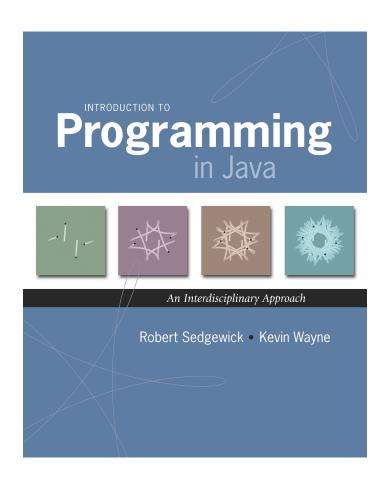
# 4.3 Stacks and Queues



# Data Types and Data Structures

## Data types. Set of values and operations on those values.

- Some are built into the Java language: int, double[], String, ...
- Most are not: Complex, Picture, Stack, Queue, ST, Graph, ...

this lecture

next lecture

#### Data structures.

- Represent data or relationships among data.
- Some are built into Java language: arrays.
- Most are not: linked list, circular list, tree, sparse array, graph, ...

this lecture TSP assignment next lecture

#### Collections

#### Fundamental data types.

- Set of operations (add, remove, test if empty) on generic data.
- Intent is clear when we insert.
- Which item do we remove?

#### Stack. [LIFO = last in first out] ← this lecture

- Remove the item most recently added.
- Ex: cafeteria trays, Web surfing.

# Queue. [FIFO = first in, first out] this lecture

- Remove the item least recently added.
- Ex: Hoagie Haven line.

## Symbol table.

- next lecture
- Remove the item with a given key.
- Ex: Phone book.

# Stacks



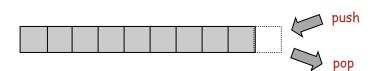
### Stack API

#### public class \*StackOfStrings

\*StackOfStrings() create an empty stack
boolean isEmpty() is the stack empty?

void push(String item) push a string onto the stack

String pop() pop the stack



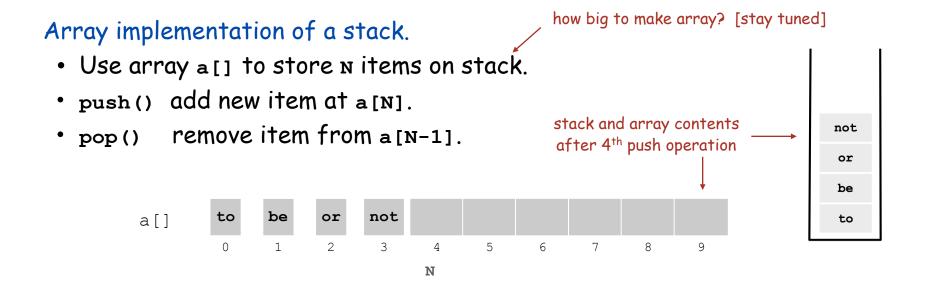
# Stack Client Example 1: Reverse

```
public class Reverse {
   public static void main(String[] args) {
      StackOfStrings stack = new StackOfStrings();
      while (!StdIn.isEmpty()) {
          String s = StdIn.readString();
          stack.push(s);
      while (!stack.isEmpty()) {
          String s = stack.pop();
         StdOut.println(s);
                                % more tiny.txt
                                it was the best of times
                                % java Reverse < tiny.txt</pre>
                                times of best the was it
 times
  of
 best
  the
              stack contents when standard input is empty
  was
  it
```

# Stack Client Example 2: Test Client

```
public static void main(String[] args) {
      StackOfStrings stack = new StackOfStrings();
     while (!StdIn.isEmpty()) {
         String s = StdIn.readString();
         if (s.equals("-"))
            StdOut.println(stack.pop());
         else
            stack.push(s);
                     % more test.txt
                     to be or not to - be - - that - - - is
                      % java StackOfStrings < test.txt</pre>
                     to be not that or be
to
not
or
be
             stack contents just before first pop operation
to
```

