

Week 2

After this lecture, you will:

- Understand the challenges of **semantic representation**
- Know about 2 techniques of **topic modeling**:
 - SVD
 - LDA





Previously in Text Representations

- Lexical Representations
- Vocabulary = list of unique token / word / term / lemma / n-grams appearing in the corpus
- 1 dimension = 1 item of the vocabulary
- Raw Counts or TF-IDF
- Preprocessing (lemmatizing, stemming, stopping, ...)
- In a lexical representation, a text is seen as an assembly of words



- Semantic = deals with meaning
- **Text** as a gathering of **topics** ("science", "business", "sport", ...)
- These **topics** are responsible for the **terms** that appear
 - Each topic has a list of **terms**
 - Topic "business" → "revenue", "operations", etc...
 - Topic "sport" → "goal", "league", "ranking", etc...
 - Think about "terms more likely to appear when talking about the topic"





TOPIC

- Weighted list of terms (word / n-gram / stem ...)
- Each term has a weight
 - Important terms with high weight
 - Less important terms with low weight





DOCUMENT

- Weighted list of topics
- Vector representation:
 - 1 dimension = 1 topic
 - Coefficient = weight of topic in document





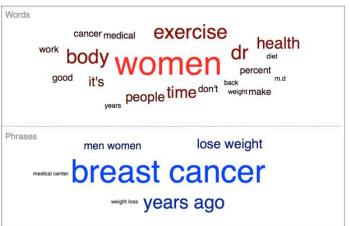
In Practice

"How did Vogue Magazine talk about Health?"

• How many articles?



• Using which words?







Challenge

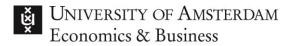
- Discover the topics from text
- We will see 2 techniques:
 - Singular Value Decomposition (SVD)
 - Latent Dirichlet Allocation (LDA)



SVD

- Discover the topics from text
- Factorization of the Term-Document Matrix
- Based on Linear Algebra
- 3 matrices
 - $U \rightarrow terms / topics$
 - $\sum \rightarrow \text{topics}$
 - $V \rightarrow documents / topics$
- Term-Document Matrix = $U * \sum * V$





Factorization U

Term-Document Matrix

| | d ₁ | d ₂ | d_3 | d ₄ | d ₅ | d ₆ |
|-------|----------------|----------------|-------|----------------|----------------|----------------|
| ship | 1 | 0 | 1 | 0 | 0 | 0 |
| boat | 0 | 1 | 0 | 0 | 0 | 0 |
| ocean | 1 | 1 | 0 | 0 | 0 | 0 |
| wood | 1 | 0 | 0 | 1 | 1 | 0 |
| tree | 0 | 0 | 0 | 1 | 0 | 1 |

| ship | -0.44 | -0.30 | 0.57 | 0.58 | 0.25 |
|-------|-------|-------|-------|-------|-------|
| boat | -0.13 | -0.33 | -0.59 | 0.00 | 0.73 |
| ocean | -0.48 | -0.51 | -0.37 | 0.00 | -0.61 |
| wood | -0.70 | 0.35 | 0.15 | -0.58 | 0.16 |
| tree | -0.26 | 0.65 | -0.41 | 0.58 | -0.09 |

| | 2.16 | 0.00 | 0.00 | 0.00 | 0.00 |
|---|------|------|------|------|------|
| | 0.00 | 1.59 | 0.00 | 0.00 | 0.00 |
| Σ | 0.00 | 0.00 | 1.28 | 0.00 | 0.00 |
| | 0.00 | 0.00 | 0.00 | 1.00 | 0.00 |
| | 0.00 | 0.00 | 0.00 | 0.00 | 0.39 |

| d ₁ | d ₂ | d_3 | d_4 | d ₅ | d ₆ |
|----------------|----------------|-------|-------|-----------------------|----------------|
| -0.75 | -0.28 | -0.20 | -0.45 | -0.33 | -0.12 |
| -0.29 | -0.53 | -0.19 | 0.63 | 0.22 | 0.41 |
| 0.28 | -0.75 | 0.45 | -0.20 | 0.12 | -0.33 |
| 0.00 | 0.00 | 0.58 | 0.00 | -0.58 | 0.58 |
| -0.53 | 0.29 | 0.63 | 0.19 | 0.41 | -0.22 |





Dimension Reduction 2 dims

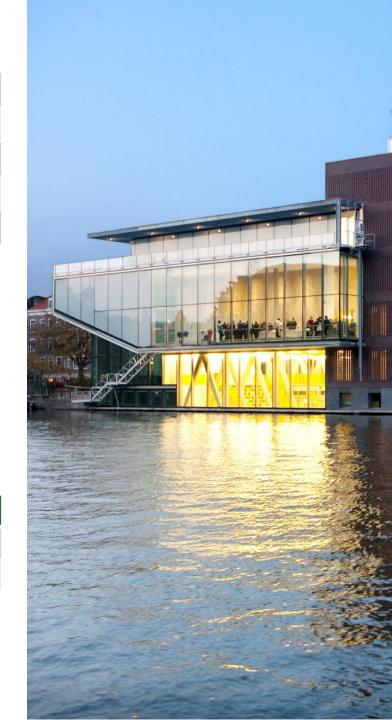
boat -0.44 -0.30 boat -0.13 -0.33 ocean -0.48 -0.51 wood -0.70 0.35 tree -0.26 0.65

