

# Mechanics-M1 - 2011-January

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## Question 1

Two particles  $B$  and  $C$  have mass  $m$  kg and 3 kg respectively. They are moving towards each other in opposite directions on a smooth horizontal table. The two particles collide directly. Immediately before the collision, the speed of  $B$  is  $4 \text{ m s}^{-1}$  and the speed of  $C$  is  $2 \text{ m s}^{-1}$ . In the collision the direction of motion of  $C$  is reversed and the direction of motion of  $B$  is unchanged. Immediately after the collision, the speed of  $B$  is  $1 \text{ m s}^{-1}$  and the speed of  $C$  is  $3 \text{ m s}^{-1}$ .

Find

- (a) the value of  $m$ , (3)
  - (b) the magnitude of the impulse received by  $C$ . (2)
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## Question 2

A ball is thrown vertically upwards with speed  $u \text{ m s}^{-1}$  from a point  $P$  at height  $h$  metres above the ground. The ball hits the ground  $0.75 \text{ s}$  later. The speed of the ball immediately before it hits the ground is  $6.45 \text{ m s}^{-1}$ . The ball is modelled as a particle.

- (a) Show that  $u = 0.9$  (3)
  - (b) Find the height above  $P$  to which the ball rises before it starts to fall towards the ground again. (2)
  - (c) Find the value of  $h$ . (3)
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### Question 3

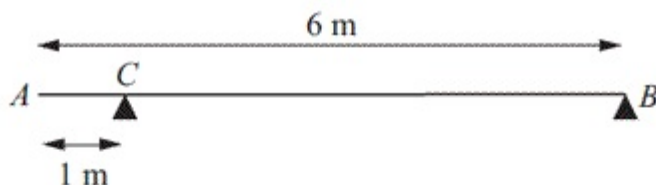


Figure 1

A uniform beam  $AB$  has mass 20 kg and length 6 m. The beam rests in equilibrium in a horizontal position on two smooth supports. One support is at  $C$ , where  $AC = 1$  m, and the other is at the end  $B$ , as shown in Figure 1. The beam is modelled as a rod.

- (a) Find the magnitudes of the reactions on the beam at  $B$  and at  $C$ . (5)

A boy of mass 30 kg stands on the beam at the point  $D$ . The beam remains in equilibrium. The magnitudes of the reactions on the beam at  $B$  and at  $C$  are now equal. The boy is modelled as a particle.

- (b) Find the distance  $AD$ . (5)

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### Question 4

A particle  $P$  of mass 2 kg is moving under the action of a constant force  $\mathbf{F}$  newtons. The velocity of  $P$  is  $(2\mathbf{i} - 5\mathbf{j}) \text{ m s}^{-1}$  at time  $t = 0$ , and  $(7\mathbf{i} + 10\mathbf{j}) \text{ m s}^{-1}$  at time  $t = 5$  s.

Find

- (a) the speed of  $P$  at  $t = 0$ , (2)
- (b) the vector  $\mathbf{F}$  in the form  $a\mathbf{i} + b\mathbf{j}$ , (5)
- (c) the value of  $t$  when  $P$  is moving parallel to  $\mathbf{i}$ . (4)
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## Question 5

A car accelerates uniformly from rest for 20 seconds. It moves at constant speed  $v \text{ m s}^{-1}$  for the next 40 seconds and then decelerates uniformly for 10 seconds until it comes to rest.

(a) For the motion of the car, sketch

(i) a speed-time graph,

(ii) an acceleration-time graph.

(6)

Given that the total distance moved by the car is 880 m,

(b) find the value of  $v$ .

(4)

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## Question 6

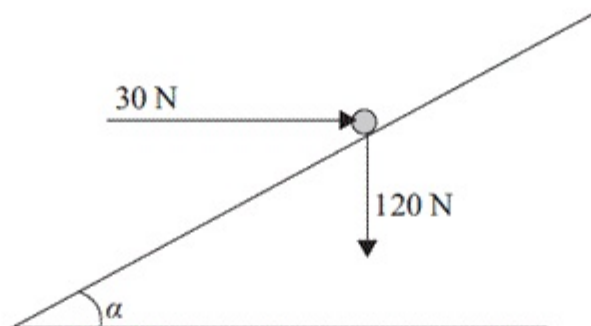


Figure 2

A particle of weight 120 N is placed on a fixed rough plane which is inclined at an angle  $\alpha$  to the horizontal, where  $\tan \alpha = \frac{3}{4}$ .

