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Basic

4

1.1 default code

```
#pragma GCC optimize("03,unroll-loops")
#pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt")
#include <bits/stdc++.h>
using namespace std;
ios_base::sync_with_stdio(0); cin.tie(0); cout.tie(0);
1.2
       .vimrc
```

```
set nu rnu ts=4 sw=4 bs=2 ai hls cin mouse=a
color default
sy on
inoremap {<CR> {<CR>}<C-o>0
inoremap jk <Esc>
nnoremap J 5j
nnoremap K 5k
nnoremap run :w<bar>!g++ -std=c++14 -DLOCAL -Wfatal-
errors -o test "%" && echo "done." && time ./test
```

1.3 Increase Stack Size (linux)

```
#include <sys/resource.h>
 void increase_stack_size() {
  const rlim_t ks = 64*1024*1024;
   struct rlimit rl;
   int res=getrlimit(RLIMIT_STACK, &rl);
   if(res==0){
     if(rl.rlim_cur<ks){</pre>
       rl.rlim_cur=ks;
       res=setrlimit(RLIMIT_STACK, &rl);
} } }
```

1.4 Misc

```
編譯參數: -std=c++14 -Wall -Wshadow (-fsanitize=
   undefined)
mt19937 gen(chrono::steady_clock::now().
    time_since_epoch().count());
int randint(int lb, int ub)
{ return uniform_int_distribution<int>(lb, ub)(gen); }
#define SECs ((double)clock() / CLOCKS_PER_SEC)
struct KeyHasher {
 size_t operator()(const Key& k) const {
   return k.first + k.second * 100000;
} };
typedef unordered_map<Key,int,KeyHasher> map_t;
__builtin_popcountll
                       // 二進位有幾個1
__builtin_clzll
                       // 左起第一個1之前0的個數
                      // 1的個數的奇偶性
__builtin_parityll
__builtin_mul_overflow(a,b,&h) // a*b是否溢位
```

1.5 check

```
for ((i=0;;i++))
do
    echo "$i"
    python3 gen.py > input
    ./ac < input > ac.out
    ./wa < input > wa.out
    diff ac.out wa.out || break
done
```

2 flow

2.1 ISAP

```
struct Maxflow {
  static const int MAXV = 20010;
  static const int INF = 1000000;
  struct Edge {
    int v, c, r;
    Edge(int _v, int _c, int _r):
      v(_v), c(_c), r(_r) {}
  int s, t;
vector<Edge> G[MAXV*2];
  int iter[MAXV*2], d[MAXV*2], gap[MAXV*2], tot;
  void init(int x) {
    tot = x+2;
    s = x+1, t = x+2;
    for(int i = 0; i <= tot; i++) {</pre>
      G[i].clear();
      iter[i] = d[i] = gap[i] = 0;
  } }
  void addEdge(int u, int v, int c) {
    G[u].push_back(Edge(v, c, SZ(G[v])));
    G[v].push_back(Edge(u, 0, SZ(G[u]) - 1));
  int dfs(int p, int flow) {
    if(p == t) return flow;
    for(int &i = iter[p]; i < SZ(G[p]); i++) {</pre>
      Edge &e = G[p][i];
      if(e.c > 0 \&\& d[p] == d[e.v]+1) {
        int f = dfs(e.v, min(flow, e.c));
          e.c -= f;
          G[e.v][e.r].c += f;
    if( (--gap[d[p]]) == 0) d[s] = tot;
    else {
      d[p]++;
      iter[p] = 0;
      ++gap[d[p]];
    return 0:
  int solve() {
    int res = 0;
    gap[0] = tot;
    for(res = 0; d[s] < tot; res += dfs(s, INF));
    return res;
  void reset() {
    for(int i=0;i<=tot;i++) {</pre>
      iter[i]=d[i]=gap[i]=0;
} } flow;
```

2.2 MinCostFlow

struct zkwflow{

```
static const int maxN=10000;
struct Edge{ int v,f,re; ll w;};
int n,s,t,ptr[maxN]; bool vis[maxN]; ll dis[maxN];
vector<Edge> E[maxN];
void init(int _n,int _s,int _t){
  n=_n,s=_s,t=_t;
  for(int i=0;i<n;i++) E[i].clear();</pre>
void addEdge(int u,int v,int f,ll w){
  E[u].push_back({v,f,(int)E[v].size(),w});
  E[v].push\_back({u,0,(int)}E[u].size()-1,-w});
bool SPFA(){
  fill_n(dis,n,LLONG_MAX); fill_n(vis,n,false);
  queue<int> q; q.push(s); dis[s]=0;
  while (!q.empty()){
    int u=q.front(); q.pop(); vis[u]=false;
    for(auto &it:E[ú]){
      if(it.f>0&&dis[it.v]>dis[u]+it.w){
```

```
dis[it.v]=dis[u]+it.w;
          if(!vis[it.v]){
            vis[it.v]=true; q.push(it.v);
    } } } }
    return dis[t]!=LLONG_MAX;
  int DFS(int u,int nf){
    if(u==t) return nf;
    int res=0; vis[u]=true;
    for(int &i=ptr[u];i<(int)E[u].size();i++){</pre>
      auto &it=E[u][i];
      if(it.f>0&&dis[it.v]==dis[u]+it.w&&!vis[it.v]){
        int tf=DFS(it.v,min(nf,it.f));
        res+=tf,nf-=tf,it.f-=tf;
        E[it.v][it.re].f+=tf;
        if(nf==0){ vis[u]=false; break; }
      }
    return res;
  }
  pair<int,ll> flow(){
    int flow=0; ll cost=0;
    while (SPFA()){
      fill_n(ptr,n,0)
      int f=DFS(s,INT_MAX);
      flow+=f; cost+=dis[t]*f;
    return{ flow,cost };
   // reset: do nothing
} flow;
```

2.3 Dinic

```
struct Dinic{
  struct Edge{ int v,f,re; };
  int n,s,t,level[MXN];
  vector<Edge> E[MXN];
  void init(int _n, int _s, int _t){
  n = _n;  s = _s;  t = _t;
  for (int i=0; i<n; i++) E[i].clear();</pre>
  void add_edge(int u, int v, int f){
    E[u].PB(\{v,f,SZ(E[v])\})
    E[v].PB({u,0,SZ(E[u])-1});
  bool BFS(){
    for (int i=0; i<n; i++) level[i] = -1;</pre>
    queue<int> que;
    que.push(s);
    level[s] = 0;
    while (!que.empty()){
       int u = que.front(); que.pop();
       for (auto it : E[u]){
         if (it.f > 0 && level[it.v] == -1){
           level[it.v] = level[u]+1;
           que.push(it.v);
    return level[t] != -1;
  int DFS(int u, int nf){
    if (u == t) return nf;
    int res = 0;
    for (auto &it : E[u]){
      if (it.f > 0 && level[it.v] == level[u]+1){
         int tf = DFS(it.v, min(nf,it.f));
         res += tf; nf -= tf; it.f -= tf;
         E[it.v][it.re].f += tf;
         if (nf == 0) return res;
    } }
    if (!res) level[u] = -1;
    return res;
  int flow(int res=0){
    while ( BFS() )
      res += DFS(s,2147483647);
    return res;
} }flow;
```

2.4 Kuhn Munkres 最大完美二分匹配

```
struct KM{ // max weight, for min negate the weights
  int n, mx[MXN], my[MXN], pa[MXN];
ll g[MXN][MXN], lx[MXN], ly[MXN], sy[MXN];
  bool vx[MXN], vy[MXN];
void init(int _n) { // 1-based
     for(int i=1; i<=n; i++) fill(g[i], g[i]+n+1, 0);</pre>
   void addEdge(int x, int y, ll w) \{g[x][y] = w;\}
  void augment(int y) {
     for(int x, z; y; y = z)
x=pa[y], z=mx[x], my[y]=x, mx[x]=y;
   void bfs(int st) {
     for(int i=1; i<=n; ++i) sy[i]=INF, vx[i]=vy[i]=0;</pre>
     queue<int> q; q.push(st);
     for(;;) {
        while(q.size()) {
           int x=q.front(); q.pop(); vx[x]=1;
for(int y=1; y<=n; ++y) if(!vy[y]){
    ll t = lx[x]+ly[y]-g[x][y];
</pre>
             if(t==0){
                pa[y]=x;
                if(!my[y]){augment(y);return;}
                vy[y]=1, q.push(my[y]);
             }else if(sy[y]>t) pa[y]=x,sy[y]=t;
        } }
        ll cut = INF;
        for(int y=1; y<=n; ++y)</pre>
           if(!vy[y]&&cut>sy[y]) cut=sy[y];
        for(int j=1; j<=n; ++j){
  if(vx[j]) lx[j] -= cut;
  if(vy[j]) ly[j] += cut;</pre>
           else sy[j] -= cut;
        for(int y=1; y<=n; ++y) if(!vy[y]&&sy[y]==0){
  if(!my[y]){augment(y);return;}</pre>
           vy[y]=1, q.push(my[y]);
  } } }
  11 solve(){
     fill(mx, mx+n+1, 0); fill(my, my+n+1, 0);
fill(ly, ly+n+1, 0); fill(lx, lx+n+1, -INF);
     for(int x=1; x<=n; ++x) for(int y=1; y<=n; ++y)
        lx[x] = max(lx[x], g[x][y]);
     for(int x=1; x<=n; ++x) bfs(x);</pre>
     ll ans = 0;
     for(int y=1; y<=n; ++y) ans += g[my[y]][y];
     return ans;
} }graph;
```

2.5 SW min-cut (不限 S-T 的 min-cut)

```
// global min cut
struct SW{ // O(V^3)
  int n,vst[MXN],del[MXN];
  int edge[MXN][MXN],wei[MXN];
  void init(int _n){
    n = _n; FZ(edge); FZ(del);
  }
  void addEdge(int u, int v, int w){
    edge[u][v] += w; edge[v][u] += w;
  }
  void search(int &s, int &t){
    FZ(vst); FZ(wei);
    s = t = -1;
    while (true){
        int mx=-1, cur=0;
        for (int i=0; i<n; i++)
            if (!del[i] && !vst[i] && mx<wei[i])
                  cur = i, mx = wei[i];
        if (mx == -1) break;
        vst[cur] = 1;
        s = t; t = cur;
        for (int i=0; i<n; i++)
            if (!vst[i] && !del[i]) wei[i] += edge[cur][i];
    }
}</pre>
```

```
int solve(){
   int res = 2147483647;
   for (int i=0,x,y; i<n-1; i++){
      search(x,y);
      res = min(res,wei[y]);
      del[y] = 1;
      for (int j=0; j<n; j++)
            edge[x][j] = (edge[j][x] += edge[y][j]);
   }
   return res;
} }graph;</pre>
```

2.6 Max flow with lower/upper bound

```
// flow use ISAP
// Max flow with lower/upper bound on edges
// source = 1 , sink = n
int in[ N ] , out[ N ];
 int l[M], r[M], a[M], b[M];//0-base,a下界,b
int solve(){
   flow.init(n); //n 點的數量,m 為邊的數量,點是1-
        base
   for( int i = 0 ; i < m ; i ++ ){
  in[ r[ i ] ] += a[ i ];
  out[ l[ i ] ] += a[ i ];
     flow.addEdge( l[ i ] , r[ i ] , b[ i ] - a[ i ] );
// flow from l[i] to r[i] must in [a[ i ], b[ i ]]
   int nd = 0;
   for( int i = 1 ; i <= n ; i ++ ){
  if( in[ i ] < out[ i ] ){
    flow.addEdge( i , flow.t , out[ i ] - in[ i ] );
    nd += out[ i ] - in[ i ];
}</pre>
      if( out[ i ] < in[ i ] )
        flow.addEdge( flow.s , i , in[ i ] - out[ i ] );
   // original sink to source
   flow.addEdge( n , 1 , INF );
   if( flow.maxflow() != nd )
     return -1; // no solution
   int ans = flow.G[ 1 ].back().c; // source to sink
   flow.G[1].back().c = flow.G[n].back().c = 0;
   // take out super source and super sink
   for( size_t i = 0 ; i < flow.G[ flow.s ].size() ; i</pre>
        ++ ){
     flow.G[\tilde{l}] = 0;
     Edge &e = flow.\overline{G}[flow.s][i];
     flow.G[ e.v ][ e.r ].c = 0;
   for( size_t i = 0 ; i < flow.G[ flow.t ].size() ; i</pre>
     ++ ){
flow.G[ flow.t ][ i ].c = 0;
Edge &e = flow.G[ flow.t ][ i ];
     flow.G[ e.v ][ e.r ].c = 0;
   flow.addEdge( flow.s , 1 , INF );
   flow.addEdge( n , flow.t , INF );
   flow.reset();
   return ans + flow.maxflow();
}
```

