# SPIKING NEURAL NETWORKS

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### **Artificial Neural Networks**

- Poorly represent the human brain
- Matrix Multiplication (GEMM)
  - More Computation -> More Energy
- Offline learning
- Backpropagation
  - High training Cost

### **Spiking Neural Networks**

- Incorporates neuron models
- Spikes convert GEMM into accumulation
  - Less Computation -> Less Energy
- Online learning
- Surrogate Gradient Descent / STDP (Unsupervised)
  - Low training cost

### **Applications**

- Robotics
- Neuroscience
- Autonomous systems
- Natural language processing
- Computer vision
- etc.



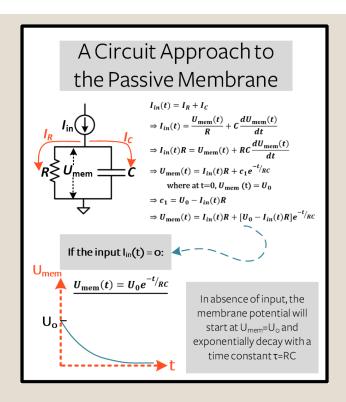
**Canada's Mars Exploration Science Rover** 

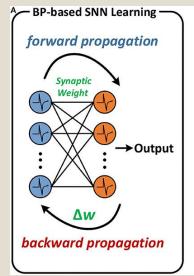
# **Leaky-Integrate and Fire**

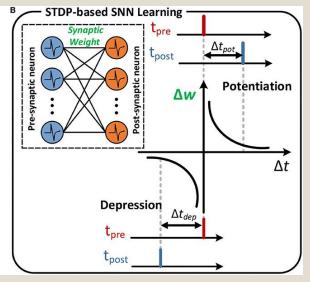
- Simple Neuron Model
- Represents neurons as an RC circuit
- Input current increase membrane potential
- When membrane potential breaks threshold, potential resets

# **Learning**

- Surrogate Gradient Descent
  - Step function learning (spike or no spike)
  - Replace derivative with a surrogate function
- STDP (Spike-Time Dependent Plasticity)
  - Unsupervised learning
  - Updates weights on spiking behavior
    - Presynaptic / Postsynaptic spikes







# Workflow Distribution

### **Brandon:**

- Visualization of model architecture
- Data Processing and Data Visualization construction
- Code Documentation

### **Daniel:**

- CNN and CSNN Architecture Design
- Generation of results and case study data
- Hyperparameter tuning

# Problem Description

# Train a SNN on MNIST Dataset for a supervised multi-class classification task.



Compare with ANN /
CNN on accuracy and
training loss

Compare computation cost in **FLOPs** (Floating Point Operations)

# Initial Approach

- LIF / STDP model
- Struggled to correlate images to labels

### Why?

- STDP struggles with classification
  - Unsupervised learning
  - Learning does not use labels
- STDP is used more commonly in TNNs (Temporal Neural Networks)
- SNNs are emerging:
  - Limited application
  - Research focused

# Attempts to salvage Initial Approach

# Normalization & Regularization

- Varying threshold voltage
- Reward modulated STDP (R-STDP)
  - Rewards/Punishes neurons based on prediction

# Hyperparameter tuning variation

- R/C/Tau
- Timesteps
- Learning Rate

#### Batch Normalization (BN)

$$\Rightarrow \text{ layer } \Rightarrow x \Rightarrow \hat{x} = \frac{x - \mu}{\sigma} \Rightarrow y = \gamma \hat{x} + \beta$$

- $\mu$ : mean of x in mini-batch
- σ: std of x in mini-batch
- γ: scale
- $\beta$ : shift

- $\mu$ ,  $\sigma$ : functions of x, analogous to responses
- $\gamma$ ,  $\beta$ : parameters to be learned, analogous to weights

**Image:** http://tzutalin.blogspot.com/2017/07/deep-learning-batch-normalization-note.html

# New Approach

- BNTT (Batch Normalization Through Time)
  - Codebase detailing implementation
  - Batch Normalization
    - Normalizes inputs across batch
    - Reduces covariant shift
    - Applies to each timestep
  - Backpropagation
    - Preferable with SNNs / Classification
- Solid foundation, but more complex than necessary.

