BLAStoff Report

Katon Luaces, Michael Jan, Jake Fisher, Jason Kao {knl2119, mj2886, jf3148, jk4248}@columbia.edu

Contents

1	Intr	oducti	on	2							
2	Tutorial 2										
	2.1	Langua	age Details	2							
		2.1.1	Data Types	2							
			2.1.1.1 Matrix Literal Definition	2							
			2.1.1.2 Graph	3							
			2.1.1.3 Number Definition	3							
			2.1.1.4 Generator Function Definition	4							
			2.1.1.5 Integers vs. Floats	5							
		2.1.2	Comments	5							
		2.1.3	Functions	6							
		2.1.4	If statements	6							
		2.1.5	For/While Loops	6							
		2.1.6	Operations	7							
			2.1.6.1 Selection []	8							
			2.1.6.2 Semiring redefinition <>	10							
			2.1.6.3 Extensions	12							
		2.1.7	Keywords	12							
		2.1.8	Memory	12							
		2.1.9	Scope	13							
			Libraries/Importing Functions	13							
		2.1.11	,	13							
	2.2		e Code	13							
		2.2.1	Some Standard Library Functions	13							
			2.2.1.1 One	13							
			2.2.1.2 Horizontal Concatenation	14							
			2.2.1.3 Plus/Times Column Reduce	14							
			2.2.1.4 Sum'	14							
			2.2.1.5 Range From Vector	15							
		2.2.2	Graph Algorithms: Breadth First Search	15							
3	Pro	ject Pl	lan	17							
4	Togt	Plan		17							
4	rest	Flan		17							
5			earned	17							
	5.1			17							
	5.2	Michae	el	17							
	5.3	Jake .		17							
	5.4	Jason		17							
6	App	endix		17							

1 Introduction

Expressing an algorithm primarily through manipulation of matrices allows an implementation to take advantage of parallel computation. Graphs are one of the most important abstract data structures and graph algorithms underlie a wide range of applications. Yet many implementations of graph algorithms rely on sequential pointer manipulations that cannot easily be parallelized. As a result of the practicality and theoretical implications of more efficient expressions of these algorithms, there is a robust field within applied mathematics focused on expressing "graph algorithms in the language of linear algebra" [KG11]. BLAStoff is a linear algebraic language focused on the primitives that allow for efficient and elegant expression of graph algorithms.

2 Tutorial

2.1 Language Details

2.1.1 Data Types

There is only one data type in BLAStoff, the matrix. Matrices can be defined four ways: as a matrix literal, as a graph, as a number, or with a generator function.

2.1.1.1 Matrix Literal Definition

A matrix literal looks as follows:

```
M = [1,3,5;
2 2,4,6;
3 0,0,-1];
```

which sets M as the matrix

$$\begin{bmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \\ 0 & 0 & -1 \end{bmatrix}$$

. The values given to M can be anything $\in \mathbb{R} \cup \pm \infty$. Here's an example of using values that aren't just integers:

```
M = [1.2, inf;
-inf, -34];
```

which sets M as the matrix

$$\begin{bmatrix} 1.2 & \infty \\ -\infty & -34 \end{bmatrix}$$

.

2.1.1.2 Graph

The graph definition looks as follows:

This will set M as the adjacency matrix for the graph described, which in this case would be:

As we can see in this code example, each line in the graph definition can be an edge $a \to b$; defining a node between vertices a and b where a, b are non-negative integers, or just a vertex c; where c is also a non-negative integer, which just defines that the vertex c exists. The matrix created will be an $n \times n$ matrix, where n is the highest vertex (in our case 4) defined plus 1. Thus, the graph created will have nodes [0, n-1]. Any vertices not mentioned in the definition but in the range [0, n-1] will be created, but not have any edges to or from it (such as vertex 3 in this case). We could easily extend this syntax to allow for bi-directional or weighted graphs, and will decide later whether to do this.

2.1.1.3 Number Definition

The number definition is quite simple, and looks like as follows:

```
M = 5;
```

This is how you would create a "scalar" in BLAStoff, but because the only data type is a matrix, scalars are really 1×1 matrices. The above code is equivalent to the following code:

```
M = [5];
```

which sets M as the matrix

[5]

A potential issue could be that not allowing scalars means you can't have scalar multiplication, but we define a convolution operator, which ends up working like scalar multiplication if the right hand side is a 1×1 matrix.

2.1.1.4 Generator Function Definition

We also have a number of generator functions for commonly-used types of matrices so that you don't waste your time typing out a 50×50 identity matrix. The first is the Zero function, which generates a matrix with all 0s. This takes in one argument, which we will call x, a non-negative integer matrix of two possible sizes. n can be a 2×1 positive integer matrix, and the elements of the n matrix are the height and width of the zero matrix, in that order. n could also be a 1×1 matrix, in which case the zero matrix will be square, with the element in n as its height and width. Here is an example:

```
A = Zero(4);
B = Zero([3;2]);
```

This code would result in the following matrices:

$$B = \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

Note that A = Zero(4); is equivalent to A = Zero([4;4]);.