2.7 Flow Method

```
Maximize c^T x subject to Ax \leq b, x \geq 0; with the corresponding symmetric dual problem, Minimize b^T y subject to A^T y \geq c, y \geq 0.

Maximize c^T x subject to Ax \leq b; with the corresponding asymmetric dual problem, Minimize b^T y subject to A^T y = c, y \geq 0.

Minimum vertex cover on bipartite graph = Maximum matching on bipartite graph

Minimum edge cover on bipartite graph = vertex number - Minimum vertex cover(Maximum matching)
```

```
Independent set on bipartite graph =
vertex number - Minimum vertex cover(Maximum matching)
找出最小點覆蓋、做完dinic之後、從源點dfs只走還有流量的
邊,左邊沒被走到的點跟右邊被走到的點就是答案,其他點為
    最大獨立集
Maximum density subgraph ( \sum W_e + \sum W_v ) / |V|
Binary search on answer:
For a fixed D, construct a Max flow model as follow:
Let S be Sum of all weight( or inf)
1. from source to each node with cap = S
2. For each (u,v,w) in E, (u->v,cap=w), (v->u,cap=w)
where deg[v] = \sum_{i=1}^{n} e^{is_i} where deg[v] = \sum_{i=1}^{n} e^{is_i}
If maxflow < S * |V|, D is an answer.
Requiring subgraph: all vertex can be reached from
   source with
edge whose cap > 0.
```

3 Math

3.1 FFT

```
// const int MAXN = 262144;
// (must be 2^k)
// before any usage, run pre_fft() first
typedef long double ld;
typedef complex<ld> cplx; //real() ,imag()
const ld PI = acosl(-1);
const cplx I(0, 1);
cplx omega[MAXN+1];
void pre_fft(){
  for(int i=0; i<=MAXN; i++)
  omega[i] = exp(i * 2 * PI / MAXN * I);</pre>
// n must be 2^k
void fft(int n, cplx a[], bool inv=false){
  int basic = MAXN / n;
  int theta = basic;
  for (int m = n; m'>= 2; m >>= 1) {
  int mh = m >> 1;
    for (int i = 0; i < mh; i++) {
      cplx w = omega[inv ? MAXN-(i*theta%MAXN)
                             : i*theta%MAXN];
       for (int j = i; j < n; j += m) {
         int k = j + mh;
cplx x = a[j] - a[k];
         a[j] += a[k];

a[k] = w * x;
    theta = (theta * 2) % MAXN;
  int i = 0;
for (int j = 1; j < n - 1; j++) {
    for (int k = n >> 1; k > (i ^= k); k >>= 1);
    if (j < i) swap(a[i], a[j]);
  if(inv) for (i = 0; i < n; i++) a[i] /= n;
cplx arr[MAXN+1];
inline void mul(int _n,ll a[],int _m,ll b[],ll ans[]){
  int n=1, sum=_n+_m-1;
  while(n<sum)</pre>
    n < < =1;
  for(int i=0;i<n;i++) {</pre>
    double x=(i<_n?a[i]:0), y=(i<_m?b[i]:0);
    arr[i]=complex<double>(x+y,x-y);
  fft(n,arr);
  for(int i=0;i<n;i++)</pre>
    arr[i]=arr[i]*arr[i];
  fft(n,arr,true);
  for(int i=0;i<sum;i++)</pre>
```

```
4
     ans[i]=(long long int)(arr[i].real()/4+0.5);
}
3.2 O(1)mul
LL mul(LL x,LL y,LL mod){
  LL ret=x*y-(LL)((long double)x/mod*y)*mod;
  // LL ret=x*y-(LL)((long double)x*y/mod+0.5)*mod;
  return ret<0?ret+mod:ret;</pre>
        Faulhaber (\sum^n i^p)
/* faulhaber' s formula -
 * cal power sum formula of all p=1\simk in O(k^2) */
#define MAXK 2500
const int mod = 1000000007;
int b[MAXK]; // bernoulli number
int inv[MAXK+1]; // inverse
int cm[MAXK+1][MAXK+1]; // combinactories
int co[MAXK][MAXK+2]; // coeeficient of x^j when p=i
inline int getinv(int x) {
  int a=x,b=mod,a0=1,a1=0,b0=0,b1=1;
  while(b) {
     int q,t;
     q=a/b; t=b; b=a-b*q; a=t;
t=b0; b0=a0-b0*q; a0=t;
     t=b1; b1=a1-b1*q; a1=t;
  return a0<0?a0+mod:a0;</pre>
inline void pre() {
  /* combinational */
  for(int i=0;i<=MAXK;i++) {</pre>
     cm[i][0]=cm[i][i]=1;
     for(int j=1;j<i;j++)</pre>
       cm[i][j]=add(cm[i-1][j-1],cm[i-1][j]);
   /* inverse */
  for(int i=1;i<=MAXK;i++) inv[i]=getinv(i);</pre>
   /* bernoulli */
  b[0]=1; b[1]=getinv(2); // with b[1] = 1/2
for(int i=2;i<MAXK;i++) {</pre>
     if(i&1) { b[i]=0; continue; }
     b[i]=1;
     for(int j=0;j<i;j++)</pre>
       b[i]=sub(b[i],
                  mul(cm[i][j],mul(b[j], inv[i-j+1])));
  /* faulhaber */
  // sigma_x=1~n \{x^p\} = 
// 1/(p+1) * sigma_j=0~p \{C(p+1,j)*Bj*n^(p-j+1)\}
  for(int i=1;i<MAXK;i++) {</pre>
     co[i][0]=0;
     for(int j=0;j<=i;j++)
co[i][i-j+1]=mul(inv[i+1], mul(cm[i+1][j], b[j]))</pre>
  }
/* sample usage: return f(n,p) = sigma_x=1\sim (x^p) */
inline int solve(int n,int p) {
  int sol=0,m=n;
  for(int i=1;i<=p+1;i++) {</pre>
     sol=add(sol,mul(co[p][i],m));
     m = mul(m, n);
  }
  return sol;
}
```

3.4 Chinese Remainder

```
LL x[N],m[N];
LL CRT(LL x\bar{1}, LL m1, LL x2, LL m2) {
 LL g = \_\_gcd(m1, m2);
```

3.5 Miller Rabin

```
// n < 4,759,123,141
                             3: 2, 7, 61
                             4 : 2, 13, 23, 1662803
// n < 1,122,004,669,633
// n < 3,474,749,660,383
                                    6
                                     :
                                        pirmes <= 13
// n < 2^{\hat{1}}64
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
// Make sure testing integer is in range [2, n□2] if
// you want to use magic.
LL magic[]={}
bool witness(LL a, LL n, LL u, int t){
  if(!a) return 0;
  LL x=mypow(a,u,n);
  for(int i=0;i<t;i++) {</pre>
   LL nx=mul(x,x,n);
    if(nx==1&&x!=1&&x!=n-1) return 1;
   x=nx;
  return x!=1;
bool miller_rabin(LL n) {
 int s=(magic number size)
  // iterate s times of witness on n
  if(n<2) return 0;</pre>
  if(!(n\&1)) return n == 2;
 ll u=n-1; int t=0;
  // n-1 = u*2^t
 while(!(u&1)) u>>=1, t++;
 while(s--){
    LL a=magic[s]%n;
    if(witness(a,n,u,t)) return 0;
  return 1;
```

3.6 Pollard Rho

```
// does not work when n is prime O(n^(1/4))
LL f(LL x, LL mod){ return add(mul(x,x,mod),1,mod); }
LL pollard_rho(LL n) {
   if(!(n&1)) return 2;
   while(true){
      LL y=2, x=rand()%(n-1)+1, res=1;
      for(int sz=2; res==1; sz*=2) {
        for(int i=0; i<sz && res<=1; i++) {
            x = f(x, n);
            res = __gcd(abs(x-y), n);
      }
      y = x;
   }
   if (res!=0 && res!=n) return res;
} }</pre>
```

3.7 Josephus Problem

```
int josephus(int n, int m){ //n人每m次
  int ans = 0;
  for (int i=1; i<=n; ++i)
    ans = (ans + m) % i;</pre>
```

```
3.8 Matrix
```

}

return ans:

```
//矩陣乘法
for(int i = 0; i < n; i++){
     for(int j = 0; j < n; j++){
for(int k = 0; k < n; k++){
             ret[i][j] += a[i][k] * b[k][j];
     }
 //矩陣快速冪
int base[2][2] = {
                       int ans[2][2] = {
  {1, 1},
{1, 0}
                        {1, 0},
                         \{0, 1\}
};
                       };
 int mypow(int y){
  while(y){
    if( y&1 ) { ans = mul(ans, base); } //實作矩陣乘法
     base = mul(base, base);//實作矩陣乘法
    y >>= 1;
   return ans[0][0];
}
```

3.9 Gaussian Elimination

```
const int GAUSS_MOD = 100000007LL;
struct GAUSS{
  int n;
  vector<vector<int>> v;
  int ppow(int a , int k){
    if(k == 0) return 1;
    if(k \% 2 == 0) return ppow(a * a % GAUSS_MOD , k >>
         1);
    if(k \% 2 == 1) return ppow(a * a % GAUSS_MOD , k >>
          1) * a % GAUSS_MOD;
  vector<int> solve(){
    vector<int> ans(n);
    REP(now, 0, n){
      REP(i , now , n) if(v[now][now] == 0 && v[i][now]
           (0 =!
      swap(v[i] , v[now]); // det = -det;
if(v[now][now] == 0) return ans;
      REP(j, now, n + 1) (v[i][j] += GAUSS\_MOD -
             tmp * v[now][j] % GAUSS_MOD) %= GAUSS_MOD;
      }
    REP(i , 0 , n) ans[i] = v[i][n + 1] * ppow(v[i][i]
      , GAUSS_MOD - 2) % GAUSS_MOD;
    return ans;
  // gs.v.clear() , gs.v.resize(n , vector<int>(n + 1 ,
        0));
} gs;
```

3.10 ax+by=gcd

```
PII gcd(int a, int b){
  if(b == 0) return {1, 0};
  PII q = gcd(b, a % b);
  return {q.second, q.first - q.second * (a / b)};
}
```

3.11 Discrete sqrt

3.12 Prefix Inverse

```
void solve( int m ){
  inv[ 1 ] = 1;
  for( int i = 2 ; i < m ; i ++ )
    inv[ i ] = ((LL)(m - m / i) * inv[m % i]) % m;
}</pre>
```

3.13 Roots of Polynomial 找多項式的根

```
const double eps = 1e-12;
const double inf = 1e+12;
double a[ 10 ], x[ 10 ]; // a[0..n](coef) must be
    filled
int n; // degree of polynomial must be filled
int sign( double x ){return (x < -eps)?(-1):(x>eps);}
double f(double a[], int n, double x){
  double tmp=1,sum=0;
  for(int i=0;i<=n;i++)</pre>
  { sum=sum+a[i]*tmp; tmp=tmp*x; }
  return sum;
double binary(double l,double r,double a[],int n){
  int sl=sign(f(a,n,l)),sr=sign(f(a,n,r));
  if(sl==0) return l; if(sr==0) return r;
  if(sl*sr>0) return inf;
  while(r-l>eps){
    double mid=(l+r)/2;
    int ss=sign(f(a,n,mid));
if(ss==0) return mid;
    if(ss*sl>0) l=mid; else r=mid;
  }
  return l;
void solve(int n,double a[],double x[],int &nx){
   if(n==1){ x[1]=-a[0]/a[1]; nx=1; return; }
  double da[10], dx[10]; int ndx;
  for(int i=n;i>=1;i--) da[i-1]=a[i]*i;
  solve(n-1,da,dx,ndx);
  nx=0;
  if(ndx==0){
    double tmp=binary(-inf,inf,a,n);
    if (tmp<inf) x[++nx]=tmp;</pre>
    return;
  double tmp;
  tmp=binary(-inf,dx[1],a,n);
  if(tmp<inf) x[++nx]=tmp;
for(int i=1;i<=ndx-1;i++){</pre>
```

```
tmp=binary(dx[i],dx[i+1],a,n);
  if(tmp<inf) x[++nx]=tmp;
}
tmp=binary(dx[ndx],inf,a,n);
  if(tmp<inf) x[++nx]=tmp;
} // roots are stored in x[1..nx]</pre>
```

3.14 Combination thearom

```
const ll mod = 1e9 + 7;
ll fac[(int)2e6 + 1], inv[(int)2e6 + 1];
ll getinv(ll a){ return qpow(a, mod-2); }
void init(int n){
  fac[0] = 1;
  for(int i = 1; i <= n; i++){
    fac[i] = fac[i-1] * i % mod;
  }
  inv[n] = getinv(fac[n]);
  for(int i = n - 1; i >= 0; i--){
    inv[i] = inv[i + 1] * (i + 1) % mod;
  }
}
ll C(int n, int m){
  if(m > n) return 0;
  return fac[n] * inv[m] % mod * inv[n-m] % mod;
}
```

