

Problem Chosen

B

**2024
MCM/ICM
Summary Sheet**

Team Control Number

2421255

my title

Summary

my abstract

Keywords: keyword1; keyword2

Contents

1	Introduction	3
1.1	Background	3
1.2	Restatement of the problem	3
1.3	Our work	3
2	Assumptions and Justifications	4
3	Notations	4
4	Model 1 : Locate the submersible over time	4
4.1	The uncertainties associated with the predictions	4
4.2	Density varying with depth	5
4.3	Model of submersible position	8
4.3.1	Depth Calculation	8
4.3.2	Density Calculation	8
4.3.3	Calculation of gravity, buoyancy and seawater resistance	8
4.3.4	Differential equations for simulating submarine motion	9
4.4	Estimating a submarine's position in the ocean	9
5	Sensitivity Analysis	10
6	Evaluate of the Mode and Further Discussion	10
7	Conclusions	10
8	Strengths and weaknesses	10
8.1	Strengths	10
8.2	How to cite?	11
	Appendices	11
	Appendix A First appendix	11

Appendix B Second appendix

12

1 Introduction

1.1 Background

In the 21st century, there has been a growing interest in the exploration of the ocean in various countries and regions. Maritime Cruises Mini-Submarines (MCMS), a Greek company, specializes in manufacturing submersibles to take people to the deepest parts of the ocean. They have set their sights on leading tourists on exciting adventures to explore sunken shipwrecks in the depths of the Ionian Sea.

To make their submersible operations a reality, we help MCMS to obtain regulatory approval and establish safety protocols to address potential communication loss and mechanical issues, such as propulsion failure. And we develop a predictive model that can track the submersible's location over time. This model considers factors such as sea floor positioning, buoyancy, currents, sea density, and geography.

1.2 Restatement of the problem

Considering the background information and restricted conditions identified in the problem statement, we need to solve the following problems:

- Create a model to predict location of the submersible overtime, figure out the uncertainties and find what information can the submersible send back with specific equipment to reduce that.
- Determine additional equipment for searching to carry on the host ship considering the possible costs, and recommend devices for rescuing. on both the host ship and rescue ship if necessary.
- Develop a model using location data to recommend deployment points and search patterns to minimize the time to locate a lost submersible.
- Establish a function that relates the probability of finding the submersible to both time and the accumulated search results.
- Extend the model to cover other tourist destinations and adapt it for multiple submersibles moving in the same general vicinity.

1.3 Our work

to my eq (??)

- the angular velocity of the bat,
- the velocity of the ball, and
- the position of impact along the bat.

center of percussion [Brody 1986]

Theorem 1.1. *TEX*

Lemma 1.2. *TEX*.

Proof. The proof of theorem. □

2 Assumptions and Justifications

Considering that practical problems always contain many complex factors, first of all, we need to make reasonable assumptions to simplify the model, and each hypothesis is closely followed by its corresponding explanation.

- **Assumptions 1: Rationalize the assumptions for the submersible by considering it as a point mass.**

When moving in the deep sea, the size and shape of the submersible are negligible compared to the problem we are studying, and the movement of each point on the submersible can be considered to be the same. Therefore, the submersible can be represented by a mass point, following the principle of the center of **mass theorem**.

- **Assumptions 2: Assume that the submarine will no longer provide propulsion.**

Unless under extreme special circumstances, the submersible pilot will cease all operations and await rescue after experiencing distress. Therefore, it can be inferred that the submersible is powerless on its own once in distress.

- **Assumptions 3: The decision factors only include ocean currents, density, and topography.**

Based on the principles of fluid mechanics, the motion of the submersible is primarily influenced by water flow and its own dynamics. Ocean currents play a significant role in governing the movement of water bodies in the ocean, and density is associated with the flow of water bodies. so these factors are emphasized and other factors are ignored.

