

Topic 2: Physical Layer

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Digital Transmission in Computer Networks

- ✦ The purpose is to transfer a data sequence of 0s and 1s from a transmitter to a receiver
- ✦ It uses pulses or sinusoids to transmit binary information over a physical transmission medium
- ✦ We are particularly interested in the bit rate measured in bits/second (bps)

0110101...  0110101...

discrete symbols : finite symbol set $\{0, 1\}$
finite # possible symbols
finite # signal formats (pulses)

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$$\text{bit rate} = \frac{\# \text{ bits}}{\text{second}} = \frac{\# \text{ bits}}{\text{pulse}} \times \frac{\# \text{ pulses}}{\text{second}}$$

\uparrow Coding rate \uparrow Baud rate
 - pulse shape - Channel bandwidth
 - # diff pulses - Pulse shape

$$\left\{ \begin{array}{l} 1 \text{ bits per pulse} \\ 2 \\ \vdots \\ m \end{array} \right. \Rightarrow \left\{ \begin{array}{l} 2 \text{ diff pulses} \\ 4 \\ \vdots \\ 2^m \end{array} \right.$$

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Bit Rate vs. Baud Rate

⊕ Definitions

- ➡ Bit Rate = # of bits transmitted per second
- ➡ Baud Rate = # of signal transitions per second

⊕ Baud Rate depends on the channel bandwidth

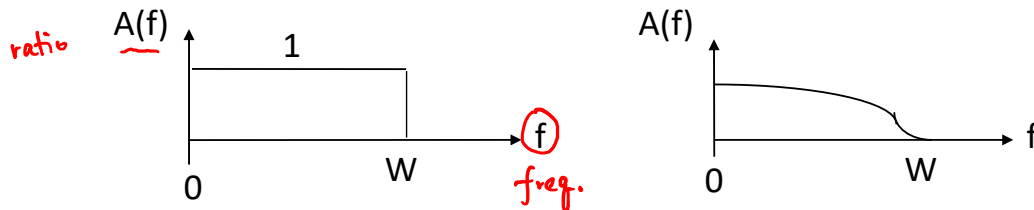
⊕ Bit Rate = (Baud Rate) × (# bits per pulse)

- ➡ It depends on the channel bandwidth as well as the coding scheme

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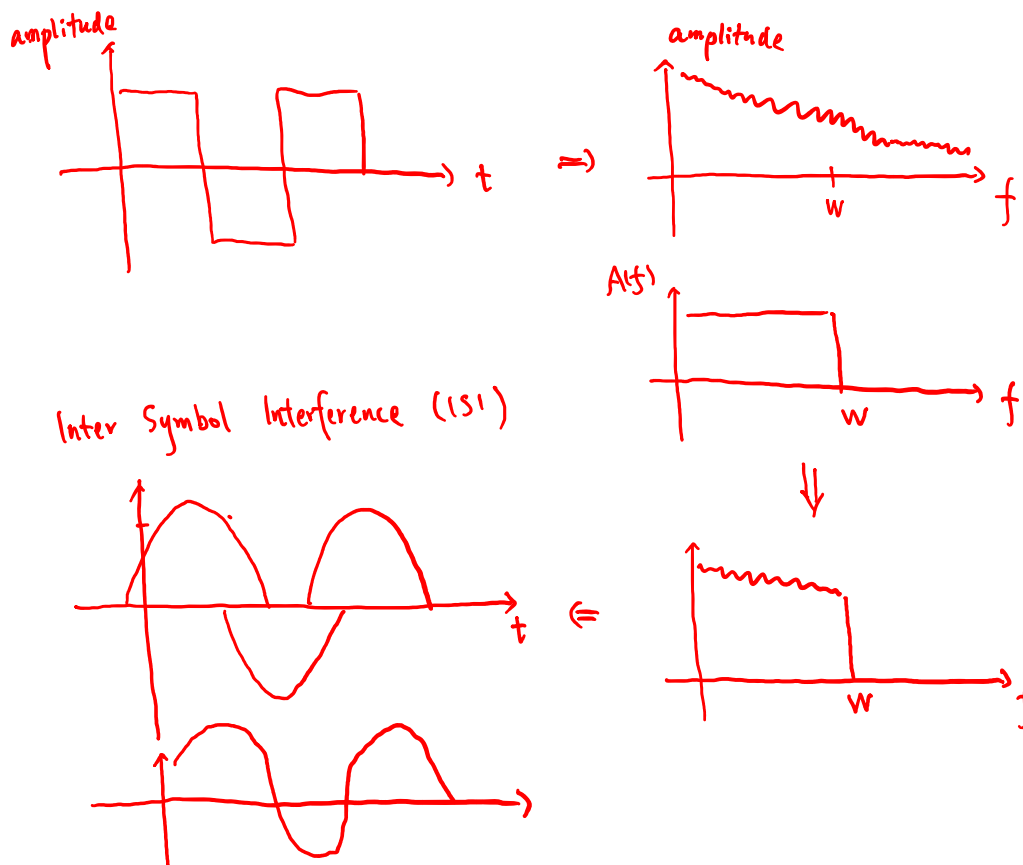
Transmission Channel and Channel Bandwidth

