Deep Learning Face Representation from Predicting 10,000 Classes

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Abstract

This paper proposes to learn a set of high-level feature representations through deep learning, referred to as Deep hidden IDentity features (DeepID), for face verification. We argue that DeepID can be effectively learned through challenging multi-class face identification tasks, whilst they can be generalized to other tasks (such as verification) and new identities unseen in the training set. Moreover, the generalization capability of DeepID increases as more face classes are to be predicted at training. DeepID features are taken from the last hidden layer neuron activations of deep convolutional networks (ConvNets). When learned as classifiers to recognize about 10,000 face identities in the training set and configured to keep reducing the neuron numbers along the feature extraction hierarchy, these deep ConvNets gradually form compact identity-related features in the top layers with only a small number of hidden neurons. The proposed features are extracted from various face regions to form complementary and over-complete representations. Any state-of-the-art classifiers can be learned based on these high-level representations for face verification. 97.45% verification accuracy on LFW is achieved with only weakly aligned faces.

1. Introduction

Face verification in unconstrained conditions has been studied extensively in recent years [21, 15, 7, 34, 17, 26, 18, 8, 2, 9, 3, 29, 6] due to its practical applications and the publishing of LFW [19], an extensively reported dataset for face verification algorithms. The current best-performing face verification algorithms typically represent faces with over-complete low-level features, followed by shallow models [9, 29, 6]. Recently, deep models such as ConvNets [24] have been proved effective for extracting high-level visual features [11, 20, 14] and are used for face verification [18, 5, 31, 32, 36]. Huang et al. [18] learned a generative deep model without supervision. Cai
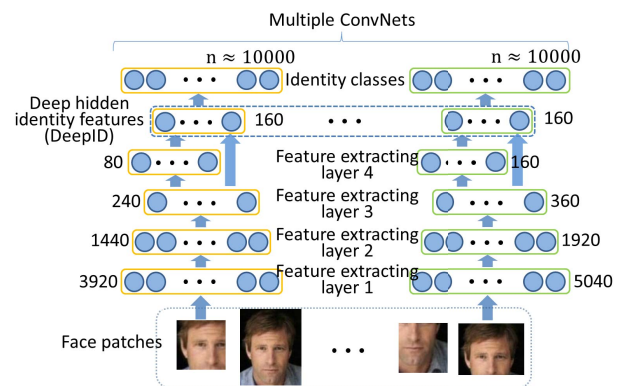

Figure 1. An illustration of the feature extraction process. Arrows indicate forward propagation directions. The number of neurons in each layer of the multiple deep ConvNets are labeled beside each layer. The DeepID features are taken from the last hidden layer of each ConvNet, and predict a large number of identity classes. Feature numbers continue to reduce along the feature extraction cascade till the DeepID layer.

et al. [5] learned deep nonlinear metrics. In [31], the deep models are supervised by the binary face verification target. Differently, in this paper we propose to learn high-level face identity features with deep models through face identification, i.e. classifying a training image into one of n identities ($n \approx 10,000$ in this work). This high-dimensional prediction task is much more challenging than face verification, however, it leads to good generalization of the learned feature representations. Although learned through identification, these features are shown to be effective for face verification and new faces unseen in the training set.

We propose an effective way to learn high-level over-complete features with deep ConvNets. A high-level illustration of our feature extraction process is shown in Figure 1. The ConvNets are learned to classify all the faces available for training by their identities, with the last hidden layer neuron activations as features (referred to as

Deep hidden IDentity features or DeepID). Each ConvNet takes a face patch as input and extracts local low-level features in the bottom layers. Feature numbers continue to reduce along the feature extraction cascade while gradually more global and high-level features are formed in the top layers. Highly compact 160-dimensional DeepID is acquired at the end of the cascade that contain rich identity information and directly predict a much larger number (*e.g.*, $10,000$) of identity classes. Classifying all the identities simultaneously instead of training binary classifiers as in [21, 2, 3] is based on two considerations. First, it is much more difficult to predict a training sample into one of many classes than to perform binary classification. This challenging task can make full use of the super learning capacity of neural networks to extract effective features for face recognition. Second, it implicitly adds a strong regularization to ConvNets, which helps to form shared hidden representations that can classify all the identities well. Therefore, the learned high-level features have good generalization ability and do not over-fit to a small subset of training faces. We constrain DeepID to be significantly fewer than the classes of identities they predict, which is key to learning highly compact and discriminative features. We further concatenate the DeepID extracted from various face regions to form complementary and over-complete representations. The learned features can be well generalized to new identities in test, which are not seen in training, and can be readily integrated with any state-of-the-art face classifiers (*e.g.*, Joint Bayesian [8]) for face verification.

