

Master Thesis

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1 Introduction

1.1 Existing Algorithms

Chen et al. [1] used the Centroid and Weighted Centroid algorithms, amongst others, to examine the positioning accuracy of a GSM beacon-based location system in a metropolitan environment. Yang et al. [2] studied the Weighted Centroid and Strongest Received Signal Strength algorithms for cell tower localization.

1.1.1 Centroid

The Centroid algorithm estimates a cell tower's position to be the geometric center of the measurements for that cell. It is the mean of the measurements' longitudes and latitudes.

Below follows the mathematical expression for a cell tower's position in a cell with n measurements, where lon =longitude and lat =latitude, and the pseudocode for the algorithm.

$$lon_{cellTower} = \frac{1}{n} \sum_{i=1}^n (lon_i), \text{ and}$$
$$lat_{cellTower} = \frac{1}{n} \sum_{i=1}^n (lat_i)$$

Algorithm 1 Centroid

```
1: procedure CENTROID(measurements  $\leftarrow$  a list of measurements for a
   cell)
2:   sumOfLongitudes  $\leftarrow$  0.0
3:   sumOfLatitudes  $\leftarrow$  0.0
4:   for each m  $\in$  measurements do
5:     sumOfLongitudes  $\leftarrow$  sumOfLongitudes + m.longitude
6:     sumOfLatitudes  $\leftarrow$  sumOfLatitudes + m.latitude
7:   end for
8:   cellTowerLongitude  $\leftarrow$  sumOfLongitudes  $\div$  measurements.size
9:   cellTowerLatitude  $\leftarrow$  sumOfLatitudes  $\div$  measurements.size
10:  return cellTowerLongitude, cellTowerLatitude
11: end procedure
```

1.1.2 Weighted Centroid

The Weighted Centroid algorithm is an extension of the Centroid algorithm. Here, the measurements are given weights based on the *received signal strength* (RSS) at each measurement. The measurements with strong signals are likely to be closer to the cell tower's real position than those with weaker signals, so we want to emphasize these measurements when calculating the cell tower's position. The unit of measurement for these kind of signals are *Decibel-milliwatts* (dBm) and they range from approximately -30 dBm and lower. Due to the negative values we want to translate them into weights with positive values to make them viable to use for calculations.

Below follows the mathematical expression for a cell tower's position in a cell with n measurements, where lon =longitude, lat =latitude and w is a measurement's weight based on the RSS, and the pseudocode for the algorithm.

$$lon_{cellTower} = \frac{1}{\sum_{j=1}^n w_j} \sum_{i=1}^n (lon_i \times w_i), \text{ and}$$
$$lat_{cellTower} = \frac{1}{\sum_{j=1}^n w_j} \sum_{i=1}^n (lat_i \times w_i)$$

Algorithm 2 Weighted Centroid

```
1: procedure WEIGHTEDCENTROID(measurements  $\leftarrow$  a list of measure-
   measurements for a cell)
2:   sumOfWeights  $\leftarrow$  0
3:   for each m  $\in$  measurements do
4:     sumOfWeights  $\leftarrow$  sumOfWeights+m.signal
5:   end for
6:   x  $\leftarrow$  0.0
7:   y  $\leftarrow$  0.0
8:   for each m  $\in$  measurements do
9:     x  $\leftarrow$  x+(m.longitude $\times$ m.signal)
10:    y  $\leftarrow$  y+(m.latitude $\times$ m.signal)
11:   end for
12:   cellTowerLongitude  $\leftarrow$  x  $\div$  sumOfWeights
13:   cellTowerLatitude  $\leftarrow$  y  $\div$  sumOfWeights
14:   return cellTowerLongitude, cellTowerLatitude
15: end procedure
```

1.1.3 Strongest Received Signal Strength

The Strongest RSS algorithm estimates a cell tower's position as the position of the measurement with the strongest observed RSS from that cell tower. If multiple measurements qualify, we apply algorithm 1 on these.

