

# Ok Then, here it is

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## ABSTRACT

During the asymptotic giant branch (AGB) phase of stellar evolution for a  $2M_{\odot}$  star, the periodic thermal pulses have temperatures as high as  $2.9 \times 10^8$  K. The  $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$  reaction after the formation of the  $^{13}\text{C}$  pocket

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**Key words:** AGB – Diffusion Coefficient – Pre-solar Grains

## 1 INTRODUCTION

The Zr isotopes are produced from the  $s$ -process with  $^{56}\text{Fe}$  as the seed. To start the  $s$ -process the neutron densities must reach above  $1 \times 10^8 \text{ cm}^{-3}$  and get past the first peak for many of the Zr isotopes. One of the  $s$ -process sites in middle mass stars is during the thermal pulses caused by successive He-flashes during their asymptotic giant branch (AGB) phase. In between these thermal pulses the  $^{13}\text{C}$  pocket develops and through the  $^{13}\text{C}(\alpha, n)^{16}\text{O}$  reaction the  $s$ -process can occur. Then, this material will be mixed through a He-flash pulse driven convection zone (PDCZ) and the  $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$  reaction will activate the  $s$ -process for a short period of time. The neutron densities that are achieved through these two processes differs significantly and depends on the conditions in the star. The Zr isotopic ratios can be used to understand the conditions within the AGB stars as they are sensitive to the neutron densities that they are exposed to (Battino et al. 2016).

The  $^{95}\text{Zr}$  isotope is unstable with a lifetime of 64 days. Within the  $^{13}\text{C}$  pocket, the neutron densities do not get large enough to allow for this branch to open so most of the  $^{95}\text{Zr}$  will decay to  $^{95}\text{Mo}$  rather than undergo  $^{95}\text{Zr}(n, \gamma)^{96}\text{Zr}$ . This skews the isotopic ratios of  $^{96}\text{Zr} / ^{94}\text{Zr}$  as there will be production of  $^{94}\text{Zr}$  but almost none of  $^{96}\text{Zr}$  during the  $^{13}\text{C}$  pocket formation. However, once the He-flash PDCZ forms, the  $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$  reaction can generate neutron densities as large as  $1 \times 10^{10} \text{ cm}^{-3}$  which will open the branch for the  $^{95}\text{Zr}(n, \gamma)^{96}\text{Zr}$  to occur shifting the isotopic ratios again. Many of these thermal pulses happen throughout the AGB phase and some of the material left behind from the He-flash PDCZ can be mixed into the H envelope from the third dredge up that happens after. Due to the significant mass loss during the AGB phase, the isotopic ratios of Zr can be measured directly from the pre-solar SiC grains that form from the material lost during the AGB phase (Barzyk et al. 2006). Battino et al. (2016) compared the H envelope  $^{96}\text{Zr} /$

$^{94}\text{Zr}$  ratios produced in  $3M_{\odot}$  and  $2M_{\odot}$  stellar models with the ratios measured in SiC grains from Barzyk et al. (2006). The stellar model results overestimated the ratio in all models (Fig. 6).

The goal of this work is to test if minor changes, suggested by hydrodynamic simulations, to the diffusion coefficient as a function of mass will affect the Zr isotopic ratios that the He-flash PDCZ produces. The ratios that are computed with the changes to the diffusion coefficient will be compared to those without and their impact on results that (Battino et al. 2016) predicts will be discussed. The analysis will be conducted on a  $2M_{\odot}$ ,  $Z = 0.02$  stellar model.