Our method achieves 97.45% face verification accuracy on LFW using only weakly aligned faces, which is almost as good as human performance of 97.53%. We also observe that as the number of training identities increases, the verification performance steadily gets improved. Although the prediction task at the training stage becomes more challenging, the discrimination and generalization ability of the learned features increases. It leaves the door wide open for future improvement of accuracy with more training data.

2. Related work

Many face verification methods represent faces by high-dimensional over-complete face descriptors, followed by shallow models. Cao *et al*. [7] encoded each face image into 26K learning-based (LE) descriptors, and then calculated the L_2 distance between the LE descriptors after PCA. Chen *et al*. [9] extracted 100K LBP descriptors at dense facial landmarks with multiple scales and used Joint Bayesian [8] for verification after PCA. Simonyan *et al*. [29] computed 1.7M SIFT descriptors densely in scale and space, encoded the dense SIFT features into Fisher vectors, and learned linear projection for discriminative dimensionality reduction. Huang *et al*. [17] combined 1.2M CMD [33] and SLBP [1] descriptors, and learned sparse Mahalanobis metrics for

face verification.

Some previous studies have further learned identity-related features based on low-level features. Kumar *et al*. [21] trained attribute and simile classifiers to detect facial attributes and measure face similarities to a set of reference people. Berg and Belhumeur [2, 3] trained classifiers to distinguish the faces from two different people. Features are outputs of the learned classifiers. They used SVM classifiers, which are shallow structures, and their learned features are still relatively low-level. In contrast, we classify all the identities from the training set simultaneously. Moreover, we use the last hidden layer activations as features instead of the classifier outputs. In our ConvNets, the neuron number of the last hidden layer is much smaller than that of the output, which forces the last hidden layer to learn shared hidden representations for faces of different people in order to well classify all of them, resulting in highly discriminative and compact features with good generalization ability.

A few deep models have been used for face verification or identification. Chopra *et al*. [10] used a Siamese network [4] for deep metric learning. The Siamese network extracts features separately from two compared inputs with two identical sub-networks, taking the distance between the outputs of the two sub-networks as dissimilarity. [10] used deep ConvNets as the sub-networks. In contrast to the Siamese network in which feature extraction and recognition are jointly learned with the face verification target, we conduct feature extraction and recognition in two steps, with the first feature extraction step learned with the target of face identification, which is a much stronger supervision signal than verification. Huang *et al*. [18] generatively learned features with CDBNs [25], then used ITML [13] and linear SVM for face verification. Cai *et al*. [5] also learned deep metrics under the Siamese network framework as [10], but used a two-level ISA network [23] as the sub-networks instead. Zhu *et al*. [35, 36] learned deep neural networks to transform faces in arbitrary poses and illumination to frontal faces with normal illumination, and then used the last hidden layer features or the transformed faces for face recognition. Sun *et al*. [31] used multiple deep ConvNets to learn high-level face similarity features and trained classification RBM [22] for face verification. Their features are jointly extracted from a pair of faces instead of from a single face.

3. Learning DeepID for face verification

3.1. Deep ConvNets

Our deep ConvNets contain four convolutional layers (with max-pooling) to extract features hierarchically, followed by the fully-connected DeepID layer and the softmax output layer indicating identity classes. The input is $39 \times$
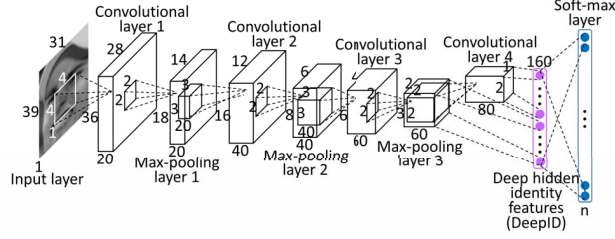
Figure 2. ConvNet structure. The length, width, and height of each cuboid denotes the map number and the dimension of each map for all input, convolutional, and max-pooling layers. The inside small cuboids and squares denote the 3D convolution kernel sizes and the 2D pooling region sizes of convolutional and max-pooling layers, respectively. Neuron numbers of the last two fully-connected layers are marked beside each layer.

