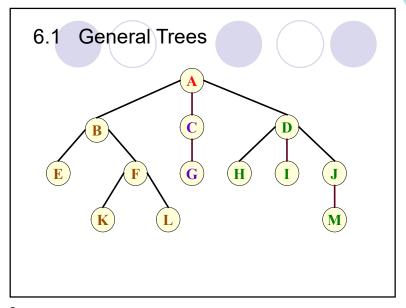
Chapter 6. Non-Binary Trees

1





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- 6.4 k-ary Trees(k叉树)
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- 6.6 Sequential tree Implementations



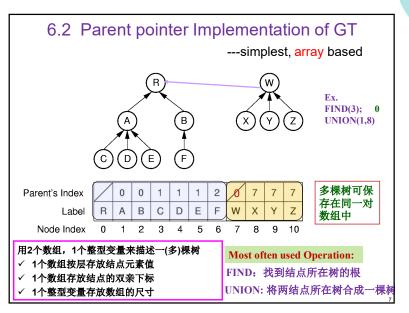
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```
General Tree Node ADT
template <class Elem> class GTNode { // General tree node ADT
public:
 GTNode(const Elem&); // Constructor
 ~GTNode();
                  // Destructor
 Elem value();
                 // Return value
 bool isLeaf();
               // TRUE if is a leaf
 GTNode* parent(); // Return parent
 GTNode* leftmost_child(); // Return First child
 GTNode* right_sibling(); // Return Right sibling
 void setValue(Elem&); // Set value
 void insert first(GTNode<Elem>* n); //insert First child
 void insert next(GTNode<Elem>* n); //insert right next sibling
 void remove_first(); // Remove first child
 void remove_next(); // Remove next sibling
```

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6