\* Why problem is interesting\*

- Zr ratios in pre solar grains from AGB stars show isotopic signatures of material that left the star. - This is from envelope and Zr is produced in  $^{13}\text{C}$  pocket, then readjusted in the thermal pulse - Tracer of conditions that were in the star at that time

\* what have other people done \*

- battino tried varying  $f$  and how diffusion happens for effects (couldnt get ratios seen) - barzyk for xe128 ratio

\* My problem, the gap! \*

- Try a different functionality of diffusion coefficient, hydro leads to this form - It contains lower diffusion at base of convection zone, less  $^{22}\text{Ne}$  reaction, less Zr96

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## 2 METHODS AND MODELS

### 2.1 MESA Models

Only a  $2M_{\odot}$ ,  $Z = 0.02$ , stellar evolution model was used. This was computed using the MESA (Paxton et al. 2011) stellar code and taken from the NuGrid set1ext, set1.2 models (Ritter et al. 2017). These models were evolved from the pre-main sequence to a white dwarf. For this work, a singular thermal pulse, the  $24^{th}$ , was analyzed and a Kippenhahn diagram of this particular thermal pulse can be seen in Figure 1.

For these models, the mixing lengths theory (Cox & Giuli 1968), MLT, is used for the convection zones with a mixing length,  $\alpha_{MLT} = 1.73$ . Overshoot is implemented in MESA with the formula from Herwig (2000) and Freytag et al. (1996):

$$D = D_0 \exp^{-2z/fH_{p0}} \quad (1)$$

Where  $D_0$  and  $H_{p0}$  are taken at the convective boundary (§2.3). The models were also post processed with `mppnpas` part of the work done in (Ritter et al. 2017). The methods used in this work to post process the He-flash PDCZ are outlined in §2.5.

### 2.2 Neutron Density and Temperature

Within the PDCZ, there is a significant amount in mass fraction of  $^{22}\text{Ne}$  that has been produced as well as a high mass fraction of alpha particles. There are a lot of alpha particles from the H-shell burning products as well as the helium burning is not significant at this point (Fig. 1). Once temperatures reach close to  $T_8 \approx 2.8$  the  $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$  reaction is activated. This can be seen from the high neutron densities shown in Figs. 9 and ???. When looking at a particular model number, the neutron density as a function of mass within the convective boundaries has a significant peak near the lower boundary. This is due to the  $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$  reaction being very sensitive to temperature and a huge portion of the reactions will take place at the bottom of the convection zone. Then, the neutrons will diffuse and mix throughout the convection zone allowing for the *s*-process to take place again.

In Fig. 9 the average neutron density steadily rises until the maximum temperature that will occur within the convection zone and then slowly drops. This peak in the average neutron densities is very short lived as it is only sustained for a few years. However, this will have an impact on the isotopic ratios of  $^{94}\text{Zr}$  as discussed in §2.4. The importance of this is that some of the material from the PDCZ will be mixed to the H envelope from the periodic third dredge-up that occurs between thermal pulses (Fig. 1).

### 2.3 Diffusion Coefficient Modifications

The MESA models use the MLT and the diffusion equation to estimate how the mass fraction of isotopic species are transported and mixed throughout convection zones. To calculate the change in mass fraction of a particular species at a particular mass coordinate in time, the stellar evolution codes

solve the differential equation

$$\frac{d\mathbf{X}_i}{dt} = \left. \frac{d\mathbf{X}_i}{dt} \right|_{burn} + \left. \frac{d\mathbf{X}_i}{dt} \right|_{mix} \quad (2)$$

which contains the changes due to the possible reactions that the particular species can be involved in and the spatial diffusion of matter due to the mixing in a convection zone. Using the diffusion formalism, this mixing term is given by

$$\left. \frac{d\mathbf{X}_i}{dt} \right|_{mix} = \frac{\partial}{\partial m} [(4\pi r^2 \rho)^2 D(m) \frac{d\mathbf{X}_i}{dm}] \quad (3)$$

Where  $D(m)$  is the diffusion coefficient at mass coordinate  $m$ .