$31 \times k$ for rectangle patches, and $31 \times 31 \times k$ for square patches, where $k = 3$ for color patches and $k = 1$ for gray patches. Figure 2 shows the detailed structure of the ConvNet which takes $39 \times 31 \times 1$ input and predicts n (*e.g.*, $n = 10,000$) identity classes. When the input sizes change, the height and width of maps in the following layers will change accordingly. The dimension of the DeepID layer is fixed to 160, while the dimension of the output layer varies according to the number of classes it predicts. Feature numbers continue to reduce along the feature extraction hierarchy until the last hidden layer (the DeepID layer), where highly compact and predictive features are formed, which predict a much larger number of identity classes with only a few features.

The convolution operation is expressed as

$$y^{j(r)} = \max\left(0,\ b^{j(r)} + \sum_i k^{ij(r)} * x^{i(r)}\right), \quad (1)$$

where x^i and y^j are the i-th input map and the j-th output map, respectively. k^{ij} is the convolution kernel between the i-th input map and the j-th output map. $*$ denotes convolution. b^j is the bias of the j-th output map. We use ReLU nonlinearity ($y = \max(0, x)$) for hidden neurons, which is shown to have better fitting abilities than the sigmoid function [20]. Weights in higher convolutional layers of our ConvNets are locally shared to learn different mid- or high-level features in different regions [18]. r in Equation 1 indicates a local region where weights are shared. In the third convolutional layer, weights are locally shared in every 2×2 regions, while weights in the fourth convolutional layer are totally unshared. Max-pooling is formulated as

$$y_{j,k}^i = \max_{0 \le m,n < s}\left\{x_{j \cdot s + m,\ k \cdot s + n}^i\right\}, \quad (2)$$

where each neuron in the i-th output map y^i pools over an $s \times s$ non-overlapping local region in the i-th input map x^i.

Figure 3. Top: ten face regions of medium scales. The five regions in the top left are global regions taken from the weakly aligned faces, the other five in the top right are local regions centered around the five facial landmarks (two eye centers, nose tip, and two mouse corners). Bottom: three scales of two particular patches.

The last hidden layer of DeepID is fully connected to both the third and fourth convolutional layers (after max-pooling) such that it sees multi-scale features [28] (features in the fourth convolutional layer are more global than those in the third one). This is critical to feature learning because after successive down-sampling along the cascade, the fourth convolutional layer contains too few neurons and becomes the bottleneck for information propagation. Adding the bypassing connections between the third convolutional layer (referred to as the skipping layer) and the last hidden layer reduces the possible information loss in the fourth convolutional layer. The last hidden layer takes the function

$$y_j = \max\left(0,\ \sum_i x_i^1 \cdot w_{i,j}^1 + \sum_i x_i^2 \cdot w_{i,j}^2 + b_j\right), \quad (3)$$

where x^1, w^1, x^2, w^2 denote neurons and weights in the third and fourth convolutional layers, respectively. It linearly combines features in the previous two convolutional layers, followed by ReLU non-linearity.

The ConvNet output is an n-way softmax predicting the probability distribution over n different identities.

$$y_i = \frac{\exp(y_i')}{\sum_{j=1}^{n} \exp(y_j')}, \quad (4)$$

where $y_j' = \sum_{i=1}^{160} x_i \cdot w_{i,j} + b_j$ linearly combines the 160 DeepID features x_i as the input of neuron j, and y_j is its output. The ConvNet is learned by minimizing $-\log y_t$, with the t-th target class. Stochastic gradient descent is used with gradients calculated by back-propagation.

