, r, pos, v); //
            右邊節點連向新節點
        }
    }
};
```

```

    x->val = x->l->val + x->r->val;
    return x;
} } seg;

void add_ver(int x,int v){ //修改位置 x 的值为 v
    ver.push_back(seg.update_ver(ver.back(), 0, seg.n
        -1, x, v));
}

```

7.3 持久化並查集

```

struct DSU {
    int n;
    vector<int> fa, sz;
    vector<tuple<int, int, int, int>> ver;
    DSU(int _n): n(_n), fa(n), sz(n, 1) {
        iota(fa.begin(), fa.end(), 0);
    }
    int find(int x) {
        return fa[x] == x ? x : find(fa[x]);
    }
    void merge(int x, int y) {
        x = find(x), y = find(y);
        if(sz[x] < sz[y]) swap(x, y);
        ver.push_back({x, sz[x], y, fa[y]});
        if(x == y) return;
        sz[x] += sz[y];
        fa[y] = x;
    }
    void undo() {
        if(ver.empty()) return;
        auto [x, szx, y, fy] = ver.back();
        ver.pop_back();
        sz[x] = szx;
        fa[y] = fy;
    }
};

```

7.4 Trie

```

struct trie{
    trie *nxt[26];
    int cnt; //紀錄有多少個字串以此節點結尾
    int sz; //有多少字串的前綴包括此節點
    trie():cnt(0),sz(0){
        memset(nxt,0,sizeof(nxt));
    }
};

trie *root = new trie(); //創建新的字典樹

void insert(string& s){
    trie *now = root; // 每次從根結點出發
    for(auto i:s){
        now->sz++;
        if(now->nxt[i-'a'] == NULL){
            now->nxt[i-'a'] = new trie();
        }
        now = now->nxt[i-'a']; //走到下一個字母
    }
    now->cnt++; now->sz++;
}

int query_prefix(string& s){ //查詢有多少前綴為 s
    trie *now = root; // 每次從根結點出發
    for(auto i:s){
        if(now->nxt[i-'a'] == NULL){
            return 0;
        }
        now = now->nxt[i-'a'];
    }
    return now->sz;
}

int query_count(string& s){ //查詢字串 s 出現次數
    trie *now = root; // 每次從根結點出發
    for(auto i:s){

```

```

        if(now->nxt[i-'a'] == NULL){
            return 0;
        }
        now = now->nxt[i-'a'];
    }
    return now->cnt;
}

```

7.5 Treap (interval reverse)

```

//拆出[a,b]區間就如同下面所展示先使用splitByTh()拆出
//左右,再把左區間拆成l, m最後merge()回去
//反轉區間時又記得使用^=可以直接反轉01

//treap拆區間時從後面拆是因為這樣[a,b]的關係
//不用重新考慮·要是先拆前面b的位置會變成b-a+1
//0-base
//splitByTh(root,a-1,l,m);
//splitByTh(m,b-a+1,m,r);

mt19937 gen(chrono::steady_clock::now().
    time_since_epoch().count());
struct Treap {
    int key, pri, sz, tag, sum;
    Treap *L, *R;
    Treap( int val ) {
        sum=key=val, pri=gen(), sz=1, tag=0;
        L=R=NULL;
    };
    int Size( Treap *a ) { return !a?0:a->sz; }
    void pull( Treap *a ) {
        a->sz=Size(a->L)+Size(a->R)+1;
        a->sum=a->key;
        if( a->L ) a->sum+=a->L->sum;
        if( a->R ) a->sum+=a->R->sum;
    }
    void push( Treap *a ) {
        if( a && a->tag ) {
            swap(a->L,a->R);
            if( a->L ) a->L->tag^=1;
            if( a->R ) a->R->tag^=1;
            a->tag=0;
        }
    }
    Treap *merge(Treap *a, Treap *b) {
        if( !a || !b ) return a?b;
        push(a), push(b);
        if( a->pri > b->pri ) {
            a->R=merge(a->R,b);
            pull(a); return a;
        }
        b->L=merge(a,b->L);
        pull(b); return b;
    }
    void print(Treap *a) {
        if( !a ) return;
        push(a);
        print(a->L);
        cout.put(a->key);
        print(a->R);
    }
    Treap *buildTreap( int n, string& str ) {
        Treap *root=NULL;
        for( int i=0 ; i < n ; i++ )
            root=merge(root,new Treap(str[i]));
        return root;
    }
    void splitbyk( Treap *x, int k, Treap *&a, Treap *&b )
    {
        if(!x) a=b=NULL;
        else if( x->key <= k ) {
            a=x;
            splitbyk(x->R,k,a->R,b);
            pull(a);
        }
        else {
            b=x;
            splitbyk(x->L,k,a,b->L);
            pull(b);
        }
    }
}

```