Below follows the mathematical expression for a cell tower's position in a cell with n measurements, where lon =longitude, lat =latitude and w is a measurement's weight based on the RSS, and the pseudocode for the algorithm.

$$lon_{cellTower} = \frac{1}{m} \sum_{i=1}^m (lon_i), \text{ and}$$
$$lat_{cellTower} = \frac{1}{m} \sum_{i=1}^m (lat_i), \text{ where}$$
$$m = |W| = \{w : w \in \max(w_1, w_2, \dots, w_n)\}$$

Algorithm 3 Strongest Received Signal Strength

```
1: procedure STRONGESTRSS(measurements  $\leftarrow$  a list of measurements  
   for a cell)  
2:   strongestSignalMeasurements  $\leftarrow$  a list to store the measurements with  
   the strongest signal  
3:   currentStrongestSignal  $\leftarrow -1$   
4:   for each m  $\in$  measurements do  
5:     if m.signal > currentStrongestSignal then  
6:       clear strongestSignalMeasurements  
7:       add m to strongestSignalMeasurements  
8:       currentStrongestSignal  $\leftarrow$  m.signal  
9:     else if m.signal = currentStrongestSignal then  
10:      add m to strongestSignalMeasurements  
11:    end if  
12:  end for  
13:  x  $\leftarrow$  0.0  
14:  y  $\leftarrow$  0.0  
15:  for each m  $\in$  strongestSignalMeasurements do  
16:    x  $\leftarrow$  x + m.longitude  
17:    y  $\leftarrow$  y + m.latitude  
18:  end for  
19:  cellTowerLongitude  $\leftarrow$  x  $\div$  strongestSignalMeasurements.size  
20:  cellTowerLatitude  $\leftarrow$  y  $\div$  strongestSignalMeasurements.size  
21:  return cellTowerLongitude, cellTowerLatitude  
22: end procedure
```

1.2 Testdata

We wrote a small Java program for generating testdata. Below follow three example screenshots where we apply algorithm 1, 2 and 3 on three random generated cells with 10, 20 and 40 measurements, respectively. The cell tower is placed in the middle and the measurements are generated randomly around it.

- Black circles: Measurements
- Black square: Real position of cell tower
- Blue square: Position of cell tower calculated by Centroid
- Green square: Position of cell tower calculated by Weighted Centroid
- Red square: Position of cell tower calculated by Strongest RSS