Using the MLT, the diffusion coefficient is given by

$$D = \frac{1}{3} v_{MLT} \alpha_{MLT} H_p \quad (4)$$

Where  $\alpha_{MLT} H_p$  is called the mixing length. If just using the MLT, this diffusion would immediately go to zero at the Schwarzschild boundary (convective boundary). The Schwarzschild boundary is the mass coordinate where the Schwarzschild criterion, the condition in which the gas will be convectively unstable, is located. The Schwarzschild criterion is when the condition

$$\nabla_{rad} > \nabla_{ad} \quad (5)$$

is satisfied.  $\nabla_{rad} = \left( \frac{\partial \ln T}{\partial \ln P} \right)_{rad}$  is the gradient that the star would have if all of the energy is transported by radiation while  $\nabla_{ad} = \left( \frac{\partial \ln T}{\partial \ln P} \right)_{ad}$  is the gradient from all of the energy being transported by convection.

The functionality of the MLT diffusion coefficient across the convection zone is similar to what is calculated from 3D hydrodynamic simulations. However, a main qualitative difference is that the diffusion coefficient begins to drop well before the convective boundary while the MLT diffusion coefficient will not. A model for the diffusion coefficient that has been able to reproduce results from 3D hydro simulations is provided by (Jones et al. 2017). The formula for the diffusion coefficient is

$$D_{hydro} = v_{MLT} \min(\alpha_{MLT} H_p, |r - r_0|) \quad (6)$$

where  $r_0 = r_{SC} - f_{CBM} H_p^{SC}$  which are quantities that are evaluated at the Schwarzschild boundary. This does not make major changes to the functionality and magnitude of the diffusion coefficient except that it falls off quicker when approaching the convective boundaries. This can be seen in Figure 7. With the temperature being highest at the lower convective boundary (Fig. ???) and with using Equation (6) for the diffusion coefficient rather than Equation (4), there would be less matter diffusing to the higher temperatures of the lower boundary. The possible nucleosynthetic consequences of this are discussed in §2.4 and shown in §3.1.

### 2.4 $^{95}\text{Zr}$ and $^{128}\text{I}$ Branching

Within the  $^{13}\text{C}$  pocket, the reaction that causes the high neutron densities for the *s*-process is  $^{13}\text{C}(\alpha, n)^{16}\text{O}$ . The neutron densities do not reach  $N_n \approx 5 \times 10^8 \text{ cm}^{-3}$  that are required to open the  $^{95}\text{Zr}$  branch (Battino et al. 2016). This causes a situation in which there is production of  $^{94}\text{Zr}$  from the *s*-process but due to low neutron densities not as much  $^{96}\text{Zr}$  is produced. This can be seen from the isotope mass

fractions of Zirconium in Fig. 2. The  $s$ -process path and  $^{95}\text{Zr}$  branch can be seen in Figure 4

During the He-flash PDCZ temperatures get high enough for the  $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$  reaction to occur. Neutron densities can exceed the lower limit for the  $^{95}\text{Zr}$  branching (Fig. 9). This will shift the isotopic mass fractions of  $^{96}\text{Zr}$  and  $^{94}\text{Zr}$  to what is shown in Figure 3. Their mass fractions dropped significantly due to the dilution of the  $^{13}\text{C}$  pocket into the PDCZ however the change in the ratio,  $\log_{10}(^{96}\text{Zr} / ^{94}\text{Zr})$ , went from -2.7 to -0.9. This is directly from the opening of the  $^{95}\text{Zr}$  branch. This branch is only open for a very short amount of time as the neutron density is only larger than  $5 \times 10^8 \text{ cm}^{-3}$  for a few years (Fig. 9) but its effects on the Zirconium isotopic ratios are significant.

To compare with the measurements made by (Barzyk et al. 2006), the isotopic ratios need to be represented into the per mil,  $\delta$ , form. For a given isotopic ration, this is defined as

$$\delta(^{96}\text{Zr}/^{94}\text{Zr}) = \left[ \left( \frac{^{96}\text{Zr}}{^{94}\text{Zr}} / \frac{^{96}\text{Zr}_{\odot}}{^{94}\text{Zr}_{\odot}} \right) - 1 \right] \times 1000 \quad (7)$$

The comparison of  $\delta(^{96}\text{Zr}/^{94}\text{Zr})$  from the pre-solar grains measured by (Barzyk et al. 2006) and what stellar evolution models predict from (Battino et al. 2016) is in Figure 6.

