Programming in Python

Lecture 2
Numeral systems.
Real numbers.

Strings

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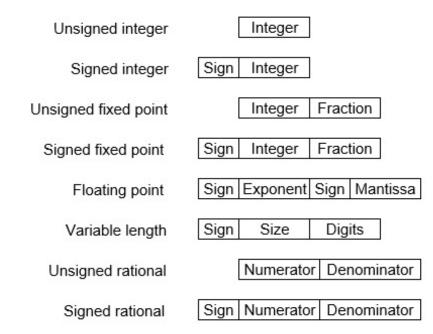
- → Real numbers
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Type float

- Limited precision. Use them only if integers are completely impossible to use.
- Type conversion float().
- You can use real numbers together with integers in one expression.
 The result will be a float.
- → Type float has the same set of arithmetic operations as the integer, except integer division.
- ◆ Operation division (X/Y) always has a real result, even if X and Y are both integers.

Float. Numbers representations

- Digital Computers use Binary number system to represent all types of information inside the computers.
- There are two major approaches to store real numbers (i.e., numbers with fractional component) in modern computing:
 - Fixed Point Notation. There are a fixed number of digits after the decimal point: 0.000011
 - Floating Point Notation. Allows for a varying number of digits after the decimal point: 11E-6



Fixed-point representation

Has fixed number of bits for integer part and for fractional part.

Example: Assume number is using 32-bit format which reserve 1 bit for the sign, 15 bits for the integer part and 16 bits for the fractional part. Then, -43.625 is represented as following:

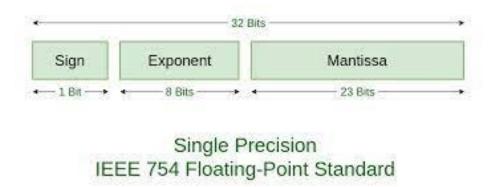
1	000000000101011	10100000000000000
Sign bit	Integer part	Fractional part

Where, in **Sing bit** 0 is used to represent '+' and 1 is used to represent '-'. 000000000101011 is 15-bit binary value for decimal 43 and 101000000000000 is 16-bit binary value for fractional 0.625.

The advantage of using a fixed-point representation is performance and disadvantage is relatively limited range of values that they can represent.

Floating point representation

- → Does not reserve a specific number of bits for the integer or fractional parts.
- → It has two parts: the first represents a signed fixed-point number called mantissa. The second part denotes the position of the decimal point and is called the exponent.
- Only the Mantissa and the Exponent are physically represented in the memory (including their signs).



Most common for Python – using 64 bits to store type *float*. 1 bit for sign, 52 – mantissa, 11 – exponent.

Floating point representation

Example: Suppose number is using 32-bit format: the 1-bit - sign bit, 8 bits for signed exponent, and 23 bits for the fractional part.

Then -53.5 is normalized as -53.5= $(-110101.1)_2$ = $(-1.101011)^*2^5$, which is represented as following below,

Where 00000101 is the 8-bit binary value of exponent value +5.

Note that 8-bit exponent field is used to store integer exponents $-126 \le n \le 127$.

1	00000101	101011000000000000000000000000000000000
Sign bit	Exponent part	Mantissa part

Real numbers

For output a real number in a fixed-point notation use the method *format():*

```
x= 0.1
print('{0:.25f}'.format(x))

0.1000000000000000055511151
```

Two real numbers are equal if they differ by no more than epsilon:

$$X - Y < \epsilon$$

```
if 0.1 + 0.2 == 0.3:
    print('All right!')
else:
    print('What?')
```

Real numbers. Accuracy

Let's see at the real number X as at the line segment : $[X - \mathcal{E}; X + \mathcal{E}]$.

Example. Let X and Y be real numbers with accuracy 6 decimal places, $\mathcal{E} = 5 * 10^{-7}$ and $|X| < 10^{9}$, $|Y| < 10^{9}$.