3.15 Primes

```
/* 12721, 13331, 14341, 75577, 123457, 222557, 556679
* 999983, 1097774749, 1076767633, 100102021, 999997771
* 1001010013, 1000512343, 987654361, 999991231
* 999888733, 98789101, 987777733, 999991921, 1010101333
* 1010102101, 1000000000039, 100000000000037
* 2305843009213693951, 4611686018427387847
* 9223372036854775783, 18446744073709551557 */
int mu[N], p_tbl[N];
vector<int> primes;
void sieve() {
   mu[1] = p_tbl[1] = 1;
   for( int i = 2 ; i < N ; i ++ ){
     if( !p_tbl[ i ] ){
   p_tbl[ i ] = i;
        primes.push_back( i );
        mu[i] = -1;
     for( int p : primes ){
  int x = i * p;
        if( x >= M ) break;
        p_tbl[ x ] = p;
mu[ x ] = -mu[ i ];
if( i % p == 0 ){
          mu[x] = 0;
          break;
} } } }
vector<int> factor( int x ){
   vector<int> fac{ 1 };
   while (x > 1)
     int fn = SZ(fac), p = p_tbl[ x ], pos = 0;
     while( x \% p == 0){
        for( int i = 0 ; i < fn ; i ++ )
fac.PB( fac[ pos ++ ] * p );
   } }
   return fac;
}
```

3.16 Phi

```
if(a>1) res=res/a*(a-1);
   return res;
3.17
            Result
   • Lucas' Theorem :
       For n,m\in\mathbb{Z}^* and prime P, C(m,n)\mod P=\Pi(C(m_i,n_i)) where
       m_i is the i-th digit of m in base P.
   • Stirling approximation :
      n! \approx \sqrt{2\pi n} (\frac{n}{\epsilon})^n e^{\frac{1}{12n}}
   • Stirling Numbers(permutation |P|=n with k cycles):
      S(n,k) = \text{coefficient of } x^k \text{ in } \prod_{i=0}^{n-1} (x+i)
   • Stirling Numbers(Partition n elements into k non-empty set):
      S(n,k) = \frac{1}{k!} \sum_{j=0}^{k} (-1)^{k-j} {k \choose j} j^n
   • Pick' s Theorem : A = i + b/2 - 1
      A: Area i: grid number in the inner b: grid number on the side
   • Catalan number : C_n = \binom{2n}{n}/(n+1) C_n^{n+m} - C_{n+1}^{n+m} = (m+n)! \frac{n-m+1}{n+1} for n \geq m C_n = \frac{1}{n+1} \binom{2n}{n} = \frac{(2n)!}{(n+1)!n!}
      C_0 = 1 and C_{n+1} = 2(\frac{2n+1}{n+2})C_n

C_0 = 1 and C_{n+1} = \sum_{i=0}^{n} C_i C_{n-i} for n \ge 0
   • Euler Characteristic:
      planar graph: V-E+F-C=1 convex polyhedron: V-E+F=2
       V,E,F,C: number of vertices, edges, faces(regions), and compo-
   • Kirchhoff's theorem : A_{ii}=deg(i), A_{ij}=(i,j)\in E ?-1:0, Deleting any one row, one column, and cal the det(A)
   • Polya' theorem (c is number of color m is the number of cycle \};
      (\sum_{i=1}^{m} c^{\gcd(i,m)})/m
   • Burnside lemma: |X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|

    錯排公式: (n 個人中,每個人皆不再原來位置的組合數):

      dp[0] = 1; \dot{dp}[1] = 0;
      \hat{dp[i]} = (i-1) * (dp[i-1] + dp[i-2]);
   • Bell y (有 n 個人, 把他們拆組的方法總數):
      B_n = \sum_{k=0}^{n} s(n, k) (second – stirling)
       B_{n+1} = \sum_{k=0}^{n} \binom{n}{k} B_k
   • Wilson's theorem :
      (p-1)! \equiv -1 \pmod{p}
   • Fermat's little theorem :
      a^p \equiv a (mod \ p)
   • Euler's totient function:
      A^{B^C} mod p = pow(A, pow(B, C, p - 1)) mod p
   • 歐拉函數降冪公式: A^B \mod C = A^B \mod \phi(c) + \phi(c) \mod C
   • 6 的倍數:
      (a-1)^3 + (a+1)^3 + (-a)^3 + (-a)^3 = 6a
```

4 Geometry

4.1 definition

```
typedef long double ld;
const ld eps = 1e-8;
int dcmp(ld x) {
  if(abs(x) < eps) return 0;
  else return x < 0 ? -1 : 1;
}
struct Pt {
  ld x, y;
  Pt(ld _x=0, ld _y=0):x(_x), y(_y) {}
  Pt operator+(const Pt &a) const {
    return Pt(x+a.x, y+a.y); }</pre>
```

```
Pt operator-(const Pt &a) const {
    return Pt(x-a.x, y-a.y);
  Pt operator*(const ld &a) const {
    return Pt(x*a, y*a);
  Pt operator/(const ld &a) const {
    return Pt(x/a, y/a);
  ld operator*(const Pt &a) const {
    return x*a.x + y*a.y;
  ld operator^(const Pt &a) const {
    return x*a.y - y*a.x;
  bool operator<(const Pt &a) const {</pre>
    return x < a.x | | (x == a.x && y < a.y); }
    //return dcmp(x-a.x) < 0 \mid \mid (dcmp(x-a.x) == 0 \&\&
        dcmp(y-a.y) < 0); }
  bool operator==(const Pt &a) const {
    return dcmp(x-a.x) == 0 &\& dcmp(y-a.y) == 0; }
ld norm2(const Pt &a) {
  return a*a; }
ld norm(const Pt &a) {
  return sqrt(norm2(a)); }
Pt perp(const Pt &a) {
return Pt(-a.y, a.x); }
Pt rotate(const Pt &a, ld ang) {
  return Pt(a.x*cos(ang)-a.y*sin(ang), a.x*sin(ang)+a.y
       *cos(ang)); }
struct Line {
  Pt s, e, v; // start, end, end-start
  ld ang;
  Line(Pt _s=Pt(0, 0), Pt _e=Pt(0, 0)):s(_s), e(_e) { v
  = e-s; ang = atan2(v.y, v.x); }
bool operator<(const Line &L) const {
    return ang < L.ang;
} };
struct Circle {
  Pt o; ld r;
  Circle(Pt _o=Pt(0, 0), ld _r=0):o(_o), r(_r) {}
```

4.2 Intersection of 2 lines

```
Pt LLIntersect(Line a, Line b) {
  Pt p1 = a.s, p2 = a.e, q1 = b.s, q2 = b.e;
  ld f1 = (p2-p1)^(q1-p1), f2 = (p2-p1)^(p1-q2), f;
  if(dcmp(f=f1+f2) == 0)
    return dcmp(f1)?Pt(NAN,NAN):Pt(INFINITY,INFINITY);
  return q1*(f2/f) + q2*(f1/f);
}
```

4.3 halfPlaneIntersection

```
// for point or line solution, change > to >=
bool onleft(Line L, Pt p) {
  return dcmp(L.v^(p-L.s)) > 0;
  // segment should add Counterclockwise
// assume that Lines intersect
vector<Pt> HPI(vector<Line>& L) {
  sort(L.begin(), L.end()); // sort by angle
int n = L.size(), fir, las;
  Pt *p = new Pt[n];
  Line *q = new Line[n];
  q[fir=las=0] = L[0];
  for(int i = 1; i < n; i++) {
    while(fir < las && !onleft(L[i], p[las-1])) las--;</pre>
    while(fir < las && !onleft(L[i], p[fir])) fir++;</pre>
    q[++las] = L[i];
    if(dcmp(q[las].v^q[las-1].v) == 0) {
      if(onleft(q[las], L[i].s)) q[las] = L[i];
    if(fir < las) p[las-1] = LLIntersect(q[las-1], q[</pre>
         las]);
  while(fir < las && !onleft(q[fir], p[las-1])) las--;</pre>
  if(las-fir <= 1) return {};</pre>
  p[las] = LLIntersect(q[las], q[fir]);
  int m = 0;
  vector<Pt> ans(las-fir+1);
```

```
for(int i = fir ; i <= las ; i++) ans[m++] = p[i];
return ans;
```

4.4 Convex Hull

```
double cross(Pt o, Pt a, Pt b){
 return (a-o) ^ (b-o);
vector<Pt> convex_hull(vector<Pt> pt){
  sort(pt.begin(),pt.end());
  int top=0;
 vector<Pt> stk(2*pt.size());
  for (int i=0; i<(int)pt.size(); i++){</pre>
   while (top >= 2 && cross(stk[top-2],stk[top-1],pt[i
        ]) <= 0)
      top--:
   stk[top++] = pt[i];
 for (int i=pt.size()-2, t=top+1; i>=0; i--){
   while (top >= t && cross(stk[top-2],stk[top-1],pt[i
        ]) <= 0)
      top--;
   stk[top++] = pt[i];
 stk.resize(top-1);
  return stk;
```

Convex Hull trick 4.5

```
/* Given a convexhull, answer querys in O(\l N) CH should not contain identical points, the area should
be > 0, min pair(x, y) should be listed first */
double det( const Pt& p1 , const Pt& p2 )
{ return p1.X * p2.Y - p1.Y * p2.X; }
struct Conv{
  int n;
  vector<Pt> a;
  vector<Pt> upper, lower;
  Conv(vector < Pt > _a) : a(_a){}
    n = a.size();
    int ptr = 0;
    for(int i=1; i<n; ++i) if (a[ptr] < a[i]) ptr = i;</pre>
    for(int i=0; i<=ptr; ++i) lower.push_back(a[i]);
for(int i=ptr; i<n; ++i) upper.push_back(a[i]);</pre>
    upper.push_back(a[0]);
  int sign( LL x ){ // fixed when changed to double
  return x < 0 ? -1 : x > 0; }
  pair<LL,int> get_tang(vector<Pt> &conv, Pt vec){
    int l = 0, r = (int)conv.size() - 2;
    for(; l + 1 < r; ){
      int mid = (l + r) / 2
      if(sign(det(conv[mid+1]-conv[mid],vec))>0)r=mid;
      else l = mid;
    void upd_tang(const Pt &p, int id, int &i0, int &i1){
  if(det(a[i0] - p, a[id] - p) > 0) i0 = id;
    if(det(a[i1] - p, a[id] - p) < 0) i1 = id;
  void bi_search(int l, int r, Pt p, int &i0, int &i1){
    if(l == r) return;
    upd_tang(p, 1 % n, i0, i1);
    int sl=sign(det(a[l % n] - p, a[(l + 1) % n] - p));
    for(; l + 1 < r; )
      int mid = (l + r) / 2;
      int smid=sign(det(a[mid%n]-p, a[(mid+1)%n]-p));
      if (smid == sl) l = mid;
      else r = mid;
    upd_tang(p, r % n, i0, i1);
  int bi_search(Pt u, Pt v, int l, int r) {
    int sl = sign(det(v - u, a[1 % n] - u));
```

```
for( ; l + 1 < r; ) {
  int mid = (l + r) / 2;</pre>
      int smid = sign(det(v - u, a[mid % n] - u));
      if (smid == s\tilde{l}) l = mid;
      else r = mid;
    return 1 % n;
  // 1. whether a given point is inside the CH
  bool contain(Pt p)
    if (p.X < lower[0].X || p.X > lower.back().X)
         return 0;
    int id = lower_bound(lower.begin(), lower.end(), Pt
         (p.X, -INF)) - lower.begin();
    if (lower[id].X == p.X) {
      if (lower[id].Y > p.Y) return 0;
    }else if(det(lower[id-1]-p,lower[id]-p)<0)return 0;</pre>
    id = lower_bound(upper.begin(), upper.end(), Pt(p.X
          INF), greater<Pt>()) - upper.begin();
    if (upper[id].X == p.X) {
      if (upper[id].Y < p.Y) return 0;</pre>
    }else if(det(upper[id-1]-p,upper[id]-p)<0)return 0;</pre>
    return 1;
  // 2. Find 2 tang pts on CH of a given outside point
  // return true with i0, i1 as index of tangent points
  // return false if inside CH
  bool get_tang(Pt p, int &i0, int &i1) {
    if (contain(p)) return false;
    i0 = i1 = 0;
    int id = lower_bound(lower.begin(), lower.end(), p)
          lower.begin();
    bi_search(0, id, p, i0, i1);
bi_search(id, (int)lower.size(), p, i0, i1);
    id = lower_bound(upper.begin(), upper.end(), p,
         greater<Pt>()) - upper.begin();
    bi_search((int)lower.size() - 1, (int)lower.size()
         - 1 + id, p, i0, i1);
    bi_search((int)lower.size() - 1 + id, (int)lower.
         size() - 1 + (int)upper.size(), p, i0, i1);
    return true:
  // 3. Find tangent points of a given vector
  // ret the idx of vertex has max cross value with vec
  int get_tang(Pt vec){
    pair<LL, int> ret = get_tang(upper, vec);
ret.second = (ret.second+(int)lower.size()-1)%n;
    ret = max(ret, get_tang(lower, vec));
    return ret.second;
  // 4. Find intersection point of a given line
  // return 1 and intersection is on edge (i, next(i))
  // return 0 if no strictly intersection
  bool get_intersection(Pt u, Pt v, int &i0, int &i1){
   int p0 = get_tang(u - v), p1 = get_tang(v - u);
if(sign(det(v-u,a[p0]-u))*sign(det(v-u,a[p1]-u))<0){</pre>
     if (p0 > p1) swap(p0, p1);
     i0 = bi_search(u, v, p0, p1);
     i1 = bi_search(u, v, p1, p0 + n);
     return 1;
   }
   return 0;
  };
4.6 Intersection of 2 segments
```

```
int ori( const Pt& o , const Pt& a , const Pt& b ){
  LL ret = ( a - o ) ^ ( b - o );
  return (ret > 0) - (ret < 0);</pre>
// p1 == p2 || q1 == q2 need to be handled
bool banana( const Pt& p1 , const Pt& p2 , const Pt& q1 , const Pt& q2 ){

if( ( p2 - p1 ) ^ ( q2 - q1 ) ) == 0 ){ // parallel
     ((q1 - p2) * (q2 - p2)) <= 0;
```

```
return (ori( p1, p2, q1 ) * ori( p1, p2, q2 )<=0) && (ori( q1, q2, p1 ) * ori( q1, q2, p2 )<=0);
}
```