3.2. Feature extraction

We detect five facial landmarks, including the two eye centers, the nose tip, and the two mouth corners, with the facial point detection method proposed by Sun *et al.* [30]. Faces are globally aligned by similarity transformation according to the two eye centers and the mid-point of the two mouth corners. Features are extracted from 60 face patches with ten regions, three scales, and RGB or gray channels. Figure 3 shows the ten face regions and the three scales of two particular face regions. We trained 60 ConvNets, each of which extracts two 160-dimensional DeepID vectors from a particular patch and its horizontally flipped counterpart. A special case is patches around the two eye centers and the two mouth corners, which are not flipped themselves, but the patches symmetric with them (for example, the flipped counterpart of the patch centered on the left eye is derived by flipping the patch centered on the right eye). The total length of DeepID is $19,200$ $(160 \times 2 \times 60)$, which is ready for the final face verification.

3.3. Face verification

We use the Joint Bayesian [8] technique for face verification based on the DeepID. Joint Bayesian has been highly successful for face verification [9, 6]. It represents the extracted facial features x (after subtracting the mean) by the sum of two independent Gaussian variables

$$x = \mu + \epsilon \,, \qquad (5)$$

where $\mu \sim N(0, S_\mu)$ represents the face identity and $\epsilon \sim N(0, S_\epsilon)$ the intra-personal variations. Joint Bayesian models the joint probability of two faces given the intra- or extra-personal variation hypothesis, $P(x_1, x_2 \mid H_I)$ and $P(x_1, x_2 \mid H_E)$. It is readily shown from Equation 5 that these two probabilities are also Gaussian with variations

$$\Sigma_I = \left[\begin{array}{cc} S_\mu + S_\epsilon & S_\mu \\ S_\mu & S_\mu + S_\epsilon \end{array} \right] \qquad (6)$$

and

$$\Sigma_E = \left[\begin{array}{cc} S_\mu + S_\epsilon & 0 \\ 0 & S_\mu + S_\epsilon \end{array} \right] \,, \qquad (7)$$

respectively. S_μ and S_ϵ can be learned from data with EM algorithm. In test, it calculates the likelihood ratio

$$r(x_1, x_2) = \log \frac{P(x_1, x_2 \mid H_I)}{P(x_1, x_2 \mid H_E)} \,, \qquad (8)$$

which has closed-form solutions and is efficient.

We also train a neural network for verification and compare it to Joint Bayesian to see if other models can also learn from the extracted features and how much the features and a good face verification model contribute to the performance, respectively. The neural network contains one input layer
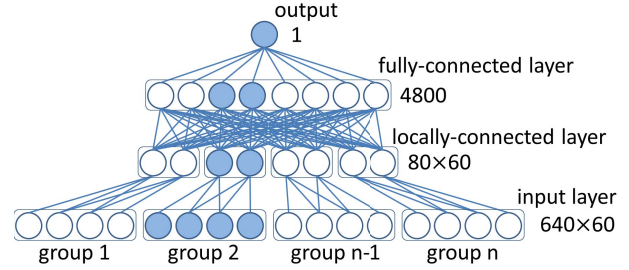

Figure 4. The structure of the neural network used for face verification. The layer type and dimension are labeled beside each layer. The solid neurons form a subnetwork.

taking the DeepID, one locally-connected layer, one fully-connected layer, and a single output neuron indicating face similarities. The input features are divided into 60 groups, each of which contains 640 features extracted from a particular patch pair with a particular ConvNet. Features in the same group are highly correlated. Neurons in the locally-connected layer only connect to a single group of features to learn their local relations and reduce the feature dimension at the same time. The second hidden layer is fully-connected to the first hidden layer to learn global relations. The single output neuron is fully connected to the second hidden layer. The hidden neurons are ReLUs and the output neuron is sigmoid. An illustration of the neural network structure is shown in Figure 4. It has $38,400$ input neurons with $19,200$ DeepID features from each patch, and $4,800$ neurons in the following two hidden layers, with every 80 neurons in the first hidden layer locally connected to one of the 60 groups of input neurons.

