## Assignment 4 of Algorithm

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### 1. Linear-inequality feasibility

#### **Proof**:

suppose that we have an algorithm for linear programming, that means we can solve

$$\begin{array}{ll} \max & \boldsymbol{c}^T \boldsymbol{x} \\ \text{s.t.} & \boldsymbol{A} \boldsymbol{x} \leq \boldsymbol{b} \\ & \boldsymbol{x} \geq \boldsymbol{0} \end{array}$$

given a linear inequality feasibility problem, our goal is to check whether there exist  $x^*$ ,

$$A'x^* \leq b', x^* \geq 0$$

which equals to

$$\begin{array}{ll} \max & \mathbf{0} \cdot \mathbf{x} \\ \text{s.t.} & \mathbf{A}' \mathbf{x} \leq \mathbf{b}' \\ & \mathbf{x} \geq \mathbf{0} \end{array}$$

this problem can be solved using the same algorithm.

### 2. Airplane Landing Problem

Let  $x_1, x_2, ..., x_n$  be the exact landing time of each airplane respectively, the problem can be written as

$$\begin{aligned} & \max & & \min(x_2 - x_1, x_3 - x_2, ..., x_n - x_{n-1}) \\ & \text{s.t.} & & s_1 \leq x_1 \leq t_1 \\ & & & s_2 \leq x_2 \leq t_2 \\ & & & \ddots \\ & & & s_n \leq x_n \leq t_n \end{aligned}$$

for instance, we have n=4,[10,20],[40,60],[75,80],[100,120] ( here the minute is the metric of time), using tool cvxpy we can obtain the optimal solution 35 with optimal variables  $x_1=10,45,80,116$ .

# 3. Dual Simplex Algorithm

the result is showed below.