```

void splitByTh( Treap *x, int k, Treap *&a, Treap *&b )
{
    if( !x ) { a=b=NULL; return; }
    push(x);
    if( Size(x->L)+1 <= k ) {
        a=x;
        splitByTh(x->R,k-Size(x->L)-1,a->R,b);
        pull(a);
    }
    else {
        b=x;
        splitByTh(x->L,k,a,b->L);
        pull(b);
    }
}

signed main() {
    string str;
    int n, m;
    cin>>n>>m>>str;
    Treap *root;
    root=buildTreap(n,str);
    for( int i=0 ; i < m ; i++ ) {
        int a, b;
        cin>>a>>b;
        Treap *l, *m, *r;
        splitByTh(root,b,l,r);
        splitByTh(l,a-1,l,m);
        m->tag^=1;
        root=merge(l,merge(m,r));
    }
    print(root);
}

```

7.6 BIT

```

#define lowbit(x) (x&-x)
struct BIT {
    int n;
    vector<int> bit;
    BIT(int _n):n(_n), bit(_n + 1), C(_n + 1) {}
    void update(int x, int val) {
        for(; x <= n; x += lowbit(x)) bit[x] += val;
    }
    void update(int L, int R, int val) {
        update(L, val), update(R + 1, -val);
    }
    int query(int x) {
        int res = 0;
        for(; x; x -= lowbit(x)) res += bit[x];
        return res;
    }
    int query(int L, int R) {
        return query(R) - query(L - 1);
    }
    int getMax(int l, int r) {
        int ans = 0;
        while(l <= r) {
            ans = max(ans, bit[r--]);
            for (; l <= r - lowbit(r); r -= lowbit(r))
                ans = max(ans, C[r]);
        }
        return ans;
    }
    int kth(int k) {
        int sum = 0, x = 0;
        for (int i = __lg(n); ~i; i--) {
            x += 1 << i;
            if (x >= n || sum + bit[x] >= k) x -= 1 << i;
            else sum += bit[x];
        }
        return x + 1;
    }
};

```

7.7 Black Magic

```

#include <bits/extc++.h>
using namespace __gnu_pbds;
typedef tree<int,null_type,less<int>,rb_tree_tag,
tree_order_statistics_node_update> set_t;
typedef tree<int,null_type,less_equal<int>,rb_tree_tag,
tree_order_statistics_node_update> mt_t;
#include <ext/pb_ds/assoc_container.hpp>
typedef cc_hash_table<int,int> umap_t;
// gp_hash_table<int, int>
typedef priority_queue<int> heap;
#include<ext/rope>
using namespace __gnu_cxx;
int main(){
    // Insert some entries into s.
    set_t s; s.insert(12); s.insert(505);
    // The order of the keys should be: 12, 505.
    assert(*s.find_by_order(0) == 12);
    assert(*s.find_by_order(3) == 505);
    // The order of the keys should be: 12, 505.
    assert(s.order_of_key(12) == 0);
    assert(s.order_of_key(505) == 1);
    // Erase an entry.
    s.erase(12);
    // The order of the keys should be: 505.
    assert(*s.find_by_order(0) == 505);
    // The order of the keys should be: 505.
    assert(s.order_of_key(505) == 0);
    // if we want to delete less_equal tag tree
    mt_t.erase(mt_t.find_by_order(mt_t.order_of_key(val))
    );

    heap h1 , h2; h1.join( h2 );

    rope<char> r[ 2 ];
    r[ 1 ] = r[ 0 ]; // persistenet
    string t = "abc";
    r[ 1 ].insert( 0 , t.c_str() );
    r[ 1 ].erase( 1 , 1 );
    cout << r[ 1 ].substr( 0 , 2 );
}

```

8 Others

8.1 SOS dp