- **Assumptions 4: For the simplicity of the model, decision factors do not interfere with each other.**

3 Notations

The key mathematical notations used in this paper are listed in Table 1

4 Model 1 : Locate the submersible over time

4.1 The uncertainties associated with the predictions

There are many factors that will affect the results of model predictions, mainly the following:

Symbol	Definitions	Units

Table 1: Notations used in this paper

- **Ocean current interference**,The influence of ocean currents on the movement of the submersible, which in turn affects the trajectory.
- **Changes in seawater density**,When the temperature and salinity correlation change, it will affect the density of seawater, thereby affecting the buoyancy and resistance. The buoyancy will change the vertical acceleration, and the resistance will change the velocity in the direction of motion.
- **Measure noise and communication delays**, Due to measure noise and communication delays, navigation accuracy is affected,communication efficiency is reduced ,so the results are interfered.
- **Change in the probability of finding the submersible caused by long search and rescue time**, it will lead to difficulty in accumulating data, decreased search efficiency, uncertainty in mission objectives, changes in communication requirements, and impact on location prediction.
- **Neutral buoyancy condition**,Neutral buoyancy conditions cause drift risk, risk of getting wet, depth changes, environmental variations, and changes in forecast results.

4.2 Density varying with depth

We developed a model to predict how a submersible's position will change over time

In the model, the density of seawater is a crucial factor determining the water resistance and buoyancy of the submarine, which is essential for predicting the trajectory after a submarine accident.The Ionian Sea is small and closed, so horizontal density changes can be ignored. Therefore, the relationship between density and submarine depth is first solved.

The relationship between pressure and density, gravitational acceleration and depth is related by this formula.

$$P = \rho gh \quad (1)$$

On the left side of the equation is the pressure at a certain underwater location, while the right side represents the product of seawater density (ρ), local gravity acceleration (g), and diving depth (h). Since the change in depth is significant during the descent, after consulting the data and calculating, It is known that the product of seawater density (ρ) and local gravity acceleration (g)

is approximately 0.10045. Therefore, in the formula, it is reasonable to consider $P = 0.10045h$, therefore we can calculate a certain Pressure corresponding to depth.

By reviewing literature^[2] and analyzing the information, we obtained scatter diagrams illustrating the relationship between seawater salinity and pressure, as well as seawater temperature and pressure. This enables us to determine the corresponding temperature and salinity values for a specific depth.