# Stack: Array Implementation



# Array Stack: Test Client Trace

	C+dTn	StdOut	N	a[]				
	Sturii			0	1	2	3	4
			0					
push	to		1	to				
	be		2	to	be			
	or		3	to	be	or		
	not		4	to	be	or	not	
	to		5	to	be	or	not	to
pop	_	to	4	to	be	or	not	to
	be		5	to	be	or	not	be
	-	be	4	to	be	or	not	be
	-	not	3	to	be	or	not	be
	that		4	to	be	or	that	be
	-	that	3	to	be	or	that	be
	-	or	2	to	be	or	that	be
	-	be	1	to	be	or	that	be
	is		2	to	is	or	not	to

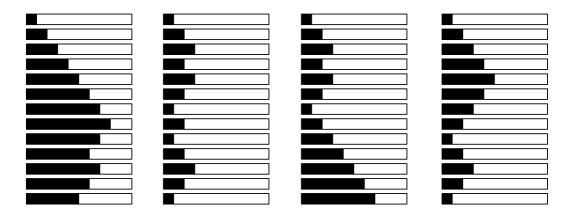
# Array Stack: Performance

Running time. Push and pop take constant time.

Memory. Proportional to client-supplied capacity, not number of items.

#### Problem.

- Original API does not take capacity as argument (bad to change API).
- Client might not know what capacity to use.
- Client might use multiple stacks.



Challenge. Stack where capacity is not known ahead of time.

# Linked Lists

# Sequential vs. Linked Allocation

#### Sequential allocation. Put items one after another.

- TOY: consecutive memory cells.
- Java: array of objects.

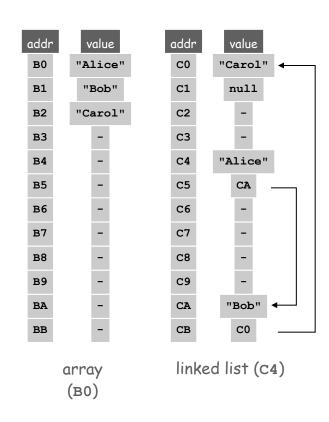
### Linked allocation. Include in each object a link to the next one.

- TOY: link is memory address of next item.
- Java: link is reference to next item.

# Key distinctions. get ith item

- · Array: random access, fixed size.
- Linked list: sequential access, variable size.

get next item



#### Linked Lists

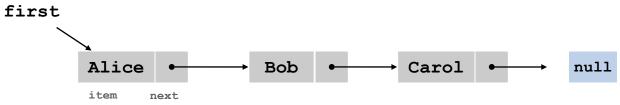
#### Linked list.

- A recursive data structure.
- An item plus a pointer to another linked list (or empty list).
- Unwind recursion: linked list is a sequence of items.

# Node data type.

- A reference to a string.
- A reference to another Node.

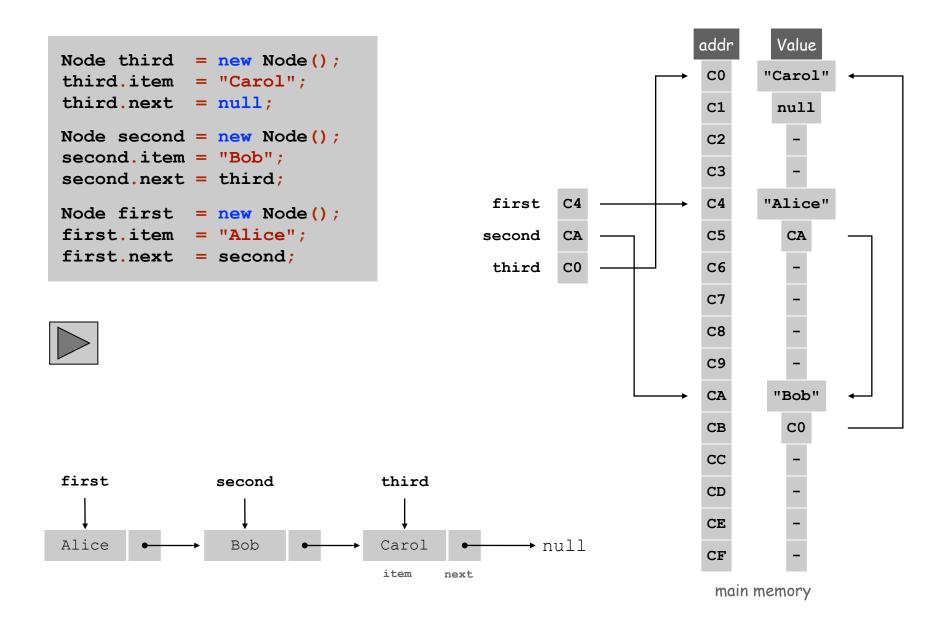
```
private class Node {
   private String item;
   private Node next;
}
```