4.7 Point In Polygon

4.8 Tangent line of two circles

4.9 Minimum distance of two convex

4.10 Area of Rectangles

```
struct AreaofRectangles{
#define cl(x) (x<<1)
#define cr(x) (x<<1|1)
    ll n, id, sid;</pre>
```

```
pair<ll,ll> tree[MXN<<3];</pre>
                               // count, area
vector<ĺl> ind;
tuple<ll, ll, ll, ll> scan[MXN<<1];</pre>
void pull(int i, int l, int r){
   if(tree[i].first) tree[i].second = ind[r+1] -
         ind[l];
    else if(l != r){
         int mid = (l+r)>>1;
         tree[i].second = tree[cl(i)].second + tree[
              cr(i)].second;
    else
              tree[i].second = 0;
void upd(int i, int l, int r, int ql, int qr, int v
    if(ql \leftarrow l \& r \leftarrow qr){
         tree[i].first += v;
pull(i, l, r); return;
    int mid = (l+r) \gg 1;
    if(ql <= mid) upd(cl(i), l, mid, ql, qr, v);</pre>
    if(qr > mid) upd(cr(i), mid+1, r, ql, qr, v);
    pull(i, l, r);
void init(int _n){
    n = _n; id = sid = 0;
ind.clear(); ind.resize(n<<1);
    fill(tree, tree+(n<<2), make_pair(0, 0));</pre>
void addRectangle(int lx, int ly, int rx, int ry){
    ind[id++] = lx; ind[id++] = rx;
    scan[sid++] = make\_tuple(ly, 1, lx, rx);
    scan[sid++] = make_tuple(ry, -1, lx, rx);
ll solve(){
    sort(ind.begin(), ind.end());
    ind.resize(unique(ind.begin(), ind.end()) - ind
         .begin());
    sort(scan, scan + sid);
ll area = 0, pre = get<0>(scan[0]);
    for(int i = 0; i < sid; i++){
         auto [x, v, l, r] = scan[i];
area += tree[1].second * (x-pre);
         upd(1, 0, ind.size()-1, lower_bound(ind.
              begin(), ind.end(), l)-ind.begin(),
              lower_bound(ind.begin(),ind.end(),r)-
              ind.begin()-1, v);
         pre = x;
    return area;
}rect;
```

4.11 Min dist on Cuboid

4.12 Heart of Triangle

```
Pt inCenter( Pt &A, Pt &B, Pt &C) { // 內心 double a = norm(B-C), b = norm(C-A), c = norm(A-B); return (A * a + B * b + C * c) / (a + b + c); }

Pt circumCenter( Pt &a, Pt &b, Pt &c) { // 外心 Pt bb = b - a, cc = c - a; double db=norm2(bb), dc=norm2(cc), d=2*(bb ^ cc); return a-Pt(bb.Y*dc-cc.Y*db, cc.X*db-bb.X*dc) / d; }

Pt othroCenter( Pt &a, Pt &b, Pt &c) { // 垂心 Pt ba = b - a, ca = c - a, bc = b - c; double Y = ba.Y * ca.Y * bc.Y, A = ca.X * ba.Y - ba.X * ca.Y, x0= (Y+ca.X*ba.Y*b.X-ba.X*ca.Y*c.X) / A, y0= -ba.X * (x0 - c.X) / ba.Y + ca.Y; return Pt(x0, y0); }
```

5 Graph

5.1 DSU 並查集 & MST

```
struct DSU {// 並查集
    vector<int> fa, sz;
DSU(int n = 0) : fa(n), sz(n, 1) {
        iota(fa.begin(), fa.end(), 0);
    int Find(int x) { // 路徑壓縮
    while (x != fa[x])
           x = fa[x] = fa[fa[x]];
        return x;
    bool Merge(int x, int y) { //合併
        x = Find(x), y = Find(y);
        if (x == y) return false; // 是否為連通
        if (sz[x] > sz[y]) swap(x, y);
        fa[x] = y;
        sz[y] += sz[x];
        return true;
int MST(int n, int m, vector<tuple<int, int, int>> &edge
    sort(edge.begin(), edge.end());
    DSU dsu(n); // 初始化並查集
    int result = 0; // 最小生成樹邊權和
    for (auto &[w, u, v] : edge) if (dsu.Merge(u, v))
        result += w; //合併並統計答案
    cout << result << endl;</pre>
    return 0;
int main(){
    int n, m; //點數,邊數
    cin >> n >> m;
    vector<tuple<int, int, int>> edge(m);
for (auto &[w, u, v] : edge) cin >> u >> v >> w;
    cout << MST(n, m, edge);</pre>
```

5.2 Lowest Common Ancestor O(lgn)

```
|//詢問 O(logn)
|//先 dfs 一遍·紀錄每個點的父節點 (2^0 倍祖先)以及 time
|/然後 build 預處理
|vector<int> edge[MXN]; // 圖
|int anc[MXN + 5][__lg(MXN) + 1] = {0};
|int ti = 0;
|int time_in[MXN] = {0};
|int time_out[MXN] = {0};
|void dfs(int now, int f) {
|ti++;
|anc[now][0] = f;
```

```
time_in[now] = ti;
  for (int i : edge[now])
    dfs(i, now);
  time_out[now] = ti;
void build(){
  for (int i = 1; i <= __lg(n); ++i)
    for (int u = 0; u < n; ++u)
      anc[u][i] = anc[anc[u][i - 1]][i - 1];
bool isAncestor(int x, int y) {
  if (time_in[x] <= time_in[y] && time_out[x] >=
      time_out[y]) return true;
  return false;
int getLCA(int u, int v) {
  if (isAncestor(u, v)) return u;
if (isAncestor(v, u)) return v;
  for (int i = _-lg(n); i >= 0; --i) {
    if (!isAncestor(anc[u][i], v))
      u = anc[u][i];
  return anc[u][0];
```

5.3 Hamiltonian path $O(n^22^n)$

```
|//dp[i][j] = 目前在i節點走過{j}節點的路徑
| for(int i=1; i < (1 << (n); i++ ) {
| for(int j = 1; j < n; j++ ) {
| if(!((1 << j) & i)&&(i&1)) {
| for( int k = 0; k < n; k++ ) {
| if(j == k) continue;
| if( (1<<k)&i ) dp[j][i|(1<<j)]=
| min(dp[j][i|(1<<j)],dp[k][i]+dis[k][j]);
| }
| }
| }
| }
```

5.4 MaximumClique 最大團

```
#define N 111
struct MaxClique{ // 0-base
  typedef bitset<N> Int;
  Int linkto[N] , v[N];
  int n;
  void init(int _n){
    n = _n;
for(int i = 0 ; i < n ; i ++){</pre>
       linkto[i].reset(); v[i].reset();
  void addEdge(int a_, int b)
  \{ v[a][b] = v[b][a] = 1; \}
  int popcount(const Int& val)
  { return val.count(); }
  int lowbit(const Int& val)
  { return val._Find_first(); } int ans , stk[N]; int id[N] , di[N] , deg[N];
  Int cans;
  void maxclique(int elem_num, Int candi){
     if(elem_num > ans){
       ans = elem_num; cans.reset();
for(int i = 0; i < elem_num; i ++)</pre>
          cans[id[stk[i]]] = 1;
     int potential = elem_num + popcount(candi);
     if(potential <= ans) return;</pre>
    int pivot = lowbit(candi);
Int smaller_candi = candi & (~linkto[pivot]);
     while(smaller_candi.count() && potential > ans){
       int next = lowbit(smaller_candi);
       candi[next] = !candi[next];
       smaller_candi[next] = !smaller_candi[next];
```

```
potential --:
        if(next == pivot || (smaller_candi & linkto[next
             ]).count()){
          stk[elem_num] = next;
          maxclique(elem_num + 1, candi & linkto[next]);
  } } }
   int solve(){
     for(int i = 0; i < n; i ++){
       id[i] = i; deg[i] = v[i].count();
     sort(id , id + n , [&](int id1, int id2){
    return deg[id1] > deg[id2]; });
     for(int i = 0; i < n; i ++) di[id[i]] = i;
for(int i = 0; i < n; i ++)
for(int j = 0; j < n; j ++)
          if(v[i][j]) linkto[di[i]][di[j]] = 1;
     Int cand; cand.reset();
for(int i = 0 ; i < n ; i ++) cand[i] = 1;</pre>
     cans.reset(); cans[0] = 1;
     maxclique(0, cand);
     return ans;
} }solver;
```

5.5 MaximalClique 極大團

```
#define N 80
struct MaxClique{ // 0-base
  typedef bitset<N> Int;
  Int lnk[N], v[N];
  int n:
  void init(int _n){
    n = _n;
    for(int i = 0; i < n; i ++){
       lnk[i].reset(); v[i].reset();
  void addEdge(int a , int b)
{ v[a][b] = v[b][a] = 1; }
  int ans , stk[N], id[N] , di[N] , deg[N];
  Int cans;
  void dfs(int elem_num, Int candi, Int ex){
    if(candi.none()&ex.none()){
       cans.reset();
       for(int i = 0 ; i < elem_num ; i ++)</pre>
         cans[id[stk[i]]] = 1;
       ans = elem_num; // cans is a maximal clique
       return;
    int pivot = (candilex)._Find_first();
    Int smaller_candi = candi & (~lnk[pivot]);
    while(smaller_candi.count()){
       int nxt = smaller_candi._Find_first();
       candi[nxt] = smaller_candi[nxt] = 0;
       ex[nxt] = 1;
       stk[elem_num] = nxt;
       dfs(elem_num+1,candi&lnk[nxt],ex&lnk[nxt]);
  } }
  int solve(){
    for(int i = 0; i < n; i ++){
       id[i] = i; deg[i] = v[i].count();
    sort(id , id + n , [&](int id1, int id2){
    return deg[id1] > deg[id2]; });
for(int i = 0 ; i < n ; i ++) di[id[i]] = i;</pre>
     for(int i = 0 ; i < n ; i ++)</pre>
       for(int j = 0; j < n; j ++)
  if(v[i][j]) lnk[di[i]][di[j]] = 1;</pre>
    ans = 1; cans.reset(); cans[0] = 1;
    dfs(0, Int(string(n,'1')), 0);
     return ans;
} }solver;
```

5.6 Strongly Connected Component

```
struct Scc{
  int n, nScc, vst[MXN], bln[MXN];
  vector<int> E[MXN], rE[MXN], vec;
  void init(int _n){
```

```
n = _n;
for (int i=0; i<MXN; i++)</pre>
      E[i].clear(), rE[i].clear();
  void addEdge(int u, int v){
    E[u].PB(v); rE[v].PB(u);
  void DFS(int u){
    vst[u]=1;
    for (auto v : E[u]) if (!vst[v]) DFS(v);
    vec.PB(u);
  }
  void rDFS(int u){
    vst[u] = 1; bln[u] = nScc;
    for (auto v : rE[u]) if (!vst[v]) rDFS(v);
  void solve(){
    nScc = 0;
    vec.clear();
    FZ(vst);
    for (int i=0; i<n; i++)
      if (!vst[i]) DFS(i);
    reverse(vec.begin(),vec.end());
    FZ(vst);
    for (auto v : vec)
      if (!vst[v]){
        rDFS(v); nScc++;
  }
};
```