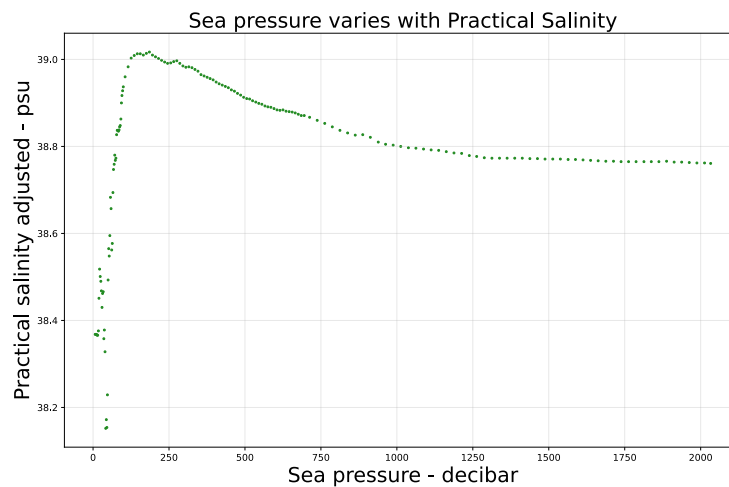


Figure 1: Seawater salinity-pressure scatter point

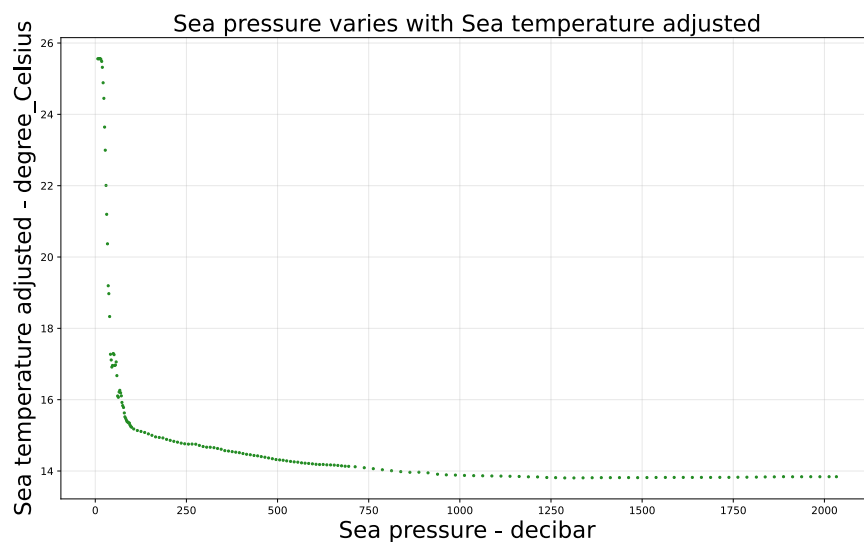


Figure 2: Seawater temperature-pressure scatter plot

After calculating the seawater temperature and salinity, and then considering the relationship

between seawater salinity, temperature and seawater density, we can use the Thermodynamic Equation of Seawater to calculate the density of seawater.

$$\rho = \rho_0 + \alpha(T - T_0) + \beta(S - S_0) \quad (2)$$

On the left side of the equation, ρ represents the density at a certain underwater location, ρ_0 is the reference density that is taken as the density of pure water, and $(T - T_0)$ and $(S - S_0)$ denote the temperature and salinity differences from their respective reference values. Moreover, α and β are their respective correlation coefficients, where α is the thermal expansion coefficient and β is the salinity expansion coefficient.

From the formula, we can infer that ρ is determined by the three-dimensional linear relationship between T and S . However, because factors such as sea currents and temperature will stabilize after reaching a certain depth, the change in seawater density no longer shows an obvious linear relationship, so we need to add a correction formula to calculate more accurate value of seawater density.

$$\rho = \begin{cases} \rho_0 + \alpha(T - T_0) + \beta(S - S_0) & \text{if } h < 2,000 \text{ m} \\ C_1 & \text{if } h \geq 2,000 \text{ m} \end{cases} \quad (3)$$

By consulting information and data, we calculated that the density of seawater is 1070 kg/m^3 when the depth is more than 2000 meters. So the density of seawater can be given at a specific depth. Therefore we plotted the density of seawater as a function of depth.