special pointer value null terminates list

why private?

# Building a Linked List



### Linked List Demo

```
Node third = new Node();
third.item = "Carol";
third.next = null;

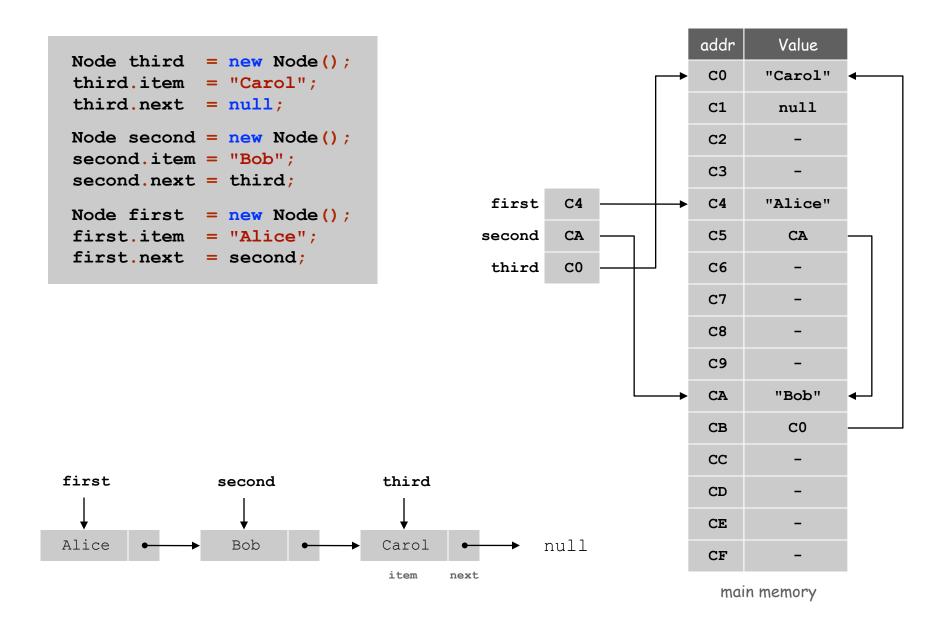
Node second = new Node();
second.item = "Bob";
second.next = third;

Node first = new Node();
first.item = "Alice";
first.next = second;
```

addr	Value
C0	-
C1	-
C2	-
C3	-
C4	-
C5	-
С6	-
C7	-
C8	-
С9	-
CA	-
СВ	-
CC	-
CD	-
CE	-
CF	-

main memory

#### Linked List Demo



# List Processing Challenge 1

Q. What does the following code fragment do?

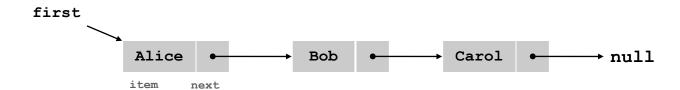
```
Node last = new Node();
last.item = StdIn.readString();
last.next = null;
Node first = last;
while (!StdIn.isEmpty()) {
   last.next = new Node();
   last = last.next;
   last.item = StdIn.readString();
   last.next = null;
}
```