5.7 Maximum General graph Matching

```
// should shuffle vertices and edges
const int N=100005, E=(2e5)*2+40;
struct Graph{ // 1-based; match: i <-> lnk[i]
  int to[E],bro[E],head[N],e,lnk[N],vis[N],stp,n;
  void init(int _n){
    stp=0; e=1; n=_n;
    for(int i=1;i<=n;i++) head[i]=lnk[i]=vis[i]=0;</pre>
  void add_edge(int u,int v){
    to[e]=v,bro[e]=head[u],head[u]=e++;
    to[e]=u,bro[e]=head[v],head[v]=e++;
  bool dfs(int x){
    vis[x]=stp;
    for(int i=head[x];i;i=bro[i]){
      int v=to[i];
      if(!lnk[v]){ lnk[x]=v,lnk[v]=x; return true; }
    for(int i=head[x];i;i=bro[i]){
      int v=to[i];
      if(vis[lnk[v]]<stp){</pre>
        int w=lnk[v]; lnk[x]=v,lnk[v]=x,lnk[w]=0;
        if(dfs(w)) return true;
        lnk[w]=v, lnk[v]=w, lnk[x]=0;
      }
    return false;
  int solve(){
    int ans=0;
    for(int i=1;i<=n;i++) if(!lnk[i]) stp++,ans+=dfs(i)</pre>
    return ans:
}graph;
```

5.8 Minimum General Weighted Matching

```
struct Graph {
   // Minimum General Weighted Matching (Perfect Match)
   static const int MXN = 105;
   int n, edge[MXN][MXN];
   int match[MXN],dis[MXN],onstk[MXN];
   vector<int> stk;
   void init(int _n) {
```

```
n = _n;
for( int i = 0 ; i < n ; i ++ )</pre>
      for( int j = 0; j < n; j ++ )
edge[ i ][ j ] = 0;
  void add_edge(int u, int v, int w)
  \{ edge[u][v] = edge[v][u] = w; \}
  bool SPFA(int u){
    if (onstk[u]) return true;
    stk.PB(u);
    onstk[u] = 1;
    for (int v=0; v<n; v++){</pre>
       if (u != v && match[u] != v && !onstk[v]){
         int m = match[v];
         if (dis[m] > dis[u] - edge[v][m] + edge[u][v]){
           dis[m] = dis[u] - edge[v][m] + edge[u][v];
           onstk[v] = 1;
           stk.PB(v)
           if (SPFA(m)) return true;
           stk.pop_back();
           onstk[v] = 0;
    } } }
    onstk[u] = 0;
    stk.pop_back();
    return false;
  int solve() {
    // find a match
    for (int i=0; i<n; i+=2){
  match[i] = i+1;</pre>
      match[i+1] = i;
    while (true){
  int found = 0;
       for( int i = 0 ; i < n ; i ++ )</pre>
         onstk[i] = dis[i] = 0;
       for (int i=0; i< n; i++){
         stk.clear();
         if (!onstk[i] && SPFA(i)){
           found = 1
           while (SZ(stk)>=2){
             int u = stk.back(); stk.pop_back();
             int v = stk.back(); stk.pop_back();
             match[u] = v;
             match[v] = u;
      } } }
      if (!found) break;
    }
    int ret = 0;
    for (int i=0; i < n; i++)
      ret += edge[i][match[i]];
    ret /= 2;
    return ret;
}graph;
```

5.9 Maximum General Weighted Matching

```
struct WeightGraph {
  static const int INF = INT_MAX;
  static const int N = 514;
  struct edge{
    int u,v,w; edge(){}
    edge(int ui,int vi,int wi)
      :u(ui),v(vi),w(wi){}
  int n,n_x;
  edge g[N*2][N*2];
  int lab[N*2];
  int match[N*2],slack[N*2],st[N*2],pa[N*2];
  int flo_from[N*2][N+1],S[N*2],vis[N*2];
 vector<int> flo[N*2];
  queue<int> q;
  int e_delta(const edge &e){
    return lab[e.u]+lab[e.v]-g[e.u][e.v].w*2;
  void update_slack(int u,int x){
    if(!slack[x]||e_delta(g[u][x])<e_delta(g[slack[x]][</pre>
        x]))slack[x]=u;
 }
```

```
void set_slack(int x){
  slack[x]=0;
  for(int u=1;u<=n;++u)</pre>
    if(g[u][x].w>0&&st[u]!=x&&S[st[u]]==0)
      update_slack(u,x);
void q_push(int x){
  if(x<=n)q.push(x);</pre>
  else for(size_t i=0;i<flo[x].size();i++)</pre>
    q_push(flo[x][i]);
void set_st(int x,int b){
  st[x]=b;
  if(x>n)for(size_t i=0;i<flo[x].size();++i)</pre>
    set_st(flo[x][i],b);
int get_pr(int b,int xr){
  int pr=find(flo[b].begin(),flo[b].end(),xr)-flo[b].
      begin();
  if(pr%2==1){
    reverse(flo[b].begin()+1,flo[b].end());
    return (int)flo[b].size()-pr;
  }else return pr;
void set_match(int u,int v){
  match[u]=g[u][v].v;
  if(u<=n) return;</pre>
  edge e=g[u][v];
  int xr=flo_from[u][e.u],pr=get_pr(u,xr);
  for(int i=0;i<pr;++i)set_match(flo[u][i],flo[u][i</pre>
      ^1]);
  set_match(xr,v);
  rotate(flo[u].begin(),flo[u].begin()+pr,flo[u].end
      ());
void augment(int u,int v){
  for(;;){
    int xnv=st[match[u]];
    set_match(u,v);
    if(!xnv)return;
    set_match(xnv,st[pa[xnv]]);
    u=st[pa[xnv]],v=xnv;
} }
int get_lca(int u,int v){
  static int t=0;
  for(++t;u|v;swap(u,v)){
    if(u==0)continue
    if(vis[u]==t)return u;
    vis[u]=t;
    u=st[match[u]]
    if(u)u=st[pa[u]];
  }
  return 0;
void add_blossom(int u,int lca,int v){
  int b=n+1;
  while(b<=n_x&&st[b])++b;</pre>
  if(b>n_x)++n_x
  lab[b]=0,S[b]=0;
  match[b]=match[lca];
  flo[b].clear();
  flo[b].push_back(lca);
  for(int_x=u,y;x!=lca;x=st[pa[y]])
    flo[b].push_back(x),flo[b].push_back(y=st[match[x
        ]]),q_push(y);
  reverse(flo[b].begin()+1,flo[b].end());
  for(int x=v,y;x!=lca;x=st[pa[y]])
    flo[b].push_back(x),flo[b].push_back(y=st[match[x
        ]]),q_push(y);
  set_st(b,b);
  for(int x=1;x<=n_x;++x)g[b][x].w=g[x][b].w=0;
  for(int x=1;x<=n;++x)flo_from[b][x]=0;
  for(size_t i=0;i<flo[b].size();++i){</pre>
    int xs=flo[b][i];
    for(int x=1;x<=n_x;++x)</pre>
      if(g[b][x].w==0||e_delta(g[xs][x])< e_delta(g[b]
          T(x)
        g[b][x]=g[xs][x],g[x][b]=g[x][xs];
    for(int x=1;x<=n;++x)</pre>
      if(flo_from[xs][x])flo_from[b][x]=xs;
  set_slack(b);
```

```
memset(match+1,0,sizeof(int)*n);
void expand_blossom(int b){
                                                                int n_matches=0;
  for(size_t i=0;i<flo[b].size();++i)</pre>
    set_st(flo[b][i],flo[b][i]);
                                                                long long tot_weight=0;
  int xr=flo_from[b][g[b][pa[b]].u],pr=get_pr(b,xr);
                                                                for(int u=0;u<=n;++u)st[u]=u,flo[u].clear();</pre>
  for(int i=0;i<pr;i+=2){
                                                                int w_max=0;
    int xs=flo[b][i],xns=flo[b][i+1];
                                                                for(int u=1;u<=n;++u)</pre>
    pa[xs]=g[xns][xs].u;
                                                                  for(int v=1;v<=n;++v){</pre>
    S[xs]=1,S[xns]=0;
                                                                    flo_from[u][v]=(u==v?u:0);
    slack[xs]=0,set_slack(xns);
                                                                    w_{max}=max(w_{max},g[u][v].w);
    q_push(xns);
                                                                for(int u=1;u<=n;++u)lab[u]=w_max;</pre>
  S[xr]=1,pa[xr]=pa[b];
                                                                while(matching())++n_matches;
  for(size_t i=pr+1;i<flo[b].size();++i){</pre>
                                                                for(int u=1;u<=n;++u)</pre>
                                                                  if(match[u]&&match[u]<u)</pre>
    int xs=flo[b][i];
    S[xs]=-1, set\_slack(xs);
                                                                    tot_weight+=g[u][match[u]].w;
                                                                return make_pair(tot_weight,n_matches);
  st[b]=0;
                                                              void add_edge( int ui , int vi , int wi ){
bool on_found_edge(const edge &e){
                                                                g[ui][vi].w = g[vi][ui].w = wi;
  int u=st[e.u],v=st[e.v];
  if(S[v]==-1){
                                                              void init( int _n ){
                                                                n = _n;
for(int u=1;u<=n;++u)</pre>
    pa[v]=e.u,S[v]=1;
    int nu=st[match[v]];
    slack[v]=slack[nu]=0;
                                                                  for(int v=1;v<=n;++v)</pre>
                                                                    g[u][v]=edge(u,v,0);
    S[nu]=0,q_push(nu);
  }else if(S[v]==0){
    int lca=get_lca(u,v);
                                                           } graph;
    if(!lca)return augment(u,v),augment(v,u),true;
    else add_blossom(u,lca,v);
                                                                    BCC based on vertex
  return false;
bool matching(){
                                                            struct BccVertex {
  memset(S+1,-1,sizeof(int)*n_x);
                                                              int n,nScc,step,dfn[MXN],low[MXN];
  memset(slack+1,0,sizeof(int)*n_x);
                                                              vector<int> E[MXN],sccv[MXN];
  q=queue<int>();
                                                              int top,stk[MXN];
  for(int x=1;x<=n_x;++x)</pre>
                                                              void init(int _n) {
    if(st[x]==x\&\&!match[x])pa[x]=0,S[x]=0,q_push(x);
                                                                n = _n; nScc = step = 0;
  if(q.empty())return false;
                                                                for (int i=0; i<n; i++) E[i].clear();</pre>
  for(;;){
    while(q.size()){
                                                              void addEdge(int u, int v)
      int u=q.front();q.pop();
                                                              { E[u].PB(v); E[v].PB(u); }
      if(S[st[u]]==1)continue;
                                                              void DFS(int u, int f) {
      for(int v=1;v<=n;++v)</pre>
                                                                dfn[u] = low[u] = step++;
        if(g[u][v].w>0&&st[u]!=st[v]){
                                                                stk[top++] = u;
          if(e_delta(g[u][v])==0){
                                                                for (auto v:E[u]) {
             if(on_found_edge(g[u][v]))return true;
                                                                  if (v == f) continue;
                                                                  if (dfn[v] == -1) {
          }else update_slack(u,st[v]);
                                                                    DFS(v,u);
    int d=INF;
                                                                    low[u] = min(low[u], low[v]);
    for(int b=n+1;b<=n_x;++b)</pre>
                                                                    if (low[v] >= dfn[u]) {
      if(st[b]==b&&S[b]==1)d=min(d,lab[b]/2);
                                                                      int z;
    for(int x=1;x<=n_x;++x)</pre>
                                                                      sccv[nScc].clear();
      if(st[x]==x\&slack[x]){
                                                                      do {
        if(S[x]==-1)d=min(d,e_delta(g[slack[x]][x]));
                                                                        z = stk[--top]
        else if(S[x]==0)d=min(d,e_delta(g[slack[x]][x
                                                                        sccv[nScc].PB(z);
             ])/2);
                                                                      } while (z != v);
                                                                      sccv[nScc++].PB(u);
    for(int u=1;u<=n;++u){</pre>
      if(S[st[u]]==0){
                                                                  }else
        if(lab[u]<=d)return 0;</pre>
                                                                    low[u] = min(low[u],dfn[v]);
        lab[u]-=d;
      }else if(S[st[u]]==1)lab[u]+=d;
                                                              vector<vector<int>> solve() {
                                                                vector<vector<int>> res;
    for(int b=n+1;b<=n_x;++b)
                                                                for (int i=0; i<n; i++)</pre>
      if(st[b]==b){
                                                                  dfn[i] = low[i] = -1;
        if(S[st[b]]==0)lab[b]+=d*2;
                                                                for (int i=0; i < n; i++)
        else if(S[st[b]]==1)lab[b]-=d*2;
                                                                  if (dfn[i] == -1) {
                                                                    top = 0:
    q=queue<int>();
                                                                    DFS(i,i);
    for(int x=1;x<=n_x;++x)</pre>
      if(st[x]==x&&slack[x]&&st[slack[x]]!=x&&e_delta
                                                                REP(i,nScc) res.PB(sccv[i]);
           (g[slack[x]][x])==0)
                                                                return res;
        if(on_found_edge(g[slack[x]][x]))return true;
    for(int b=n+1;b<=n_x;++b)</pre>
                                                            }graph;
      if(st[b]==b&&S[b]==1&&lab[b]==0)expand_blossom(
          b):
  return false;
pair<long long,int> solve(){
```