In worst case, when X and Y equal 10^9 and maximum deviation: $(X + \mathcal{E}) * (Y + \mathcal{E}) = XY + (X + Y) * \mathcal{E} + \mathcal{E}^2$, the value of \mathcal{E}^2 is negligible, XY - right answer, $(X + Y) * \mathcal{E}$ inaccuracy.

```
(X + Y) * \mathcal{E} = 2 * 10^{9} * 5 * 10^{-7} = 10^{3}
Absolute accuracy is 1000 \odot
```

```
x = float(input())
y = float(input())
epsilon = 5 * 10**-7
if abs(x - y) < 2 * epsilon:
    print('Equal')
else:
    print('Not Equal')</pre>
```

Real numbers rounding

- int discard the fractional part
- → round rounds to the nearest integer;
 if there are several nearest integers, then to even
- → floor rounds down
- ◆ ceil rounds up

	<pre>import math</pre>
print	<pre>(math.floor(-2.5))</pre>
print	<pre>(math.ceil(-2.5))</pre>

function	2.5	3.5	-2.5
int	2	3	-2
round	2	4	-2
floor	2	3	-3
ceil	3	4	-2

```
from math import
    floor, ceil
print(floor(-2.5))
print(ceil(-2.5))
```

while loop

The *while* statement allows you to repeatedly execute the *statements1* command block while the *test1* condition is satisfied. It may also have an optional *else* clause.



Example. **Print in increasing order all numbers from 1 to N**:

```
n = int(input ())
i = 1 # counter
while i <= n:
    print(i)
    i = i + 1</pre>
```

Example. Search for the minimum sequence of numbers ending by zero:

```
now = int(input ())
nowMin = now
while now != 0:
    if now < nowMin:
        nowMin = now
        now = int(input ())
print(nowMin)</pre>
```



```
Example. Guess the number.
number = 23
running = True
while running:
     guess = int(input(Input integer: '))
     if guess == number:
        print(Congratulations, you are right!')
       running = False # stop the loop while
     elif guess < number:
         print(No, the number guessed is bigger than this. ')
     else:
         print(No, the number guessed is smaller than this.')
else: print('the end of while')
# Here you can do anything else you need
print(The end.')
```



Break & continue

The meaningful use of **break** is possible only if some condition is met, that is, **break** should be called only inside the **if** (inside the loop). Using **break** is a bad tone; it's best to do without it.

```
i = 1
while True :
    print(i)
    i = i + 1
    if i > 100:
        break
```

The *continue* command starts the execution of the loop body again, starting with checking the condition. It should be used if, starting from some place in the body of the loop, under certain conditions, further execution is undesirable.

Example. Print all the positive numbers in the sequence:

```
now = -1 # the variable is initialized with a known appropriate value
while now != 0:
    now = int(input ())
    if now <= 0:
        continue;
    print(now)</pre>
```



for loop

When the interpreter executes a *for* loop, it alternately, one by one assigns the elements of the sequence object to the loop variable and executes the loop body for each of them. To access the current element in a sequence, the loop variable is usually used in the body of the loop, as if it were a cursor that moves from element to element.

After exiting the loop, the variable <target> usually still refers to the last element of the sequence if the loop was not finished by the break statement.

Loop often uses function **range** as an iterable object. It has three types of records: with one, two or three integer parameters.

- 1) range(a) generates iterable, which contains consecutive numbers from 0 to a-1
- 2) range(a, b) generates iterable with integers from a to b-1 inclusive
- 3) range(a, b, c) generates iterable with integers from a to b-1 inclusive with step c



Number systems.

- 1. What is a number system?
- 2. A bit of history.
- 3. Positional number systems. Conversion.
- 4. Mixed-based systems.

1. What is a number system?

Meaning I: A collection of things (usually called numbers) together with operations on those numbers and the properties that the operations satisfy.

Example: The counting numbers (1, 2, 3, ...) together with the operations of addition, subtraction, multiplication, and division and the properties they satisfy.