Dropout learning [16] is used for all the hidden neurons. The input neurons cannot be dropped because the learned features are compact and distributed representations (representing a large number of identities with very few neurons) and have to collaborate with each other to represent the identities well. On the other hand, learning high-dimensional features without dropout is difficult due to gradient diffusion. To solve this problem, we first train 60 subnetworks, each with features of a single group as input. A particular subnetwork is illustrated in Figure 4. We then use the first-layer weights of the subnetworks to initialize those of the original network, and tune the second and third layers of the original network with the first layer weights clipped.

4. Experiments

We evaluate our algorithm on LFW, which reveals the state-of-the-art of face verification in the wild. Though LFW contains 5749 people, only 85 have more than 15 images, and 4069 people have only one image. It is inadequate to train identity classifiers with so few images per person. Instead, we trained our model on CelebFaces

and tested on LFW (Section 4.1 - 4.3). CelebFaces contains $87,628$ face images of 5436 celebrities from the Internet, with approximately 16 images per person on average. People in LFW and CelebFaces are mutually exclusive.

We randomly choose 80% (4349) people from Celeb-Faces to learn the DeepID, and use the remaining 20% people to learn the face verification model (Joint Bayesian or neural networks). For feature learning, ConvNets are supervised to classify the 4349 people simultaneously from a particular kind of face patches and their flipped counterparts. We randomly select 10% images of each training person to generate the validation data. After each training epoch, we observe the top-1 validation set error rates and select the model that provides the lowest one.

In face verification, our feature dimension is reduced to 150 by PCA before learning the Joint Bayesian model. Performance almost retains in a wide range of dimensions. In test, each face pair is classified by comparing the Joint Bayesian likelihood ratio to a threshold optimized in the training data.

To evaluate the performance of our approach at an even larger training scale in Section 4.4, we extend CelebFaces to the CelebFaces+ dataset, which contains $202,599$ face images of $10,177$ celebrities. Again, people in LFW and CelebFaces+ are mutually exclusive. The ConvNet structure and feature extraction process described in the previous section remains unchanged.

4.1. Multi-scale ConvNets

We verify the effectiveness of directly connecting neurons in the third convolutional layer (after max-pooling) to the last hidden layer (the DeepID layer), such that it sees both the third and fourth convolutional layer features, forming the so-called multi-scale ConvNets. It also results in reducing feature numbers from the convolutional layers to the DeepID layer (shown in Figure 1), which helps the latter to learn higher-level features in order to well represent the face identities with fewer neurons. Figure 5 compares the top-1 validation set error rates of the 60 ConvNets learned to classify the 4349 classes of identities, either with or without the skipping layer. The lower error rates indicate the better hidden features learned. Allowing the DeepID to pool over multi-scale features reduces validation errors by an average of 4.72%. It actually also improves the final face verification accuracy from 95.35% to 96.05% when concatenating the DeepID from the 60 ConvNets and using Joint Bayesian for face verification.

4.2. Learning effective features

Classifying a large number of identities simultaneously is key to learning discriminative and compact hidden features. To verify this, we increase the identity classes
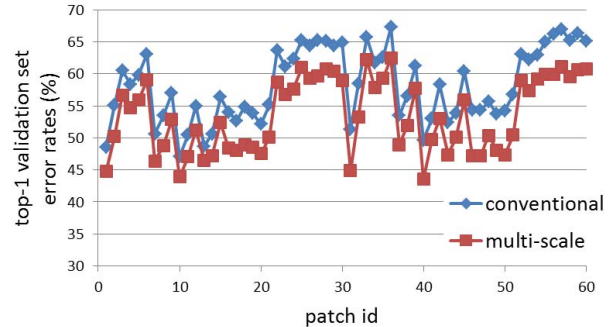

Figure 5. Top-1 validation set error rates of the 60 ConvNets trained on the 60 different patches. The blue and red markers show error rates of the conventional ConvNets (without the skipping layer) and the multi-scale ConvNets, respectively.

