Project Proposal: Register Machine Interpreter

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1 Background

In theoretical computer science, there have been many computational models proposed to study computability and complexity that are equivalent to one another in terms of computational power. Two best-known models are Turing machine and λ -calculus. Register machine, a lesser known model is put forth to discuss the Halting Problem and other decidability problems in the book Mathematical Logic by H.-D. Ebbinghaus, J. Flum and W. Thomas.

A register machine is associated with a fixed alphabet $\mathcal{A} = \{a_0, \dots, a_r\}$ and has countably many registers, each of which can store a string over \mathcal{A} of an arbitrary (finite) length.

A program for a register machine with alphabet \mathcal{A} is a finite nonempty sequence of instructions that each takes one of the forms below:

- L LET $R_i = R_i + a_j$, where $L, i, j \in \mathbb{N}$ and $j \leq r$ (Add-instruction: Add the letter a_j at the end of the string in register $mathrm R_i$);
- L LET $R_i = R_i a_j$, where $L, i, j \in \mathbb{N}$ and $j \leq r$ (Subtract-instruction: If the string in register R_i ends with the letter a_j , delete this a_j ; otherwise leave the word unchanged);
- L IF $R_i = \epsilon$ THEN L' ELSE L_0 OR ... OR L_r , for $L, i, L', L_0, \ldots, L_r \in \mathbb{N}$, where ϵ denotes the empty string (Jump-instruction: If register R_i contains the empty string go to instruction labelled L'; if the string in register R_i ends with a_0 (or a_1, \ldots, a_r , respectively) go to instruction labelled L_0 (or L_1, \ldots, L_r , respectively));
- L PRINT, for $L \in \mathbb{N}$ (Print-instruction: Print as output the string stored in register R_0);
- L HALT, for $L \in \mathbb{N}$ (Halt-instruction: Halt).

In a program of length n+1, the prefixing labels of instructions enumerate over $0, 1, 2, \ldots, n$, every jump instruction refers to labels no greater than n, and only the last instruction is a halt instruction.

2 Goal and Motivation

We have found this book an excellent reference for mathematical logic, and would like to write a register-machine interpreter in Haskell to run the programs given in this book for a deeper level of understanding and to experiment our ideas concerning the computatioal model of register machine.

3 Work Schedule and Risk Assessment

Week 4.

Week 5.

Week 6.

Week 7.

Week 8. Complete short paper; prepare presentation.