

# Fixed Point Numbers Homework

You should refer to the **homework policy** for details on how this homework should be submitted.

**Attempt all questions and show all working.**

## Question 1

Using one byte to hold each number, with an imaginary binary point fixed after the fourth digit, convert the following decimal numbers to binary:

1. 3.75

8	4	2	1	1/2	1/4	1/8
0	0	1	1	1	1	0

3.75 = 0011110 in binary

2. 5.1875

4	2	1	1/2	1/4	1/8	1/16
1	0	1	0	0	1	1

5.1875 = 1010011 in binary

3. 7.562

4	2	1	1/2	1/4	1/8	1/16
1	1	1	1	0	0	0

7.562 = 0.562

$0.562 \times 2 = 1.124$

$0.124 \times 2 = 0.248$

$0.248 \times 2 = 0.496$

binary after point =100  
7.562 = 1111000 in binary

4. 7.5627

4	2	1	1/2	1/4	1/8	1/16
1	1	1	1	0	0	1

7.5627 = 0.5627  
0.5627 x 2 = 1.1254  
0.1254 x 2 = 0.2508  
0.2508 x 2 = 0.5016  
0.5016 x 2 = 1.0032  
binary after point = 1001  
7.5627 = 1111001 in binary

(8 marks)

## Question 2

Convert the following numbers to decimal, assuming 4-bits after the point:

1. 000000001011000

1024	512	256	128	64	32	16	8	4	2	1	1/2	1/4	1/8	1/16
0	0	0	0	0	0	0	0	1	0	1	1	0	0	0

$4 + 1 + 1/2 = 5.5$

2. 0000000000110010

2048	1024	512	256	128	64	32	16	8	4	2	1	1/2	1/4	1/8	1/16
0	0	0	0	0	0	0	0	0	0	1	1	0	0	1	0

$2 + 1 + 1/8 = 3.125$

(4 marks)

## Question 3

What is:

1. The largest positive number that can be held in **two bytes**

2048	1024	512	256	128	64	32	16	8	4	2	1	1/2	1/4	1/8	1/16
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1

$$2048+1024+512+256+128+64+32+16+8+4+2+1+1/2+1/4+1/8+1/16 = \mathbf{4095.9375}$$

2. The smallest positive number that can be held in **two bytes**

*The smallest number= **1/16***

In both instances assume that there are **four** bits after the point.

**(2 marks)**

## Question 4

Using one byte to hold each number, with an imaginary binary point fixed after the fourth digit

1. What is the largest number that can be stored?

8	4	2	1	1/2	1/4	1/8	1/16
1	1	1	1	1	1	1	1

$$8+4+2+1+1/2+1/4+1/8+1/16= 15.9375$$

2. What is the difference between two consecutive values?

*1/16*

3. How could the precision of storing fractional numbers be improved?

*Increase the number of bits after the binary point will increase precision.*

4. What effect would this have on the range of numbers that could be stored?

*This unfortunately causes the range of numbers to go down because less are able to be represented before the binary point.*

**(4 marks)**

**Total 18 marks**