5.11 Min Mean Cycle

```
/* minimum mean cycle O(VE) */
struct MMC{
#define E 101010
#define V 1021
#define inf 1e9
#define eps 1e-6
  struct Edge { int v,u; double c; };
  int n, m, prv[V][V], prve[V][V], vst[V];
  Edge e[E];
  vector<int> edgeID, cycle, rho;
  double d[V][V];
  void init( int _n )
  \{ n = _n; m = 0; \}
  // WARNING: TYPÉ matters
  void addEdge( int vi , int ui , double ci )
{ e[ m ++ ] = { vi , ui , ci }; }
  void bellman_ford() {
    for(int i=0; i<n; i++) d[0][i]=0;
for(int i=0; i<n; i++) {
  fill(d[i+1], d[i+1]+n, inf);
  fill(d[i+1], d[i+1]+n, inf);
       for(int j=0; j<m; j++) {
  int v = e[j].v, u = e[j].u;
  if(d[i][v]<inf && d[i+1][u]>d[i][v]+e[j].c) {
            d[i+1][u] = d[i][v]+e[j].c;
            prv[i+1][u] = v;
            prve[i+1][u] = j;
  double solve(){
    // returns inf if no cycle, mmc otherwise
     double mmc=inf;
     int st = -1;
     bellman_ford();
     for(int i=0; i<n; i++) {</pre>
       double avg=-inf;
       for(int k=0; k<n; k++) {</pre>
         if(d[n][i] < inf-eps) avg=max(avg,(d[n][i]-d[k][i]
              ])/(n-k));
         else avg=max(avg,inf);
       if (avg < mmc) tie(mmc, st) = tie(avg, i);</pre>
     fill(vst,0); edgeID.clear(); cycle.clear(); rho.
         clear();
     for (int i=n; !vst[st]; st=prv[i--][st]) {
       vst[st]++;
       edgeID.PB(prve[i][st]);
       rho.PB(st);
     while (vst[st] != 2) {
       if(rho.empty()) return inf;
       int v = rho.back(); rho.pop_back();
       cycle.PB(v);
       vst[v]++;
    reverse(ALL(edgeID));
     edgeID.resize(SZ(cycle));
     return mmc;
} }mmc;
```

5.12 Directed Graph Min Cost Cycle

}

```
int n, bn, bsz, hd[N];
void b_insert(LL d, int u){
  int i = d/mu;
  if(i >= bn) return;
  b[++bsz] = node(d, u, hd[i]);
  hd[i] = bsz;
void init( int _n ){
  n = _n;
  for( int i = 1 ; i <= n ; i ++ )
g[ i ].clear();</pre>
void addEdge( int ai , int bi , LL ci )
{ g[ai].push_back(edge(bi,ci)); }
LL solve(){
  fill(dp[0], dp[0]+n+1, 0);
  dp[i][g[j][k].to] =min(dp[i][g[j][k].to]
                                       dp[i-1][j]+g[j][k].w);
  mu=INF; LL bunbo=1;
  for(int i=1; i<=n; i++) if(dp[n][i] < INF){</pre>
     LL a=-INF, b=1;
     for(int j=0; j<=n-1; j++) if(dp[j][i] < INF){
   if(a*(n-j) < b*(dp[n][i]-dp[j][i])){</pre>
          a = dp[n][i]-dp[j][i];
          b = n-j;
     if(mu*b > bunbo*a)
       mu = a, bunbo = b;
  if(mu < 0) return -1; // negative cycle</pre>
  if(mu == INF) return INF; // no cycle
  if(mu == 0) return 0;
  for(int i=1; i<=n; i++)</pre>
     for(int j=0; j<(int)g[i].size(); j++)
g[i][j].w *= bunbo;</pre>
  memset(p, 0, sizeof(p));
  queue<int> q;
  for(int i=1; i<=n; i++){</pre>
     q.push(i);
     inq[i] = true;
  while(!q.empty()){
     int i=q.front(); q.pop(); inq[i]=false;
     for(int j=0; j<(int)g[i].size(); j++){
  if(p[g[i][j].to] > p[i]+g[i][j].w-mu){
          p[g[i][j].to] = p[i]+g[i][j].w-mu;
          if(!inq[g[i][j].to]){
            q.push(g[i][j].to);
            inq[g[i][j].to] = true;
  } } } }
for(int i=1; i<=n; i++) grev[i].clear();</pre>
  for(int i=1; i<=n; i++)</pre>
     for(int j=0; j<(int)g[i].size(); j++){
  g[i][j].w += p[i]-p[g[i][j].to];</pre>
       grev[g[i][j].to].push_back(edge(i, g[i][j].w));
  LL mldc = n*mu;
  for(int i=1; i<=n; i++){</pre>
    bn=mldc/mu, bsz=0;
memset(hd, 0, sizeof(hd));
fill(d+i+1, d+n+1, INF);
     b_insert(d[i]=0, i);
     for(int j=0; j<=bn-1; j++) for(int k=hd[j]; k; k=
   b[k].next){</pre>
       int u = b[k].u;
       LL du = b[k].d;
       if(du > d[u]) continue;
       for(int l=0; l<(int)g[u].size(); l++) if(g[u][l</pre>
          ].to > i){
    if(d[g[u][l].to] > du + g[u][l].w){
        d[g[u][l].to] = du + g[u][l].w;
        b_insert(d[g[u][l].to], g[u][l].to);
     } } }
     for(int j=0; j<(int)grev[i].size(); j++) if(grev[</pre>
          i][j].to > i)
       mldc=min(mldc,d[grev[i][j].to] + grev[i][j].w);
```

```
return mldc / bunbo;
|} }graph;
```

5.13 K-th Shortest Path

```
// time: O(|E| \setminus |E| + |V| \setminus |E| + K)
// memory: 0(|E| \lg |E| + |V|)
struct KSP{ // 1-base
  struct nd{
     int u, v; ll d;
     nd(int ui = 0, int vi = 0, ll di = INF)
     { u = ui; v = vi; d = di; '}
  };
  struct heap{
    nd* edge; int dep; heap* chd[4];
  static int cmp(heap* a,heap* b)
  { return a->edge->d > b->edge->d; }
  struct node{
    int v; ll d; heap* H; nd* E;
    node(){}
    node(ll _d, int _v, nd* _E)
{ d =_d; v = _v; E = _E; }
node(heap* _H, ll _d)
     {H = _H; d = _d; }
     friend bool operator<(node a, node b)
     { return a.d > b.d; }
  int n, k, s, t;
ll dst[_N ];
  nd *nxt[ N ];
  vector<nd*> g[ N ], rg[ N ];
  heap *nullNd, *head[ N ];
  void init( int _n , int _k , int _s , int _t ){
    n = _n; k = _k; s = _s; t = _t;
for( int i = 1 ; i <= n ; i ++ ){
    g[ i ].clear(); rg[ i ].clear();
    nxt[ i ] = NULL; head[ i ] = NULL;
    dst[ i ] = -1;
}</pre>
  void addEdge( int ui , int vi , ll di ){
    nd* e = new nd(ui, vi, di);
     g[ ui ].push_back( e );
     rg[ vi ].push_back( e );
  queue<int> dfsQ;
  void dijkstra(){
     while(dfsQ.size()) dfsQ.pop();
    priority_queue<node> Q;
     Q.push(node(0, t, NULL));
     while (!Q.empty()){
       node p = Q.top(); Q.pop();
if(dst[p.v] != -1) continue;
       dst[ p.v ] = p.d;
nxt[ p.v ] = p.E;
       dfsQ.push( p.v );
       for(auto e: rg[ p.v ])
         Q.push(node(p.d + e->d, e->u, e));
  heap* merge(heap* curNd, heap* newNd){
     if(curNd == nullNd) return newNd;
     heap* root = new heap;
    memcpy(root, curNd, sizeof(heap));
if(newNd->edge->d < curNd->edge->d){
       root->edge = newNd->edge;
       root->chd[2] = newNd->chd[2];
root->chd[3] = newNd->chd[3];
       newNd->edge = curNd->edge;
       newNd->chd[2] = curNd->chd[2];
       newNd - > chd[3] = curNd - > chd[3];
     if(root->chd[0]->dep < root->chd[1]->dep)
       root->chd[0] = merge(root->chd[0],newNd);
       root->chd[1] = merge(root->chd[1],newNd);
     root->dep = max(root->chd[0]->dep, root->chd[1]->
          dep) + 1;
     return root;
  vector<heap*> V;
```

```
void build(){
     nullNd = new heap;
     nullNd->dep = 0;
     nullNd->edge = new nd;
     fill(nullNd->chd, nullNd->chd+4, nullNd);
     while(not dfsQ.empty()){
       int u = dfsQ.front(); dfsQ.pop();
if(!nxt[ u ]) head[ u ] = nullNd;
       else head[ u ] = head[nxt[ u ]->v];
       V.clear();
       for( auto&& e : g[ u ] ){
         int v = e \rightarrow v;
          if( dst[ v ] == -1 ) continue;
          e->d += dst[ v ] - dst[ u ];
if( nxt[ u ] != e ){
            heap* p = new heap;
            fill(p->chd, p->chd+4, nullNd);
            p->dep = 1;
            p->edge = e;
            V.push_back(p);
       if(V.empty()) continue;
       make_heap(V.begin(), V.end(), cmp);
#define L(X) ((X<<1)+1)
#define R(X) ((X<<1)+2)
       for( size_t i = 0 ; i < V.size() ; i ++ ){
  if(L(i) < V.size()) V[i]->chd[2] = V[L(i)];
          else V[i]->chd[2]=nullNd;
          if(R(i) < V.size()) V[i]->chd[3] = V[R(i)];
         else V[i]->chd[3]=nullNd;
       head[u] = merge(head[u], V.front());
  } }
  vector<ll> ans
  void first_K(){
     ans.clear();
     priority_queue<node> Q;
     if( dst[ s ] == -1 ) return;
     ans.push_back( dst['s ] );
if( head[s] != nullNd )
       Q.push(node(head[s], dst[s]+head[s]->edge->d));
     for( int _ = 1 ; _ < k and not Q.empty() ; _ ++ ){
  node p = Q.top(), q; Q.pop();</pre>
       ans.push_back( p.d );
       if(head[ p.H->edge->v ] != nullNd){
          q.H = head[p.H->edge->v];
          q.d = p.d + q.H->edge->d;
          Q.push(q);
       for( int i = 0 ; i < 4 ; i ++ )
  if( p.H->chd[ i ] != nullNd ){
            q.H = p.H->chd[i];
            q.d = p.d - p.H->edge->d + p.H->chd[i]->
                 edge->d;
            Q.push( q );
  void solve(){ // ans[i] stores the i-th shortest path
     dijkstra();
     build();
     first_K(); // ans.size() might less than k
} }solver;
```

5.14 SPFA

```
#define MXN 200005
struct SPFA{
   int n;
   LL inq[MXN], len[MXN];
   vector<LL> dis;
   vector<pair<int, LL>> edge[MXN];
   void init(int _n){
      n = _n;
      dis.clear(); dis.resize(n, 1e18);
      for(int i = 0; i < n; i++){
        edge[i].clear();
        inq[i] = len[i] = 0;
   } }
   void addEdge(int u, int v, LL w){
      edge[u].push_back({v, w});
   }</pre>
```

```
vector<LL> solve(int st = 0){
    deque<int> dq; //return {-1} if has negative cycle
    dq.push_back(st); //otherwise return dis from st
    inq[st] = 1; dis[st] = 0;
    while(!dq.empty()){
      int u = dq.front(); dq.pop_front();
      inq[u] = 0;
      for(auto [to, d] : edge[u]){
        if(dis[to] > d+dis[u]){
          dis[to] = d+dis[u];
          len[to] = len[u]+1;
          if(len[to] > n) return {-1};
          if(inq[to]) continue;
          (!dq.empty()&&dis[dq.front()] > dis[to]?
              dq.push_front(to) : dq.push_back(to));
          inq[to] = 1;
    return dis;
} }spfa;
```

5.15 Tree Hash

```
//限定root = 1
//從 dfs(1,1) 開始
int subtree_sz[MXN]:
vector<int> edge[MXN];
int dfs(int u, int f) {
  vector<pair<int, int>> h;
  subtree\_sz[u] = 1;
  for (int child : edge[u]) {
  if (child == f) continue;
    int tmp = dfs(child, u);
    h.push_back(make_pair(tmp, subtree_sz[child]));
    subtree_sz[u] += subtree_sz[child];
  sort(h.begin(), h.end());
  int ret = subtree_sz[u];
  for (auto v : h) {
    ret = ((ret * p) % MOD + v.first) % MOD;
    ret = ret * v.second % MOD;
  return ret;
```