for training exponentially (and output neuron numbers correspondingly) from 136 to 4349 while fixing the neuron numbers in all previous layers (the DeepID is kept to be 160 dimensional). We observe the classification ability of ConvNets (measured by the top-1 validation set error rates) and the effectiveness of the learned hidden representations for face verification (measured by the test set verification accuracy) with the increasing identity classes. The input is a single patch covering the whole face in this experiment. As shown in Figure 6, both Joint Bayesian and neural network improve linearly in verification accuracy when the identity classes double. The improvement is significant. When identity classes increase 32 times from 136 to 4349, the accuracy increases by 10.13% and 8.42% for Joint Bayesian and neural networks, respectively, or 2.03% and 1.68% on average, respectively, whenever the identity classes double. At the same time, the validation set error rates drop, even when the predicted classes are tens of times more than the last hidden layer neurons, as shown in Figure 7. This phenomenon indicates that ConvNets can learn from classifying each identity and form shared hidden representations that can classify all the identities well. More identity classes help to learn better hidden representations that can distinguish more people (discriminative) without increasing the feature length (compact). The linear increasing of test accuracy with respect to the exponentially increasing training data indicates that our features would be further improved if even more identities are available. Examples of the 160-dimensional DeepID learned from the 4349 training identities and extracted from LFW test pairs are shown in Figure 8. We find that faces of the same identity tend to have more commonly activated neurons (positive features being in the same position) than those of different identities. So the learned features extract identity information.

We also test the 4349-dimensional classifier outputs as features for face verification. Joint Bayesian only achieves approximately 66% accuracy on these features, while the neural network fails, where it accounts all the face pairs as
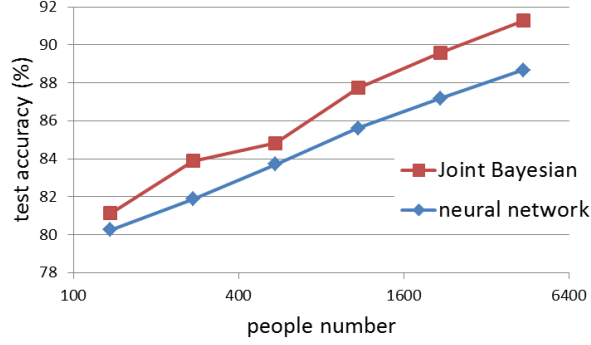
Figure 6. Face verification accuracy of Joint Bayesian (red line) and neural network (blue line) learned from the DeepID, where the ConvNets are trained with 136, 272, 544, 1087, 2175, and 4349 classes, respectively.
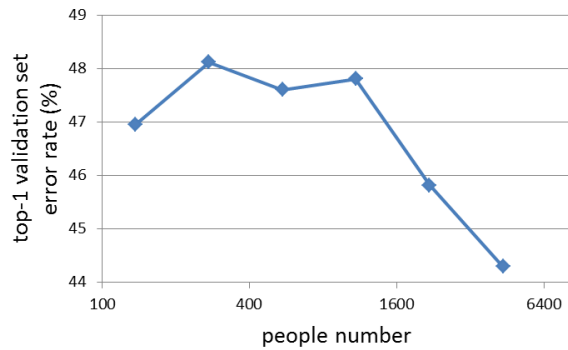

Figure 7. Top-1 validation set error rates of ConvNets learned to classify 136, 272, 544, 1087, 2175, and 4349 classes, respectively.

positive or negative pairs. With so many classes and few samples for each class, the classifier outputs are diverse and unreliable, therefore cannot be used as features.

