

## HW5 - Coms 311

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1.

Vertex	s	t	x	y	z
Initial Values	0	$\infty$	$\infty$	$\infty$	$\infty$
Iteration 1	0	6	$\infty$	7	$\infty$
Iteration 2	0	6	4	7	2
Iteration 3	0	2	4	7	2
Iteration 4	0	2	4	7	-2

2.

a)

$$\text{LCS}(\text{String } s1, \text{String } s2, \text{int } m, \text{int } n) = \begin{cases} 0 & \text{if } i = 0 \text{ or } j = 0 \\ 1 + \text{LCS}(s1, s2, m-1, n-1) & \text{if } s1[m] = s2[n] \\ \max(\text{LCS}(s1, s2, i-1, j), \text{LCS}(s1, s2, i, j-1)) & \text{otherwise} \end{cases}$$

b)

```
LCS(String s1, String s2)
    HashMap<String, Integer> map = new HashMap<String, Integer>();

    int m = s1.length();
    int n = s2.length();

    for(int i = 0; i <= m; i++)
    {
        for(int j = 0; j <= n; j++)
        {
            if(i == 0 || j == 0)
            {
                map.put(i + ", " + j, 0);
            }
            else if(s1.charAt(i - 1) == s2.charAt(j - 1))
            {
                int val = 1 + map.get((i-1) + ", " + (j-1));
                map.put(i + ", " + j, val);
            }
        }
    }
}
```

```

        }
        else
        {
            int val = Math.max(map.get((i-1) + ", " + j), map.get(i + ", " + (j-1)));
            map.put(i + ", " + j, val);
        }
    }
}

return map.get(m + ", " + n );

```

c)

Runtime =  $O(n * m)$ , this is because you have to run through both loops one going  $n$  times the other going  $m$  times. All operations inside of the inside loop are constant time assuming constant lookup time for the dictionary.