```

for(int i = 0; i<(1<<N); ++i)
    F[i] = A[i];
for(int i = 0; i < N; ++i) for(int mask = 0; mask < (1<<N); ++mask){
    if(mask & (1<<i))
        F[mask] += F[mask^(1<<i)];
}

```

8.2 De Bruijn sequence

```

// return cyclic array of length k^n such that every
// array of length n using 0~k-1 appears as a subarray.
vector<int> DeBruijn(int k,int n){
    if(k==1) return {0};
    vector<int> aux(k*n),res;
    function<void(int,int)> f=[&](int t,int p)->void{
        if(t>n){ if(n%p==0)
            for(int i=1;i<=p;++i) res.push_back(aux[i]);
        }else{
            aux[t]=aux[t-p]; f(t+1,p);
            for(aux[t]=aux[t-p]+1;aux[t]<k;++aux[t]) f(t+1,t)
                ;
        }
    };
    f(1,1); return res;
}

```

8.3 CDQ 分治

```

//cdq分治使用的結構u, v, w為排序物的三個維度
//ans記錄了有幾項三維都小於等於自己
//cnt記錄了相同物有幾個，在使用cdq之前必先去重，
//並且將相同元素紀錄至cnt中，可使用map來做到這步
//cdq使用的BIT就是普通求和的BIT，大小就開維度的
//值域範圍，若值域大於2e6則要先進行離散化
struct triple {int u, v, w, ans, cnt;};
BIT *bt;
void cdq(int L, int R, vector<triple>& arr) {
    if(R - L <= 1) return;
    int mid = L + R >> 1;
    vector<triple> temp;
    cdq(L, mid, arr), cdq(mid, R, arr);
    for(int i = L, j = mid; i < mid || j < R; ) {
        for(; i < mid && (j >= R || arr[i].v <= arr[j].v); i++) {
            bt->update(arr[i].w, arr[i].cnt);
            temp.push_back(arr[i]);
        }
        if(j < R) {
            arr[j].ans += bt->query(arr[j].w);
            temp.push_back(arr[j]);
            j++;
        }
    }
    for(int i = L; i < mid; i++)
        bt->update(arr[i].w, -arr[i].cnt);
    copy(temp.begin(), temp.end(), arr.begin() + L);
}
signed main()
{
    // n 個數 k 值域範圍
    int n, k;
    cin >> n >> k;
    map<tuple<int, int, int>, int> mp;
    vector<int> res(n, 0);
    vector<triple> arr;
    bt = new BIT(k + 1);
    for(int i = 0; i < n; i++) {
        int x, y, z;
        cin >> x >> y >> z;
        mp[{x, y, z}]++;
    }
    for(auto t : mp)
        arr.push_back({get<0>(t.first), get<1>(t.first),
            get<2>(t.first), 0, t.second});
    cdq(0, arr.size(), arr);
    for(auto &[x,y,z,a,b] : arr) res[a + b - 1] += b;
    for(int i : res) cout << i << '\n';
}

```

8.4 3D LIS