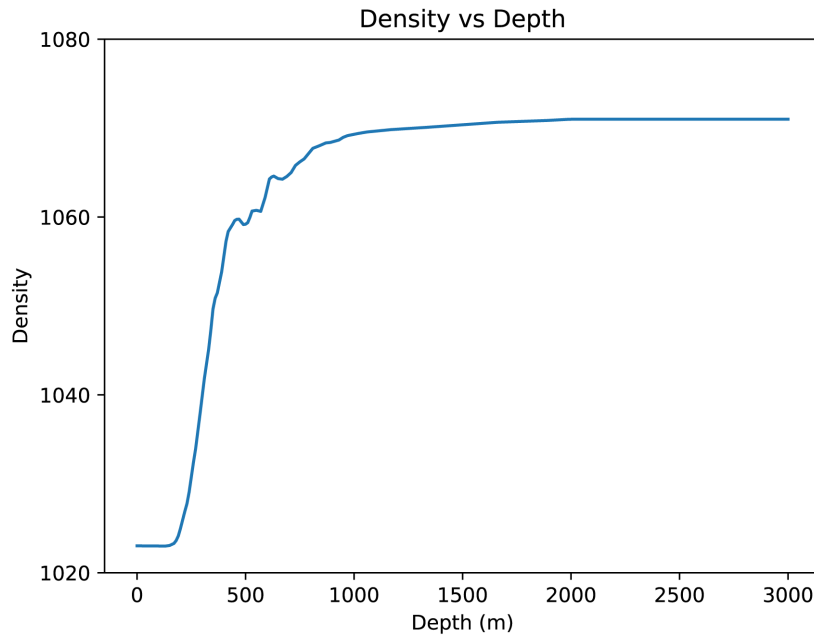


Figure 3: Seawater Density changes with depth

4.3 Model of submersible position

4.3.1 Depth Calculation

Depth computation is a critical part of our model. It is based on elevation information provided by geographic data files. By using lookups and data we are able to obtain elevation data on the earth's surface, and also obtain the latitude and longitude of various points. The curvature of the earth's surface can be calculated by simplifying latitude and longitude, and we can obtain new geographical coordinates, given by this formula.

$$x = y + \frac{z}{111.32} \quad (4)$$

$$w = v + \frac{u}{111.32 \cdot \cos(\text{radians}(y))} \quad (5)$$

where x represents the new latitude, y represents the latitude of the origin position, and z represents the offset of the latitude. w represents the new longitude, v represents the longitude of the origin position, and u represents the longitude of the origin position.

And 1 degree of latitude is approximately 111.32 kilometers. After obtaining the new geographical coordinates, we can obtain the elevation information of the target location.

4.3.2 Density Calculation

We considered the impact of water depth on the density of submarines. In order to obtain accurate data, we performed calculations between depth and density. By consulting information and data, and after calculation, we obtained a density value ranging from 1025 to 1070, and took into account the change in seawater density through linear interpolation.

$$x = y + \frac{\max(w) - \min(w)}{z \cdot (u - \min(w))} \quad (6)$$

Where x represents the calculated density value, y represents the minimum density value, z represents the density range, w represents the density value list, and u represents the value calculated by consulting the data. We account for changes in water depth and provide the density information required in the submarine model.

4.3.3 Calculation of gravity, buoyancy and seawater resistance

The calculation of water resistance is a key factor in the movement of submarines in the water, which involves factors such as drag coefficient, reference area and speed.

$$P = \frac{1}{2} \cdot C_d \cdot \rho \cdot A \cdot v_z^2 \quad (7)$$

The calculation represents an expression for water resistance. In the formula, water resistance corresponds to P , density to ρ , and velocity to v_z .

Gravity and buoyancy calculations are two opposing forces experienced by a submarine moving in the water. It is also a key factor in the movement of submarines in the water.

$$G = m \cdot g \quad (8)$$

$$F = \rho_w \cdot g \cdot V \quad (9)$$

Where gravity corresponds to G , mass corresponds to m , gravitational acceleration corresponds to g , buoyancy corresponds to F , density corresponds to ρ_w , gravitational acceleration corresponds to g , and volume corresponds to V .

4.3.4 Differential equations for simulating submarine motion

We describe the motion process of the submarine in the water through the calculation of differential equations. We take into account several physical factors, including water resistance, buoyancy and gravity. By solving a system of differential equations, the motion trajectories of submarines at different depths can be simulated, taking into account the influence of terrain elevation on submarine motion and the characteristics of density changes with depth.

