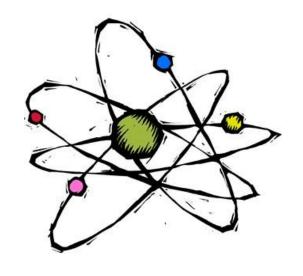
Chapter 6 Parallel Program Development



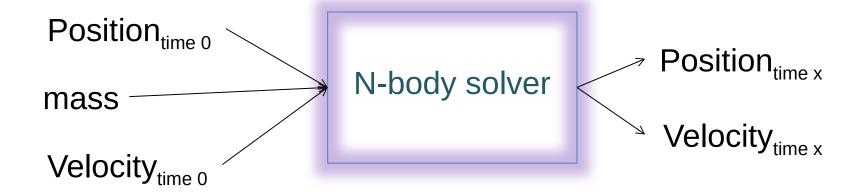


TWO N-BODY SOLVERS

The n-body problem

 Find the positions and velocities of a collection of interacting particles over a period of time.

 An n-body solver is a program that finds the solution to an n-body problem by simulating the behavior of the particles.



Simulating motion of planets

- Determine the positions and velocities:
 - Newton's second law of motion.
 - Newton's law of universal gravitation.

$$\mathbf{f}_{qk}(t) = -\frac{Gm_q m_k}{\left|\mathbf{s}_q(t) - \mathbf{s}_k(t)\right|^3} \left[\mathbf{s}_q(t) - \mathbf{s}_k(t)\right]$$

(6.2)

$$\mathbf{F}_{q}(t) = \sum_{\substack{k=0\\k\neq q}}^{n-1} \mathbf{f}_{qk} = -Gm_{q} \sum_{\substack{k=0\\k\neq q}}^{n-1} \frac{m_{k}}{\left|\mathbf{s}_{q}(t) - \mathbf{s}_{k}(t)\right|^{3}} \left[\mathbf{s}_{q}(t) - \mathbf{s}_{k}(t)\right]$$



$$\mathbf{s}_{q}^{"}(t) = -G \sum_{\substack{j=0\\j\neq q}}^{n-1} \frac{m_{j}}{\left|\mathbf{s}_{q}(t) - \mathbf{s}_{j}(t)\right|^{3}} \left[\mathbf{s}_{q}(t) - \mathbf{s}_{j}(t)\right]$$

$$\therefore F_{a}(t) = m_{a} a_{a}(t) = m_{a} s_{a}^{"}(t)$$

We either want to find the positions and velocities at the times $t = 0, \Delta t, 2\Delta t, \dots, T\Delta t$



Serial pseudo-code

```
Get input data;
for each timestep {
   if (timestep output) Print positions and velocities of particles;
   for each particle q
        Compute total force on q;
   for each particle q
        Compute position and velocity of q;
}
Print positions and velocities of particles;
```

Computation of the forces

```
for each particle q {
   for each particle k != q {
     x_diff = pos[q][X] - pos[k][X];
     y_diff = pos[q][Y] - pos[k][Y];
     dist = sqrt(x_diff*x_diff + y_diff*y_diff);
     dist_cubed = dist*dist*dist;
     forces[q][X] -= G*masses[q]*masses[k]/dist_cubed * x_diff;
     forces[q][Y] -= G*masses[q]*masses[k]/dist_cubed * y_diff;
}
```

$$\mathbf{f}_{qk}(t) = -\frac{Gm_q m_k}{\left|\mathbf{s}_q(t) - \mathbf{s}_k(t)\right|^3} \left[\mathbf{s}_q(t) - \mathbf{s}_k(t)\right]$$

A Reduced Algorithm for Computing N-Body Forces

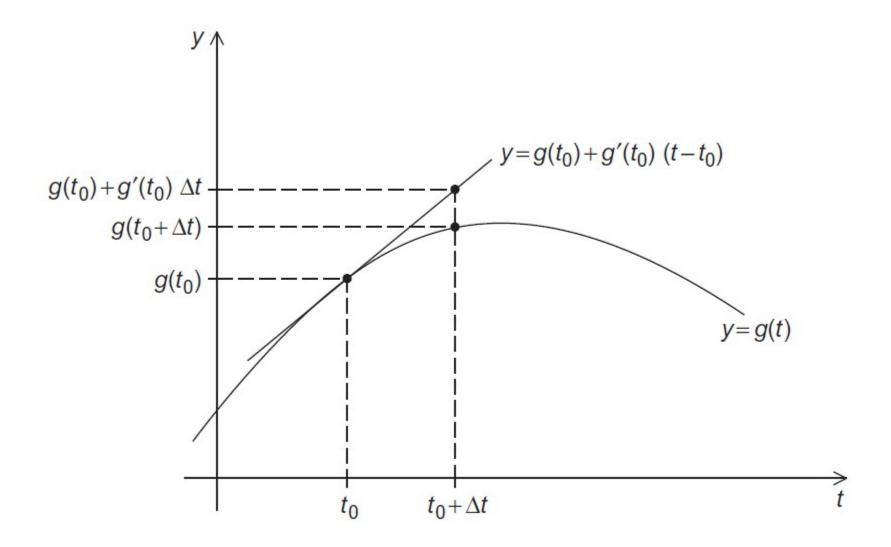
```
for each particle q
   forces[q] = 0;
for each particle q {
   for each particle k > q {
      x_diff = pos[q][X] - pos[k][X];
      y_diff = pos[q][Y] - pos[k][Y];
      dist = sqrt(x_diff*x_diff + y_diff*y_diff);
      dist cubed = dist*dist*dist;
      force_qk[X] = G*masses[q]*masses[k]/dist_cubed * x_diff;
      force_qk[Y] = G*masses[q]*masses[k]/dist_cubed * y_diff
      forces[q][X] += force_qk[X];
      forces[q][Y] += force_qk[Y];
      forces[k][X] -= force_qk[X];
      forces[k][Y] -= force_qk[Y];
                       For every action there is an equal and opposite
                       reaction (Newton's third law of motion)
```