The coefficient of friction between the particle and the plane is  $\frac{1}{2}$ .

The particle is held at rest in equilibrium by a horizontal force of magnitude 30 N, which acts in the vertical plane containing the line of greatest slope of the plane through the particle, as shown in Figure 2.

- (a) Show that the normal reaction between the particle and the plane has magnitude 114 N. (4)

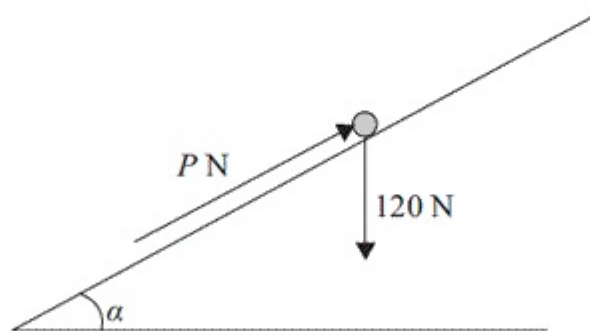


Figure 3

The horizontal force is removed and replaced by a force of magnitude  $P$  newtons acting up the slope along the line of greatest slope of the plane through the particle, as shown in Figure 3. The particle remains in equilibrium.

- (b) Find the greatest possible value of  $P$ . (8)
- (c) Find the magnitude and direction of the frictional force acting on the particle when  $P = 30$ . (3)
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## Question 7

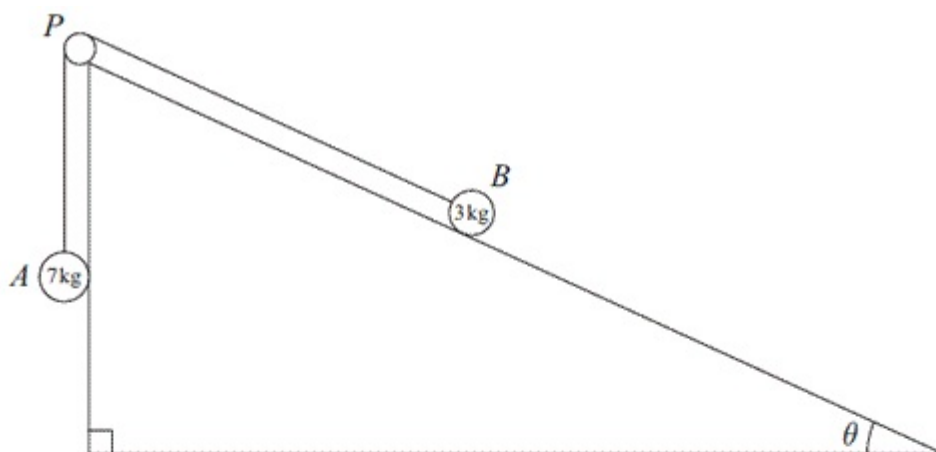


Figure 4

Two particles  $A$  and  $B$ , of mass  $7\text{ kg}$  and  $3\text{ kg}$  respectively, are attached to the ends of a light inextensible string. Initially  $B$  is held at rest on a rough fixed plane inclined at angle  $\theta$  to the horizontal, where  $\tan \theta = \frac{5}{12}$ . The part of the string from  $B$  to  $P$  is parallel to a line of greatest slope of the plane. The string passes over a small smooth pulley,  $P$ , fixed at the top of the plane. The particle  $A$  hangs freely below  $P$ , as shown in Figure 4. The coefficient of friction between  $B$  and the plane is  $\frac{2}{3}$ . The particles are released from rest with the string taut and  $B$  moves up the plane.

(a) Find the magnitude of the acceleration of  $B$  immediately after release. (10)

(b) Find the speed of  $B$  when it has moved  $1\text{ m}$  up the plane. (2)

When  $B$  has moved  $1\text{ m}$  up the plane the string breaks. Given that in the subsequent motion  $B$  does not reach  $P$ ,

(c) find the time between the instants when the string breaks and when  $B$  comes to instantaneous rest. (4)

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