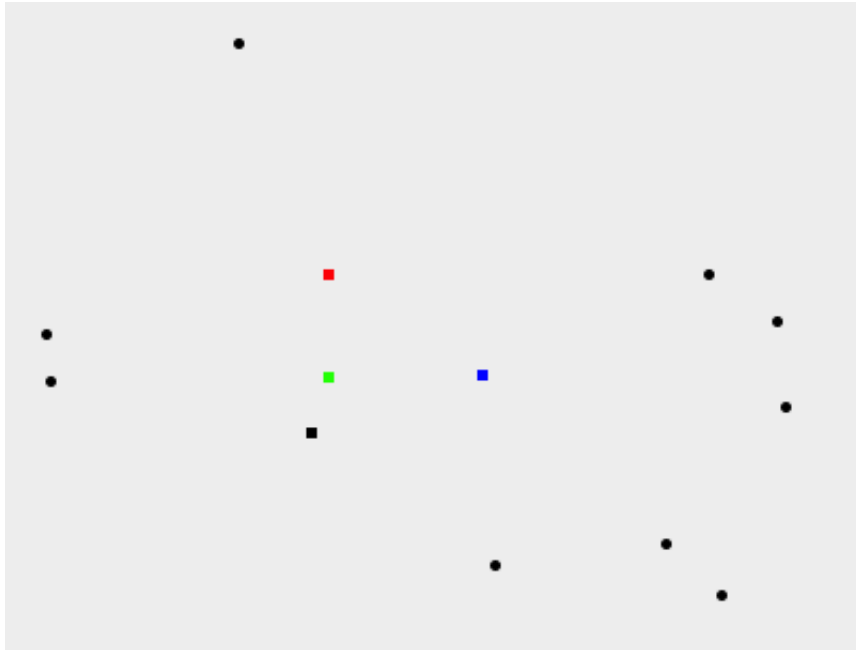


Figure 1: Random generated cell with 10 measurements

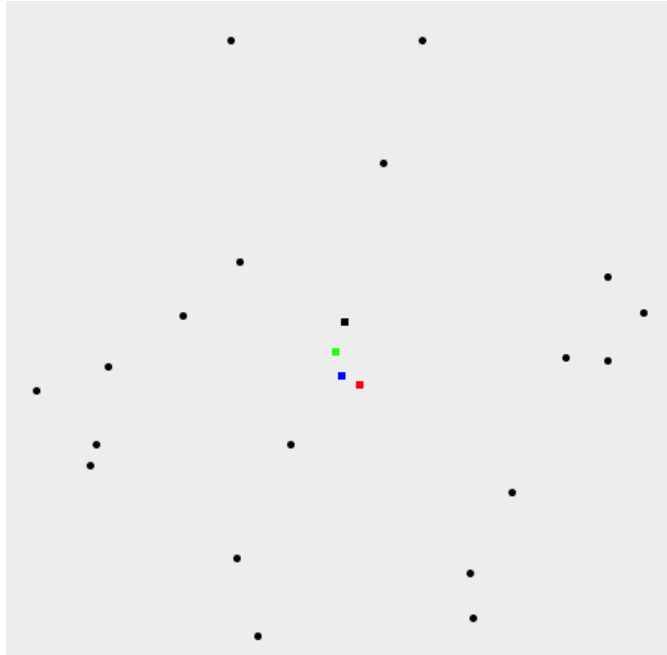


Figure 2: Random generated cell with 20 measurements

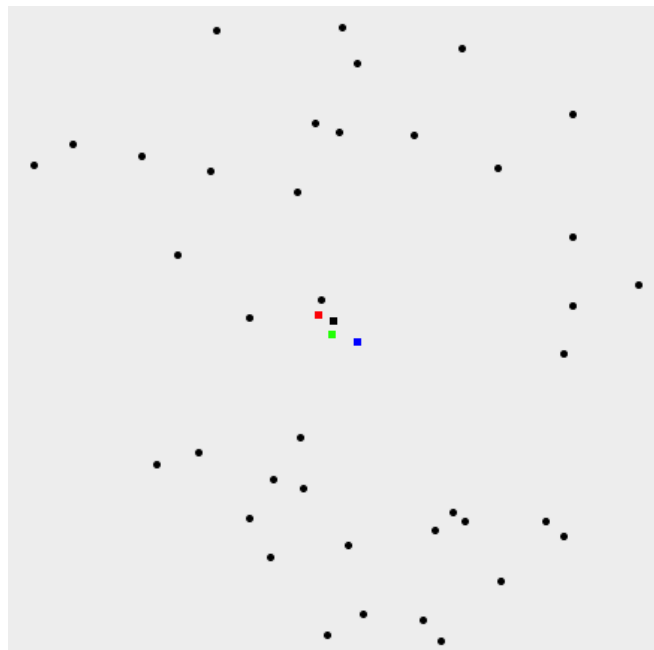


Figure 3: Random generated cell with 40 measurements

References

- [1] M. Y. Chen, T. Sohn, D. Chmlev, D. Hachmel, J. Hightower, J. Hughes, A. LaMarca, F. Potter, I. Smith, and A. Varshavsky. Practical Metropolitan-Scale Positioning for GSM Phones. *UbiComp*, 2006.
- [2] J. Yang, A. Varshavsky, H. Liu, Y. Chen, and M. Gruteser. Accuracy Characterization of Cell Tower Localization. *UbiComp*, 2010.