Meaning II: A system for representing numbers of a certain type.

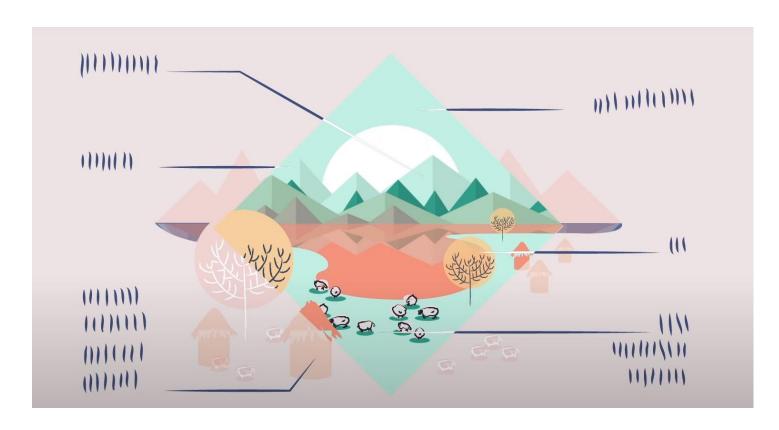
Example: The usual "base ten" or "decimal" system: 1, 2, 3, ..., 10, 11, 12, ... 99, 100,

- Roman numerals: I, II, III, IV, V, VI, VII, VIII, IX, X, ...
- The binary system: 1, 10, 11, 100, 101, ...(read as "one", "one, zero", "one, one", "one, zero, zero", etc.)

Meaning III: A combination of Meanings I and II. In other words, a collection of numbers together with operations, properties of the operations, and a system of representing these numbers.

Example: If we consider the counting numbers as a number system using **Meaning I, it doesn't matter** whether we expressed 4 as 4 (decimal), IV (Roman numeral), or 100 (binary), but using **Meaning III, it will matter.**

2. A bit of history



- Animals in a flock
 - ...
- Members in a tribe

https://ed.ted.com/lessons/a-brief-history-of-numerical-systems-alessandra-king

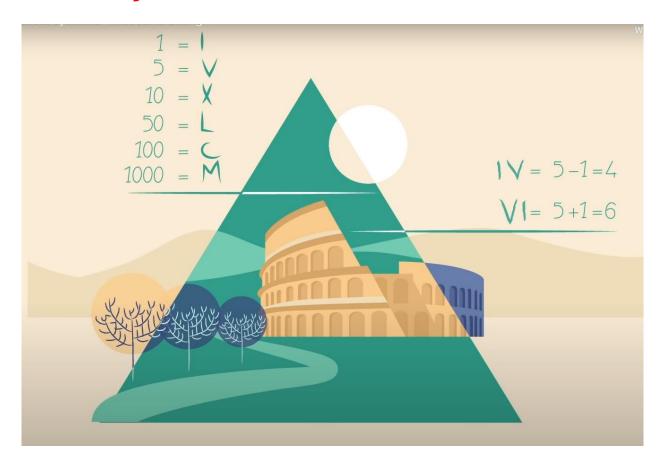
As the complexity of life increased, along with the number of things to count, these methods were no longer sufficient.



Different civilizations came up with ways of recording higher numbers.

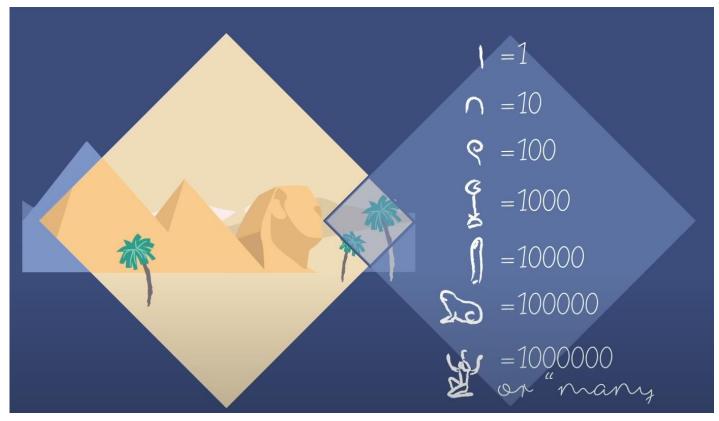
Many of them were **just extensions of tally marks** with new symbols added to represent larger magnitudes of value.