4.3. Over-complete representation

We evaluate how much combining features extracted from various face patches would contribute to the performance. We train the face verification model with features from k patches ($k = 1, 5, 15, 30, 60$). It is impossible to numerate all the possible combinations of patches, so we select the most representative ones. We report the best-performing single patch ($k = 1$), the global color patches in a single scale ($k = 5$), all the global color patches ($k = 15$), all the color patches ($k = 30$), and all the patches ($k = 60$). As shown in Figure 9, adding more features from various regions, scales, and color channels consistently improves the performance. Combing 60 patches increases the accuracy by 4.53% and 5.27% over best single patch for Joint Bayesian and neural networks, respectively. We achieve **96.05**% and 94.32% accuracy using Joint Bayesian and neural networks, respectively. The curves show that the performance may be further improved if more features are extracted.
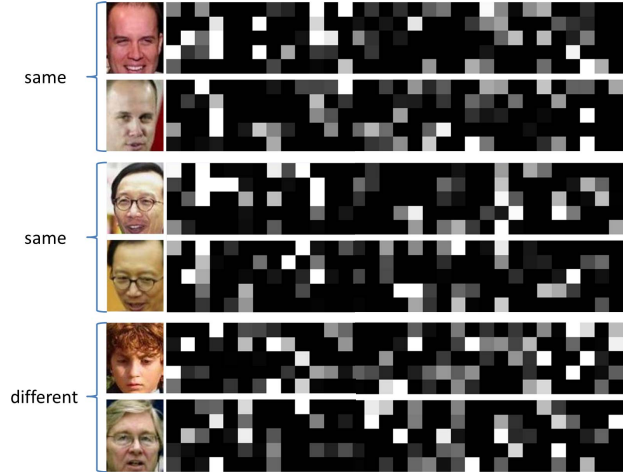

Figure 8. Examples of the learned 160-dimensional DeepID. The left column shows three test pairs in LFW. The first two pairs are of the same identity, the third one is of different identities. The corresponding features extracted from each patch are shown in the right. The features are in one dimension. We rearrange them as 5×32 for the convenience of illustration. The feature values are non-negative since they are taken from the ReLUs. Approximately 40% features have positive values. The brighter squares indicate higher values.
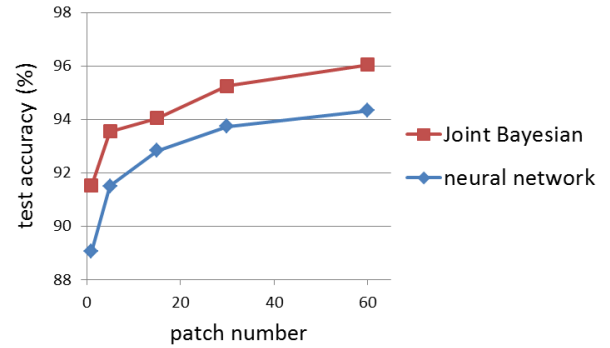

Figure 9. Test accuracy of Joint Bayesian (red line) and neural networks (blue line) using features extracted from 1, 5, 15, 30, and 60 patches. Performance consistently improves with more features. Joint Bayesian is approximately 1.8% better on average than neural networks.

4.4. Method comparison

To show how our algorithm would benefit from more training data, we enlarge the CelebFaces dataset to Celeb-Faces+, which contains $202,599$ face images of $10,177$ celebrities. People in CelebFaces+ and LFW are mutually exclusive. We randomly choose 8700 people from Celeb-Faces+ to learn the DeepID, and use the remaining 1477 people to learn Joint Bayesian for face verification. Since extracting DeepID from many different face patches also helps, we increase the patch number to 100 by using five different scales of patches instead of three. This results in

a 32, 000-dimensional DeepID feature vector, which is then reduced to 150 dimensions by PCA. Joint Bayesian learned on this 150-dimensional feature vector achieves **97.20**% test accuracy on LFW.

Due to the difference in data distributions, models well fitted to CelebFaces+ may not have equal generalization ability on LFW. To solve this problem, Cao et al. [6] proposed a practical transfer learning algorithm to adapt the Joint Bayesian model from the source domain to the target domain. We implemented their algorithm by using the 1477 people from CelebFaces+ as the source domain data and nine out of ten folders from LFW as the target domain data for transfer learning Joint Bayesian, and conduct ten-fold cross validation on LFW. The transfer learning Joint Bayesian based on our DeepID features achieves **97.45**% test accuracy on LFW, which is on par with the human-level performance of 97.53%.

We compare with the state-of-the-art face verification methods on LFW. In the comparison, we report three results. The first two are trained on CelebFaces and CelebFaces+, respectively, without transfer learning, and tested on LFW. The third one is trained on CelebFaces+ with transfer learning on LFW. Table 1 comprehensively compares the accuracies, the number of facial points used for alignment, the number of outside training images (if applicable), and the final feature dimensions for each face (if applicable). Low feature dimensions indicate efficient face recognition systems. Figure 10 compares the ROC curves. Our DeepID learning method achieves the best performance on LFW. The first four best methods compared used dense facial landmarks, while our faces are weakly aligned with only five points. The deep learning work (DeepFace) [32] independently developed by Facebook at the same time of this paper achieved the second best performance of 97.25% accuracy on LFW. It utilized 3D alignment and pose transform as preprocessing, and more than seven million outside training images plus training images from LFW.