Approximate Term-Document Matrix

| | d ₁ | d ₂ | d_3 | d ₄ | d ₅ | d ₆ |
|-------|----------------|----------------|-------|----------------|----------------|----------------|
| ship | 0.85 | 0.52 | 0.28 | 0.13 | 0.21 | -0.08 |
| boat | 0.36 | 0.36 | 0.16 | -0.20 | -0.02 | -0.18 |
| ocean | 1.01 | 0.72 | 0.36 | -0.04 | 0.16 | -0.21 |
| wood | 0.97 | 0.12 | 0.20 | 1.03 | 0.62 | 0.41 |
| tree | 0.12 | -0.39 | -0.08 | 0.90 | 0.41 | 0.49 |

| abla | 2.16 | 0.00 |
|------|------|------|
| 2 | 0.00 | 1.59 |

| | d ₁ | d ₂ | d_3 | d ₄ | d ₅ | d_6 |
|----|----------------|----------------|-------|----------------|-----------------------|-------|
| V' | -0.75 | -0.28 | -0.20 | -0.45 | -0.33 | -0.12 |
| | -0.29 | -0.53 | -0.19 | 0.63 | 0.22 | 0.41 |



Dimension Reduction

The term-document matrix we have could correspond to the texts:

D2: I cruised the ocean on a boat.

D3: I sail on a ship

(hypothesis: cruise / sail are stopwords)

$$\cos(d_2, d_3) = 0.95$$

Topic-Document Matrix

| d ₁ | d ₂ | d_3 | d_4 | d_5 | d ₆ |
|----------------|----------------|-------|-------|-------|----------------|
| -0.75 | -0.28 | -0.20 | -0.45 | -0.33 | -0.12 |
| -0.29 | -0.53 | -0.19 | 0.63 | 0.22 | 0.41 |

$$\cos(d_2, d_3) = 0.0$$

Term-Document Matrix

| | d ₁ | d ₂ | d ₃ | d ₄ | d_5 | d ₆ |
|-------|----------------|----------------|----------------|----------------|-------|----------------|
| ship | 1 | 0 | 1 | 0 | 0 | 0 |
| boat | 0 | 1 | 0 | 0 | 0 | 0 |
| ocean | 1 | 1 | 0 | 0 | 0 | 0 |
| wood | 1 | 0 | 0 | 1 | 1 | 0 |
| tree | 0 | 0 | 0 | 1 | 0 | 1 |



SVD

See the notebook "SVD"



Document Topics: Computer 01

Religion

Space

Joe,

ideas.

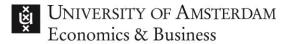
Computer_02

: 0.07

: 0.09

: 0.05 : 0.32

your description sounds like one of the gravity probe spacecraft



- Discover the topics from text
- Generative Model
- The Bag of Word is generated by random process
- Process:
 - 1 document = sum of weighted topics
 - 1 topic = probability distribution over dictionary



- 2 Topics:
 - "Sports" with words:
 - "football" P=0.4
 - "ronaldo" P=0.2
 - "goal" P=0.2
 - "world cup" P=0.2
 - "Business"
 - "revenue" P=0.6
 - "tax" P=0.3
 - "benefit" P=0.1



- 1 Document
 - 0.8 "Sport" + 0.2 "Business"
- Bag of Words:
 - 80% of the time we draw from "Sport"
 - 20% of the time we draw from "Business"
- 5-word long BoW
 - Football: 1, Ronaldo: 1, goal: 2
 - Business: revenue: 1
 - "Football star Ronaldo's revenue grows as he scores goal after goal."



- Given a collection of documents
- Given a **number of topics**
- Infer the distribution of topics in documents
- Infer the distribution of words in topics







- Discover Distribution
 - Of topics in documents
 - Of words in topics
- Machine Learning task
 - Python implementation in gensim or sklearn
 - Details of the learning task are out of scope





LDA - Evaluation

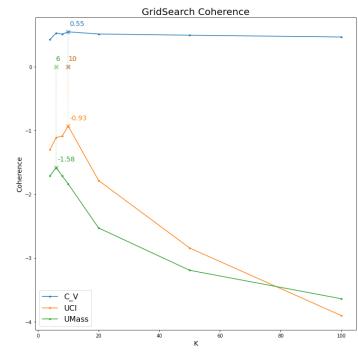
• Intrinsic Evaluation = evaluation of the topic / word

distributions

• Coherence metrics

• Umass, CV, UCI

- Given a collection of documents
 - Try multiple values of K
 - Select highest coherence





See the notebook "LDA"