- ✦ A transmission channel can be characterized by its effect on input sinusoidal signals (tones) of various frequencies
- ✦ The ability of the channel to transfer a tone of **frequency f** is given by the **amplitude-response function $A(f)$** , which is defined as the ratio of the amplitude of the output tone to the amplitude of the input tone



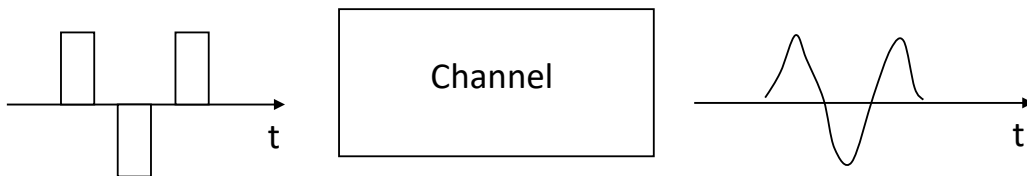
- ✦ The **bandwidth of a transmission channel (W)** is the range of frequencies that is passed by the channel

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Nyquist Rate

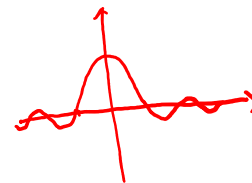


Nyquist Pulse : sinc function
 $\text{sinc}(x) = \begin{cases} 1 & \text{for } x=0 \\ \frac{\sin(x)}{x} & \text{else} \end{cases}$

- The fastest rate at which (ideal) pulses can be transmitted over the channel (called the Nyquist Rate) is:

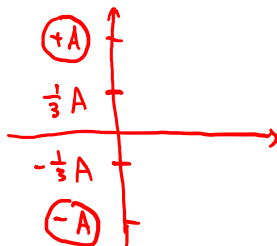
$$r_{\max} = 2W \text{ pulses/second}$$

max. Band rate

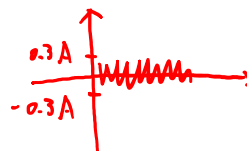


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Signal

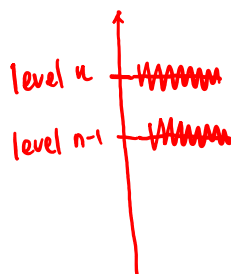


additive noise



max coding rate = ?

min separation between pulse levels
 $= 0.3 - (-0.3) = 0.6 A$



$$\left\lfloor \frac{A - (-A)}{0.6 A} \right\rfloor + 1 = 4 \text{ levels} \\ \Rightarrow 2 \text{ bits/pulse}$$

"line coding"

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Multilevel Pulse Transmission