A Code

```
package testdata;

import java.awt.geom.Point2D;
import java.util.Random;

public class Measurement {

    private Point2D.Double coordinates;

    // Signal Strength = sqrt((x2-x1)^2 + (y2-y1)^2) multiplied by -1 to achieve realistic dBm
    private int signalStrength;

    // Weight = 113 - (-1 * Signal Strength)
    private int weight;

    public Measurement(double longitude, double latitude) {
        this.coordinates = new Point2D.Double(longitude, latitude);
        this.signalStrength = 99;
        this.weight = -99;
    }

    public Point2D.Double getCoordinates() {
        return coordinates;
    }

    public void setCoordinates(Point2D.Double coordinates) {
        this.coordinates = coordinates;
    }

    public int getSignalStrength() {
        return signalStrength;
    }

    public void setSignalStrength(int signalStrength) {
        this.signalStrength = signalStrength;
    }

    public int getWeight() {
        return weight;
    }

    public void setWeight(int weight) {
        this.weight = weight;
    }

    @Override
    public String toString() {
        String s = String.format("Measurement coordinates: [%1f,%1f] - Signal Strength: %d dBm - Weight: %d",
            this.coordinates.x, this.coordinates.y, this.signalStrength, this.weight);
        return s;
    }

    public static Measurement generateRandomMeasurement(int maxX, int maxY) {
        double x = (double) new Random().nextInt(maxX+1);
        double y = (double) new Random().nextInt(maxY+1);

        return new Measurement(x, y);
    }
}

package testdata;

import java.awt.geom.Point2D;
import java.util.ArrayList;
import java.util.List;

public class Cell {

    protected static final String MEASUREMENTS_ALL = "all measurements";
    protected static final String MEASUREMENTS_THRESHOLD = "measurements filtered";

    protected static final int CELL_X_Y_VALUE = 113;
    protected static final int MEASUREMENT_X_Y_LIMIT = 226;

    private Point2D.Double cellTowerCoordinates;

    // Pointer
    private List<Measurement> measurements;
```

```

// List for storing all measurements
private List<Measurement> measurementsAll;

// List for storing measurements above a certain weight threshold
private List<Measurement> measurementsWithThreshold;

public Cell() {
    this.cellTowerCoordinates = new Point2D.Double((double) CELL_X.Y.VALUE, (double) CELL_X.Y.VALUE);
    this.measurementsAll = new ArrayList<Measurement>();
    this.measurementsWithThreshold = new ArrayList<Measurement>();
}

public Point2D.Double getCellTowerCoordinates() {
    return cellTowerCoordinates;
}

public void setCellTowerCoordinates(Point2D.Double cellTowerCoordinates) {
    this.cellTowerCoordinates = cellTowerCoordinates;
}

public List<Measurement> getMeasurements() {
    return measurements;
}

public void setMeasurements(List<Measurement> measurements) {
    this.measurements = measurements;
}

public void addRandomMeasurements(int measurements, int maxX, int maxY) {

    for(int i = 0; i < measurements; i++) {

        Measurement measurement;
        double d;
        do {
            measurement = Measurement.generateRandomMeasurement(maxX, maxY);
            d = this.cellTowerCoordinates.distance(measurement.getCoordinates());
        } while(d > 113.0);

        int dBm = Surface.doubleToInt(d)*-1;
        measurement.setSignalStrength(dBm);

        int weight = 113 - (-1*measurement.getSignalStrength());
        measurement.setWeight(weight);

        this.measurementsAll.add(measurement);

        this.useMeasurements(MEASUREMENTS_ALL);
    }
    return;
}

protected Cell applyWeightThreshold(int minimumWeight) {
    this.measurementsWithThreshold.clear();
    for(Measurement measurement : this.measurementsAll) {
        if(measurement.getWeight() >= minimumWeight) {
            this.measurementsWithThreshold.add(measurement);
        }
    }
    return this;
}

protected Cell useMeasurements(String measurementsList) {
    if(measurementsList.equals(MEASUREMENTS_ALL)) {
        this.measurements = this.measurementsAll;
    }
    else if (measurementsList.equals(MEASUREMENTS_THRESHOLD)) {
        this.measurements = this.measurementsWithThreshold;
    }
    else {
        throw new IllegalArgumentException("There is no such list");
    }
    return this;
}

@Override
public String toString() {
    String s = String.format("Cell Tower Coordinates: [%1f,%1f]\n\tMeasurements: %d",
        this.cellTowerCoordinates.x, this.cellTowerCoordinates.y, this.measurements.size());
    for(Measurement measurement : this.measurements) {
        s += "\n\t" + measurement.toString();
    }
}

```

```

        s += "\n";
        return s;
    }

    public static Cell generateCellWithRandomMeasurements(int measurements) {

        Cell cell = new Cell();

        if(measurements > 0) {
            cell.addRandomMeasurements(measurements, MEASUREMENT_X_Y_LIMIT, MEASUREMENT_X_Y_LIMIT);
        }

        return cell;
    }
}

package testdata;

import java.awt.geom.Point2D;
import java.util.ArrayList;
import java.util.List;

public class Statistics {

    private Cell cell;

    private Point2D.Double centroidCoordinates;
    private Point2D.Double weightedCentroidCoordinates;
    private Point2D.Double strongestRSSCoordinates;

    private Point2D.Double centroidWithThresholdCoordinates;
    private Point2D.Double weightedCentroidWithThresholdCoordinates;
    private Point2D.Double strongestRSSWithThresholdCoordinates;

    public Statistics(int measurements) {
        this.cell = Cell.generateCellWithRandomMeasurements(measurements);
        this.centroidCoordinates = centroid(this.cell);
        this.weightedCentroidCoordinates = weightedCentroid(this.cell);
        this.strongestRSSCoordinates = strongestRSS(this.cell);

        int threshold = 50;

        this.centroidWithThresholdCoordinates =
            centroid(this.cell.applyWeightThreshold(threshold).useMeasurements(Cell.MEASUREMENTS_THRESHOLD));
        this.weightedCentroidWithThresholdCoordinates = weightedCentroid(this.cell);
        this.strongestRSSWithThresholdCoordinates = strongestRSS(this.cell);

        System.out.println(this.toString());
    }

    public static void main(String[] args) {

        Statistics statistics = new Statistics(5);

        System.out.println("\nEND OF PROGRAM");
    }

    public Cell getCell() {
        return cell;
    }

    public void setCell(Cell cell) {
        this.cell = cell;
    }

    public Point2D.Double getCentroidCoordinates() {
        return centroidCoordinates;
    }

    public void setCentroidCoordinates(Point2D.Double centroidCoordinates) {
        this.centroidCoordinates = centroidCoordinates;
    }

    public Point2D.Double getWeightedCentroidCoordinates() {
        return weightedCentroidCoordinates;
    }

    public void setWeightedCentroidCoordinates(
        Point2D.Double weightedCentroidCoordinates) {
        this.weightedCentroidCoordinates = weightedCentroidCoordinates;
    }
}