Roman number system

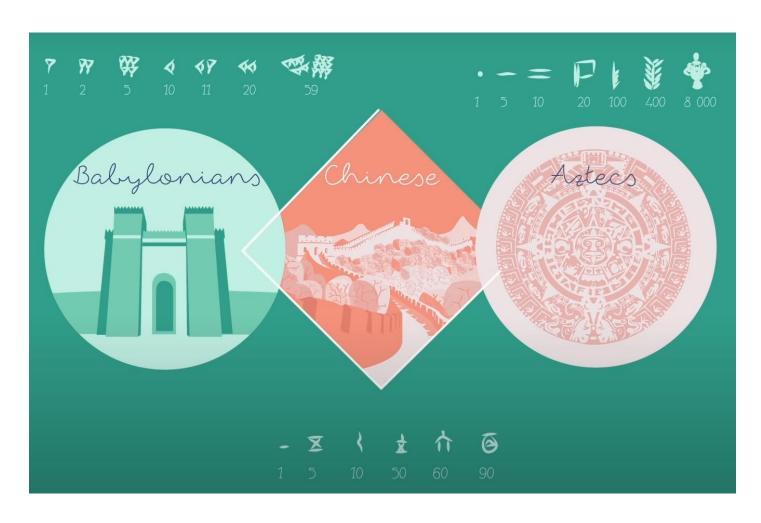


If a numeral appeared before one with a higher value, it would be subtracted rather than added.

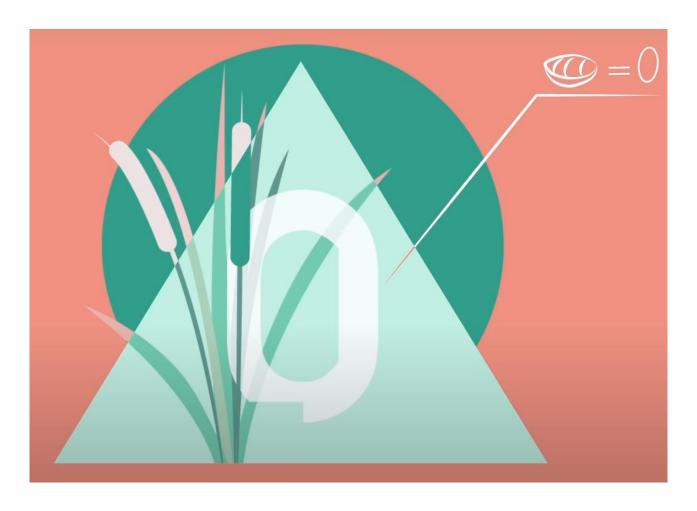
Egyptian number system



It was needed to draw many symbols repeatedly and invent a new symbol for each larger magnitude.



A positional system could reuse the same symbols, assigning them different values based on their position in the sequence



A key breakthrough of this system, which is also independently developed by the Mayans, was the **number zero**.

3. Positional number systems

b – base of number system: the number of different digits used in this system

$$(a_i a_{i-1} ... a_2 a_1 a_0, a_{-1} ...)_b = a_i b^i + a_{i-1} b^{i-1} + + a_2 b^2 + a_1 b^1 + a_0 b^0 + a_{-1} b^{-1} + ...$$

$$13_{10} = 15_8 = 23_5 = 1101_2$$

$$253_7 = 2^*7^2 + 5^*7^1 + 3^*7^0$$
 Convert to base 10: $2^*49 + 5^*7 + 3^*1 = 136_{10}$