5. Conclusion and Discussion

This paper proposed to learn effective high-level features revealing identities for face verification. The features are built on top of the feature extraction hierarchy of deep ConvNets and are summarized from multi-scale mid-level features. By representing a large amount of different identities with a small number of hidden variables, highly compact and discriminative features are acquired. The features extracted from different face regions are complementary and further boost the performance. It achieved 97.45% face verification accuracy on LFW, while only requiring weakly aligned faces.

Even more compact and discriminative DeepID can be learned if more identities are available to increase the
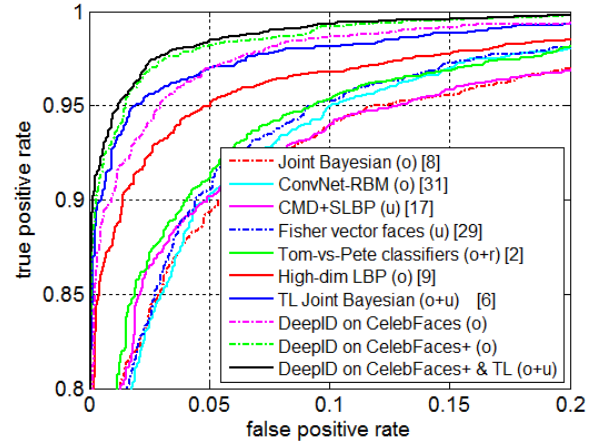

Figure 10. ROC comparison with the state-of-the-art face verification methods on LFW. TL in our method means transfer learning Joint Bayesian.

dimensionality of prediction at the training stage. We look forward to larger training sets to further boost our performance. A recent work [27] reported 98.52% accuracy on LFW with Gaussian Processes and multi-source training sets, achieving even higher than human performance. This could be due to the fact that the nonparametric Bayesian kernel method can adapt model complexity to data distribution. Gaussian processes can also be modeled with deep learning [12]. This could be another interesting direction to be explored in the future.

Acknowledgement

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Method	Accuracy (%)	No. of points	No. of images	Feature dimension
Joint Bayesian [8]	92.42 (o)	5	99,773	2000 × 4
ConvNet-RBM [31]	92.52 (o)	3	87,628	N/A
CMD+SLBP [17]	92.58 (u)	3	N/A	2302
Fisher vector faces [29]	93.03 (u)	9	N/A	128 × 2
Tom-vs-Pete classifiers [2]	93.30 (o+r)	95	20,639	5000
High-dim LBP [9]	95.17 (o)	27	99,773	2000
TL Joint Bayesian [6]	96.33 (o+u)	27	99,773	2000
DeepFace [32]	97.25 (o+u)	6 + 67	4,400,000 + 3,000,000	4096 × 4
DeepID on CelebFaces	**96.05** (o)	5	87,628	150
DeepID on CelebFaces+	**97.20** (o)	5	202,599	150
DeepID on CelebFaces+ & TL	**97.45** (o+u)	5	202,599	150

Table 1. Comparison of state-of-the-art face verification methods on LFW. Column 2 compares accuracy. Letters in the parentheses denote the training protocols used. r denotes the restricted training protocol, where the 6000 face pairs given by LFW are used for ten-fold cross-validation. u denotes the unrestricted protocol, where additional training pairs can be generated from LFW using the identity information. o denotes using outside training data, however, without using training data from LFW. o+r denotes using both outside data and LFW data in the restricted protocol for training. (o+u) denotes using both outside data and LFW data in the unrestricted protocol for training. Column 3 compares the number of facial points used for alignment. Column 4 compares the number of outside images used for training (if applicable). The last column compares the final feature dimensions for each face (if applicable). DeepFace used six 2D points and 67 3D points for alignment. TL in our method means transfer learning Joint Bayesian.

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