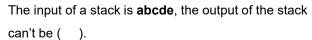


- 4.2 Stack
- 4.2.1 Stack ADT
- 4.2.2 Array-based stack
- 4.2.3 Linked stack



Stack



- (A) edacb
- (B) bcdae
- (C) bcade
- (D) aedcb

09:05

Stack(栈)

LIFO List: Last In, First Out. 后进先出

Restricted form of list 有限制的线性表:

Insert and remove only at front of list.插入和 删除只能发生在线性表的前端。

Notation:

Insert: Push

Remove: Pop

 The accessible element(前端元素) is called TOP(顶部元素).

09:05

73

```
4.2.1 Stack ADT 栈的抽象数据类型定义
```

ADT Stack {

数据对象:

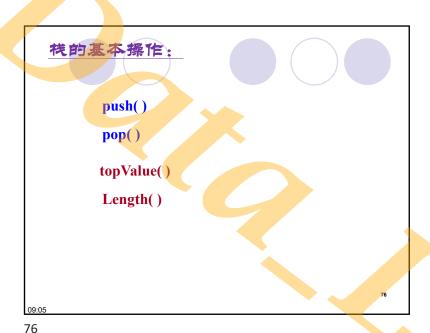
 $D = \{ a_i \mid a_i \in ElemSet, i=0,2,...,n-1, n \ge 0 \}$ 数据关系:

R1 ={ $\langle a_{i-1}, a_i \rangle | a_{i-1}, a_i \in \text{ElemSet}, i=1,...,n-1$ } 约定 a_{n-1} 端为栈顶, a_0 端为栈底。

基本操作:

} ADT Stack

09:0 75



4.2.2 Array-based stack (顺序存储株)

1 个数组, 2 个整型变量即可描述stack

✓ 1 个数组ListArray存储栈元素

✓ 1 个整型变量maxSize描述数组的大小

✓ 1 个整型变量top描述栈顶索引 (同时也代表栈中元素个数)

空栈 a 进栈 b 进栈

maxSize=5

09.05

```
Stack ADT class
// Stack abtract class
template <class Elem> class Stack {
public:
  Stack() {}
  virtual ~Stack() {}
  // Reinitialize the stack
  virtual void clear() = 0;
  // Push an element onto the top of the stack.
  virtual void push(const Elem&) = 0;
  // Remove the element at the top of the stack.
  virtual Elem pop() = 0;
  // Get a copy of the top element in the stack
  virtual Elem topValue() const = 0;
  // Return the number of elements in the stack.
  virtual int length() const = 0;
};
```

77

顺序栈的进栈和业栈原则

■ 进栈时: 将新元素放入top 位置,即ListArray [top]。

再 top++

■ 出栈时: 先top--,

再将top位置的元素,即ListArray [top]弹出。

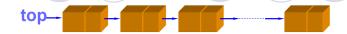
- 栈满时再进栈将溢出出错;
- 栈空时再出栈将栈空出错。

09:

Array-Based Stack class(1) // Array-based stack implementation template <class Elem> class AStack{ private: // Maximum size of stack int maxSize; int top; // Index for top element Elem *listArray; // Array holding elements public: AStack(int size) { top = 0; maxSize = size; listArray = new Elem[maxSize]; ~AStack() { delete [] listArray; } int length() const { return top; } void clear() { top = 0; }

80

4.2.3 link-based stack (链式栈)



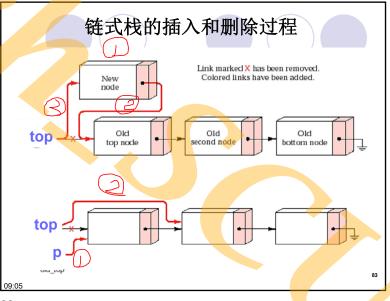
- 1个指针和1个整型变量即可描述一个链式栈
- ✓ 指向栈头结点的指针top
- ✓ 描述栈中元素个数的变量size
- 链式栈的栈顶在链头
- 链式栈无栈满问题, 空间可扩充
- 有栈空问题

09:05 82 82

Array-Based Stack Class (2)

```
void push(const Elem& it) {
   Assert( top < maxSize, "Stack is full");
   listArray[top]= it; top++;
}
Elem pop() {
   Assert( top > 0, "Stack is empty");
   top--; return listArray[top];
}
Elem topValue() const {
   Assert( top > 0, "Stack is empty");
   return listArray[top-1];
}
};
```

81



Linked Stack class(1) // Linked stack implementation template <class Elem> class LStack { private: Link<Elem>* top; // Pointer to first elem int size; public: LStack() { top = NULL; size = 0; } ~LStack() { clear(); } // Destructor void clear() { while (top != NULL) { Link<Elem>* temp = top; top = top->next; delete temp; } size=0; <u>09:05</u> }

84

86



请思考



- What is the cost of the operations in arrayedbased stack and Linked stack?
- How about do space requirements of the arraybased stack and Linked stack implementation?
- ●自由链表可与链式栈结合以降低new, delete操作的时间吗?