# List Processing Challenge 2

Q. What does the following code fragment do?

```
for (Node x = first; x != null; x = x.next) {
   StdOut.println(x.item);
}
```



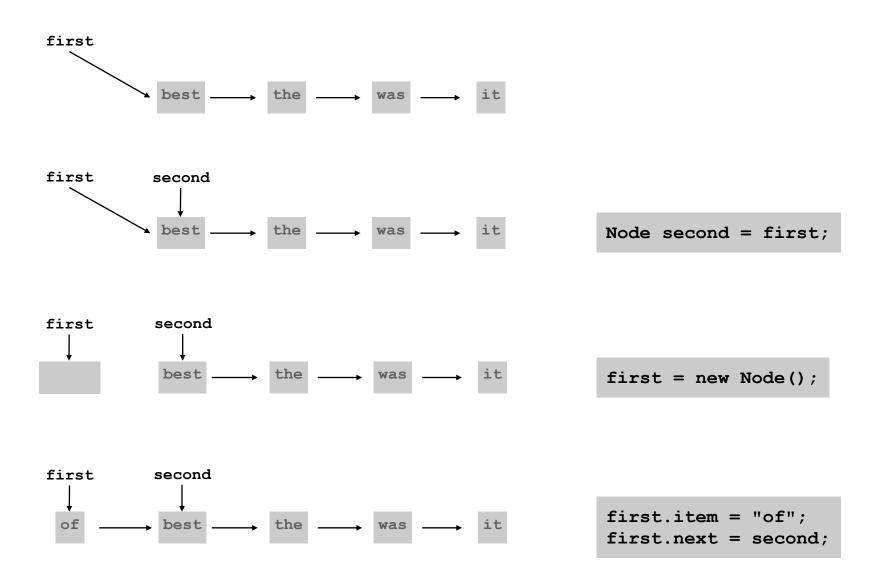


# Enough with the Idioms

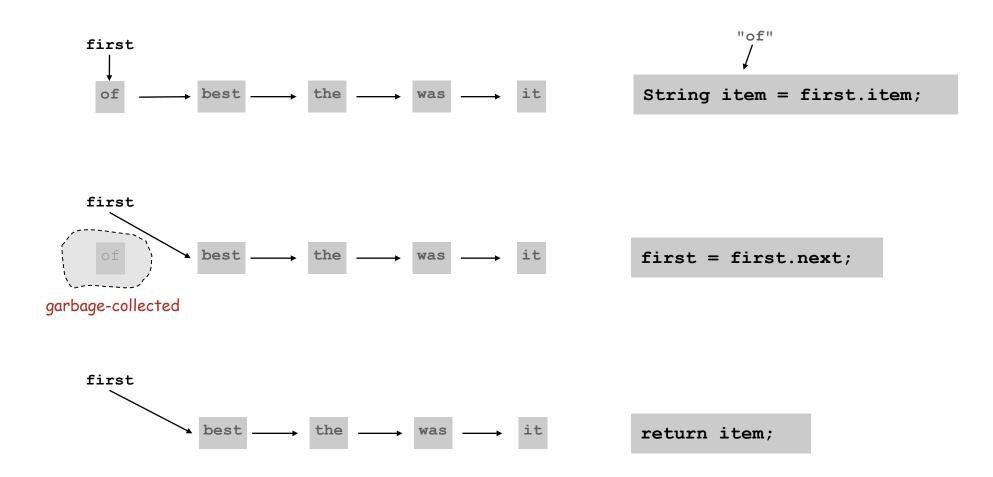
### How about this idea:

• Use a linked list to implement a stack

# Stack Push: Linked List Implementation



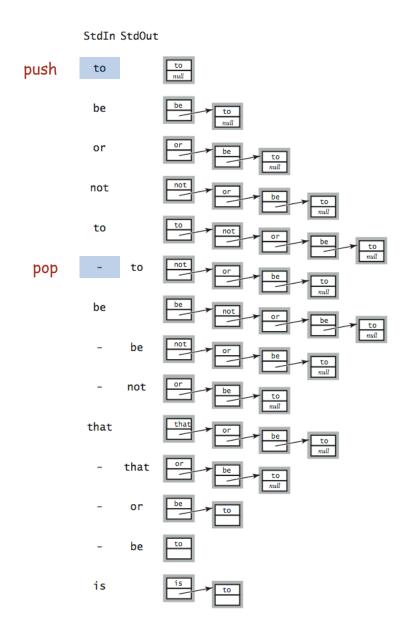
# Stack Pop: Linked List Implementation



# Stack: Linked List Implementation

```
public class LinkedStackOfStrings {
   private Node first = null;
   private class Node {
      private String item;
                                                special reserved name
      private Node next;
                   "inner class"
   public boolean isEmpty() { return first == null; }
   public void push(String item) {
      Node second = first;
       first = new Node();
                                                                      not
       first.item = item;
                                                                       or
       first.next = second;
                                            stack and linked list contents
                                                                      be
                                             after 4th push operation
   public String pop() {
       String item = first.item;
                                              first
       first = first.next;
       return item;
```

# Linked List Stack: Test Client Trace



#### Stack Data Structures: Tradeoffs

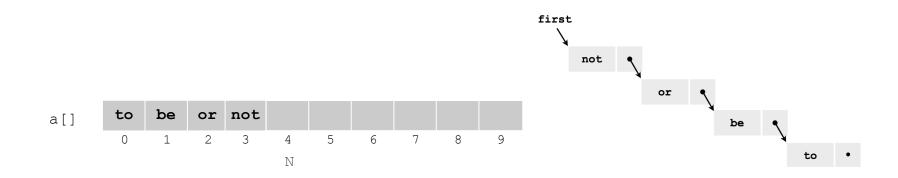
Two data structures to implement stack data type.

#### Array.

- Every push/pop operation take constant time.
- But... must fix maximum capacity of stack ahead of time.

#### Linked list.

- Every push/pop operation takes constant time.
- Memory is proportional to number of items on stack.
- But... uses extra space and time to deal with references.



# Parameterized Data Types

# Stack: Linked List Implementation

```
public class LinkedStackOfStrings {
   private Node first = null;
   private class Node {
      private String item;
     private Node next;
                 "inner class"
   public boolean isEmpty() { return first == null; }
   public void push(String item) {
      Node second = first;
      first = new Node();
      first.item = item;
      first.next = second;
   public String pop() {
      String item = first.item;
      first = first.next;
      return item;
```

# Parameterized Data Types

We just implemented: StackOfStrings.

We also want: StackOfInts, StackOfURLs, StackOfVans, ...

Strawman. Implement a separate stack class for each type.

- Rewriting code is tedious and error-prone.
- Maintaining cut-and-pasted code is tedious and error-prone.



#### Generics

Generics. Parameterize stack by a single type.

```
"stack of apples"

Stack Apple > stack = new Stack Apple > ();
Apple a = new Apple ();
Orange b = new Orange ();
stack.push (a);
stack.push (b); // compile-time error
a = stack.pop();

sample client

can't push an orange onto
a stack of apples
```

# Generic Stack: Linked List Implementation

```
public class Stack<Item> {
   private Node first = null;
                                parameterized type name
   private class Node {
                                (chosen by programmer)
      private Item item;
      private Node next;
   public boolean isEmpty() { return first == null; }
   public void push(Item item) {
      Node second = first;
      first = new Node();
      first.item = item;
      first.next = second;
   public Item pop() {
      Item item = first.item;
      first = first.next;
      return item;
```

## Autoboxing

Generic stack implementation. Only permits reference types.

#### Wrapper type.

- Each primitive type has a wrapper reference type.
- Ex: Integer is wrapper type for int.

Autoboxing. Automatic cast from primitive type to wrapper type.

Autounboxing. Automatic cast from wrapper type to primitive type.