For the submarine position x, y, z and its velocity v_x, v_y, v_z . It can be seen that when the depth of the submarine exceeds the terrain elevation and is close to the terrain elevation, the speed and acceleration are set to zero to simulate the situation where the submarine stops moving. When the depth of the submarine is less than zero, the position and speed are recalculated to simulate the situation when the submarine floats to the surface. We calculated the displacement velocity in the x and y directions, taking into account the effect of Gaussian noise. We then calculate the velocity and acceleration in the z direction, taking into account the effects of water drag, buoyancy and gravity. In this way, the result of the differential equation is solved, that is, the change of the submarine's position and speed in time. The formula is as follows

$$\frac{dv_x}{dt} = -\frac{R \cdot \text{sgn}(v_x)}{m} + N_x \quad (10)$$

$$\frac{dv_y}{dt} = -\frac{R \cdot \text{sgn}(v_y)}{m} + N_y \quad (11)$$

$$\frac{dv_z}{dt} = \frac{g - R \cdot \text{sgn}(v_z)}{m} + N_z \quad (12)$$

Where v_x, v_y , and v_z represent the speed in the horizontal and vertical directions respectively. $dv_x/dt, dv_y/dt, dv_z/dt$ is the rate of change of the corresponding speed. R is the drag coefficient. m is mass. g is the acceleration due to gravity. $\text{sgn}(a)$ is the symbolic function. N_x, N_y and N_z represent the influence of Gaussian noise. These noises can affect the dynamic behavior of the system.

4.4 Estimating a submarine's position in the ocean

To infer the likely location of the submarine in three-dimensional space, we used three-dimensional Bayesian inference. Through the observation data, the corresponding posterior probability distribution is obtained. In the absence of observational information, we make an initial estimate of the submarine's position. We simplified the prior probability function and set it to a constant 1.0, which means that the prior probability of all positions is equal. $P(X)$ represents the prior probability of the submarine position.

$$P(X) = 1.0$$

Based on observational data, we estimate the likelihood of a submarine being at a given location. Observation errors are taken into account using a multivariate normal distribution, where the mean is the observation location and the covariance matrix is calculated with the given standard deviation.

$$P(x|X) = \frac{1}{(2\pi\sigma^2)^{3/2}} e^{-\frac{1}{2}(\mathbf{x}-\mu)^T \Sigma^{-1}(\mathbf{x}-\mu)} \quad (13)$$

Where X represents a given position, x represents the observed position coordinates, μ represents the mean of the observed position, represents the covariance matrix, and σ represents the standard deviation of the observation error.

Combining the prior probability and likelihood function, we can calculate the posterior probability. given by the formula. When the observation data, observation error and position range are given, we simulate Bayesian inference to obtain the posterior probability distribution of the submarine's position.

$$P(X|O) = \frac{P(X) \times P(O|X)}{\sum P(X) \times P(O|X)} \quad (14)$$

Where $P(X)$ represents the prior probability. $P(O|X)$ represents the likelihood function.

5 Sensitivity Analysis

6 Evaluate of the Mode and Further Discussion

7 Conclusions

8 Strengths and weaknesses

8.1 Strengths

- **Applies widely**

This system can be used for many types of airplanes, and it also solves the interference during the procedure of the boarding airplane, as described above we can get to the optimization boarding time. We also know that all the service is automate.

- **Improve the quality of the airport service**

Balancing the cost of the cost and the benefit, it will bring in more convenient for airport and passengers. It also saves many human resources for the airline.

8.2 How to cite?

bibliography cite use [1, 2, 3]

AI cite use [AI: 1, 2, 3]

References

- [1] VirtualEXPO GROUP. “NauticEXPO,” n.d. <https://www.nauticexpo.com/>
- [2] Argo (2024). Argo float data and metadata from Global Data Assembly Centre (Argo GDAC) - Snapshot of Argo GDAC of January 09st 2024. SEANOE. <https://doi.org/10.17882/42182#107470> Addison-Wesley Publishing Company, 1986.
- [3] Gebco.net. “GEBCO,” n.d. https://www.gebco.net/data_and_products/gridded_bathymetry_data/. gebco.net. https://www.gebco.net/data_and_products/gridded_bathymetry_data/GE
- [4] CAO Hong-tao, ZHANG Qi-feng, TANG Shi. Current status and key technologies of Remotely Operated Vehicles in international submarine rescue and deep-sea salvage. Ship Science and Technology, 2021, 43(12): 16-20
- [5] Zhihui, YAN Kexue, HUANG Rong. Search and rescue helicopter capability requirement analysis[J]. Aeronautical Science & Technology, 2021, 32(01): 60-64