86 09:05

```
Linked Stack Class (2)
 void push(Elem& it) {
   top = new Link<Elem>(it,top);
   size++;
 Elem pop(){
  Assert( top!=NULL, "Stack is empty");
  link<Elem> *temp = top;
  top = top->next;
                     size--;
  Elem it = temp->element;
  delete temp;
  return it;
 Elem topValue() const {
   Assert( top!=NULL, "Stack is empty");
   return top->element;
 int length() const { return size;}
```

85

栈的应用举例1:

十进制数N和其他d进制数的转换

除d求余法: 迭代 N = (N / d)......N % d

例如: (1348)10 = (2504)8, 其运算过程如下:

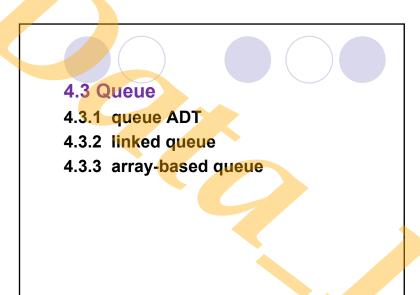
N	N div 8	N mod 8
1348	168	4
168	21	0
21	2	5
2	0	2

09:09

```
Main函数
#include "Astack.h"
// #include "Lstack.h"
void main() {
AStack<int> myStack(100);
// LStack<int> myStack;
int N,M,d, e;
cout<<"请输入一个十进制数: "; cin >>N; M=N;
cout<<"请输入拟转化的进制基数: "; cin >> d;
 while(N) {
      myStack.push(N%d);
      N=N/d;
 cout<<"十进制数"<<M<<" 对应的"<<d<<"进制为: ";
 while ( myStack.length() ) {
      e=myStack.pop();
      cout<<e;
```

89

```
LStack.h (课件p29,p84-85)
     // Singly-linked list node
     template < class Elem > class Link {
     public:
     Elem element: // Value for this node
      Link *next; // Pointer to next node
      Link(const Elem& elemval,
        Link* nextval = NULL)
      { element = elemval; next = nextval; }
      Link(Link* nextval = NULL)
      { next = nextval; }
    };
    // Linked stack implementation
    template <class Elem> class LStack {
      Link<Elem>* top; // Pointer to first elem
      int size;
    public:
      .....
    };
09:05
```



4.3.1 queue ADT

ADT Queue {

数据对象:

$$D = \{a_i \mid a_i \in ElemSet, i=0,1,...,n-1, n \ge 0\}$$

数据关系:

R1 = {
$$\langle a_{i-1}, a_i \rangle | a_{i-1}, a_i \in D, i=1,...,n-1$$
}

94

基本操作:

ADT Queue

Pront a₀ a₁ a₂ a_{n-1}

FIFO List: First in, First Out

Restricted form of list:
Insert at one end (Rear)
remove from the other end (Front)

Notation:
Insert: Enqueue (入队)
Remove: Dequeue (出队)
First element: Front (队头)
Last element: Rear (队尾)

93



94

4.3.1 Queue ADT class

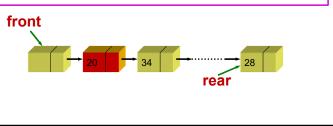
```
// Queue abtract class
template <class Elem> class Queue {
public:
 Queue() {}
 virtual ~Queue() {}
  // Reinitialize the queue
 virtual void clear() = 0;
  // Append an element into the rear of the queue.
 virtual void enQueue (const Elem&) = 0;
  // Remove the element at the front of the queue.
 virtual Elem deQueue() = 0;
  // get a copy of the front element in the queue
 virtual Elem frontValue() const = 0;
  // Return the number of elements in the gueue.
 virtual int length() const = 0;
};
```

96

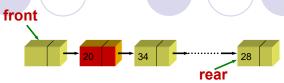
4.3.2 Linked queue (链式队列)

2个指针和1个整型变量即可描述一个链式栈

- ✓ 指向队头空数据结点的指针 front
- ✓ 指向队尾结点的指针 rear
- ✓ 描述队列中元素个数的变量size



4.3.2 Linked queue (链式队列)



- front在链头, rear在链尾。跟Llist一样, 有一专门的空数据结点作为头结点。
- 链式队列在进队时无队满问题,但在出队 时有队空问题。
- 队空条件为 front->next == NULL