```

```

public Point2D.Double getStrongestRSSCoordinates() {
    return strongestRSSCoordinates;
}

public void setStrongestRSSCoordinates(Point2D.Double strongestRSSCoordinates) {
    this.strongestRSSCoordinates = strongestRSSCoordinates;
}

public Point2D.Double getCentroidWithThresholdCoordinates() {
    return centroidWithThresholdCoordinates;
}

public void setCentroidWithThresholdCoordinates(
    Point2D.Double centroidWithThresholdCoordinates) {
    this.centroidWithThresholdCoordinates = centroidWithThresholdCoordinates;
}

public Point2D.Double getWeightedCentroidWithThresholdCoordinates() {
    return weightedCentroidWithThresholdCoordinates;
}

public void setWeightedCentroidWithThresholdCoordinates(
    Point2D.Double weightedCentroidWithThresholdCoordinates) {
    this.weightedCentroidWithThresholdCoordinates = weightedCentroidWithThresholdCoordinates;
}

public Point2D.Double getStrongestRSSWithThresholdCoordinates() {
    return strongestRSSWithThresholdCoordinates;
}

public void setStrongestRSSWithThresholdCoordinates(
    Point2D.Double strongestRSSWithThresholdCoordinates) {
    this.strongestRSSWithThresholdCoordinates = strongestRSSWithThresholdCoordinates;
}

@Override
public String toString() {
    String s = "";
    if (this.cell.useMeasurements(Cell.MEASUREMENTS_ALL).getMeasurements().size() <= 5) {
        s += this.cell.useMeasurements(Cell.MEASUREMENTS_ALL).toString();
        s += "\n";
    }

    s += "\t\tCell Tower Longitude\tCell Tower Latitude\tError\n";
    s += String.format("Real\t\t%.1f\t\t%.1f\t\t%.1f\n", this.cell.getCellTowerCoordinates().getX(),
        this.cell.getCellTowerCoordinates().getY(),
        this.cell.getCellTowerCoordinates().distance(this.cell.getCellTowerCoordinates()));
    s += String.format("Centroid\t\t%.1f\t\t%.1f\t\t%.1f\n", this.centroidCoordinates.getX(),
        this.centroidCoordinates.getY(),
        this.cell.getCellTowerCoordinates().distance(this.getCentroidCoordinates()));
    s += String.format("Centroid >= 50\t\t%.1f\t\t%.1f\t\t%.1f\n", this.centroidWithThresholdCoordinates.getX(),
        this.centroidWithThresholdCoordinates.getY(),
        this.cell.getCellTowerCoordinates().distance(this.getCentroidWithThresholdCoordinates()));
    s += String.format("Weighted Centroid\t\t%.1f\t\t%.1f\t\t%.1f\n", this.weightedCentroidCoordinates.getX(),
        this.weightedCentroidCoordinates.getY(),
        this.cell.getCellTowerCoordinates().distance(this.getWeightedCentroidCoordinates()));
    s += String.format("Weighted Centroid >= 50\t\t%.1f\t\t%.1f\t\t%.1f\n", this.weightedCentroidWithThresholdCoordinates.getX(),
        this.weightedCentroidWithThresholdCoordinates.getY(),
        this.cell.getCellTowerCoordinates().distance(this.getWeightedCentroidWithThresholdCoordinates()));
    s += String.format("Strongest RSS\t\t%.1f\t\t%.1f\t\t%.1f\n", strongestRSSCoordinates.getX(),
        strongestRSSCoordinates.getY(),
        this.cell.getCellTowerCoordinates().distance(this.getStrongestRSSCoordinates()));
    s += String.format("Strongest RSS >= 50\t\t%.1f\t\t%.1f\t\t%.1f\n", this.strongestRSSWithThresholdCoordinates.getX(),
        this.strongestRSSWithThresholdCoordinates.getY(),
        this.cell.getCellTowerCoordinates().distance(this.getStrongestRSSWithThresholdCoordinates()));

    return s;
}

private static Point2D.Double weightedCentroid(Cell cell) {
    int sumOfWeights = 0;
    for (Measurement measurement : cell.getMeasurements()) {
        sumOfWeights += measurement.getWeight();
    }

    double cellTowerLongitude = 0.0;
    double cellTowerLatitude = 0.0;
    for (Measurement measurement : cell.getMeasurements()) {