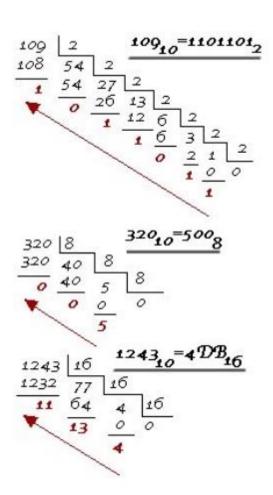
$$1302,2_4 = 1*4^3 + 3*4^2 + 0*4^1 + 2*4^0 + 2*4^{-1} =$$

=1*64 +3*16 + 0*4 + 2*1 + 2*0.25 = 64 + 48 + 2 + 0.5 = 114,5₁₀

Conversion from decimal

In general, to converse the integer part of a number from the decimal to a system with some other base:

- Perform sequential division with the remainder of the original number and each resulting quotient by new base
- Write the calculated residuals starting from the last one (i.e. in reverse order)



Conversion from decimal

To converse the fractional part of a number into other number systems, you need to turn the integer part to zero and start multiplying the resulting number by the base of the new system.

If, as a result of multiplication, whole parts appear again, they must be turned to zero, having previously memorized their values. The operation ends when the fractional part becomes zero or the required accuracy is achieved.

```
10,625<sub>10</sub> \rightarrow base 2

0,625*2 = 1,25

0,250*2 = 0,5

0,5*2 = 1,0

10,625<sub>10</sub> = (1010), (101) = 1010,101<sub>2</sub>
```

Conversion from decimal

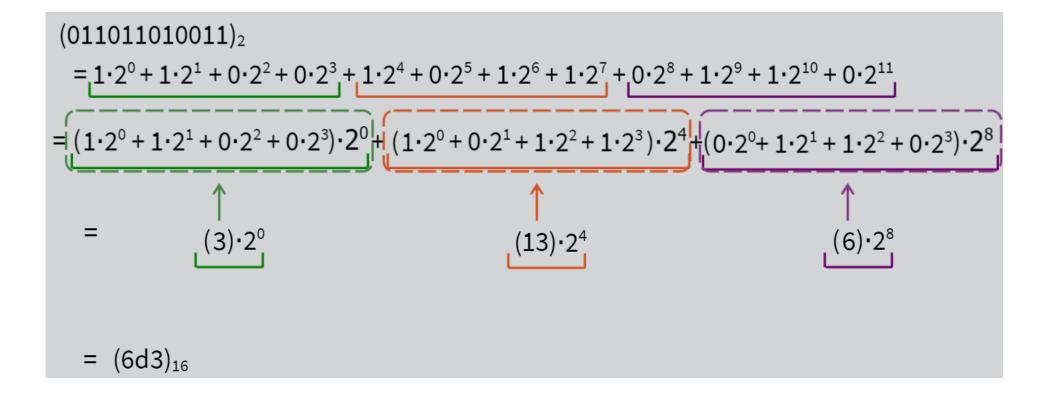
Binary ←→ hexadecimal

Hex Digit	4 Bit Binary	Hex Digit	4 Bit Binary
0	0000	8	1000
1	0001	9	1001
2	0010	а	1010
3	0011	b	1011
4	0100	С	1100
5	0101	d	1101
6	0110	е	1110
7	0111	f	1111

$$(3b9)_{16} = (001110111001)_2$$

$$(011011010011)_2 = (6d3)_{16}$$

Binary ←→ hexadecimal



Mixed-based systems

In each digit (position) of the number, the set of valid values may differ from the sets of other digits.