97

09:05

接式队列的入队和迎队过程
front
enQueue
front
temp deQueue
出队前需判断是否为空 99

Linked Queue class(1) // Linked Queue implementation template < class Elem> class LOueue { private: Link<Elem>* front: // Pointer to front elem Link<Elem>* rear; // Pointer to rear elem int size; // Count number of elems public: LQueue() { front = rear = new Link<Elem>(); size = 0; } ~LQueue() { clear(); delete front; } void clear() { while(front->next!= NULL) { rear = front; front = front->next; delete rear; rear = front; size=0;

100

```
Linked Queue Class (3)

Elem frontValue() const {
    Assert ( size!=0, " Queue is empty");
    return front->next->element;
    }
    int length() const { return size; }
};
```

```
Linked Queue Class (2)

void enQueue(Elem& it) {
    rear->next = new Link<Elem>(it,NULL);
    rear=rear->next; size++;
}

Elem deQueue(){
    Assert ( size!=0, " Queue is empty");;
    Link<Elem> *temp = front->next;
    it = temp->element;    front->next = temp->next;
    if (rear == temp)    rear = front;
    size--; delete temp;
    return it;
}
```

101

4.3.3 array-based queue(顺序存储队列)

1个数组,3个整型变量可描述顺序队列

- ✓ 用1个数组存储队列元素
- ✓1个整型变量maxSize描述数组的大小
- ✓1个整型变量front描述队头索引(指向队头的 当前位置)
- ✓1个整形变量rear描述队尾索引(一般指向队尾的后一个位置)



103

09:0

队列的进队和业队原则

- ■进队时: 先将新元素插入rear 位置, 然后rear=rear+1。
- ■出队时: 先将下标为 front 的元素取出,

然后 front=front+1。 BCD

- front rear ■ 队初始化: front = rear = 0
- 队满时再进队将溢出出错;
- 队空时再出队将队空出错。

104

106

污溢业(pseudo-overflow)最直接的解决办法

每次出队都将剩余所有元素向前移动。即front永远为0

虽然可解决伪溢出问题, 但出队操作复杂度 由 ⊕ (1) 增加到 ⊕ (n)

此解决办法不好! 丟弃!!

Maxsize=7 队列的进队和出队示例 front rear空队列 front rear A进队 AB ABCD front rear C, D进队 front rear B进队 BCD CD front rear A退队 H进队,伪溢出 CDEFG CDEFG front E,F,G进队^{rear} front rear

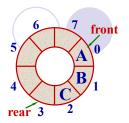
105

更好的解决办法——环形队列

将存放队列元素的数组首尾相 接,形成循环(环形)队列 Circular Queue .

循环队列 (Circular Queue)

存放队列的数组被当作首尾相接的环。



■ 队头、队尾索引加1后若等于数组最大尺寸 maxSize,则从maxSize-1直接进到0,可用取模 运算实现。

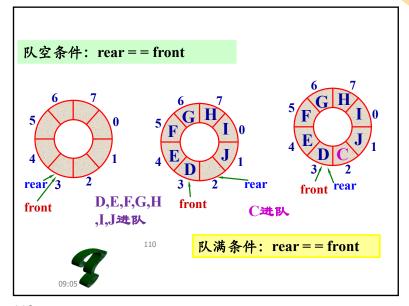
☞队头指针加1: front = (front+1) % maxSize

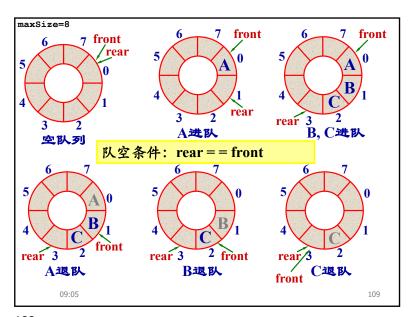
☞队尾指针加1: rear = (rear+1)% maxSize

☞队列初始化(空对列): front = rear = 0

09:05

108





109

解决方案一:

设置计数器count, 记录队列中的元素个数

☞队列初始化: front = rear = count = 0

☞ 队空条件: count = 0

☞队满条件: count = maxSize

1个数组(listArray), 4个整型变量(maxSize, front, rear, count) 描述循环顺序队列

09:05

111

解决方案一觉结:

- 将队列首尾相连构成循环队列 (逻辑上)
 - 解决了伪溢出问题
 - 出队: front=(front+1)% maxSize
 - 入队: real=(real+1)% maxSize
- · 设置计数器count
 - 解决了队满队空条件相同的问题
 - 队空: count=0
 - 队满: count=maxSize