```
// Parent pointer Implementation of General tree for UNION/FIND
template <class Elem> Class ParPtrTrees {
                                             UNION(6, 9)
private:
                                                                     (X) (V) (Z)
Elem *data:
 int *parentIndex;
      maxSize;
                                             Parent's Index 0 0 1 1 1 2 0 7 7 :
 int FIND(int curr) const {
                                               Node Index 0 1 2 3 4 5 6 7 8 9 10
     while (parentIndex [curr]!=ROOT) curr = parentIndex[curr];
     return curr; // At root
public:
  void UNION(int a, int b) {
       int root1 = FIND(a); int root2 = FIND(b);
       if (root1 != root2) parentIndex[root2] = root1;
```

An application of Parent pointer Implementation of GT

----Equiv Class(等价类) Processing (1)

等价关系

已知10个元素组成的集合 S={A, B,C, D, E, F, G, H, I, J}, 上的<u>连通(相等)关系R为:</u> {<A,B>, <A,C>, <B,H>, <C,H>, <A,H>, <H,E>, <E,G>, <D,E>, <D,F>, <E,F>, <F,G>, <F,I>}

省略环和传 遊边

P关系図的簡化表

(1)

(I)

(D)-

要解决的问题:

对S中元素进行聚类(求R对应的分划)

用计算机编程实现

输入: 1) 集合S; 2) S上的连通关系R 输出: 所有等价类(分划块):

1) 等价类个数; 2) 每个等价类中的元素

R关系图的简化表示,根据自反性去掉了环,根据自反性去掉了环,根据传递性去掉了传递边,根据对称性省掉了箭头

[A]={A, B, C, D, E, F, G, H, I} [J]={J}

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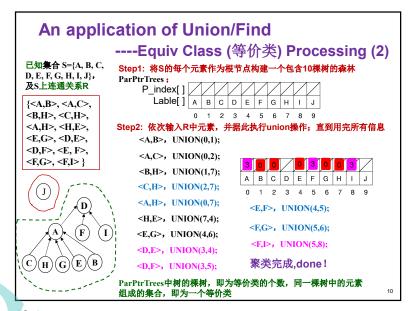
Want to keep the height of united tree smaller under low cost

Weighted union rule

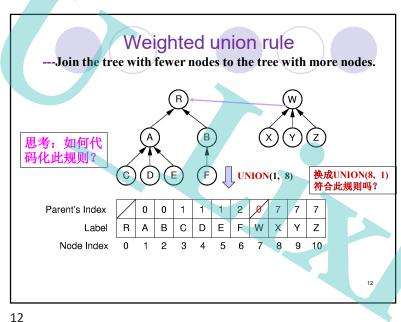
Rule1: Join the tree with fewer nodes to the tree with more nodes.

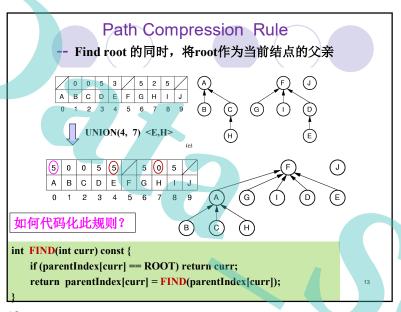
Rule2: Find root 的同时, set root 作为当前结点的父亲

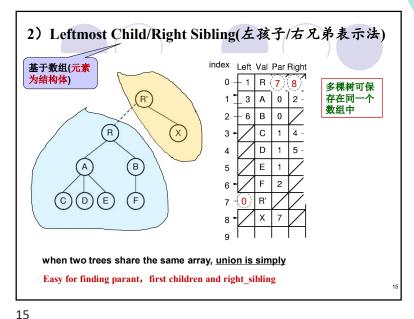
Path Compression Rule

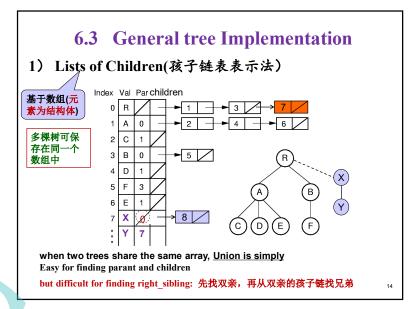


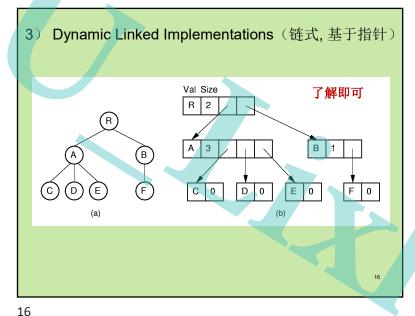
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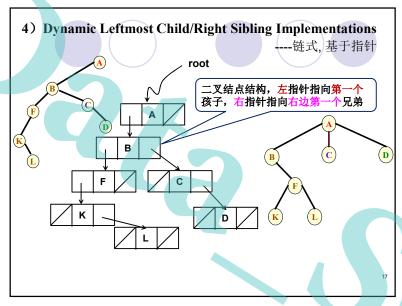










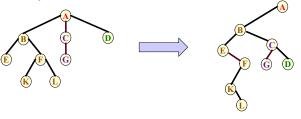


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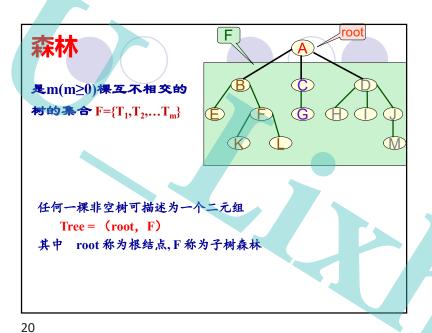
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6.4 Converting General tree to a Binary Tree

- 1. make mostLeft child as left child, and make right sibling as right child (Leftmost Child/Right Sibling)
- 2. Begin from the root, 从上到下从左到右,for each node, Use step 1) will convert any general tree to a binary tree.



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森林与二叉树的转换 T1 A T2 F T3 H B C D T3 H B C C T3 H A T1 F T2 H T3 H B C C T3 H B C C A T1 F B C C A T2 F C C A T3 F A T2 F B C C C A A T2 F B C C C A A T2 F C C A A T2 F A A T2 F A A T2 F B C C C A A T2 F C D K D K D C C A A T2 F A A T2 F A A T2 F B C C A A T2 F A A T2 F<

6.6 Sequential tree Implementations/树的序列表示 有兴趣的同学可课后自学

Goal: Store a series of nodes values with minimum information needed to reconstruct the tree structure

Method: List node values in the order they would be visited (preorder/inorder/postorder/ Breadth-first traversal), at the same time add some symbol to guard the reconstruct the of tree

Example1: AB/D//CEG///FH//I//

Or ABC/DEF////G/HI Here '/' stands for NULL



Example2: RAC)D)E))BF)))

here, ')' mark the end of each subtree

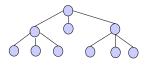
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6.5 k-ary Trees(k叉树)

For k-ary tree(k 又树), any node cannot have more than k sub-trees



full 3-ary tree

Complete 4-ary tree

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Sequential Implementations (2)

Advantage: Saves space.

Disadvantage: allows only sequential access

Using: save the node value on disk, transmit between computer, do operations after reconstruction tree structure

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