The time measurement system:

- ◆ seconds and minutes from "00" to "59"
- ♦ hours from "00" to "23"
- → days 365

The digit a_i in any number $a_n a_{n-1} ... a_0$ lies in the range 0 to R_i , where R_i is not the same for every i. The number is then interpreted as

$$(...(a_nR_{n-1}) + a_{n-1})R_{n-2} + ... + a_1)R_0 + a_0$$

Example:

122 days 17 hours 35 minutes 22 seconds =

$$((((1\times10)+2)10+2)24+17)60+35)60+22$$
 seconds

Python data types

Python has 4 types categories:

- ◆ Numbers (integer, real, complex). Supports addition, multiplication, etc.
- ◆ Sequencies (string, list, tuple). Support indexing, slice extraction, concatenation, etc..
- → Mappings (Dictionaries). Support key indexing operation, etc.
- ◆ **Sets.** They form a separate category of types (they do not map keys to values and are not ordered sequences).

Built-in types

- → Built-in objects simplify the creation of programs. Since they eliminate the need to implement own data structures.
- → Built-in objects give the possibility to quick extension. To solve complex problems, the user can create his own objects using the built-in classes of the Python language.
- → Built-in objects are often more efficient than user-created data structures. They use the already optimized data structures implemented in the C language to achieve high performance.
- → Built-in objects are a standard part of the language. Python takes a lot from languages that rely on the use of built-in tools (such as LISP) as well as from languages that rely on the skill of a programmer who must implement their own data structures (such as C ++). In Python, you can create your own types of objects, but this is not recommended at the very beginning. Moreover, built-in components are standard components of the Python language, they always remain unchanged, while user's structures can be unexpectedly changed.

Object generation

Object type	Example literals/creation
Numbers	1234, 3.1415, 3+4j, Ob111, Decimal(), Fraction()
Strings	'spam',"Bob's",b'a\x01c',u'sp\xc4m'
Lists	<pre>[1, [2, 'three'], 4.5], list(range(10))</pre>
Dictionaries	<pre>{'food': 'spam', 'taste': 'yum'},dict(hours=10)</pre>
Tuples	<pre>(1, 'spam', 4, 'U'),tuple('spam'),namedtuple</pre>
Files	open('eggs.txt'),open(r'C:\ham.bin', 'wb')
Sets	set('abc'),{'a', 'b', 'c'}

A literal is an expression that generates an object.

Python does not have a type declaration construct; the syntax of executed expressions itself defines the types of objects to be created and used.

As soon as an **object** is **created**, it will be **associated with its own set of operations** throughout its existence - only string operations for strings, only list operations for lists, etc.

Strings

Strings are used to write text information, as well as sequences of bytes.

As a sequence a string **support the order of elements**, from left to right: elements are stored and retrieved based on their positions in the sequences.

Strictly speaking, strings are sequences of characters.

```
>>> S = 'Spam' #A variable is
created when it is assigned a value.
>>> len(S) # length
4
>>> S[0] # The first element
'S'
>>> S[1] # The second element
'p'
```

Reverse Indexing:

S[-1] # The last element S[-2] # The second element from the end S[len(S)-1] # The last element

Strings. Literals.

- 'spa"m'
- "spa'm"
- → ""... spam ..."", """... spam ..."""
- ◆ Escaped sequences allow you to insert characters that are difficult to enter from the keyboard: "s\tp\na\0m":

```
s p
am
```

- ♦ R "C:\new\test.spm" raw strings
- ♦ Byte string: b'sp\x01am'

Escaped sequences

Sequence	Description		
\\	The backslash character itself (one character \ remains)		
\'	Apostrophe (one character remains ')		
\"	Quotation mark (one character remains ")		
\b	Backspace		
\n	Newline (linefeed)		
\r	Carriage return		
\t	Horizontal tab		
\v	Vertical tab		
\xhh	Character with hex value hh (exactly 2 digits)		
\000	Character with octal value ooo (up to 3 digits)		
\0	Null: binary 0 character (doesn't end string)		
\N{id}	Unicode database ID		
\uhhhh	Unicode character with 16-bit hex value		
\Uhhhhhhhh	Unicode character with 32-bit hex valuea		

Often there are situations when you need to **make a string**, substituting some **data obtained during the execution** of the program.