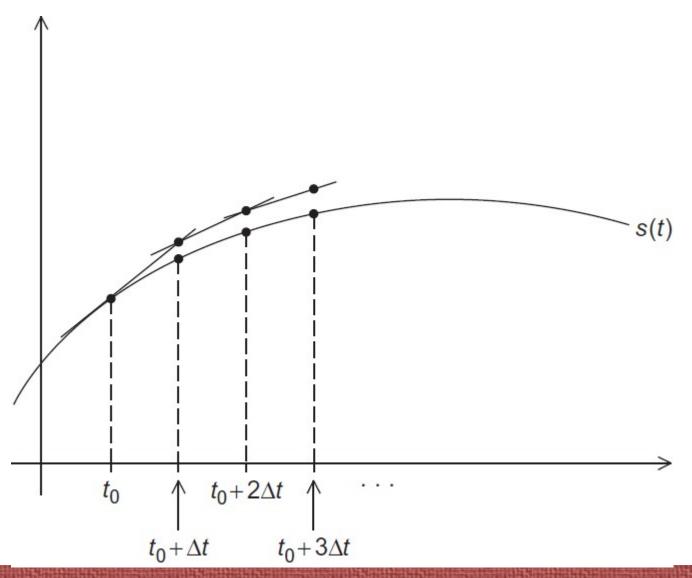
The individual forces

$$\begin{bmatrix} 0 & \mathbf{f}_{01} & \mathbf{f}_{02} & \cdots & \mathbf{f}_{0,n-1} \\ -\mathbf{f}_{01} & 0 & \mathbf{f}_{12} & \cdots & \mathbf{f}_{1,n-1} \\ -\mathbf{f}_{02} & -\mathbf{f}_{12} & 0 & \cdots & \mathbf{f}_{2,n-1} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ -\mathbf{f}_{0,n-1} & -\mathbf{f}_{1,n-1} & -\mathbf{f}_{2,n-1} & \cdots & 0 \end{bmatrix}$$

Using the Tangent Line to Approximate a Function



Euler's Method



$$\begin{split} y &= g(t_0) + g'(t_0)(t - t_0). \\ g(t + \Delta t) &\approx g(t_0) + g'(t_0)(t + \Delta t - t) = g(t_0) + \Delta t g'(t_0). \\ s_q(\Delta t) &\approx s_q(0) + \Delta t s_q'(0) = s_q(0) + \Delta t v_q(0), \\ v_q(\Delta t) &\approx v_q(0) + \Delta t v_q'(0) = v_q(0) + \Delta t \mathbf{a}_q(0) = v_q(0) + \Delta t \frac{1}{m_q} \mathbf{F}_q(0). \\ & \text{pos[q][X] += delta_t*vel[q][X];} \\ &\text{pos[q][Y] += delta_t*vel[q][Y];} \\ &\text{vel[q][X] += delta_t/masses[q]*forces[q][X];} \end{split}$$

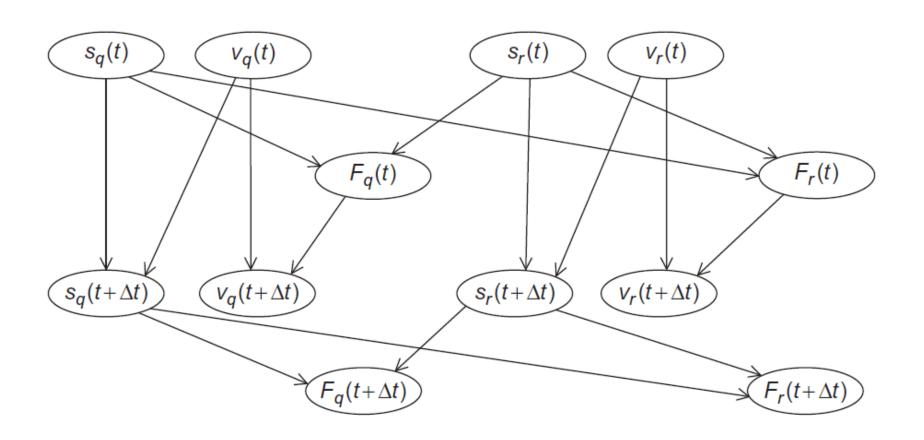
 $vel[q][Y] += delta_t/masses[q]*forces[q][Y];$



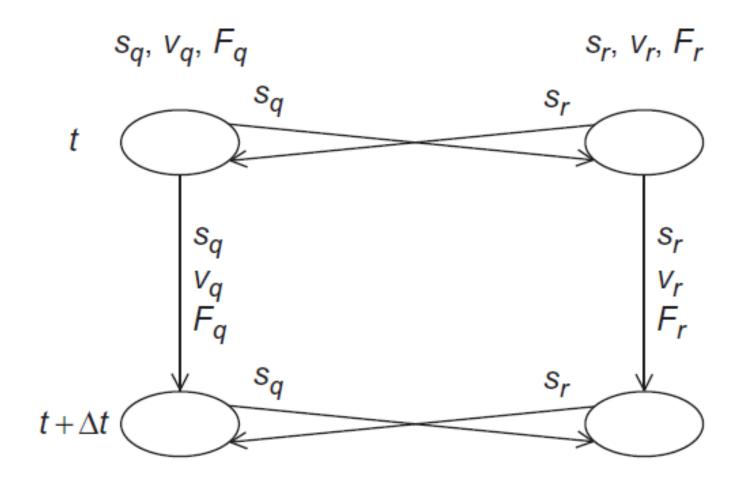
Parallelizing the N-Body Solvers

- Apply Foster's methodology.
- Initially, we want a lot of tasks.
- Start by making our tasks the computations of the positions, the velocities, and the total forces at each timestep.

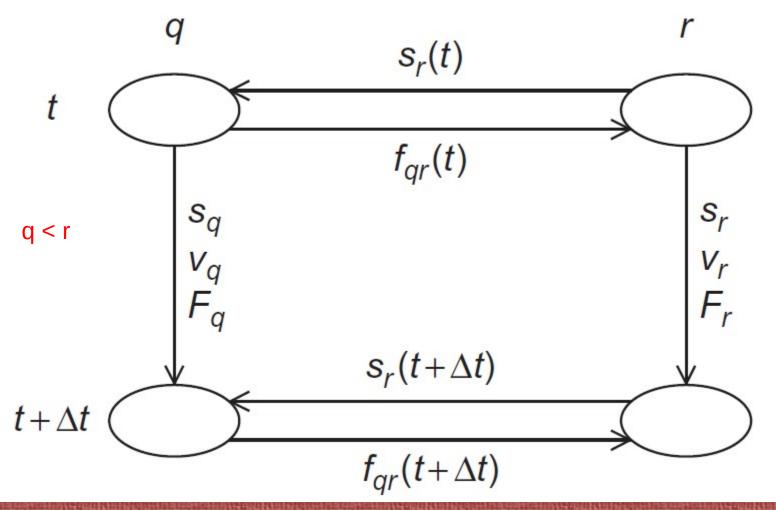
Communications Among Tasks in the Basic N-Body Solver



Communications Among Agglomerated Tasks in the Basic N-Body Solver



Communications Among Agglomerated Tasks in the Reduced N-Body Solver



Computing the total force on particle q in the reduced algorithm

```
for each particle k > q {
   x_diff = pos[q][X] - pos[k][X];
   y_diff = pos[q][Y] - pos[k][Y];
  dist = sqrt(x_diff*x_diff + y_diff*y_diff);
   dist_cubed = dist*dist*dist;
   force_qk[X] = G*masses[q]*masses[k]/dist_cubed * x_diff;
   force_qk[Y] = G*masses[q]*masses[k]/dist_cubed * y_diff;
   forces[q][X] += force_qk[X];
   forces[q][Y] += force_qk[Y];
   forces[k][X] -= force_qk[X];
   forces[k][Y] = force_qk[Y];
```

Serial pseudo-code

```
if each timestep {
   if (timestep output) Print positions and velocities of particles;
   for each particle q
        Compute total force on q;
   for each particle q
        Compute position and velocity of q;
}

iterating over particles
```

In principle, parallelizing the two inner for loops will map tasks/particles to cores.