```

```

        double weightRatio = measurement.getWeight()/((double)sumOfWeights;

        cellTowerLongitude += (measurement.getCoordinates().getX()*weightRatio);
        cellTowerLatitude += (measurement.getCoordinates().getY()*weightRatio);
    }
    return new Point2D.Double(cellTowerLongitude, cellTowerLatitude);
}

private static Point2D.Double centroid(Cell cell) {
    double sumOfLongitudes = 0;
    double sumOfLatitudes = 0;
    for(Measurement measurement : cell.getMeasurements()) {
        sumOfLongitudes += measurement.getCoordinates().getX();
        sumOfLatitudes += measurement.getCoordinates().getY();
    }
    double cellTowerLongitude = sumOfLongitudes/cell.getMeasurements().size();
    double cellTowerLatitude = sumOfLatitudes/cell.getMeasurements().size();

    return new Point2D.Double(cellTowerLongitude, cellTowerLatitude);
}

private static Point2D.Double strongestRSS(Cell cell) {
    int currentStrongestWeight = -1;
    List<Measurement> strongestWeightMeasurements = new ArrayList<Measurement>();
    for(Measurement measurement : cell.getMeasurements()) {
        if(measurement.getWeight() > currentStrongestWeight) {
            strongestWeightMeasurements.clear();
            strongestWeightMeasurements.add(measurement);
            currentStrongestWeight = measurement.getWeight();
        }
        else if(measurement.getWeight() == currentStrongestWeight) {
            strongestWeightMeasurements.add(measurement);
        }
    }
    double sumOfLongitudes = 0.0;
    double sumOfLatitudes = 0.0;
    for(Measurement measurement : strongestWeightMeasurements) {
        sumOfLongitudes += measurement.getCoordinates().getX();
        sumOfLatitudes += measurement.getCoordinates().getY();
    }
    double cellTowerLongitude = sumOfLongitudes/strongestWeightMeasurements.size();
    double cellTowerLatitude = sumOfLatitudes/strongestWeightMeasurements.size();
    return new Point2D.Double(cellTowerLongitude, cellTowerLatitude);
}
}

package testdata;

import java.awt.Color;
import java.awt.Dimension;
import java.awt.EventQueue;
import java.awt.Graphics;
import java.awt.Graphics2D;
import java.awt.Insets;
import java.awt.RenderingHints;
import java.awt.geom.AffineTransform;
import java.awt.geom.Point2D;
import java.util.List;

import javax.swing.JFrame;
import javax.swing.JPanel;

class Surface extends JPanel {

    Statistics statistics ;

    public Surface() {
        this.statistics = new Statistics(40);
    }

    private void doDrawing(Graphics g) {
        Graphics2D g2d = (Graphics2D) g;

        // AffineTransform transform = AffineTransform.getTranslateInstance(0, 700);
        // transform.scale(700, -700);
        // g2d.setTransform(transform);

        g2d.setColor(Color.black);

        RenderingHints rh = new RenderingHints(RenderingHints.KEY_ANTIALIASING,
            RenderingHints.VALUE_ANTIALIAS_ON);
        rh.put(RenderingHints.KEY_RENDERING, RenderingHints.VALUE_RENDER_QUALITY);
        g2d.setRenderingHints(rh);
    }
}