**Code:** https://github.com/Intelligent-Computing-Lab-Yale/BNTT-Batch-Normalization-Through-Time/blob/main/model.py

# New Approach: Our Implementation

### **Simplify Architecture:**

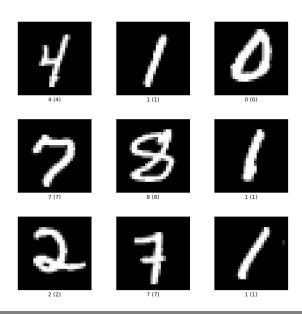
- Reduce layers from 9 to 3
- Reduce Shape / Input channels
  - Match input (MNIST)
  - Lower Complexity (hidden shapes)
- Reduce epochs and timesteps

#### Justification:

 Model is too complex for dataset

# Experimental Methodology

- Dataset: MNIST Handwritten Digits
- Model Architecture
- Hyperparameters used
- Encoding type
- Case Study
- Evaluation: Classification accuracy, training loss, and FLOPs



**MNIST Examples** 

# MNIST Dataset

A database of handwritten digits containing a training set of 60,000 examples, and a test set 10,000 examples.

Using 10% of the dataset due to training overhead (SNN)

Training on 6,000 samples.

Testing on 1,000 samples.

Goal: Correctly classify images as one of the ten digits.

## **Input: MNIST Batch** Layer 1 PoissonGen SConv2D **SBNN** Layer 2 SConv2D **SBNN** AvgPool2D Layer 3 **FCNN** FC\_SBNN **FCNN** Output Voltage

# **Model**

- Visual diagram of our model architecture and flow of our forward pass function if observing layers only.
- Baseline CNN ignores PoissonGen and uses non-spiking equivalents
  - o SConv2D -> Conv2D

# <u>Hyperparameters - Baseline</u>

#### Global Hyperparameters:

batch size, learning rate, number of epochs

#### Convolutional Layer 1

Input Channels: 1; Output Channels 64; Kernel Size:
 1; Stride: 1

#### Convolutional Layer 2

 Input Channels: 64; Output Channels: 64; Kernel Size: 3; Stride: 1

#### 2D Batch Normalization between Layers

Input Channels: 64; Epsilon: 1e-4; Momentum: 0.1;

#### Pooling (after L2 and BN)

Average Pooling; Kernel Size: 2

#### Fully-connected Layer 1

Input Dimension: 14 \* 14 \* 64; Output Dimension: 512

#### 1D Batch Normalization

Input Dimension: 512; Epsilon: 1e-4; Momentum:
0.1

#### Fully-connected Layer 2

Input Dimension: 512; Output Dimension: 10

#### Activation Function

Rectified Linear Unit following each BN operation.

# Hyperparameters - CSNN

#### Global Hyperparameters:

 number of time steps, leakage memory, batch size, learning rate, number of epochs

#### **Convolutional Layer 1**

 Input Channels: 1; Output Channels 64; Kernel Size: 1; Stride: 1

#### **Convolutional Layer 2**

 Input Channels: 64; Output Channels: 64; Kernel Size: 3; Stride: 1

## Spiking 2D Batch Normalization between Layers

Input Channels: 64; Epsilon: 1e-4; Momentum: 0.1;

#### Pooling (after L2 and BN)

Average Pooling; Kernel Size: 2

#### Fully-connected Layer 1

Input Dimension: 14 \* 14 \* 64; Output Dimension: 512

#### **Spiking 1D Batch Normalization**

Input Dimension: 512; Epsilon: 1e-4; Momentum: 0.1

#### Fully-connected Layer 2

Input Dimension: 512; Output Dimension: 10

#### **Activation Function**

N/A

# Encoding Type

### Rate Encoding

 Represents data as firing rate (frequency)