First attempt

```
for each timestep {
   if (timestep output) Print positions and velocities of particles;
   pragma omp parallel for
   for each particle q
        Compute total force on q;
   pragma omp parallel for
   for each particle q
        Compute position and velocity of q;
}
```

Let's check for race conditions caused by loop-carried dependences.

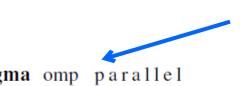
First loop

```
# pragma omp parallel for
for each particle q {
   forces[q][X] = forces[q][Y] = 0;
   for each particle k != q {
      x_diff = pos[q][X] - pos[k][X];
      y_diff = pos[q][Y] - pos[k][Y];
      dist = sqrt(x_diff*x_diff + y_diff*y_diff);
      dist_cubed = dist*dist*dist;
      forces[q][X] -= G*masses[q]*masses[k]/dist_cubed * x_diff;
      forces[q][Y] -= G*masses[q]*masses[k]/dist_cubed * y_diff;
   }
}
```

Second loop

```
# pragma omp parallel for
for each particle q {
    pos[q][X] += delta_t*vel[q][X];
    pos[q][Y] += delta_t*vel[q][Y];
    vel[q][X] += delta_t/masses[q]*forces[q][X];
    vel[q][Y] += delta_t/masses[q]*forces[q][Y];
}
```

Repeated forking and joining of threads



The same team of threads will be used in both loops and for every iteration of the outer loop.

But every thread will print all the positions and velocities.

Adding the single directive

```
# pragma omp parallel
    for each timestep {
        if (timestep output) {
            pragma omp single
                Print positions and velocities of particles;
        }

# pragma omp for
        for each particle q
            Compute total force on q;

# pragma omp for
        for each particle q
            Compute position and velocity of q;
}
```

Parallelizing the Reduced Solver Using OpenMP

```
#
   pragma omp parallel
   for each timestep {
      if (timestep output) {
         pragma omp single
#
         Print positions and velocities of particles;
#
      pragma omp for
      for each particle q
         forces[q] = 0.0;
#
      pragma omp for
      for each particle q
         Compute total force on q;
#
      pragma omp for
      for each particle q
         Compute position and velocity of q;
```



Problems



$$\mathbf{F}_3 = -\mathbf{f}_{03} - \mathbf{f}_{13} - \mathbf{f}_{23}$$

Updates to forces[3] create a race condition.

In fact, this is the case in general.

Updates to the elements of the forces array introduce race conditions into the code.

First solution attempt

```
before all the updates to forces
#
   pragma omp critical
       forces[q][X] += force_qk[X];
       forces[q][Y] += force_qk[Y];
       forces[k][X] = force_qk[X];
       forces[k][Y] -= force_qk[Y];
               Access to the forces array will be effectively
               serialized!!!
```



Second solution attempt

```
omp_set_lock(locks[q]);
forces[q][X] += force_qk[X];
forces[q][Y] += force_qk[Y];
omp_unset_lock(locks[q]);

omp_set_lock(locks[k]);
forces[k][X] -= force_qk[X];
forces[k][Y] -= force_qk[Y];
omp_unset_lock(locks[k]);
```

Use one lock for each particle.

First Phase Computations for Reduced Algorithm with Block Partition

		Thread			
Thread	Particle	0	1	2	
0	0	$\mathbf{f}_{01} + \mathbf{f}_{02} + \mathbf{f}_{03} + \mathbf{f}_{04} + \mathbf{f}_{05}$	0	0	
	1	$-\mathbf{f}_{01} + \mathbf{f}_{12} + \mathbf{f}_{13} + \mathbf{f}_{14} + \mathbf{f}_{15}$	0	0	
1	2	$-\mathbf{f}_{02}-\mathbf{f}_{12}$	$\mathbf{f}_{23} + \mathbf{f}_{24} + \mathbf{f}_{25}$	0	
	3	$-\mathbf{f}_{03} - \mathbf{f}_{13}$	$-\mathbf{f}_{23} + \mathbf{f}_{34} + \mathbf{f}_{35}$	0	
2	4	$-\mathbf{f}_{04} - \mathbf{f}_{14}$	$-\mathbf{f}_{24} - \mathbf{f}_{34}$	f ₄₅	
	5	$-\mathbf{f}_{05} - \mathbf{f}_{15}$	$-{\bf f}_{25}-{\bf f}_{35}$	$-{\bf f}_{45}$	

First Phase Computations for Reduced Algorithm with Cyclic Partition

		Thread			
Thread	Particle	0	1	2	
0	0	$\mathbf{f}_{01} + \mathbf{f}_{02} + \mathbf{f}_{03} + \mathbf{f}_{04} + \mathbf{f}_{05}$	0	0	
1	1	$-{f f}_{01}$	$\mathbf{f}_{12} + \mathbf{f}_{13} + \mathbf{f}_{14} + \mathbf{f}_{15}$	0	
2	2	$-{f f}_{02}$	$-\mathbf{f}_{12}$	$\mathbf{f}_{23} + \mathbf{f}_{24} + \mathbf{f}_{25}$	
0	3	$-\mathbf{f}_{03} + \mathbf{f}_{34} + \mathbf{f}_{35}$	$-{f f}_{13}$	$-{f f}_{23}$	
1	4	$-\mathbf{f}_{04} - \mathbf{f}_{34}$	$-\mathbf{f}_{14} + \mathbf{f}_{45}$	$-{f f}_{24}$	
2	5	$-\mathbf{f}_{05} - \mathbf{f}_{35}$	$-\mathbf{f}_{15} - \mathbf{f}_{45}$	$-{f f}_{25}$	

Revised algorithm – phase I

pragma omp for for each particle q { $force_qk[X] = force_qk[Y] = 0;$ for each particle k > q { $x_diff = pos[q][X] - pos[k][X];$ $y_diff = pos[q][Y] - pos[k][Y];$ $dist = sqrt(x_diff*x_diff + y_diff*y_diff);$ dist_cubed = dist*dist*dist; force_qk[X] = G*masses[q]*masses[k]/dist_cubed * x_diff; $force_qk[Y] = G*masses[q]*masses[k]/dist_cubed * y_diff;$ loc_forces[my_rank][q][X] += force_qk[X]; loc_forces[my_rank][q][Y] += force_qk[Y]; loc_forces[my_rank][k][X] -= force_qk[X]; loc_forces[my_rank][k][Y] -= force_qk[Y];



Revised algorithm – phase II

```
# pragma omp for
for (q = 0; q < n; q++) {
    forces[q][X] = forces[q][Y] = 0;
    for (thread = 0; thread < thread_count; thread++) {
        forces[q][X] += loc_forces[thread][q][X];
        forces[q][Y] += loc_forces[thread][q][Y];
    }
}</pre>
```

Parallelizing the Solvers Using Pthreads

- By default local variables in Pthreads are private. So all shared variables are global in the Pthreads version.
- The principle data structures in the Pthreads version are identical to those in the OpenMP version: vectors are two-dimensional arrays of doubles, and the mass, position, and velocity of a single particle are stored in a struct.
- The forces are stored in an array of vectors.