```

#define lowbit(x) (x&-x)
const int MAXN=1e5+5;
struct BIT {
    int n;
    vector<int> bit;
    BIT(int _n):n(_n), bit(_n+1,0) {}
    int query(int x) {
        int res=0;
        for(; x > 0; x-=lowbit(x)) res=max(res,bit[x]);
        return res;
    }
    void update(int x, int val) {
        for(; x <= n; x+=lowbit(x)) {
            if(val < 0) bit[x]=0;
            else bit[x]=max(bit[x],val);
        }
    }
}bt(MAXN);
struct triple {
    int u, v, w, ans, cnt;
    bool operator<(triple b) {return u<b.u;}
};
bool cmp(triple a, triple b) {return a.v<b.v;}
void cdq(int L, int R, vector<triple>& arr) {
    if(R-L <= 1) return;
    int mid=L+R>>1;

```

```

    cdq(L,mid,arr);
    sort(arr.begin()+L,arr.begin()+mid,cmp);
    sort(arr.begin()+mid,arr.begin()+R,cmp);
    for(int i=L, j=mid; i < mid || j < R; ) {
        for(; i < mid && (j >= R || arr[i].v < arr[j].v) ; i++) bt.update(arr[i].w,arr[i].ans);
        if(j < R) {
            arr[j].ans=max(bt.query(arr[j].w-1)+1,arr[j].ans);
            j++;
        }
    }
    for(int i=L; i < mid; i++) bt.update(arr[i].w,-1);
    sort(arr.begin()+L,arr.begin()+R);
    cdq(mid,R,arr);
}
signed main()
{
    ios_base::sync_with_stdio(0); cin.tie(0); cout.tie(0);
    int n, res=0;
    cin>>n;
    vector<int> ls;
    vector<triple> arr;
    for(int i=0; i < n; i++) {
        int a, b;
        cin>>a>>b;
        arr.push_back({i,a,b,1,1}); //{第一維,第二維,第三維,
            //答案,數量}
        ls.push_back(b);
    }
    sort(ls.begin(),ls.end());
    ls.resize(unique(ls.begin(),ls.end())-ls.begin());
    for(auto &t : arr) t.w=lower_bound(ls.begin(),ls.end(),t.w)-ls.begin()+1;
    n=arr.size();
    cdq(0,n,arr);
    for(int i=0; i < n; i++) res=max(res,arr[i].ans);
    cout<<res<<'\n';
}

```

8.5 Ternary Search

```

while(L <= R) {
    int ml = L + (R - L) / 3, mr = R - (R - L) / 3;
    if(L == R) return L;
    else if(checker(ml) < checker(mr)) L = ml + 1;
    else R = mr - 1;
}

```

8.6 Max Subrectangle

```

const int N = 1e5+5;
int n, a[N], l[N], r[N];
long long ans;
int main() {
    while(cin>>n) {
        ans = 0;
        for(int i = 1; i <= n; i++) cin>>a[i], l[i] = r[i] = i;
        for(int i = 1; i <= n; i++)
            while(l[i] > 1 && a[i] <= a[l[i] - 1]) l[i] = l[l[i] - 1];
        for(int i = n; i >= 1; i--)
            while(r[i] < n && a[i] <= a[r[i] + 1]) r[i] = r[r[i] + 1];
        for(int i = 1; i <= n; i++)
            ans = max(ans, (long long)(r[i] - l[i] + 1) * a[i]);
        cout<<ans<<'\n';
    }
}

```

8.7 Maximal Rectangle


```

const int MXN = 300;
int maximalRectangle(vector<vector<char>>& matrix) {
    int a[MXN][], l[MXN][], r[MXN][];
    int n = matrix.size(), m = matrix[0].size(), ans = 0;
    for(int i = 1; i <= n; i++) {
        for(int j = 1; j <= m; j++) l[j] = r[j] = j;
        char c;
        for(int j = 1; j <= m; j++) { //對每一個直行做統計，若是上一個a[j]也是1則會變成2
            c = matrix[i - 1][j - 1];
            if (c == '1') a[j]++;
            else if (c == '0') a[j] = 0;
        }
        for(int j = 1; j <= m; j++) while(l[j] != 1 && a[l[j] - 1] >= a[j]) l[j] = l[l[j] - 1];
        for(int j = m; j >= 1; j--) while(r[j] != m && a[r[j] + 1] >= a[j]) r[j] = r[r[j] + 1];
        for(int j = 1; j <= m; j++) ans = max(ans, (r[j] - l[j] + 1) * a[j]);
    }
    return ans;
}

```

8.8 p-Median