The  $^{128}\text{I}$  isotope is unstable with a lifetime of only 25 minutes and it has two competing branches. These reactions are the  $\beta^-$  decay,  $^{128}\text{I}(\beta^-)^{128}\text{Xe}$  and the electron capture  $^{128}\text{I}(\beta^+)^{128}\text{Te}$ . The electron capture branching is very sensitive to the temperature as well as the electron density (Reifarth et al. 2004). Figure 5 shows all of the isotopes that play a role in the  $^{128}\text{I}$  branching. Within the He-flash PDCZ the temperature peaks very close to the lower convective boundary. With the convective time scale (§2.5) during the PDCZ being only a few hours, fresh  $^{126}\text{I}$  from the top of the convection zone will come to the bottom and can capture a neutron easily due to the very high neutron densities there. With the short half-life of  $^{128}\text{I}$ , a significant portion of these will decay while being at the higher temperatures near the lower convective boundary. This will lead to a significant portion of the [128] to undergo  $^{128}\text{I}(\beta^+)^{128}\text{Te}$  rather than  $^{128}\text{I}(\beta^-)^{128}\text{Xe}$ . Since the  $p$ -process is not occurring within the He-flash PDCZ, the only production of  $^{128}\text{Xe}$  comes from the  $^{128}\text{I}(\beta^-)^{128}\text{Xe}$  and the losses are due to neutron captures. Because of this, the  $^{128}\text{Xe} / ^{130}\text{Xe}$  ratio can be used as a tracer of what the dominating branch of  $^{128}\text{I}$  is.

## 2.5 mppnp Post Processing

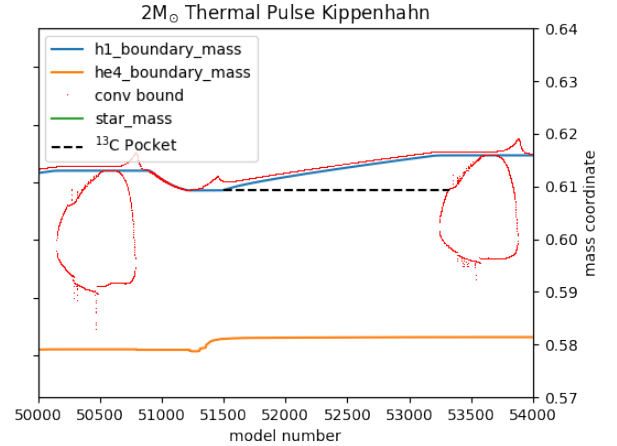
## 3 RESULTS

### 3.1 Effects on $\delta(^{96}\text{Zr} / ^{94}\text{Zr})$

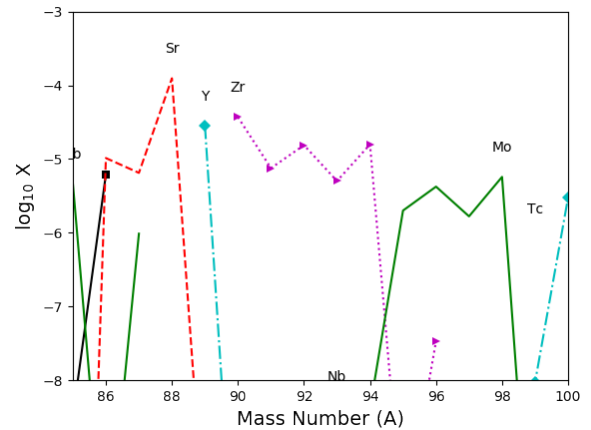
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$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad (8)$$

Refer back to them as e.g. equation (8).