1. % Operator

A format string containing one or more **format specifiers**, whose value should be substituted for the specifiers on the left side of the expression.

for example, % d (digit)) % <an object (or objects, in the form of a tuple)>.

Once you start using several parameters and longer strings, your code will quickly become much less easily readable

```
first_name = "Eric"
last_name = "Idle"
age = 74
profession = "comedian"
affiliation = "Monty Python"
print("Hello, %s %s. You are %s. You were a member of %s." %
(first_name, last_name, age, profession, affiliation))
```

Hello, Eric Idle. You are 74. You are a comedian. You were a member of Monty Python.

2. The format method

str.format() is an improvement on %-formatting, it uses normal function call syntax.
<Replacement Fields> .format parameters>

The replacement fields are marked by curly braces.

```
>>> '{}, {}, {}'.format('a', 'b', 'c')
                                      s1='a'; s2='b'; s3='c'
'a, b, c'
                                      print('{2}, {1}, {0}'.format(s1,
                                      s2, s3))
>>> '{0}, {1}, {2}'.format('a', 'b', 'c')
                                      c, b, a
'a, b, c'
>>> '{2}, {1}, {0}'.format('a', 'b', 'c')
'c, b, a'
person = {'name': 'Eric', 'age': 74}
print("Hello, {name}. You
are{age}.".format(name=person['name'],age=person['age']))
Hello, Eric. You are 74.
```

2. The format method

Code using *str.format()* is much more easily readable than code using *%-formatting*, but str.format() can still be quite verbose when you are dealing with multiple parameters and longer strings.

```
first name = "Eric"
last name = "Idle"
age = 74
profession = "comedian"
affiliation = "Monty Python"
print(("Hello, {first_name} {last_name}. You are {age}. " +
"You are a {profession}. You were a member of
{affiliation}.") \
.format(first_name=first_name, last_name=last_name,
age=age, \
profession=profession, affiliation=affiliation))
Hello, Eric Idle. You are 74. You are a comedian. You were a
```

member of Monty Python.

3. f-Strings

Also called "formatted string literals", *f-strings* are string literals that have an *f* at the beginning and curly braces containing expressions that will be replaced with their values.

```
name = "Eric"
age = 74
print(f"Hello, {name}. You are {age}.")
Hello, Eric. You are 74.
print(F"Hello, {name}. You are {age}.")
Hello, Eric. You are 74.
```

3. f-Strings

Because **f-strings** are evaluated at runtime, you can put any valid Python expressions in them.

```
>>> f"{2 *37}"
'74'

You could also call functions:

def to_lowercase(input):
    return input.lower()
    name = "Eric Idle"
    print(f"{to_lowercase(name)} is funny.")

eric idle is funny.
You also have the option of calling a method directly:

>>> f"{name.lower()} is funny."

'eric idle is funny.'
```

String operations

base	description	
len('abc') = 3	Length: number of elements	
'abc' + 'def' = 'abcdef'	Concatenation	
'Hi!' * 4 = 'Hi!Hi!Hi!Hi!'	Replication	
s[i]	Indexing by position	
s[i:j]	Slicing	
S.find('pa'); S.rfind('pa')	Search for a substring in a string (returns index of 1^{st} or last substring, or -1)	
'spam' in S	Is 'spam' in S?	
S.count('pa', i, j)	Count the number of occurrences of a substring in a slice [i :j] of the string S (till j-1)	
S.lstrip() и S.rstrip()	Removing whitespace from the beginning (Istrip) and the end (rstrip)	
S.replace('pa', 'xx')	Replacing one substring with another (all occurrences)	
S.split(',')	Separation by a character - separator	
S.isdigit()	Checking the string's content	
S.lower(); S.upper()	Character case conversion	
S.endswith('spam')	String ending check	
for c in mystr: print(c, end=' ')	Loop through string items	
s.rjust(n, 'c')	Increasing string s to length n by filling left with 'c'	

Slices

[start:end]
Indexes refer to places the knife "cuts."