Parallelizing the Solvers Using Pthreads

- Startup for Pthreads is basically the same as the startup for OpenMP: the main thread gets the command line arguments, and allocates and initializes the principle data structures.
- The main difference between the Pthreads and the OpenMP implementations is in the details of parallelizing the inner loops.
- Since Pthreads has nothing analogous to a parallel for directive, we must explicitly determine which values of the loop variables correspond to each thread's calculations.



Parallelizing the Solvers Using Pthreads

- Another difference between the Pthreads and the OpenMP versions has to do with barriers.
- At the end of a parallel for OpenMP has an implied barrier.
- We need to add explicit barriers after the inner loops when a race condition can arise.
- The Pthreads standard includes a barrier.
- However, some systems don't implement it.
- If a barrier isn't defined we must define a function that uses a Pthreads condition variable to implement a barrier.



Parallelizing the Basic Solver Using MPI

- Choices with respect to the data structures:
 - Each process stores the entire global array of particle masses.
 - Each process only uses a single n-element array for the positions.
 - Each process uses a pointer loc_pos that refers to the start of its block of pos.
 - So on process 0 local_pos = pos; on process 1 local_pos = pos + loc_n; etc.

Pseudo-code for the MPI version of the basic n-body solver

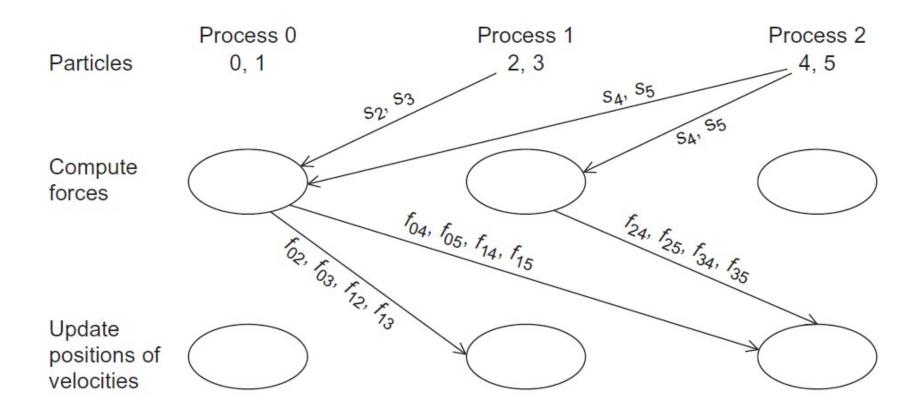
```
Get input data;
for each timestep {
   if (timestep output)
      Print positions and velocities of particles;
   for each local particle loc_q
      Compute total force on loc_q;
    for each local particle loc_q
      Compute position and velocity of loc_q;
   Allgather local positions into global pos array;
}
Print positions and velocities of particles;
```

Pseudo-code for output

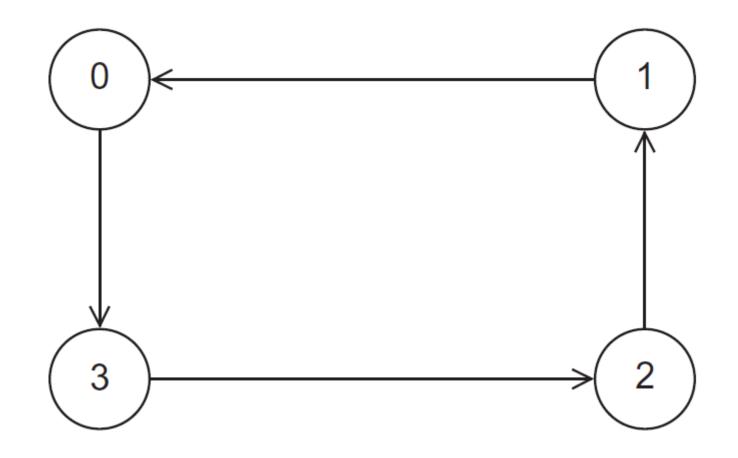
```
Gather velocities onto process 0;
if (my_rank == 0) {
   Print timestep;
   for each particle
      Print pos[particle] and vel[particle]
}
```



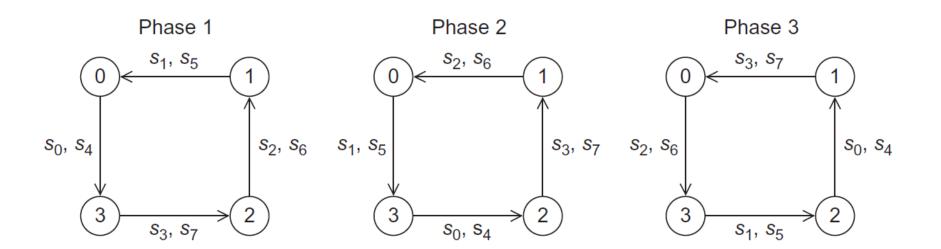
Communication In A Possible MPI Implementation of the N-Body Solver (for a reduced solver)



A Ring of Processes



Ring Pass of Positions



Computation of Forces in Ring Pass (1)

Time	Variable	Process 0	Process 1
Start	loc_pos	$\mathbf{s}_0, \mathbf{s}_2$	$\mathbf{s}_1, \mathbf{s}_3$
	loc_forces	0,0	0,0
	tmp_pos	$\mathbf{s}_0, \mathbf{s}_2$	$\mathbf{s}_1, \mathbf{s}_3$
	tmp_forces	0,0	0,0
After	loc_pos	$\mathbf{s}_0, \mathbf{s}_2$	$\mathbf{s}_1, \mathbf{s}_3$
Comp of	loc_forces	$\mathbf{f}_{02}, 0$	$\mathbf{f}_{13},0$
Forces	tmp_pos	$\mathbf{s}_0, \mathbf{s}_2$	$\mathbf{s}_1, \mathbf{s}_3$
	tmp_forces	$0, -\mathbf{f}_{02}$	$0, -\mathbf{f}_{13}$
After	loc_pos	$\mathbf{s}_0, \mathbf{s}_2$	$\mathbf{s}_1, \mathbf{s}_3$
First	loc_forces	$\mathbf{f}_{02}, 0$	$\mathbf{f}_{13}, 0$
Comm	tmp_pos	$\mathbf{s}_1, \mathbf{s}_3$	$\mathbf{s}_0, \mathbf{s}_2$
	tmp_forces	$0, -\mathbf{f}_{13}$	$0, -\mathbf{f}_{02}$
After	loc_pos	$\mathbf{s}_0, \mathbf{s}_2$	$\mathbf{s}_1, \mathbf{s}_3$
Comp of	loc_forces	$\mathbf{f}_{01} + \mathbf{f}_{02} + \mathbf{f}_{03}, \mathbf{f}_{23}$	$\mathbf{f}_{12} + \mathbf{f}_{13}, 0$
Forces	tmp_pos	$\mathbf{s}_1, \mathbf{s}_3$	$\mathbf{s}_0, \mathbf{s}_2$
	tmp_forces	$-\mathbf{f}_{01}, -\mathbf{f}_{03} - \mathbf{f}_{13} - \mathbf{f}_{23}$	$0, -\mathbf{f}_{02} - \mathbf{f}_{12}$