- ✦ Assume channel bandwidth of W
- ✦ If pulse amplitudes are either $-A$ or $+A$, then each pulse conveys 1 bit,
Bit Rate = $(2W \text{ pulses/sec}) \times (1 \text{ bit/pulse}) = 2W \text{ bps}$
- ✦ If amplitudes are from $\{-A, -A/3, +A/3, +A\}$, then each pulse conveys 2 bits,
Bit Rate = $(2W \text{ pulses/sec}) \times (2 \text{ bits/pulse}) = 4W \text{ bps}$
- ✦ By going with $M = 2^m$ amplitude levels, we achieve
Bit Rate = $(2W \text{ pulses/sec}) \times (m \text{ bits/pulse}) = 2mW \text{ bps}$
- ✦ In the absence of noise, the bit rate can be increased without limit by increasing the pulse level m

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Noise & Reliable Communication

- ✦ All physical systems have noise
 - Electrons always vibrate at non-zero temperature
 - Motion of electrons induces noise
- ✦ Presence of noise limits the accuracy of measurement of received signal amplitude
- ✦ Noise places a limit on how many amplitude levels can be used in multilevel pulse transmission
- ✦ Errors occur if signal separation is comparable to noise level
- ✦ Bit Error Rate (BER) increases with decreasing Signal-to-Noise Ratio (SNR)

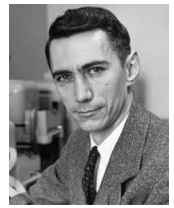
$$= \frac{\text{avg. signal power}}{\text{avg. noise power}}$$

$$10 \log_{10}(\text{SNR}) = \text{SNR in dB}$$

$\frac{10000}{10} \quad 40 \text{ dB}$
 $\quad \quad 10 \text{ dB}$

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Shannon Channel Capacity



$$C = W \log_2 (1 + \text{SNR}) \text{ bps}$$

Handwritten notes:
BW (above W) with an arrow pointing to W
absolute value ratio (above SNR) with an arrow pointing to SNR

- ⊕ Channel Bandwidth (W) & Signal to Noise Ratio (SNR) determine C
- ⊕ If transmission rate $R > C$, reliable communication is not possible
- ⊕ If transmission rate $R \leq C$, arbitrarily reliable communication is possible
 - ➡ “Arbitrarily reliable” means the BER can be made arbitrarily small through sufficiently complex coding
- ⊕ The relation between R_{\max} and C is used as a measure of how well a communication system is designed

Handwritten notes:
AWGN channel
Additive White Gaussian Noise

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Example

- ⊕ Find the Shannon channel capacity for a telephone channel with
 $W = 3.4 \text{ KHz}$ and $\text{SNR (dB)} = 40 \text{ dB}$

$$\begin{aligned} C &= W \cdot \log_2 (1 + \text{SNR}) \\ &= 3.4 \text{ KHz} \cdot \log_2 (1 + 10000) \\ &= 45.2 \text{ Kbps} \end{aligned}$$

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Example

- ⊕ Consider an AWGN channel with a bandwidth of 27 KHz and SNR = 35 dB. Is it possible to transmit reliably over this channel at $R = 350$ Kbps?

bit rate

$$\begin{aligned} C &= W \cdot \log_2(1 + \text{SNR}) \\ &= 27 \text{ KHz} \cdot \log_2(1 + 3162) \\ &= 313.93 \text{ Kbps} \\ &< R = 350 \text{ Kbps} \end{aligned}$$
$$\begin{aligned} 35 \text{ dB} &= 10 \log_{10}(\text{SNR}) \\ \Rightarrow \text{SNR} &= 10^{3.5} \\ &= 3162 \end{aligned}$$

so: not possible

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Example

- ⊕ Consider an AWGN channel with a bandwidth of 27 KHz. To transmit reliably over this channel at 200 Kbps, what is the minimum required SNR?

$$\begin{aligned} C &= W \cdot \log_2(1 + \text{SNR}) \geq 200 \text{ Kbps} \\ 27 \text{ KHz} \cdot \log_2(1 + \text{SNR}) &\geq 200 \text{ Kbps} \\ \text{SNR} &\geq \left(2^{\frac{200}{27}} \right) - 1 \\ &\approx 169 \text{ dB} \\ \Rightarrow 10 \log_{10}(169) &\approx 22.3 \text{ dB} \quad \checkmark \end{aligned}$$

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