5.16 HeavyLightDecomposition

```
#define REP(i, s, e) for(int i = (s); i <= (e); i++)
#define REPD(i, s, e) for(int i = (s); i \ge (e); i - -)
const int MAXN = 100010;
const int LOG = 19;
struct HLD{
  int n;
  vector<int> g[MAXN];
  int sz[MAXN], dep[MAXN];
  int ts, tid[MAXN], tdi[MAXN], tl[MAXN], tr[MAXN];
      ts': timestamp', useless'after yutruli
tid[u]: pos. of node u in the seq.
tdi[i]: node at pos i of the seq.
 11
       tl , tr[ u ] : subtree interval in the seq. of
       node u
  int prt[MAXN][LOG], head[MAXN];
  // head[ u ] : head of the chain contains u
  void dfssz(int u, int p){
  dep[u] = dep[p] + 1;
    prt[u][0] = p; sz[u] = 1; head[u] = u;
for(int& v:g[u]) if(v != p){
       dep[v] = dep[u] + 1;
       dfssz(v, u);
       sz[u] += sz[v];
  void dfshl(int u){
    tid[u] = tl[u] = tr[u] = ts;
    tdi[tid[u]] = u;
    sort(ALL(g[u]),
           [&](int a, int b){return sz[a] > sz[b];});
```

```
bool flag = 1;
    for(int& v:g[u]) if(v != prt[u][0]){
       if(flag) head[v] = head[u], flag = 0;
       dfshl(v);
       tr[u] = tr[v];
  inline int lca(int a, int b){
    if(dep[a] > dep[b]) swap(a, b);
int diff = dep[b] - dep[a];
REPD(k, LOG-1, 0) if(diff & (1<<k)){</pre>
      b = prt[b][k];
     if(a == b) return a;
    REPD(k, LOG-1, 0) if(prt[a][k] != prt[b][k]){
      a = prt[a][k]; b = prt[b][k];
    return prt[a][0];
  void init( int _n ){
    n = _n; REP( i , 1 , n ) g[ i ].clear();
  void addEdge( int u , int v ){
  g[ u ].push_back( v );
    g[ v ].push_back( u );
  void yutruli(){ //build function
    dfssz(1, 0);
    ts = 0:
    dfshl(1);
REP(k, 1, LOG-1) REP(i, 1, n)
       prt[i][k] = prt[prt[i][k-1]][k-1];
  vector< PII > getPath( int u , int v ){
    vector< PII > res;
    while( tid[ u ] < tid[ head[ v ] ] ){</pre>
       res.push_back( PII(tid[ head[ v ] ] , tid[ v ]) )
       v = prt[ head[ v ] ][ 0 ];
    res.push_back( PII( tid[ u ] , tid[ v ] ) );
    reverse( ALL( res ) );
    return res;
    /* res : list of intervals from u to v
     * u must be ancestor of \boldsymbol{v}
      * usage :
        vector< PII >& path = tree.getPath( u , v )
      * for( PII tp : path ) {
          int l , r;tie( l , r ) = tp;
          upd( l , r );
          uu = tree.tdi[ l ] , vv = tree.tdi[ r ];
          uu ~> vv is a heavy path on tree
} tree;
```

5.17 差分約束

約束條件 $V_j - V_i \leq W$ addEdge(V_i, V_j, W) and run bellman-ford or spfa

6 String

6.1 PalTree

```
|// len[s]是對應的回文長度
|// num[s]是有幾個回文後綴
|// cnt[s]是這個回文子字串在整個字串中的出現次數
|// fail[s]是他長度次長的回文後綴·aba的fail是a
const int MXN = 1000010;
struct PalT{
  int nxt[MXN][26],fail[MXN],len[MXN];
  int tot,lst,n,state[MXN],cnt[MXN],num[MXN];
  int diff[MXN],sfail[MXN],fac[MXN],dp[MXN];
  char s[MXN]={-1};
  int newNode(int l,int f){
  len[tot]=l,fail[tot]=f,cnt[tot]=num[tot]=0;
```

```
memset(nxt[tot],0,sizeof(nxt[tot]));
    diff[tot]=(1>0?1-len[f]:0);
    sfail[tot]=(l>0&&diff[tot]==diff[f]?sfail[f]:f);
    return tot++;
  int getfail(int x){
    while(s[n-len[x]-1]!=s[n]) x=fail[x];
  int getmin(int v){
    dp[v]=fac[n-len[sfail[v]]-diff[v]];
    if(diff[v]==diff[fail[v]])
        dp[v]=min(dp[v],dp[fail[v]]);
    return dp[v]+1;
  int push(){
    int c=s[n]-'a',np=getfail(lst);
    if(!(lst=nxt[np][c])){
      lst=newNode(len[np]+2,nxt[getfail(fail[np])][c]);
      nxt[np][c]=lst; num[lst]=num[fail[lst]]+1;
    fac[n]=n;
    for(int v=lst;len[v]>0;v=sfail[v])
        fac[n]=min(fac[n],getmin(v));
    return ++cnt[lst],lst;
  void init(const char *_s){
    tot=lst=n=0;
    newNode(0,1), newNode(-1,1);
    for(;_s[n];) s[n+1]=_s[n],++n,state[n-1]=push();
    for(int i=tot-1;i>1;i--) cnt[fail[i]]+=cnt[i];
}palt;
```

6.2 Longest Increasing Subsequence O(lgn)

```
vector<int> getLIS(vector<int> a){
  vector<int> lis;
  for(int i : a){
    if(lis.empty() || lis.back() < i) lis.push_Back(
        i);
    else *lower_bound(lis.begin(), lis.end(), i) =
        i;
  }
  return lis;
}</pre>
```

6.3 Longest Common Subsequence O(lgn)

6.4 KMP

```
| /* len-failure[k]:
在k結尾的情況下·這個子字串可以由開頭
|長度為(len-failure[k])的部分重複出現來表達
|
| failure[k]為次長相同前綴後綴
```

```
如果我們不只想求最多,而且以0-base做為考量
 ·那可能的長度由大到小會是
failuer[k] \ failure[failuer[k]-1]
 failure[failure[failuer[k]-1]-1]..
 直到有值為0為止 */
int failure[MXN];
vector<int> KMP(string& t, string& p){
    vector<int> ret;
    if (p.size() > t.size()) return;
    for (int i=1, j=failure[0]=-1; i<p.size(); ++i){</pre>
        while (j \ge 0 \&\& p[j+1] != p[i])
             j = failureΓi];
         if (p[j+1] == p[i]) j++;
         failure[i] = j;
    for (int i=0, j=-1; i<t.size(); ++i){</pre>
        while (j >= 0 && p[j+1] != t[i])
    j = failure[j];
         if (p[j+1] == t[i]) j++;
         if (j == p.size()-1){
            ret.push_bck( i - p.size() + 1 );
             j = failure[j];
}
    }
        }
```

6.5 SAIS

```
const int N = 300010;
struct SA{
#define REP(i,n) for ( int i=0; i<int(n); i++ )</pre>
#define REP1(i,a,b) for ( int i=(a); i <= int(b); i++)
  bool _t[N*2];
  int _s[N*2], _sa[N*2], _c[N*2], x[N], _p[N], _q[N*2],
        hei[N], r[N];
  int operator [] (int i){ return _sa[i]; }
void build(int *s, int n, int m){
    memcpy(_s, s, sizeof(int) * n);
    sais(_s, _sa, _p, _q, _t, _c, n, m);
    mkhei(n):
  void mkhei(int n){
    REP(i,n) r[_sa[i]] = i;
    hei[0] = 0;
    REP(i,n) if(r[i]) {
       int ans = i>0? max(hei[r[i-1]] - 1, 0) : 0;
       \label{eq:while} \begin{tabular}{ll} while(\_s[i+ans] == \_s[\_sa[r[i]-1]+ans]) & ans++; \\ \end{tabular}
       hei[r[i]] = ans;
  }
  void sais(int *s, int *sa, int *p, int *q, bool *t,
       int *c, int n, int z){
    bool uniq = t[n-1] = true, neq;
    int nn = 0, nmxz = -1, *nsa = sa + n, *ns = s + n,
         lst = -1:
#define MSO(x,n) memset((x),0,n*sizeof(*(x)))
#define MAGIC(XD) MS0(sa, n); \
    memcpy(x, c, sizeof(int) * z); \
    XD;
    memcpy(x + 1, c, sizeof(int) * (z - 1)); \
    REP(i,n) if(sa[i] && !t[sa[i]-1]) sa[x[s[sa[i]
    ]-1]]++] = sa[i]-1; \
memcpy(x, c, sizeof(int) * z); \
     for(int i = n - 1; i >= 0; i--) if(sa[i] && t[sa[i
         ]-1]) sa[--x[s[sa[i]-1]]] = sa[i]-1;
    MSO(c, z);
    REP(i,n) uniq \&= ++c[s[i]] < 2;
    REP(i,z-1) c[i+1] += c[i];
    if (uniq) { REP(i,n) sa[--c[s[i]]] = i; return; }
    for(int i = n - 2; i >= 0; i--) t[i] = (s[i]==s[i
+1] ? t[i+1] : s[i]<s[i+1]);
    MAGIC(REP1(i,1,n-1) if(t[i] && !t[i-1]) sa[--x[s[i
         ]]]=p[q[i]=nn++]=i);
    REP(i, n) if (sa[i] && t[sa[i]] && !t[sa[i]-1]) {
       neq=lst<0||memcmp(s+sa[i],s+lst,(p[q[sa[i]]+1]-sa]
            [i])*sizeof(int));
       ns[q[lst=sa[i]]]=nmxz+=neq;
    sais(ns, nsa, p + nn, q + n, t + n, c + z, nn, nmxz
          + 1);
    MAGIC(for(int i = nn - 1; i >= 0; i--) sa[--x[s[p[
         nsa[i]]]]] = p[nsa[i]]);
```

```
}
}sa;
int H[ N ], SA[ N ];
void suffix_array(int* ip, int len) {
    // should padding a zero in the back
    // ip is int array, len is array length
    // ip[0..n-1] != 0, and ip[len] = 0
    ip[len++] = 0;
    sa.build(ip, len, 128);
    for (int i=0; i<len; i++) {
        H[i] = sa.hei[i + 1];
        SA[i] = sa._sa[i + 1];
    }
    // resulting height, sa array \in [0,len)
}</pre>
```

6.6 Z Value

```
int z[MAXN];
void Z_value(const string& s) { //z[i] = lcp(s[1...],s[
    i...])
int i, j, left, right, len = s.size();
left=right=0; z[0]=len;
for(i=1;i<len;i++) {
    j=max(min(z[i-left],right-i),0);
    for(;i+j<len&&s[i+j]==s[j];j++);
    z[i]=j;
    if(i+z[i]>right) {
        right=i+z[i];
        left=i;
    }
}
```

6.7 ZValue Palindrome

6.8 Smallest Rotation

```
//rotate(begin(s),begin(s)+minRotation(s),end(s))
int minRotation(string s) {
  int a = 0, N = s.size(); s += s;
  rep(b,0,N) rep(k,0,N) {
    if(a+k == b || s[a+k] < s[b+k])
      {b += max(0, k-1); break;}
    if(s[a+k] > s[b+k]) {a = b; break;}
  } return a;
}
```

6.9 Cyclic LCS

```
#define L 0
#define U 1
#define U 2
const int mov[3][2]={0,-1, -1,-1, -1,0};
int al,bl;
char a[MAXL*2],b[MAXL*2]; // 0-indexed
int dp[MAXL*2][MAXL];
char pred[MAXL*2][MAXL];
inline int lcs_length(int r) {
  int i=r+al,j=bl,l=0;
  while(i>r) {
    char dir=pred[i][j];
    if(dir==LU) l++;
```

```
i+=mov[dir][0];
    j+=mov[dir][1];
  return 1:
inline void reroot(int r) { // r = new base row
  int i=r,j=1;
  while(j<=bl&&pred[i][j]!=LU) j++;</pre>
  if(j>bl) return;
  pred[i][j]=L;
while(i<2*al&&j<=bl) {</pre>
    if(pred[i+1][j]==Ú) {
       pred[i][j]=L;
    } else if(j<bl&&pred[i+1][j+1]==LU) {</pre>
       i++;
       1++:
       pred[i][j]=L;
    } else {
       j++;
} } }
int cyclic_lcs() {
  // a, b, al, bl should be properly filled
// note: a WILL be altered in process
              -- concatenated after itself
  char tmp[MAXL];
  if(al>bl) {
    swap(al,bl);
    strcpy(tmp,a);
    strcpy(a,b);
    strcpy(b,tmp);
  strcpy(tmp,a);
  strcat(a,tmp);
  // basic lcs
  for(int i=0;i<=2*al;i++) {</pre>
    d\hat{p}[i][0]=\hat{0};
    pred[i][0]=U;
  for(int j=0;j<=bl;j++) {
  dp[0][j]=0;</pre>
    pred[0][j]=L;
  for(int i=1;i<=2*al;i++) {</pre>
    for(int j=1; j<=bl; j++) +</pre>
       if(a[i-1]==b[j-1]) dp[i][j]=dp[i-1][j-1]+1;
       else dp[i][j]=max(dp[i-1][j],dp[i][j-1]);
       if(dp[i][j-1]==dp[i][j]) pred[i][j]=L;
       else if(a[i-1]==b[j-1]) pred[i][j]=LU;
       else pred[i][j]=U;
  } }
  // do cyclic lcs
  int clcs=0;
  for(int i=0;i<al;i++) {</pre>
    clcs=max(clcs,lcs_length(i));
    reroot(i+1);
  // recover a
  a[al]='\0'
  return clcs;
```

