

Temporal Graph Embedding

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ABSTRACT

KEYWORDS

Temporal Graph, Embedding

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1 INTRODUCTION

To start this paper out, let's first create a level playing field for all readers by laying out what exactly a Graph is, how it can change over time and what is meant when we talk about embedding.

1.1 Graphs

A graph is a mathematical construct which is used in a variety of tasks. It is often used to model relationships between entities, thus making it possible to operate on such structures to, for example, analyze them.

Mathematically it is consisting of two sets $G = (V, E)$, where

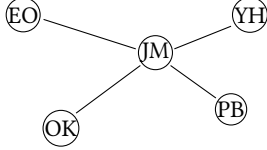


Figure 1: Part of the follower-relationship-graph of personal Instagram account.

V consists of all the vertices of the Graph, and E of all the edges, represented through a tuple of two vertices. Our graph above would thus look like following:

$$G_i = (\{E, O, Y, P, J\}, \{(J, E), (J, O), (J, P), (J, Y)\}).$$

1.2 Temporal Graphs

A temporal graph, on the other hand, is a graph that changes its structure over time. This happens when either one of our sets (V, E) changes. Our graph G is then represented through $G = \{g_1, g_2, \dots, g_t\}$ where g_i is the static graph after time $i * \Delta t$. [1]

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1.3 Embedding

Embedding is a process in which the graph $G = (V_g, E_g)$ is transformed into a set of vectors V . These capture the graph topology, vertex-to-vertex relationship as well as other relevant information. This way, it is more accessible for analyzing the graph and comparing it to others. Overall we can divide graph embedding techniques into two categories; vertex embedding and graph embedding.

When using vertex embedding, there has to be one vector v for each node in G , so that $|V| = |V_g|$. This is used to make prediction on a node level.

When using graph embedding, there is one vector representing the whole graph. Most useful is this method to analyze the data on a graph level e.g. comparing two graph structures with each other. In order to achieve this transformation there are several methods available.

1.3.1 Word2Vec. The first method is word2vec which is the foundation for many other methods. It takes a text $T = (w_1, w_2, \dots, w_n)$ as input and returns a set of vectors V , where v_i is a distribution describing how likely it is for each word to be a direct neighbor to it. The neighbors of a word w_c are defined as $\{w_i | i \in (c - \epsilon, c + \epsilon)\}$ where ϵ describes a predefined window size. With this, the whole text is represented solely through vectors, where similar words have similar vectors. One way to achieve this is to train a neural network to create the distributions. This neural network consists of one input-, one hidden- and one output layer. Each word in our text is assigned an ID through a one-hot coded vector, so that each word w_i can be represented like $(0_1, 0_2, \dots, 0_{i-1}, 1_i, 0_{i+1}, \dots, 0_n)$. It then computes how likely it is for each word to be its neighbor and transforms it into a distribution using a softmax-function[2].

Philosophers	have	debated	Hume's	problem
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Figure 2: Light-gray word, with dark-gray neighbor and $\epsilon = 1$

1.3.2 DeepWalk. This method is a continuation of the word2vec approach. Overall, the method consists of three steps. First the sampling, which is done using random walks on our graph starting

on a selected node. Hereby, a random walk describes a random succession of nodes of defined length. It is sufficient to perform 32 to 64 random Walks per node. Those random walks are now of the same form as sentences used in the word2vec method, meaning we can train a similar neural network for predicting the neighborhood of our nodes.

1.3.3 Node2Vec. Here we modify our DeepWalk method. For that purpose we introduce 2 variables P and Q , where Q defines how likely it is to go to an unvisited node, while P describes how probable it is to revisit a node.

1.3.4 Structural Deep Network Embedding. In contrast to the methods used before, SDNE does not use random walks. It aims to preserve local pairwise similarity which characterizes the local structure, and as well as the global network structure. To achieve this, we use two autoencoder neural network. These get an adjacency vector as input and want to construct node adjacency as output. We then compute the distance between the two outputs and add it to the loss function of the network. The total loss function is then computed through summation of the distance loss plus the losses of the two encoders. At the end we remain with a collection of adjacency vectors which describe the graph structure.

1.3.5 Graph2Vec. Now we don't want to represent the nodes as vectors, but the whole graph. For that we have once again three steps. In the first step we create sub-graphs for each node and encode then once again in a one-hot code. We then use these sub-graphs to train the network used in word2vec to maximize the probability that a predicted sup-graph exists in the input graph. The embedding is then the result of the network. [3]

2 METHODS

2.1 tbGraphEmbed

Starting paper

2.2 sub2vec

Is used as comparison in starting paper -> Look into

2.3 Comparison

How do Methods differ -> nodelevel / Graphlevel?

2.4 Application

Why do we use Embedding

2.4.1 Similarity. Differences Between graphs (exp - googletrends)

2.4.2 Anomaly. Where does it differ

3 CONCLUSION

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