**Figure 1.** Within the He intershell region, the  $^{13}\text{C}$  pocket forms and isotopic ratios are set by the  $s$ -process (Fig. 2). It is then mixed and diluted in the He-flash pulse driven convection zone where temperatures get high enough to activate  $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$ . This shifts the isotopic ratios to those shown in Figure 3



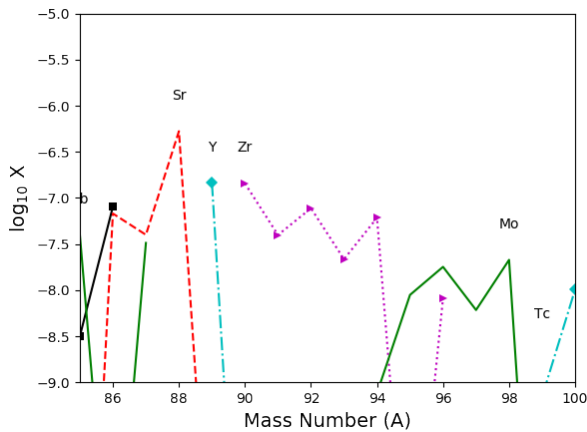
**Figure 2.** These isotope ratios are averaged across the  $^{13}\text{C}$  pocket. Within the  $^{13}\text{C}$  pocket there is a significant amount of  $^{94}\text{Zr}$  produced but almost no  $^{96}\text{Zr}$ . This is due to the low neutron densities not opening the  $^{95}\text{Zr}$  branch. The logarithm base 10 of the  $^{96}\text{Zr} / ^{94}\text{Zr}$  ratio is approximately -2.7

## 4 CONCLUSIONS

The last numbered section should briefly summarise what has been done, and describe the final conclusions which the authors draw from their work.

## ACKNOWLEDGEMENTS

The Acknowledgements section is not numbered. Here you can thank helpful colleagues, acknowledge funding agencies, telescopes and facilities used etc. Try to keep it short.



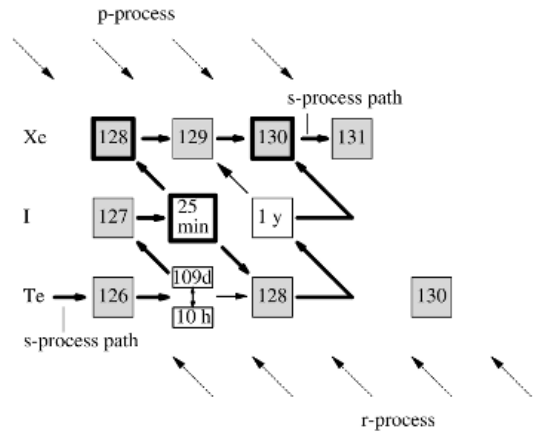
**Figure 3.** These isotope ratios are averaged across the He-flash PDCZ. After the  $^{13}\text{C}$  pocket is mixed into the He-flash pulse driven convection zone, the temperatures get high enough for the  $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$  reaction. This provides high enough neutron densities to open the  $^{95}\text{Zr}$  branch and boost the  $^{96}\text{Zr}$ . The logarithm base 10 of the  $^{96}\text{Zr} / ^{94}\text{Zr}$  ratio is approximately -0.9



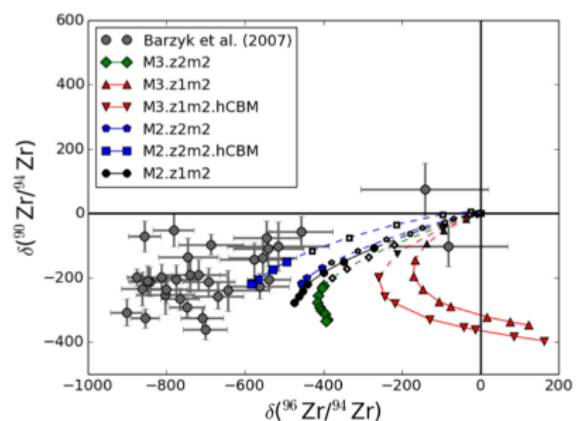
**Figure 4.** In order for there to be significant production of  $^{96}\text{Zr}$  the neutron densities must be high enough such that the  $^{95}\text{Zr}$  (half-life 64 days) formed from the reaction  $^{94}\text{Zr}(n, \gamma)^{95}\text{Zr}$  does not all decay to  $^{95}\text{Nb}$ .