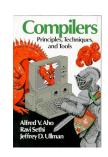
# Stack Applications

## Real world applications.

- Parsing in a compiler.
- Java virtual machine.
- Undo in a word processor.
- Back button in a Web browser.
- PostScript language for printers.
- Implementing function calls in a compiler.







#### Function Calls

#### How a compiler implements functions.

- Function call: push local environment and return address.
- Return: pop return address and local environment.

Recursive function. Function that calls itself.

Note. Can always use an explicit stack to remove recursion.

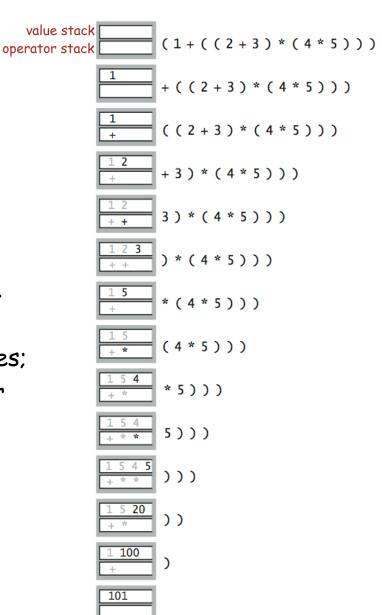
# Arithmetic Expression Evaluation

Goal. Evaluate infix expressions.

## Two stack algorithm. [E. W. Dijkstra]

- Value: push onto the value stack.
- Operator: push onto the operator stack.
- Left parens: ignore.
- Right parens: pop operator and two values; push the result of applying that operator to those values onto the value stack.

Context. An interpreter!



# Arithmetic Expression Evaluation

```
public class Evaluate {
  public static void main(String[] args) {
     Stack<String> ops = new Stack<String>();
     Stack<Double> vals = new Stack<Double>();
     while (!StdIn.isEmpty()) {
        String s = StdIn.readString();
        if
               (s.equals("("))
        else if (s.equals("*"))
                               ops.push(s);
        else if (s.equals(")")) {
           String op = ops.pop();
           if (op.equals("+")) vals.push(vals.pop() + vals.pop());
           else if (op.equals("*")) vals.push(vals.pop() * vals.pop());
        else vals.push(Double.parseDouble(s));
     StdOut.println(vals.pop());
```

```
% java Evaluate
(1+((2+3)*(4*5)))
101.0
```

#### Correctness

Why correct? When algorithm encounters an operator surrounded by two values within parentheses, it leaves the result on the value stack.

```
(1+((2+3)*(4*5)))
```

So it's as if the original input were:

```
(1+(5 * (4 * 5 ) ))
```

Repeating the argument:

```
(1 + (5 * 20 ))
(1 + 100 )
101
```

Extensions. More ops, precedence order, associativity, whitespace.

```
1 + (2 - 3 - 4) * 5 * sqrt(6*6 + 7*7)
```

# Stack-Based Programming Languages

Observation 1. Remarkably, the 2-stack algorithm computes the same value if the operator occurs after the two values.

Observation 2. All of the parentheses are redundant!

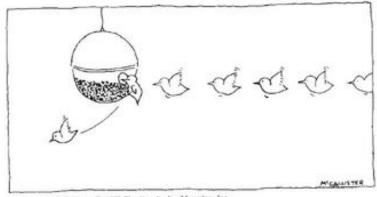
Bottom line. Postfix or "reverse Polish" notation.



Jan Lukasiewicz

Applications. Postscript, Forth, calculators, Java virtual machine, ...

# Queues



Drawing by McCallister, © 1977 The New Yorker Magazine, Inc.