Computation of Forces in Ring Pass (2)

Time	Variable	Process 0	Process 1			
After	loc_pos	$\mathbf{s}_0, \mathbf{s}_2$	s_1, s_3			
Second		$\mathbf{f}_{01} + \mathbf{f}_{02} + \mathbf{f}_{03}, \mathbf{f}_{23}$	$\mathbf{f}_{12} + \mathbf{f}_{13}, 0$			
Comm	tmp_pos		$\mathbf{s}_1, \mathbf{s}_3$			
	tmp_forces	$0, -\mathbf{f}_{02} - \mathbf{f}_{12}$	$-\mathbf{f}_{01}, -\mathbf{f}_{03} - \mathbf{f}_{13} - \mathbf{f}_{23}$			
After	loc_pos	$\mathbf{s}_0, \mathbf{s}_2$	$\mathbf{s}_1, \mathbf{s}_3$			
Comp of			$-\mathbf{f}_{01} + \mathbf{f}_{12} + \mathbf{f}_{13}, -\mathbf{f}_{03} - \mathbf{f}_{13} - \mathbf{f}_{23}$			
Forces	tmp_pos	$\mathbf{s}_0, \mathbf{s}_2$	$\mathbf{s}_1, \mathbf{s}_3$			
	tmp_forces	$0, -\mathbf{f}_{02} - \mathbf{f}_{12}$	$-\mathbf{f}_{01}, -\mathbf{f}_{03} - \mathbf{f}_{13} - \mathbf{f}_{23}$			

Pseudo-code for the MPI implementation of the reduced n-body solver

```
source = (my_rank + 1) % comm_sz;
dest = (my_rank - 1 + comm_sz) \% comm_sz;
Copy loc pos into tmp pos;
loc\_forces = tmp\_forces = 0;
Compute forces due to interactions among local particles;
for (phase = 1; phase < comm_sz; phase++) {</pre>
   Send current tmp_pos and tmp_forces to dest;
   Receive new tmp_pos and tmp_forces from source;
   /* Owner of the positions and forces we're receiving */
   owner = (my_rank + phase) % comm_sz;
   Compute forces due to interactions among my particles
      and owner's particles;
Send current tmp_pos and tmp_forces to dest;
Receive new tmp_pos and tmp_forces from source;
```



Loops iterating through global particle indexes

```
for (loc_part1 = 0, glb_part1 = my_rank;
    loc_part1 < loc_n-1;
    loc_part1++, glb_part1 += comm_sz)

for (glb_part2 = First_index(glb_part1, my_rank, owner, comm_sz),
    loc_part2 = Global_to_local(glb_part2, owner, loc_n);
    loc_part2 < loc_n;
    loc_part2++, glb_part2 += comm_sz)
    Compute_force(loc_pos[loc_part1], masses[glb_part1],
        tmp_pos[loc_part2], masses[glb_part2],
    loc_forces[loc_part1], tmp_forces[loc_part2]);</pre>
```

Performance of the MPI n-body solvers

Processes	Basic	Reduced
1	17.30	8.68
2	8.65	4.45
4	4.35	2.30
8	2.20	1.26
16	1.13	0.78

(in seconds)

Run-Times for OpenMP and MPI N-Body Solvers

Processes/	Op	enMP	MPI			
Threads	Basic	Reduced	Basic	Reduced		
1	15.13	8.77	17.30	8.68		
2	7.62	4.42	8.65	4.45		
4	3.85	2.26	4.35	2.30		

(in seconds)

TREE SEARCH



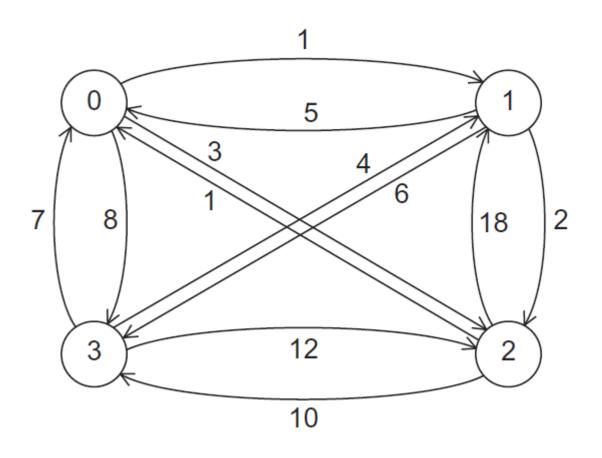
Tree search problem (TSP)

An NP-complete problem.

 No known solution to TSP that is better in all cases than exhaustive search.

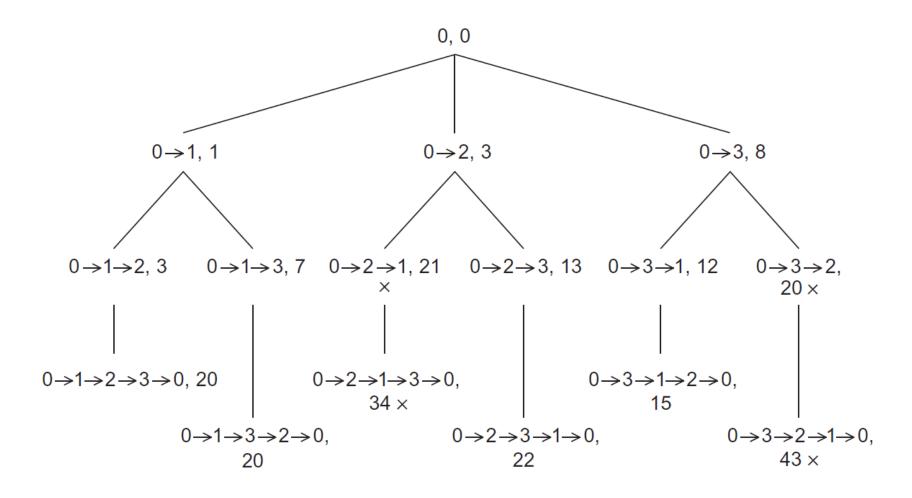
 Ex., the travelling salesperson problem, finding a minimum cost tour.