6.10 Hash

```
const ll P2;
const ll MOD;
pair<ll,ll> Hash[MXN];

void build(const string& s){
    pair<ll,ll> val = make_pair(0,0);
    for(int i=0; i<s.size(); i++){
        val.first = (val.first * P1 + s[i]) % MOD;
        val.second = (val.second * P2 + s[i]) % MOD;
        Hash[i] = val;
    }
}</pre>
```

6.11 Aho-Corasick

```
struct ACautomata{
  struct Node{
    int cnt.i
    Node *go[26], *fail, *dic;
    Node (){
      cnt = 0; fail = 0; dic = 0; i = 0;
      memset(go,0,sizeof(go));
  }pool[1048576],*root;
  int nMem,n_pattern;
 Node* new_Node(){
    pool[nMem] = Node();
    return &pool[nMem++];
  void init() {
    nMem=0;root=new_Node();n_pattern=0;
    add("");
  void add(const string &str) { insert(root,str,0); }
  void insert(Node *cur, const string &str, int pos){
    for(int i=pos;i<str.size();i++){</pre>
      if(!cur->go[str[i]-'a'])
        cur->go[str[i]-'a'] = new_Node();
      cur=cur->go[str[i]-'a'];
    }
    cur->cnt++; cur->i=n_pattern++;
  }
  void make_fail(){
    queue<Node*> que;
    que.push(root);
    while (!que.empty()){
      Node* fr=que.front(); que.pop();
      for (int i=0; i<26; i++){
        if (fr->go[i]){
          Node *ptr = fr->fail;
          while (ptr && !ptr->go[i]) ptr = ptr->fail;
          fr->go[i]->fail=ptr=(ptr?ptr->go[i]:root);
          fr->go[i]->dic=(ptr->cnt?ptr:ptr->dic);
          que.push(fr->go[i]);
 void query(string s){
      Node *cur=root;
      for(int i=0;i<(int)s.size();i++){</pre>
          while(cur&&!cur->go[s[i]-'a']) cur=cur->fail;
          cur=(cur?cur->go[s[i]-'a']:root);
          if(cur->i>=0) ans[cur->i]++;
          for(Node *tmp=cur->dic;tmp;tmp=tmp->dic)
              ans[tmp->i]++;
  } }// ans[i] : number of occurrence of pattern i
}AC;
```

7 Data Structure

7.1 Segment tree

```
struct seg_tree{
    ll a[MXN],val[MXN*4],tag[MXN*4],NO_TAG=0;
    void push(int i,int l,int r){
        if(tag[i]!=NO_TAG){
        val[i]+=tag[i]; // update by tag
        if(l!=r){
```

```
tag[cl(i)]+=tag[i]; // push
        tag[cr(i)]+=tag[i]; // push
      tag[i]=NO_TAG;
  } }
  void pull(int i,int l,int r){
    int mid=(l+r)>>1;
    push(cl(i),l,mid);push(cr(i),mid+1,r);
    val[i]=max(val[cl(i)],val[cr(i)]); // pull
  void build(int i,int l,int r){
    if(l==r){
      val[i]=a[l]; // set value
      return;
    int mid=(l+r)>>1;
    build(cl(i),1,mid);build(cr(i),mid+1,r);
    pull(i,l,r);
  void update(int i,int l,int r,int ql,int qr,int v){
    push(i,l,r);
    if(ql <= l\&r <= qr){
      tag[i]+=v; // update tag
      return;
    int mid=(l+r)>>1;
    if(ql<=mid) update(cl(i),l,mid,ql,qr,v);</pre>
    if(qr>mid) update(cr(i),mid+1,r,ql,qr,v);
    pull(i,l,r);
  11 query(int i,int l,int r,int ql,int qr){
    push(i,l,r);
    if(ql \le l\&r \le qr)
      return val[i]; // update answer
      ll mid=(l+r)>>1,ret=0;
    if(ql<=mid) ret=max(ret,query(cl(i),l,mid,ql,qr));</pre>
    if(qr>mid) ret=max(ret,query(cr(i),mid+1,r,ql,qr));
    return ret:
}}tree;
```

7.2 Trie

```
struct trie{
   trie *nxt[26];
              //紀錄有多少個字串以此節點結尾
   int cnt;
   int sz;
              //有多少字串的前綴包括此節點
   trie():cnt(0),sz(0){
       memset(nxt,0,sizeof(nxt));
};
trie *root = new trie(); //創建新的字典樹
void insert(string& s){
   trie *now = root; // 每次從根結點出發
   for(auto i:s){
       now->sz++
       if(now->nxt[i-'a'] == NULL){
          now->nxt[i-'a'] = new trie();
       now = now->nxt[i-'a']; //走到下一個字母
   now->cnt++;
   now->sz++;
int query_prefix(string& s){ //查詢有多少前綴為 s
   trie *now = root;
                      // 每次從根結點出發
   for(auto i:s){
       if(now->nxt[i-'a'] == NULL){
          return 0;
       now = now->nxt[i-'a'];
   return now->sz;
}
int query_count(string& s){ //查詢字串 s 出現次數
                    // 每次從根結點出發
   trie *now = root;
```

```
National Ocean University XwX Team
    for(auto i:s){
                                                                           n=t:
         if(now->nxt[i-'a'] == NULL){
             return 0;
         now = now->nxt[i-'a'];
    return now->cnt;
}
7.3 Treap
struct Treap{
  int sz , val , pri , tag;
Treap *l , *r;
Treap( int _val ){
    val = _val; sz = 1;
    pri = rand(); l = r = NULL; tag = 0;
  }
                                                                          }
void push( Treap * a ){
  if( a->tag ){
    Treap *swp = a->1; a->1 = a->r; a->r = swp;
    int swp2;
                                                                      }
    if( a->l ) a->l->tag ^= 1;
                                                                };
    if( a \rightarrow r ) a \rightarrow r \rightarrow tag ^= 1;
    a \rightarrow tag = 0;
} }
inline int Size( Treap * a ){ return a ? a->sz : 0; }
void pull( Treap * a ){
   a->sz = Size( a->l ) + Size( a->r ) + 1;
                                                                 struct node{
                                                                    node *l,
Treap* merge( Treap *a , Treap *b ){
                                                                    int val;
  if( !a || !b ) return a ? a : b;
                                                                 };
  if( a->pri > b->pri ){
    push( a );
    a \rightarrow r = merge(a \rightarrow r, b);
    pull( a );
    return a;
  }else{
    push( b );
                                                                    int n;
    b->l = merge(a, b->l);
    pull( b );
    return b;
                                                                      n = _n;
void split_kth( Treap *t , int k, Treap*&a, Treap*&b ){
  if( !t ){ a = b = NULL; return; }
  push( t );
  if( Size( t->l ) + 1 <= k ){
    a = t;
    split_kth(t\rightarrow r, k-Size(t\rightarrow l)-1, a\rightarrow r, b)
    pull( a );
  }else{
    split_kth( t->l , k , a , b->l );
    pull( b );
                                                                         R);}
void split_key(Treap *t, int k, Treap*&a, Treap*&b){
  if(!t){ a = b = NULL; return; }
  push(t);
  if(k \le t - val)
    b = t;
    split_key(t->l,k,a,b->l);
    pull(b);
  else{
    split_key(t->r,k,a->r,b);
    pull(a);
                                                                         v);}
} }
7.4 BIT
                                                                      else
#define lowbit(x) (x&-x)
struct BIT {
```

```
vector<int> bit;
BIT( int t ) {
```

```
bit=vector<int>(n+1,0);
~BIT() {bit.clear();}
void update( int pos, int val ) {
   while ( pos <= n ) {</pre>
         bit[pos]+=val;
         pos+=lowbit(pos);
void range_update( int L, int R, int val ) {
    update(L,val);
    update(R+1,-val);
int query( int pos ) {
    int res=0;
    while( pos ) {
         res+=bit[pos];
         pos-=lowbit(pos);
    return res;
int range_query( int L, int R ) {
    return query(R)-query(L-1);
```

7.5 持久化 SMT

```
vector<node *> ver;
int arr[MXN] = \{0\};
struct SegmentTree{
  node *root;
  void build(int _n){
    root = build(0, n-1);
  node* build(int L, int R){
    node *x = new node();
    if(L == R){ x->val = arr[L]; return x;}
    int mid = (L+R)/2;
    x->l = build(L, mid);
    x->r = build(mid + 1, R);
    x->val = x->l->val + x->r->val;
    return x;
  int query(node *ro, int L, int R){return query(ro, 0,
       n-1, L, R);}
  int query(int L, int R){return query(root, 0, n-1, L,
  int query(node *x, int L, int R, int recL, int recR){
    if(recL <= L && R <= recR) return x->val;
    int mid = (L+R)/2, res = 0;
    if(recL <= mid) res += query(x->1, L, mid, recL,
        recR);
    if(mid < recR) res += query(x->r, mid+1, R, recL,
        recR);
    return res;
  void update(int pos, int v){update(root, 0, n-1, pos,
  void update(node *x, int L, int R, int pos, int v){
    if(L == R){x->val = v; arr[L] = v; return;}
    int mid = (L+R)/2;
    if(pos <= mid) update(x->1, L, mid, pos, v);
                  update(x->r, mid+1, R, pos, v);
    x->val = x->l->val + x->r->val;
  node *update_ver(node *pre, int 1, int r, int pos,
      int v){
    node *x = new node();
                             //當前位置建立新節點
    if(l == r){
```

```
x->val = v;
     return x;
   int mid = (l+r)>>1;
   if(pos <= mid){ //更新左邊
     x->l = update_ver(pre->l, l, mid, pos, v); //左邊
         節點連向新節點
     x->r = pre->r; //右邊連到原本的右邊
   else{ //更新右邊
     x->l = pre->l; //左邊連到原本的左邊
     x->r = update\_ver(pre->r, mid+1, r, pos, v); //
        右邊節點連向新節點
   x->val = x->l->val + x->r->val;
   return x;
}} seg;
void add_ver(int x,int v){
                          //修改位置 x 的值為 v
   ver.push_back(seg.update_ver(ver.back(), 0, seg.n
       -1, x, v));
```

7.6 Black Magic

```
#include <bits/extc++.h>
using namespace __gnu_pbds;
typedef tree<int,null_type,less<int>,rb_tree_tag,
    tree_order_statistics_node_update> set_t;
#include <ext/pb_ds/assoc_container.hpp>
typedef cc_hash_table<int,int> umap_t;
typedef priority_queue<int> heap;
#include<ext/rope>
using namespace __gnu_cxx;
int main(){
  // Insert some entries into s.
  set_t s; s.insert(12); s.insert(505);
  // The order of the keys should be: 12, 505.
  assert(*s.find_by_order(0) == 12);
  assert(*s.find_by_order(3) == 505);
  // The order of the keys should be: 12, 505.
  assert(s.order_of_key(12) == 0);
 assert(s.order_of_key(505) == 1);
  // Erase an entry.
 s.erase(12);
// The order of the keys should be: 505.
  assert(*s.find_by_order(0) == 505);
  // The order of the keys should be: 505.
  assert(s.order_of_key(505) == 0);
 heap h1 , h2; h1.join( h2 );
  rope<char> r[ 2 ];
  r[1] = r[0]; // persistenet
string t = "abc";
  r[1].insert(0, t.c_str());
r[1].erase(1,1);
  cout << r[ 1 ].súbstr( 0 , 2 );</pre>
```

8 Others

8.1 SOS dp

8.2 Max subrectangle

```
const int N = 1e5+5;
int n, a[N], l[N], r[N];
long long ans;
int main() {
  while (cin>>n) {
    ans = 0;
    for (int i = 1; i \le n; i++) cin>>a[i], l[i] = r[i]
          = i;
     for (int i = 1; i <= n; i++)
      while (l[i] > 1 \&\& a[i] <= a[l[i] - 1]) l[i] = l[
           l[i] - 1];
    for (int i = n; i >= 1; i--)
while (r[i] < n && a[i] <= a[r[i] + 1]) r[i] = r[
           r[i] + 1];
    for (int i = 1; i <= n; i++)
      ans = max(ans, (long long)(r[i] - l[i] + 1) * a[i]
    cout<<ans<<"\n";
}
```

8.3 De Brujin sequence

```
// return cyclic array of length k^n such that every
// array of length n using 0~k-1 appears as a subarray.
vector<int> DeBruijn(int k,int n){
  if(k==1) return {0};
  vector<int> aux(k*n),res;
  function<void(int,int)> f=[&](int t,int p)->void{
    if(t>n){ if(n%p==0)
        for(int i=1;i<=p;++i) res.push_back(aux[i]);
    }else{
        aux[t]=aux[t-p]; f(t+1,p);
        for(aux[t]=aux[t-p]+1;aux[t]<k;++aux[t]) f(t+1,t)
        ;
    }
  };
  f(1,1); return res;
}</pre>
```

AC All The Time