Appendices

Appendix A First appendix

Dear, Mr. Alpha Chiang

Sincerely yours,

Your friends

Input matlab source:

```
function [t, seat, aisle] = OI6Sim(n, target, seated)
pab = rand(1, n);
for i = 1:n
    if pab(i) < 0.4
        aisleTime(i) = 0;
```

```
        else
            aisleTime(i)=trirnd(3.2,7.1,38.7);
        end
    end
```

Appendix B Second appendix

MEMORANDUM

To: MCM office

From: MCM Team 2421255

Subject: MCM

Date: February 5, 2024

This is a memorandum.

some more text **Input C++ source:**

```
//=====
// Name      : Sudoku.cpp
// Author    : lst
// Version   : a.0
// Copyright  : Your copyright notice
// Description : Sudoku in C++.
//=====

#include <iostream>
#include <cstdlib>
#include <ctime>

using namespace std;

int table[9][9];

int main() {

    for(int i = 0; i < 9; i++){
        table[0][i] = i + 1;
    }

    srand((unsigned int)time(NULL));

    shuffle((int *)&table[0], 9);

    while(!put_line(1))
    {
        shuffle((int *)&table[0], 9);
    }

    for(int x = 0; x < 9; x++){
        for(int y = 0; y < 9; y++){
            cout << table[x][y] << " ";
        }

        cout << endl;
    }

    return 0;
}
```

Report on Use of AI

1. Bing AI

Query1: write a sort algorithm

Output: Sure, I can help you with that. Here is a simple implementation of the selection sort algorithm in Python:

```
def selection_sort(arr):
    for i in range(len(arr)):
        min_idx = i
        for j in range(i + 1, len(arr)):
            if arr[min_idx] > arr[j]:
                min_idx = j
        arr[i], arr[min_idx] = arr[min_idx], arr[i]
    return arr
```

This algorithm sorts an array by repeatedly finding the minimum element from the unsorted part of the array and putting it at the beginning. The time complexity of this algorithm is $O(n^2)$.

There are many other sorting algorithms available such as bubble sort, insertion sort, merge sort, quick sort, heap sort, and more. Each of these algorithms has its own advantages and disadvantages. You can learn more about them on [GeeksforGeeks](#) and [Programiz](#).

I hope this helps!

2. OpenAI Enie (Nov 5, 2023 version, Ernie 4.0)

Query1: <insert the exact wording of any subsequent input into the AI tool>

Output: <insert the complete output from the second query>

3. Github CoPilot (Feb 3, 2024 version)

Query1: <insert the exact wording you input into the AI tool>

Output: <insert the complete output from the AI tool>

4. Google Bard (Feb 2, 2024 version)

Query: <insert the exact wording of your query>

Output: <insert the complete output from the AI tool>

5. Bing AI

Query: write a FFT algorithm

Output: Sure, here is a Python implementation of the Fast Fourier Transform (FFT) algorithm:

```
import numpy as np

def fft(x):
    n = len(x)
    if n == 1:
        return x
    even = fft(x[0::2])
    odd = fft(x[1::2])
    T = [np.exp(-2j * np.pi * k / n) * odd[k] for k in range(n // 2)]
    return [even[k] + T[k] for k in range(n // 2)] + [even[k] - T[k] for k
        ↪ in range(n // 2)]
```

The FFT is a widely used algorithm for computing the **Discrete Fourier Transform (DFT)** of a sequence. It reduces the number of computations needed from $O(n^2)$ to $O(n \log n)$ 12. The basic idea of the FFT is to apply divide and conquer. We divide the coefficient vector of the polynomial into two vectors, recursively compute the DFT for each of them, and combine the results to compute the DFT of the complete polynomial 3.

I hope this helps!