A Four-City TSP





Search Tree for Four-City TSP



Pseudo-code for a recursive solution to TSP using depth-first search

```
void Depth_first_search(tour_t tour) {
   city_t city;
   if (City_count(tour) == n) {
      if (Best_tour(tour))
         Update_best_tour(tour);
   } else {
      for each neighboring city
         if (Feasible(tour, city)) {
            Add_city(tour, city);
            Depth_first_search(tour);
            Remove_last_city(tour);
  /* Depth_first_search */
```

Pseudo-code for an implementation of a depth-first solution to TSP without recursion

```
for (city = n-1; city >= 1; city--)
   Push(stack, city);
while (!Empty(stack)) {
   city = Pop(stack);
   if (city == NO_CITY) // End of child list, back up
      Remove_last_city(curr_tour);
   else {
      Add_city(curr_tour, city);
      if (City_count(curr_tour) == n) {
         if (Best_tour(curr_tour))
            Update_best_tour(curr_tour);
         Remove_last_city(curr_tour);
      } else {
         Push(stack, NO_CITY);
         for (nbr = n-1; nbr >= 1; nbr--)
            if (Feasible(curr_tour, nbr))
               Push(stack, nbr);
   \} /* if Feasible */
  /* while !Empty */
```



Pseudo-code for a second solution to TSP that doesn't use recursion

```
Push_copy(stack, tour); // Tour that visits only the hometown
while (!Empty(stack)) {
   curr_tour = Pop(stack);
   if (City_count(curr_tour) == n) {
      if (Best_tour(curr_tour))
         Update_best_tour(curr_tour);
     else {
      for (nbr = n-1; nbr >= 1; nbr--)
         if (Feasible(curr_tour, nbr)) {
            Add_city(curr_tour, nbr);
            Push_copy(stack, curr_tour);
            Remove_last_city(curr_tour);
   Free tour(curr tour);
```

Run-Times of the Three Serial Implementations of Tree Search

Recursive	First Iterative	Second Iterative
30.5	29.2	32.9

(in seconds)



The digraph contains 15 cities. All three versions visited approximately 95,000,000 tree nodes.

Making sure we have the "best tour" (1)

- When a process finishes a tour, it needs to check if it has a better solution than recorded so far.
- The global Best_tour function only reads the global best cost, so we don't need to tie it up by locking it. There's no contention with other readers.
- If the process does not have a better solution, then it does not attempt an update.



Making sure we have the "best tour" (2)

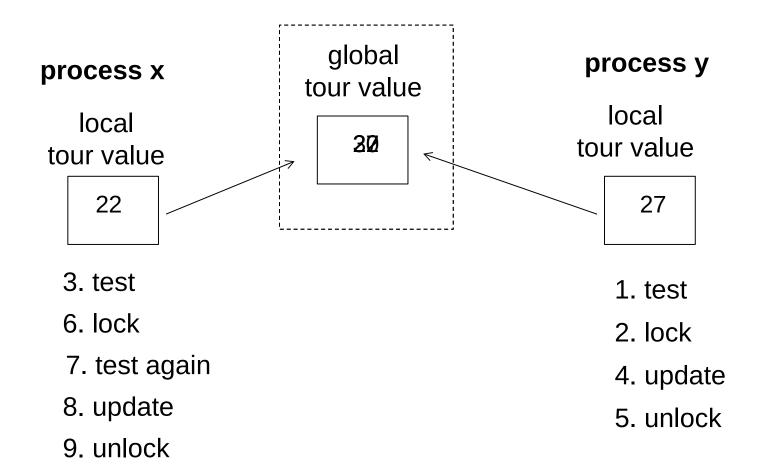
 If another thread is updating while we read, we may see the old value or the new value.

 The new value is preferable, but to ensure this would be more costly than it is worth.

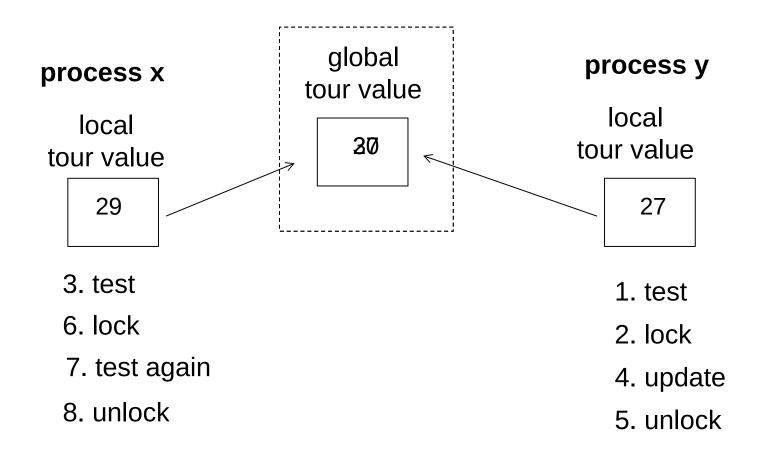
Making sure we have the "best tour" (3)

- In the case where a thread tests and decides it has a better global solution, we need to ensure two things:
 - 1) That the process locks the value with a mutex, preventing a race condition.
 - 2) In the possible event that the first check was against an old value while another process was updating, we do not put a worse value than the new one that was being written.
- We handle this by locking, then testing again.

First scenario



Second scenario



Pseudo-code for a Pthreads implementation of a statically parallelized solution to TSP

```
Partition_tree(my_rank, my_stack);
while (!Empty(my_stack)) {
   curr_tour = Pop(my_stack);
   if (City_count(curr_tour) == n) {
      if (Best_tour(curr_tour)) Update_best_tour(curr_tour);
   } else {
      for (city = n-1; city >= 1; city--)
         if (Feasible(curr_tour, city)) {
            Add_city(curr_tour, city);
            Push_copy(my_stack, curr_tour);
            Remove_last_city(curr_tour)
  Free_tour(curr_tour);
```



Dynamic Parallelization of Tree Search Using Pthreads

- Termination issues.
- Code executed by a thread before it splits:
 - It checks that it has at least two tours in its stack.
 - It checks that there are threads waiting.
 - It checks whether the new_stack variable is NULL.