### Latency Encoding

Represents data as spike timings

### BNTT uses rate encoding

- SNNs prefer Rate encoding
- TNNs prefer Latency encoding

# Case Study

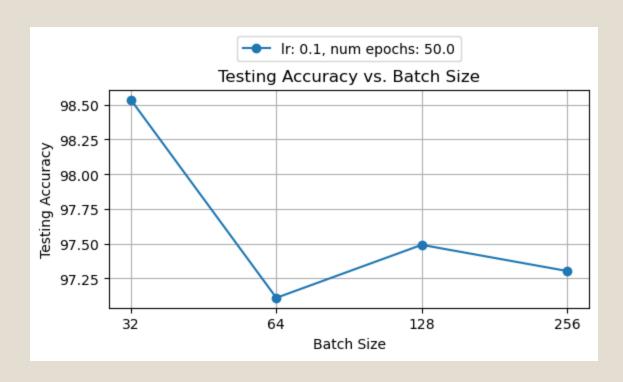
### Hyperparameter Variation

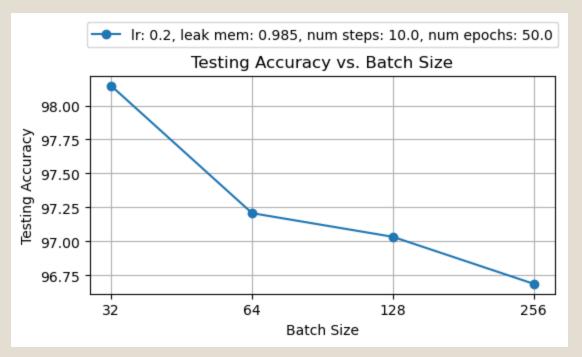
- Batch Size
- Epochs
- Timesteps
  - Steps in each forward pass of a neuron
- Leakage Voltage
  - Percentage of voltage retained between each step

#### Metrics

- Testing Accuracy
- Total FLOPs (Normalized)

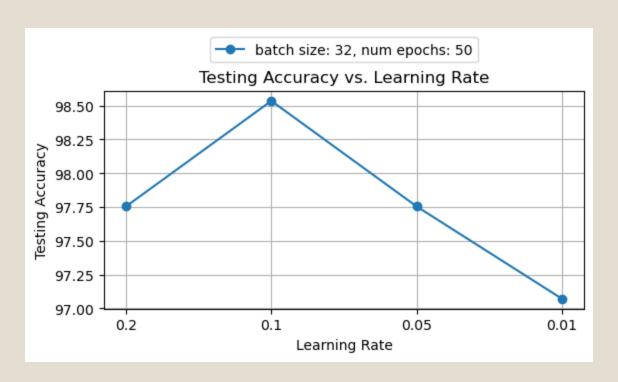
## <u>Case Study – Testing Accuracy vs. Batch Size</u>

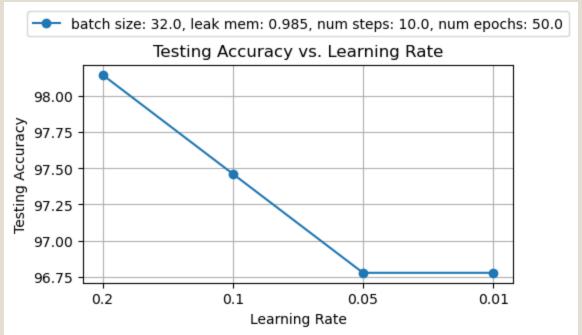




**CNN Results:** 

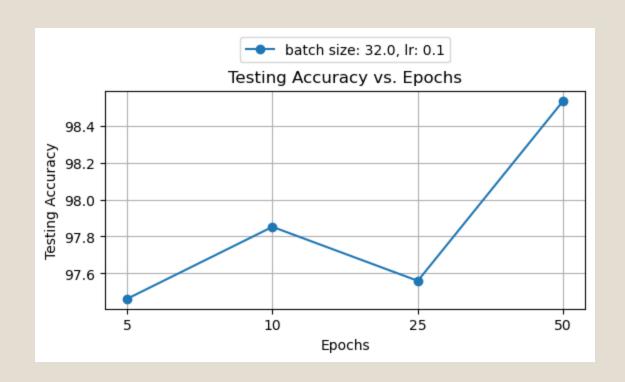
## <u>Case Study – Testing Accuracy vs Learning Rate</u>

