

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	2
3	1
4	2
5	2
6	4
7	2
8	2
9	1
10	1
11	1
12	1
13	1
14	2
15	1
16	1

#### Rs 16 - Soln 1

$$\text{rank}(\text{kron}(\text{eye}(4), 6) - \text{kron}(6', \text{eye}(4))) = 10$$

$$\text{rank}([\text{kron}(\text{eye}(4), 6) - \text{kron}(6', \text{eye}(4)); \text{kron}(\text{eye}(4), 2) - \text{kron}(4', \text{eye}(4))]) = 16$$

$$\text{rank}([\text{kron}(\text{eye}(4), 6) - \text{kron}(6', \text{eye}(4)); \text{kron}(\text{eye}(4), 2) - \text{kron}(5', \text{eye}(4))]) = 15$$

$$\text{rank}([\text{kron}(\text{eye}(4), 6) - \text{kron}(6', \text{eye}(4)); \text{kron}(\text{eye}(4), 2) - \text{kron}(7', \text{eye}(4))]) = 14$$

$$\text{rank}([\text{kron}(\text{eye}(4), 6) - \text{kron}(6', \text{eye}(4)); \text{kron}(\text{eye}(4), 2) - \text{kron}(8', \text{eye}(4))]) = 16$$

$$\text{rank}([\text{kron}(\text{eye}(4), 6) - \text{kron}(6', \text{eye}(4)); \text{kron}(\text{eye}(4), 2) - \text{kron}(14', \text{eye}(4))]) = 16$$

$$\text{rank}([\text{kron}(\text{eye}(4), 6) - \text{kron}(6', \text{eye}(4)); \text{kron}(\text{eye}(4), 4) - \text{kron}(14', \text{eye}(4))]) = 15$$

$$2 \Leftrightarrow 5 \Leftrightarrow 7$$

$$4 \Leftrightarrow 14$$

8 by itself (multiple of the identity)

$$[U, S, V] = \text{svd}([\text{kron}(\text{eye}(4), 6) - \text{kron}(6', \text{eye}(4)); \text{kron}(\text{eye}(4), \text{reshape}(\text{Rs16Rc1111}(:, 8), 4, 4)) - \text{kron}(\text{reshape}(\text{Rs16Rc1111}(:, 8), 4, 4)', \text{eye}(4))]); V(:, \text{end})$$

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	1
3	2
4	2
5	2
6	4
7	2
8	1
9	1
10	1
11	1
12	2
13	1
14	2
15	1
16	1

#### **Rs 16 - Soln 2**

$3 \Leftrightarrow 4 \Leftrightarrow 5 \Leftrightarrow 14$

7 and 12 by themselves

12 is not the identity times a constant!

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	2
3	2
4	1
5	2
6	1
7	1
8	1
9	1
10	1
11	1
12	2
13	2
14	4
15	2
16	1

#### **Rs 16 - Soln 3**

$2 \Leftrightarrow 3 \Leftrightarrow 5 \Leftrightarrow 12 \Leftrightarrow 13 \Leftrightarrow 15$

All related!?

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	2
3	2
4	1
5	2
6	1
7	1
8	1
9	2
10	1
11	2
12	2
13	1
14	4
15	1
16	1

**Rs 16 - Soln 4**

2 11 12

3 9

5 is by itself, not a multiple of the identity!

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	1
3	2
4	1
5	2
6	1
7	2
8	2
9	2
10	1
11	1
12	1
13	1
14	2
15	1
16	4

**Rs 16 - Soln 5**

$$3 \Leftrightarrow 5 \Leftrightarrow 7 \Leftrightarrow 14$$

$$8 \ 9$$

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	1
4	1
5	2
6	1
7	2
8	1
9	1
10	2
11	2
12	1
13	4
14	1
15	1
16	2

#### **Rs 16 - Soln 6**

1 7 10 16

5 by itself (multiple of the identity)

11 by itself (multiple of the identity)

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	1
4	2
5	2
6	1
7	4
8	1
9	1
10	2
11	2
12	1
13	2
14	1
15	1
16	1

#### **Rs 16 - Soln 7**

1 10 11 13

5 is by itself (not a multiple of the identity)

4 is by itself (multiple of the identity)

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	2
4	4
5	1
6	2
7	2
8	1
9	1
10	2
11	1
12	2
13	1
14	1
15	1
16	1

**Rs 16 - Soln 8** 1 3 7 12  
6 10



Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	2
3	1
4	1
5	4
6	2
7	1
8	2
9	1
10	2
11	1
12	2
13	1
14	1
15	2
16	1

**Rs 16 - Soln 9**

2 8 10 12

6 is by itself (multiple of the identity)

15 is by itself (multiple of the identity)

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	1
4	1
5	2
6	1
7	1
8	1
9	1
10	2
11	2
12	1
13	2
14	4
15	1
16	2