Pseudo-Code for Pthreads Terminated Function (1)

```
if (my\_stack\_size >= 2 \&\& threads\_in\_cond\_wait > 0 \&\&
     new_stack == NULL) {
  lock term_mutex;
   if (threads_in_cond_wait > 0 && new_stack == NULL) {
      Split my stack creating new stack;
     pthread_cond_signal(&term_cond_var);
  unlock term_mutex;
  return 0; /* Terminated = False; don't quit */
 else if (!Empty(my_stack)) { /* Stack not empty, keep working */
  return 0; /* Terminated = false; don't quit */
} else { /* My stack is empty */
  lock term_mutex;
   if (threads_in_cond_wait == thread_count-1) { /* Last thread
                                                  /* running
      threads_in_cond_wait++;
      pthread_cond_broadcast(&term_cond_var);
      unlock term_mutex;
      return 1; /* Terminated = true; quit */
```



Pseudo-Code for Pthreads Terminated Function (2)

```
} else { /* Other threads still working, wait for work */
  threads_in_cond_wait++;
   while (pthread_cond_wait(&term_cond_var, &term_mutex) != 0);
  /* We've been awakened */
   if (threads_in_cond_wait < thread_count) { /* We got work */</pre>
      my_stack = new_stack;
      new_stack = NULL;
      threads in cond wait --:
      unlock term mutex;
      return 0; /* Terminated = false */
   } else { /* All threads done */
      unlock term_mutex;
      return 1; /* Terminated = true; quit */
} /* else wait for work */
/* else my_stack is empty */
```



Grouping the termination variables

```
typedef struct {
    my_stack_t new_stack;
    int threads_in_cond_wait;
    pthread_cond_t term_cond_var;
    pthread_mutex_t term_mutex;
} term_struct;
typedef term_struct* term_t;

term_t term; // global variable
```

Run-times of Pthreads tree search programs

15-city problems

		First Pr	oblem		Second Problem				
Threads	Serial	Static	Dynamic		Serial	Static	Dyn	namic	
1	32.9	32.7	34.7 (0)		26.0	25.8	27.5	(0)	
2		27.9	28.9	(7)		25.8	19.2	(6)	
4		25.7	25.9	(47)		25.8	9.3	(49)	
8		23.8	22.4	(180)		24.0	5.7	(256)	

(in seconds)



numbers of times stacks were split

Parallelizing the Tree Search Programs Using OpenMP

- Same basic issues implementing the static and dynamic parallel tree search programs as Pthreads.
- A few small changes can be noted.

```
pthreads
if (my_rank == whatever)

# pragma omp single
```

OpenMP emulated condition wait

```
/* Global vars */
int awakened_thread = -1;
work_remains = 1; /* true */
. . .
omp_unset_lock(&term_lock);
while (awakened_thread != my_rank && work_remains);
omp_set_lock(&term_lock);
```

Condition Variables

```
got_lock = omp_test_lock(&term_lock);
if (got_lock != 0) {
   if (waiting_threads > 0 && new_stack == NULL)
      Split my_stack creating new_stack;
      awakened_thread = Dequeue(term_queue);
   omp_unset_lock(&term_lock);
```

Performance of OpenMP and Pthreads implementations of tree search

	First Problem						Second Problem					
	Static Dynamic					Static Dyna			amic			
Th	OMP	Pth	OMP		Pth		OMP	Pth	OMP		Pth	
1	32.5	32.7	33.7	33.7 (0)		(0)	25.6	25.8	26.6	(0)	27.5	(0)
2	27.7	27.9	28.0	(6)	28.9	(7)	25.6	25.8	18.8	(9)	19.2	(6)
4	25.4	25.7	33.1	(75)	25.9	(47)	25.6	25.8	9.8	(52)	9.3	(49)
8	28.0	23.8	19.2	(134)	22.4	(180)	23.8	24.0	6.3	(163)	5.7	(256)

(in seconds)

IMPLEMENTATION OF TREE SEARCH USING MPI AND STATIC PARTITIONING

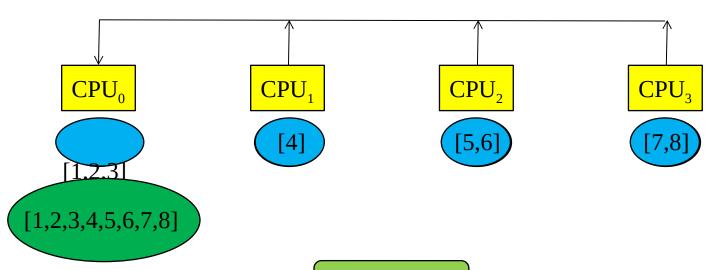
Sending a different number of objects to each process in the communicator

Gathering a different number of objects from each process in the communicator

```
int MPI_Gatherv(
    void*
         sendbuf
                         /* in */.
       sendcount /*in */,
    int
    MPI_Datatype sendtype /* in */,
    void* recvbuf /* out */,
    int* recvcounts /* in */,
       displacements /*in */,
    int*
                        /* in */,
    MPI_Datatype recvtype
                         /* in */.
    int
         root
                          /* in */)
    MPI_Comm
              comm
```

MPI_Gatherv

```
int dest = 0, Send_cnt = sizeof(Sbuf);
int rc[4] = {3,1,2,2}, disp[4] = {0,3,4,6};
MPI_Gatherv ( Sbuf, Send_cnt, MPI_INTEGER, Rbuf, rc, disp,
MPI_INTEGER , dest, MPI_COMM_WORLD);
```





A new best cost

Checking to see if a message is available

MPI_Iprobe(MPI_ANY_SOURCE, NEW_COST_TAG, comm, &msg_avail, &status);

```
MPI_Iprobe(MPI_ANY_SOURCE, NEW_COST_TAG, comm, &msg_avail,
      &status):
while (msg_avail) {
   MPI_Recv(&received_cost, 1, MPI_INT, status.MPI_SOURCE,
         NEW_COST_TAG, comm, MPI_STATUS_IGNORE);
   if (received_cost < best_tour_cost)</pre>
      best_tour_cost = received_cost;
   MPI_Iprobe(MPI_ANY_SOURCE, NEW_COST_TAG, comm, &msg_avail,
     &status):
   /* while */
```



```
if (My_avail_tour_count(my_stack) >= 2) {
  Fulfill_request(my_stack);
  return false; /* Still more work */
} else { /* At most 1 available tour */
  Send_rejects(); /* Tell everyone who's requested */
                   /* work that I have none
  if (!Empty_stack(my_stack)) {
     return false; /* Still more work */
  } else { /* Empty stack */
     if (comm_sz == 1) return true;
     Out_of_work();
     work_request_sent = false;
     while (1) {
        Clear_msqs(); /* Messages unrelated to work, termination */
        if (No_work_left()) {
           return true; /* No work left. Quit */
        } else if (!work_request_sent) {
           Send work request(); /* Request work from someone */
           work_request_sent = true;
        } else {
           Check_for_work(&work_request_sent, &work_avail);
           if (work_avail) {
              Receive_work(my_stack);
                                                         Terminated Function for
              return false;
                                                         a Dynamically
        /* while */
                                                         Partitioned TSP solver
  } /* Empty stack */
                                                         that Uses MPI.
} /* At most 1 available tour */
```