# Queue API

#### public class Queue<Item>

```
Queue<Item>()

boolean isEmpty()

void enqueue(Item item)

Item dequeue()

int length()

create an empty queue

is the queue empty?

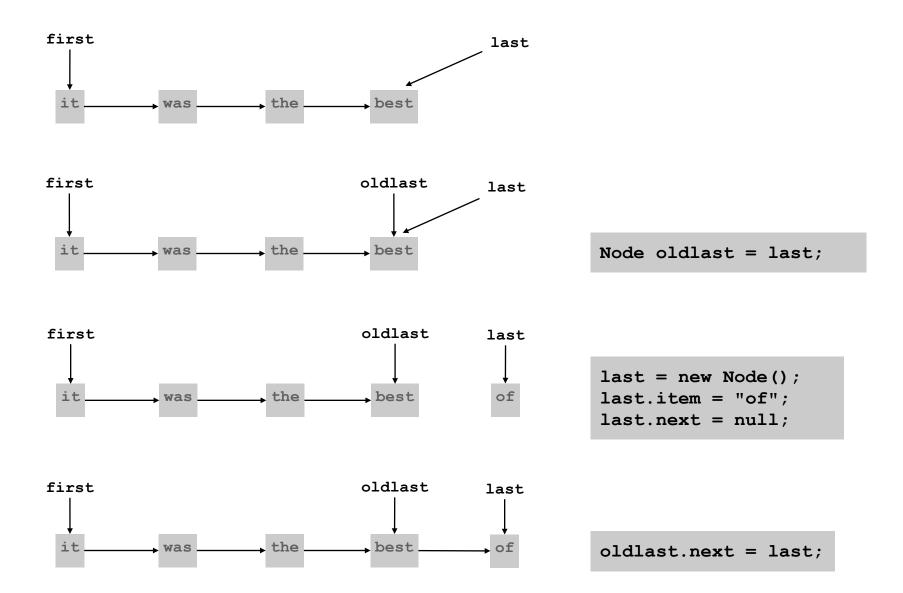
enqueue an item

dequeue an item

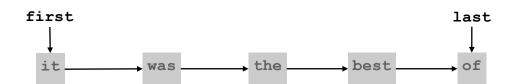
queue length
```

```
public static void main(String[] args) {
   Queue<String> q = new Queue<String>();
   q.enqueue("Vertigo");
   q.enqueue("Just Lose It");
   q.enqueue("Pieces of Me");
   q.enqueue("Pieces of Me");
   while(!q.isEmpty())
        StdOut.println(q.dequeue());
}
```

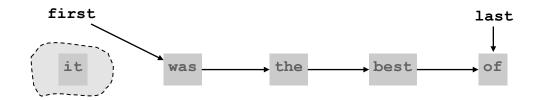
# Enqueue: Linked List Implementation



# Dequeue: Linked List Implementation

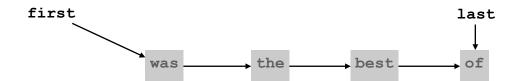


String item = first.item;



first = first.next;





return item;

## Queue: Linked List Implementation

```
public class Queue<Item> {
  private Node first, last;
  private class Node { Item item; Node next; }
   public boolean isEmpty() { return first == null; }
  public void enqueue(Item item) {
     Node oldlast = last;
      last = new Node();
      last.item = item;
     last.next = null;
     if (isEmpty()) first = last;
            oldlast.next = last;
     else
  public Item dequeue() {
      Item item = first.item;
      first = first.next;
      if (isEmpty()) last = null;
     return item;
```

# Queue Applications

## Some applications.

- iTunes playlist.
- Data buffers (iPod, TiVo).
- Asynchronous data transfer (file IO, pipes, sockets).
- Dispensing requests on a shared resource (printer, processor).

#### Simulations of the real world.

- · Guitar string.
- Traffic analysis.
- Waiting times of customers at call center.
- Determining number of cashiers to have at a supermarket.

# Singly-Linked Data Structures

# From the point of view of a particular object:

all of these structures look the same. sequential (this lecture) circular (TSP assignment) rho parent-link tree general case

Multiply-linked data structures. Many more possibilities.

### Conclusions

Sequential allocation: supports indexing, fixed size. Linked allocation: variable size, supports sequential access.

Linked structures are a central programming tool.

- Linked lists.
- Binary trees.
- Graphs.
- Sparse matrices.