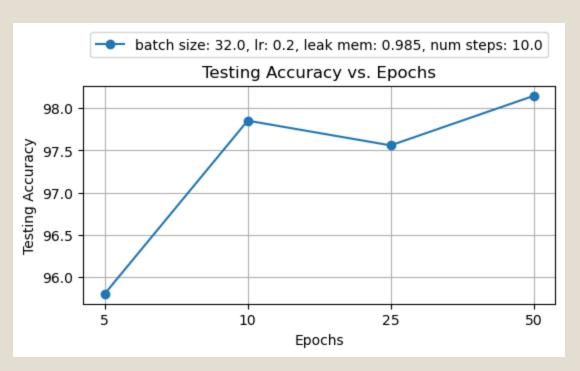




**CNN Results:** 

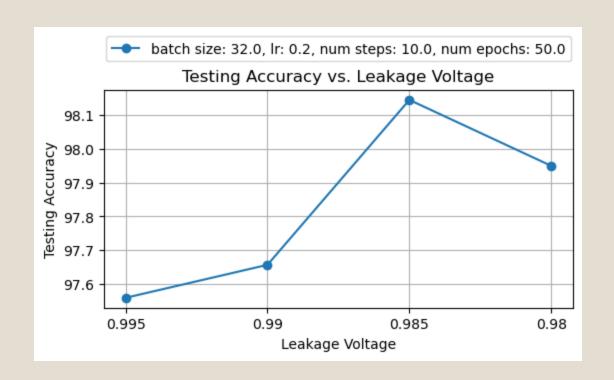
## Case Study – Testing Accuracy vs Epochs

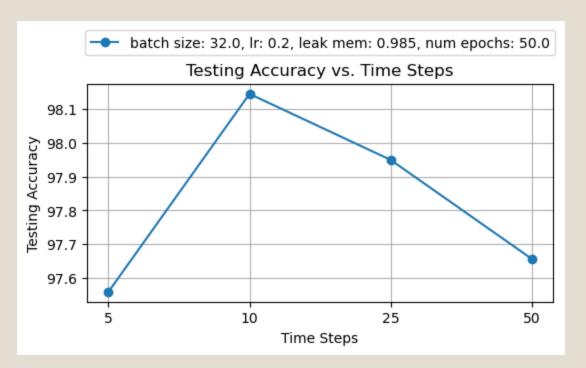




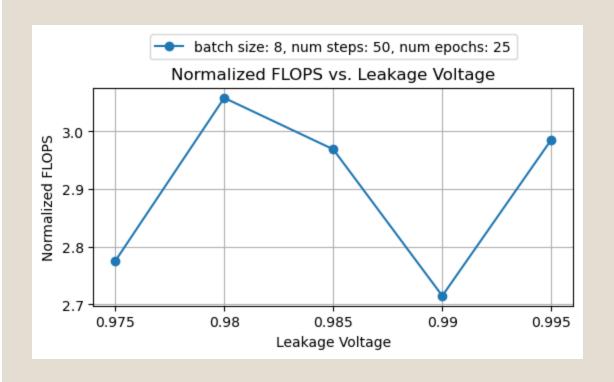
**CNN Results:** 

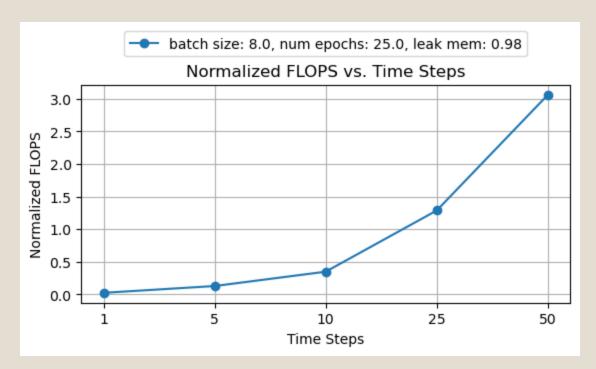
### <u>Case Study – Testing Accuracy vs Leakage Voltage / Time Steps</u>





### <u>Case Study – Norm FLOPs vs Leakage Voltage / Time Steps</u>





Model	CNN	SNN
Batch Size	32	32
Learning Rate	0.1	0.2
Epochs	50	50
Time Steps	N/A	10
Leakage Voltage	N/A	0.985
Training Loss	0.00098	0.00371
Testing Accuracy	98.535	98.145
Normalized Inference FLOPs	1x	0.428x

# **Evaluation**

- Training Loss
- Classification Testing Accuracy
- Floating Point Operations comparison

# <u>Takeaway</u>

- CSNN Model classifies with similar accuracy
- Computes 42.8% flops compared to CNN
- Ignores multiplier, majority of computational energy
- Achieves Significant decrease in energy usage.

# QUESTIONS?