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**Figure 5.** The unstable isotope,  $^{128}\text{I}$ , can either  $\beta^-$  decay or capture an electron ( $\beta^+$ ). The electron capture branching is very sensitive to the temperature. If it  $\beta^-$  decays there will be production of  $^{128}\text{Xe}$  and with high neutron densities,  $^{130}\text{Xe}$  can be produced as well. If it captures an electron, it can capture neutrons and decay to end up at  $^{130}\text{Xe}$ . This figure is from (Reifarth et al. 2004).

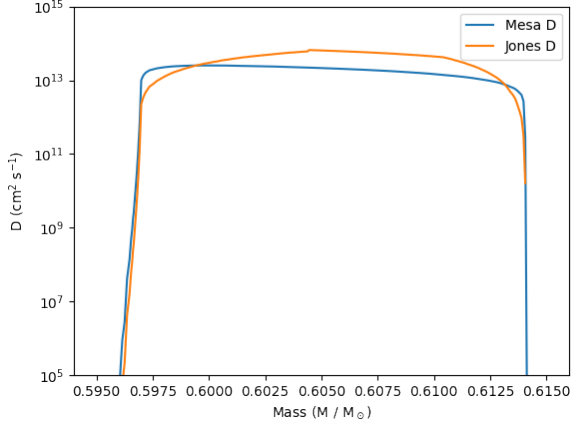


**Figure 6.** This is the Zr94 mil plot Battino et al. (2016).

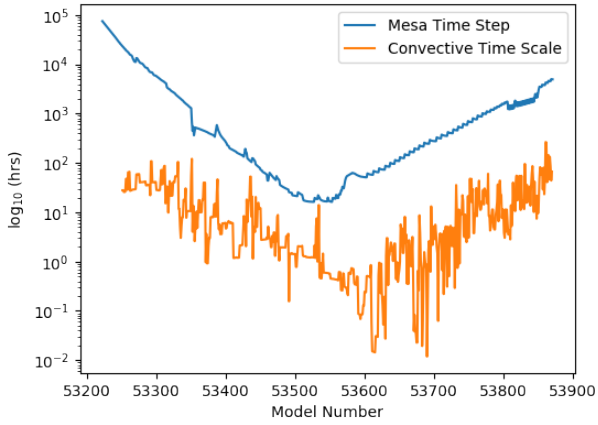
## APPENDIX A: SOME EXTRA MATERIAL

If you want to present additional material which would interrupt the flow of the main paper, it can be placed in an Appendix which appears after the list of references.

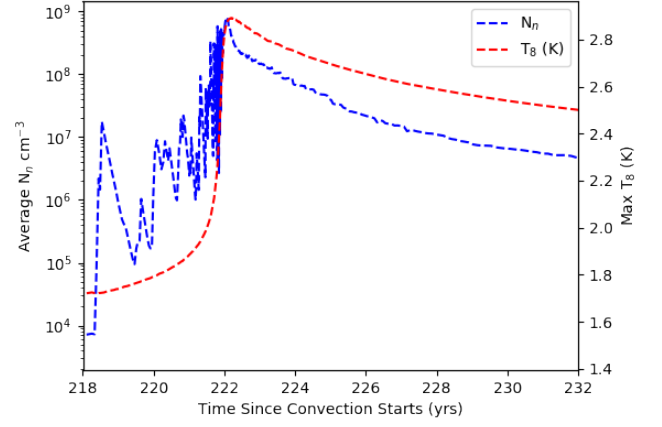
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**Figure 7.** The MLT diffusion coefficient has a more flat profile between the convective boundaries while the diffusion coefficient given by (Jones et al. 2017) (Eq. (6)) is about an order of magnitude smaller at the convective boundaries.



**Figure 8.** This is the time scale plot



**Figure 9.** This is the neutron density as a function of time