Modes and Buffered Sends

MPI provides four modes for sends.

```
    Standard

                                  MPI_Send,
Synchronous
                                  MPI_Ssend
                                                 This routine is thread-
Ready
                                  MPI_Rsend⁴
                                                 safe.

    Buffered

                                  MPI_Bsend
                                    int MPI_Xsend(
                                          void∗
                                                                   /* in */,
                                                       message
it allows the user to send messages
                                          int
                                                       message_size /* in */,
                                                       message_type /* in */,
without worring about where they are
                                          MPI_Datatype
                                                       dest
                                                                   /* in */,
buffered
                                          int
                                          int
                                                                     /* in */,
                                                       tag
                                          MPI Comm
                                                                     /* in */):
                                                       comm
```



Printing the best tour

```
struct {
  int cost:
  int rank;
} loc_data, global_data;
loc_data.cost = Tour_cost(loc_best_tour);
loc_data.rank = my_rank;
MPI_Allreduce(&loc_data, &global_data, 1, MPI_2INT, MPI_MINLOC, comm);
if (global_data.rank == 0) return; /* 0 already has the best tour */
if (my_rank == 0)
   Receive best tour from process global_data.rank;
else if (my_rank == global_data.rank)
   Send best tour to process 0;
```

Terminated Function for a Dynamically Partitioned TSP solver with MPI (1)

```
if (My_avail_tour_count(my_stack) >= 2) {
  Fulfill_request(my_stack);
   return false: /* Still more work */
} else { /* At most 1 available tour */
   Send_rejects(); /* Tell everyone who's requested */
                   /* work that I have none
   if (!Empty_stack(my_stack)) {
      return false; /* Still more work */
   \} else \{ /* Empty stack */
      if (comm_sz == 1) return true;
      Out_of_work();
     work_request_sent = false;
      while (1)
         Clear_msgs(); /* Messages unrelated to work, termination */
         if (No_work_left()) {
            return true; /* No work left. Quit */
```

Terminated Function for a Dynamically Partitioned TSP solver with MPI (2)

```
} else if (!work_request_sent) {
        Send_work_request(); /* Request work from someone */
        work_request_sent = true;
} else {
        Check_for_work(&work_request_sent, &work_avail);
        if (work_avail) {
            Receive_work(my_stack);
            return false;
        }
    }
} /* while */
} /* Empty stack */
} /* At most 1 available tour */
```

Packing data into a buffer of contiguous memory

```
int MPI_Pack(
    void*
                data_to_be_packed /*in */,
                to_be_packed_count /* in */,
     int
                                 /* in */,
    MPI_Datatype
               datatype
    void*
          contig_buf
                          /* out */,
                contig_buf_size /*in */,
     int
     int*
                position_p
                               /* in/out */,
                                  /* in
    MPI_Comm
                comm
```



Unpacking data from a buffer of contiguous memory

```
int MPI_Unpack(
     void*
                                   /* in
                 contig_buf
                 contig_buf_size /* in */,
     int
     int*
                             /* in/out */,
                 position_p
                 unpacked_data /* out */,
     void*
                                   /* in */,
     int
                 unpack_count
                                   /* in
                                            */,
     MPI_Datatype
                datatype
                                    /* in
     MPI_Comm
                 comm
```



```
typedef struct {
   int* cities; /* Cities in partial tour
                                                        * /
   int count; /* Number of cities in partial tour
   int cost; /* Cost of partial tour
} tour_struct;
typedef tour_struct* tour_t;
void Send_tour(tour_t tour, int dest) {
   int position = 0;
  MPI_Pack(tour->cities, n+1, MPI_INT, contig_buf, LARGE,
        &position, comm);
  MPI_Pack(&tour->count, 1, MPI_INT, contig_buf, LARGE,
        &position, comm);
  MPI_Pack(&tour->cost, 1, MPI_INT, contig_buf, LARGE,
        &position, comm);
   MPI_Send(contig_buf, position, MPI_PACKED, dest, 0, comm);
  /* Send_tour */
```

```
void Receive_tour(tour_t tour, int src) {
   int position = 0;
   MPI_Recv(contig_buf, LARGE, MPI_PACKED, src, 0, comm,
         MPI_STATUS_IGNORE):
   MPI_Unpack(contig_buf, LARGE, &position, tour->cities, n+1,
         MPI_INT. comm):
   MPI_Unpack(contig_buf, LARGE, &position, &tour->count, 1,
         MPI_INT, comm);
   MPI_Unpack(contig_buf, LARGE, &position, &tour->cost, 1,
         MPI_INT. comm):
  /* Receive_tour */
```



Table 6.10 Termination Events that Result in an Error										
Time	Process 0	Process 1	Process 2							
0	Out of Work Notify 1, 2 oow = 1	Out of Work Notify 0, 2 oow = 1	Working oow = 0							
1	Send request to 1 oow = 1	Send Request to 2	Recv notify fr 1 oow = 1							
2	oow = 1	Recv notify fr 0 oow = 2	Recv request fr 1 oow = 1							
3	oow = 1	oow = 2	Send work to 1							
4	oow = 1	Recv work fr 2	Recv notify fr 0							
5	oow = 1	Notify 0 oow = 1	Working							
6	oow = 1	Recv request fr 0 00w = 1	Out of work Notify 0, 1 oow = 2							
7	Recv notify fr 2	Send work to 0	Send request to 1 oow = 2							
8	Recv 1st notify fr 1	Recv notify fr 2 oow = 1	oow = 2							
9	Quit	Recv request fr 2	oow = 2							



Performance of MPI and Pthreads implementations of tree search

	First Problem					Second Problem						
	Sta	Static Dyr			namic		Static		Dynamic			
Th/Pr	Pth	MPI	Pth		MPI		Pth	MPI	Pth		MPI	
1	35.8	40.9	41.9	(0)	56.5	(0)	27.4	31.5	32.3	(0)	43.8	(0)
2	29.9	34.9	34.3	(9)	55.6	(5)	27.4	31.5	22.0	(8)	37.4	(9)
4	27.2	31.7	30.2	(55)	52.6	(85)	27.4	31.5	10.7	(44)	21.8	(76)
8		35.7			45.5	(165)		35.7			16.5	(161)
16		20.1			10.5	(441)		17.8			0.1	(173)

(in seconds)

Concluding Remarks (1)

- In developing the reduced MPI solution to the n-body problem, the "ring pass" algorithm proved to be much easier to implement and is probably more scalable.
- In a distributed memory environment in which processes send each other work, determining when to terminate is a nontrivial problem.

Concluding Remarks (2)

 When deciding which API to use, we should consider whether to use shared- or distributed-memory.

 We should look at the memory requirements of the application and the amount of communication among the processes/threads.

Concluding Remarks (3)

 If the memory requirements are great or the distributed memory version can work mainly with cache, then a distributed memory program is likely to be much faster.

 On the other hand if there is considerable communication, a shared memory program will probably be faster.

Concluding Remarks (3)

 In choosing between OpenMP and Pthreads, if there's an existing serial program and it can be parallelized by the insertion of OpenMP directives, then OpenMP is probably the clear choice.

 However, if complex thread synchronization is needed then Pthreads will be easier to use.