09:05

112

112

Circular AQueue class(方案一)

```
int length() const { return count;}
Elem frontValue() const {
   Assert (count > 0, " Queue is empty");
   return listArray[front];
}
void enQueue (const Elem& it) {
   Assert (count < maxSize, " Queue is full");
   listArray[rear] = it;
   rear = (rear+1) % maxsize; count++;
}
Elem deQueue () {
   Assert (count > 0, " Queue is empty");
   Elem it = listArray[front];
   front=(front+1) %maxSize; count--;
   return it;
}
};
og:05
```

```
Circular AQueue class(方案一)
```

```
// Array-based circular queue implementation one
template <class Elem>
class CAQueue {
private:
int maxSize; // Maximum size of queue
int front; // Index for front element
int rear: // Index for rear element
int count:
 Elem *listArray; // Array holding elements
public:
 CAQueue(int size=DefaultListSize) {
   front = rear = count = 0; maxSize = size;
   listArray = new Elem[maxSize];
  ~CAQueue() { delete [] listArray; }
  void clear() { front = rear = count = 0; }
                                                          113
```

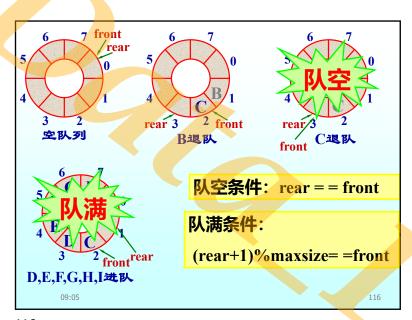
113

解决方案二:

在数组中始终留空一个单元不用。即rear所指的单元始终不用

- ☞队列初始化: front = rear = 0
- ☞队空条件: front = = rear
- ☞队满条件: (rear+1)% maxSize = = front
 - 当队尾再加1追上队头时, 队列满
 - 当队列中元素个数达到maxSize-1时,队满

09:05



118

```
Circular AQueue class(方案二)
// Array-based circular queue implementation two
template <class Elem>
class CAQueue {
private:
  int maxSize;
                    // Maximum size of queue
  int front;
                // Index for front element
  int rear;
                // Index for rear element
  Elem *listArray; // Array holding elements
public:
  CAQueue(int size) {
    front = rear = 0; maxSize = size+1;
    listArray = new Elem[maxSize];
  ~CAQueue() { delete [] listArray; }
  void clear() { front = rear = 0; }
  int length() const { return (rear+maxSize-front)%maxSize; }
    09:05
```

```
解决方案二定结:

• 将队列首尾相连构成循环队列(逻辑上)

- 解决了伪溢出问题

- 出队: front=(front+1)% maxSize

- 入队: real=(real+1)% maxSize

• 留空一个单元不用

- 解决了队满队空条件相同的问题

- 队空: front = = rear

- 队满: (rear+1)% maxSize = = front
```

117

117

```
Circular AQueue class(方案二)
 void enQueue(const Elem& it) {
   Assert ( ((rear+1)%maxsize) ! = front, " Queue is full");
   listArray[rear] = it;
    rear = (rear+1)% maxSize;
 Elem deQueue() {
   Assert (length ()! =0, "Queue is empty");
   Elem it = listArray[front];
   front=(front+1)%maxSize;
   return it;
 Elem frontValue() const {
    Assert (length ()! =0, "Queue is empty");
    return listArray[front];
};
    09:05
                                                   119
```



- What is the cost of the operations in Circular Queue and Linked Queue implementation?
- How about do space requirements of the Circular
 Queue and Linked Queue implementation?
- Linked Queue 能与freelist 结合吗,若能,how?

```
#include "LQueue.h" // #include "CAQueue,h"
#include "LStack.h" // #include "AStack.h"

template <class Elem>
void reverse(LQueue<Elem> & Q, LStack<Elem> & S)
{
    Elem X;
    .....
}

void main() {
    LQueue<int> myQueue; // CAQueue<int> myQueue(100);
    LStack<int> myStack; // AStack<int> myStack(100);
    int i, A[10] = {1 2 3 4 5 6 7 8 9 10};
    for ( i=0; i<10; i++) myQueue.enQueue(A[i]);
    reverse(myQueue, myStack);
}
```

```
An example of Stack and Queue
```

```
Given an non-empty queue Q, a empty stack S, a variable X, write an function to reverse the order of the elements in Q. (exercises 4.18)

template <class Elem>
void reverse(LQueue<Elem> & Q, LStack<Elem> & S)
{
    Elem X;
    while (Q.length ()) {
        X=Q.deQueue(); S.push(X); }
    while (S.length ()) {
        X=S.pop(); Q.enQueue(X); }
}
```

121

```
LQueue.h (课件p29, p101-103)

// Singly-linked list node
template <class Elem> class Link {
public:
    Elem element; // Value for this node
    Link *next; // Pointer to next node

.......
};

// Linked Queue implementation
template <class Elem>
class LQueue {
private:
    Link<Elem>* front; // Pointer to front elem
    Link<Elem>* rear; // Pointer to rear elem
    int size; // Count number of elems
public:
    ......
};

CAQueue.h (课件p114-1115或119-120)
```



Chapter4 End 09:05 125