**Rs 16 - Soln 10**  
1 13 16 5 10 11 All related

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	1
4	4
5	2
6	1
7	1
8	1
9	2
10	1
11	2
12	1
13	2
14	1
15	2
16	1

# Rs 16 - Soln 11

1 5 9 11 13 15 All related (all odds)

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	4
3	2
4	1
5	1
6	1
7	1
8	1
9	2
10	1
11	1
12	2
13	2
14	2
15	1
16	2

**Rs 16 - Soln 12**

3 13 14

9 16

12 is by itself (multiple of the identity)

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	1
3	1
4	4
5	2
6	1
7	1
8	1
9	2
10	2
11	2
12	2
13	1
14	2
15	1
16	1

#### **Rs 16 - Soln 13**

5 is by itself (not a multiple of the)

9 10 11 12 14

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	1
4	1
5	2
6	2
7	2
8	4
9	1
10	1
11	1
12	2
13	2
14	1
15	1
16	1

**Rs 16 - Soln 14**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	2
4	2
5	1
6	1
7	1
8	1
9	1
10	2
11	4
12	1
13	1
14	2
15	2
16	1

**Rs 16 - Soln 15**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	1
4	2
5	1
6	1
7	1
8	1
9	1
10	2
11	2
12	1
13	1
14	2
15	2
16	4

**Rs 16 - Soln 16**



Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	2
3	1
4	2
5	1
6	1
7	2
8	1
9	2
10	1
11	2
12	2
13	1
14	4
15	1
16	1

**Rs 16 - Soln 17**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	1
3	1
4	1
5	2
6	1
7	2
8	1
9	1
10	1
11	2
12	2
13	2
14	4
15	2
16	1

**Rs 16 - Soln 18**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	4
4	2
5	2
6	1
7	2
8	1
9	1
10	1
11	2
12	1
13	2
14	1
15	1
16	1

**Rs 16 - Soln 19**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	2
4	1
5	1
6	1
7	1
8	1
9	1
10	2
11	2
12	2
13	4
14	2
15	1
16	1

**Rs 16 - Soln 20**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	4
3	2
4	2
5	1
6	2
7	1
8	2
9	2
10	1
11	1
12	1
13	1
14	1
15	1
16	1

**Rs 16 - Soln 21**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	1
3	1
4	2
5	1
6	1
7	2
8	1
9	4
10	1
11	1
12	2
13	2
14	2
15	2
16	1

**Rs 16 - Soln 22**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	2
3	2
4	1
5	4
6	2
7	1
8	1
9	1
10	1
11	2
12	2
13	2
14	1
15	1
16	1

**Rs 16 - Soln 23**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	4
3	1
4	2
5	1
6	2
7	1
8	2
9	1
10	2
11	1
12	2
13	1
14	1
15	1
16	1

**Rs 16 - Soln 24**



Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	1
4	2
5	1
6	1
7	1
8	2
9	1
10	1
11	4
12	1
13	2
14	1
15	2
16	2

**Rs 16 - Soln 25**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	4
3	2
4	1
5	1
6	1
7	2
8	2
9	1
10	1
11	1
12	1
13	2
14	1
15	1
16	2

**Rs 16 - Soln 26**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	2
3	4
4	1
5	1
6	1
7	2
8	2
9	1
10	1
11	2
12	1
13	2
14	1
15	2
16	1

**Rs 16 - Soln 27**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	2
3	2
4	1
5	1
6	1
7	2
8	1
9	1
10	1
11	2
12	2
13	2
14	1
15	1
16	4

**Rs 16 - Soln 28**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	2
4	2
5	2
6	2
7	1
8	1
9	1
10	1
11	1
12	1
13	1
14	1
15	4
16	2

**Rs 16 - Soln 29**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	4
4	1
5	1
6	2
7	2
8	2
9	1
10	1
11	1
12	1
13	1
14	2
15	2
16	1

**Rs 16 - Soln 30**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	2
2	1
3	1
4	2
5	2
6	1
7	2
8	1
9	1
10	2
11	1
12	1
13	4
14	1
15	2
16	1

**Rs 16 - Soln 31**

Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	1
2	4
3	1
4	1
5	1
6	2
7	1
8	1
9	2
10	2
11	2
12	2
13	1
14	1
15	2
16	1

**Rs 16 - Soln 32**



Type	Char. Poly.	Count
name-1		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11
name-2		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11
name-3		
symmetric	$t^3(t-1)$	9
	$(t-1)^2(t+t^2+1)$	1
	$t^2(t+t^2+1)$	6
triples	$\{t^4, t^4, t^4\}$	11

Col Number	Rank
1	4
2	2
3	2
4	2
5	2
6	1
7	1
8	1
9	2
10	1
11	1
12	1
13	2
14	1
15	1
16	1

# Rs 16 - Soln 1

2, 3, 4, 5, 9, 13