Defaults are beginning of sequence and end of sequence.

Positive offsets are counted from the left end (the first element has an offset of 0), and negative ones are counted from the right end (the last element has an offset of -1).

S[i:j] - The offset to the left of the colon indicates the left border (inclusive), and to the right the upper border (it is not included in the slice).

If the left and right borders are omitted (:), the default values are 0 and the length of the object, respectively.

Slices

The full form of the substring extraction operation looks like this: S[i:j:k].

It means: **«Extract all elements of the sequence S, starting from offset i, up to offset j-1, in increments of k.»**

By default, k = 1. For k < 0, counting is performed in the opposite direction (from right to left).

```
>>> S='Spam'
>>> S[1:3] # Slice of the string S starting at offset 1 and up to 2
pa
>>> S[1:] # All exept the first element (1:len(S))
pam
>>> S[:3] # All exept the last element ( S[0:3])
Spa
>>> S[:-1] # All exept the last element
Spa
>>> S[:-1] # All exept the last element
Spa
>>> S[::-1]
```

String elements numbering

S	t	r	i	n	g
0	1	2	3	4	5
-6	-5	-4	-3	-2	-1

Immutable sequence

All operations on strings as a result create a new string, because strings in Python are immutable - once a string is created, it cannot be changed.

It is impossible to change a string by assigning a value to one of its positions, however, you can create a new string and give it the same name:

```
>>> S
Spam
>>> S[0] = 'z' # Immutable objects cannot be changed
... error message text omitted ...
>>> S = 'z' + S[1:] # But using expressions you can create new objects
>>> S
zpam
```

Numbers, strings and tuples are immutable, but lists and dictionaries are not (they can easily be changed in any part).

Example 1.

```
# Delete all symbols, which indexes are divided by 3.

s = input('Input a string: ')
for i in range(len(s)):
    if i % 3 != 0:
        print(s[i], end=")
print()
print('The end')
```

Examples 2 & 3 & 4.

```
# Double all characters except the 'o'
                                                        # Double all characters, to the character 'o'.
character.
                                                        Other characters do not display.
s = input()
                                                        s = input()
for i in s:
                                                        for i in s:
  if i == 'o':
                                                           if i == 'o':
     continue
                                                             break
  print ( i * 2, end=" )
                                                          print ( i * 2, end=" )
                         # Check if there is an 'o' in the string.
                         s = input()
                         for i in s:
                           if i == 'o':
                              print ("There is 'o' in the string")
                              break
                         else:
                            print ("There is not 'o' in the string")
```

Example 5.

```
# Display the message, and between each character it will display a '*'.

msg = input('Write a message: ')
for letter in msg:
    print(letter, end='*')

Hello
H*e*|*|*o*
```

Example 6.

Ask the user to type in their name and then tell them how many vowels are in their name

```
name = input('Enter your name: ')
count = 0
name = name.lower()
for x in name:
    if x == 'a' or x == 'e' or x == 'i' or x
== 'o' or x == 'u':
        count += 1
print("Vowels = ", count)
```

Yandex Contest

Message	Short	Meaning	Possible reason
ОК	ОК	The solution accepted	The program works correctly on the built set of tests
Compilation error	CE	Compilation error	 The program made a syntax or semantic error The language is incorrect
Wrong answer	WA	Wrong answer	1.error in the program2.incorrect algorithm
Presentation error	PE	The testing system cannot verify the output, as its format does not match the one described in the task conditions	1.Incorrect output format2.The program does not print the result3.Extra output
Time-limit exceeded	TL	Программа превысила установленный лимит времени	 ошибка в программе неэффективное решение
Memory limit exceeded	ML	The program has exceeded the memory limit	1.an error in the program (for example, infinite recursion)2.inefficient solution
Run-time error	RT	The program terminated with a non-zero return code	1. runtime error 2. a program in C or C ++ does not end with the operator return 0 3. a nonzero return code is specified explicitly