```



```

Dimension size = getSize();
Insets insets = getInsets();
int w = size.width - insets.left - insets.right;
int h = size.height - insets.top - insets.bottom;

// Cell Tower real coords
Point2D.Double cellTower = this.statistics.getCell().getCellTowerCoordinates();
int x = doubleToInt(enlarge(cellTower.getX()));
int y = invertLatitude(h, enlarge(cellTower.getY()));
g2d.fillRect(x, y, 5, 5);

// Measurements coords
List<Measurement> measurements = this.statistics.getCell().getMeasurements();
for (Measurement measurement : measurements) {
    x = doubleToInt(enlarge(measurement.getCoordinates().getX()));
    y = invertLatitude(h, enlarge(measurement.getCoordinates().getY()));
    g2d.fillOval(x, y, 5, 5);
}

// Cell Tower Centroid coords
g2d.setColor(Color.blue);
Point2D.Double centroidCoordinates = this.statistics.getCentroidCoordinates();
x = doubleToInt(enlarge(centroidCoordinates.getX()));
y = invertLatitude(h, enlarge(centroidCoordinates.getY()));
g2d.fillRect(x, y, 5, 5);

// Cell Tower Weighted Centroid coords
g2d.setColor(Color.green);
Point2D.Double weightedCentroidCoordinates = this.statistics.getWeightedCentroidCoordinates();
x = doubleToInt(enlarge(weightedCentroidCoordinates.getX()));
y = invertLatitude(h, enlarge(weightedCentroidCoordinates.getY()));
g2d.fillRect(x, y, 5, 5);

// Cell Tower Strongest RSS coords
g2d.setColor(Color.red);
Point2D.Double strongestRSSCoordinates = this.statistics.getStrongestRSSCoordinates();
x = doubleToInt(enlarge(strongestRSSCoordinates.getX()));
y = invertLatitude(h, enlarge(strongestRSSCoordinates.getY()));
g2d.fillRect(x, y, 5, 5);

// Cell Tower Centroid with threshold coords
g2d.setColor(Color.cyan);
Point2D.Double centroidWithThresholdCoordinates = this.statistics.getCentroidWithThresholdCoordinates();
x = doubleToInt(enlarge(centroidWithThresholdCoordinates.getX()));
y = invertLatitude(h, enlarge(centroidWithThresholdCoordinates.getY()));
g2d.fillRect(x, y, 5, 5);

// Cell Tower Weighted Centroid with threshold coords
g2d.setColor(Color.orange);
Point2D.Double weightedCentroidWithThresholdCoordinates =
    this.statistics.getWeightedCentroidWithThresholdCoordinates();
x = doubleToInt(enlarge(weightedCentroidWithThresholdCoordinates.getX()));
y = invertLatitude(h, enlarge(weightedCentroidWithThresholdCoordinates.getY()));
g2d.fillRect(x, y, 5, 5);

// Cell Tower Strongest RSS with threshold coords
g2d.setColor(Color.pink);
Point2D.Double strongestRSSWithThresholdCoordinates =
    this.statistics.getStrongestRSSWithThresholdCoordinates();
x = doubleToInt(enlarge(strongestRSSWithThresholdCoordinates.getX()));
y = invertLatitude(h, enlarge(strongestRSSWithThresholdCoordinates.getY()));
g2d.fillRect(x, y, 5, 5);
}

protected static int invertLatitude(int height, double latitude) {
    double newY = ((double)height - latitude);
    return doubleToInt(newY);
}

protected static int doubleToInt(double d) {
    int toInt = (int)d;
    if (d - (double)toInt >= 0.5) {
        return toInt + 1;
    }
    else
        return toInt;
}

private double enlarge(double d) {
    return d * 2;
}

```

```
@Override
public void paintComponent(Graphics g) {
    super.paintComponent(g);
    doDrawing(g);
}

public class Map extends JFrame {

    final static int WIDTH = 700;
    final static int HEIGHT = 700;

    public Map() {
        initUI();
    }

    private void initUI() {
        setTitle("Map");

        add(new Surface());

        setSize(WIDTH, HEIGHT);
        setLocationRelativeTo(null);
        setDefaultCloseOperation(EXIT_ON_CLOSE);

    }

    public static void main(String[] args) {

        EventQueue.invokeLater(new Runnable() {
            @Override
            public void run() {
                Map map = new Map();
                map.setVisible(true);
            }
        });
    }
}
```