```

for(int i = 1; i <= n; i++) {
    for(int j = i; j <= n; j++) {
        dis[i][j] = 0;
        for(int k = i; k <= j; k++) dis[i][j] += abs(arr[k] - arr[i + j >> 1]);
        if(i == 1) dp[i][j] = dis[i][j];
    }
}
for(int i = 2; i <= p; i++) {
    for(int j = i; j <= n; j++) {
        dp[i][j] = INF;
        for(int k = i; k <= j; k++) {
            if(dp[i][j] > dp[i - 1][k - 1] + dis[k][j]) {
                dp[i][j] = dp[i - 1][k - 1] + dis[k][j];
                fa[i][j] = k - 1;
            }
        }
    }
}

```

8.9 Tree Knapsack

```

int dfs(int u) {
    int p = 1;
    dp[u][1] = s[u];
    for (int v : edge[u]) {
        int siz = dfs(v);
        for (int i = min(p, m + 1); i; i--)
            for (int j = 1; j <= siz && i + j <= m + 1; j++)
                dp[u][i + j] = max(dp[u][i + j], dp[u][i] + dp[v][j]);
        p += siz;
    }
    return p;
}

```

8.10 質數個數

- 10^2 內有 25 個質數
- 10^3 內有 168 個質數
- 10^4 內有 1229 個質數
- 10^5 內有 9592 個質數
- 10^6 內有 78498 個質數
- 10^7 內有 664579 個質數
- 10^8 內有 5761455 個質數
- 10^9 內有 50847534 個質數

- 10^{12} 內有 37607912018 個質數
- 10^{18} 內有 24739954287740860 個質數

8.11 AC-Automaton

```

// use AC.init();
// need to AC.make_fail(); before AC.query(s);
int ans[MXN] = {0};
struct ACautomata{
    struct Node{
        int cnt,i;
        Node *go[26], *fail, *dic;
        Node (){
            cnt = 0; fail = 0; dic = 0; i = 0;
            memset(go,0,sizeof(go));
        }
    }pool[1048576],*root;
    int nMem,n_pattern;
    Node* new_Node(){
        pool[nMem] = Node();
        return &pool[nMem++];
    }
    void init() {
        nMem=0;root=new_Node();n_pattern=0;
        add("");
    }
    void add(const string &str) { insert(root,str,0); }
    void insert(Node *cur, const string &str, int pos){
        for(int i=pos;i<str.size();i++){
            if(!cur->go[str[i]-'a'])
                cur->go[str[i]-'a'] = new_Node();
            cur=cur->go[str[i]-'a'];
        }
        cur->cnt++; cur->i=n_pattern++;
    }
    void make_fail(){
        queue<Node*> que;
        que.push(root);
        while (!que.empty()){
            Node* fr=que.front(); que.pop();
            for (int i=0; i<26; i++){
                if (fr->go[i]){
                    Node *ptr = fr->fail;
                    while (ptr && !ptr->go[i]) ptr = ptr->fail;
                    fr->go[i]->fail=ptr=(ptr?ptr->go[i]:root);
                    fr->go[i]->dic=(ptr->cnt?ptr:ptr->dic);
                    que.push(fr->go[i]);
                }
            }
        }
    }
    void query(string s){
        Node *cur=root;
        for(int i=0;i<(int)s.size();i++){
            while(cur&&!cur->go[s[i]-'a']) cur=cur->fail;
            cur=(cur?cur->go[s[i]-'a']:root);
            if(cur->i>=0) {
                //if(!ans[cur->i]) ans[cur->i] = i+1;
                ans[cur->i]++;
            }
            for(Node *tmp=cur->dic;tmp;tmp=tmp->dic){
                ans[tmp->i]++;
                //if(!ans[tmp->i]) ans[tmp->i] = i+1;
            }
        }
    }
}AC;

```