We also have an identity function, I, which takes in one argument, a 1×1 non-negative integer matrix, the width and height of the resultant square identity matrix. Example:

```
M = I(3);
```

This would result in the following matrix:

$$M = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

The final generator function is the range function, which generates a column vector that goes through an integer range, incremented by 1. Like Zero, it takes in an integer matrix of size 1×1 or size 2×1 , which gives the bounds of the range generated (inclusive lower, exclusive upper), or, in the 1×1 case, the exclusive upper bound, and 0 is the default lower bound. Here are some examples:

```
A = range(3);
B = range(-2,2);
```

This code would result in the following matrices:

$$A = \begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \end{bmatrix}$$

$$B = \begin{bmatrix} -2\\ -1\\ 0\\ 1\\ 2 \end{bmatrix}$$

If a range where the lower bound is greater than the upper bound given to range, such as range([5;-1]), a 0×1 matrix will be returned.

2.1.1.5 Integers vs. Floats

You're probably confused now, because I said earlier that the only type in BLAStoff is a matrix, but now I'm talking about integers and floats? So, while in a perfect world we could just have everything be floats, as we're defining our linear algebra over the reals, consider the following code if (which makes use of a few operators we will define below, but you can guess how it generally works for now):

```
b = 25020359023950923059124;
a = 2;
M = [1,2;3,4];
a += b;
a -= b;
M = M^a;
```

If this code has no floating point errors, than the final line is just a simple matrix squaring. However, if some error is introduced to \mathbf{a} , then we have a problem where we're trying to calculate something like $M^{2.000001}$, which is a much more difficult problem even if it would result in a numerically similar result. So, I was lying a little. Though you don't declare any types explicitly, each matrix is implicitly a float matrix or an integer matrix depending on if it is defined with any non-integers (you can only get float matrices with the literal definition). Any operation (such as matrix addition or matrix multiplication) between a float matrix and an integer matrix results in a float matrix, while an operation between two matrices of the same type will result in a matrix of the same type, except for something like matrix inversion.

2.1.2 Comments

Comments in BLAStoff use C style, with // for a single line and /* and */ for multi-line comments. For example:

```
A = 6; // I'm a comment!
B = 5; /* I'm a comment also but

...
I'm longer!*/
```

2.1.3 Functions

Functions in BLAStoff are defined with a mix of Python and C style:

```
def foo(A, B) {
    return A;
}
```

Because there is only one data type in BLAStoff, there is no need for argument types or return types, everything is always a matrix! Even "void" functions return matrices. Consider these two functions:

These two functions both return the equivalent of Python's "None" in BLAStoff, a 0×0 matrix.

2.1.4 If statements

For and while loops also look similar to C. For example:

```
if (A > 2) {
2     A = 7;
3 } else if (A < -3) {
4     A = 5;
5 } else {
6     A = 0;
7 }</pre>
```

2.1.5 For/While Loops

For and while loops also look similar to C. For example:

```
B = 0;
for (A = [0]; A < 5; A+=1) {
```

```
B+=1;

While (B > -1) {
B-=1;
```

We allow for loops, but they are not usually the ideal paradigm. The selection operator should hopefully replace much of the use for loops.

2.1.6 Operations

Operations are where BLAStoff gets more interesting.

We aim to implement a large subset of the basic primitives described in [Gil] (several of which can be combined) as well as a few essential semirings.

Semiring	operators		domain	0	1
	\oplus	\otimes			
Standard arithmetic	+	×	\mathbb{R}	0	1
max-plus algebras	$_{\text{max}}$	+	$\{-\infty \cup \mathbb{R}\}$	$-\infty$	0
min-max algebras	\min	max	$\infty \cup \mathbb{R}_{\geq 0}$	∞	0
Galois fields (e.g., GF2)	xor	and	$\{0,1\}$	0	1
Power set algebras	U	\cap	$\mathcal{P}(\mathbb{Z})$	Ø	U

Semirings.png

Operation name	Mathematical description			
mxm	$\mathbf{C} \odot = \mathbf{A} \oplus . \otimes \mathbf{B}$			
mxv	$\mathbf{w} \odot = \mathbf{A} \oplus . \otimes \mathbf{v}$			
vxm	$\mathbf{w}^T \odot = \mathbf{v}^T \oplus . \otimes \mathbf{A}$			
eWiseMult	$\mathbf{C} \odot = \mathbf{A} \otimes \mathbf{B}$			
	$\mathbf{w} \odot = \mathbf{u} \otimes \mathbf{v}$			
eWiseAdd	$\mathbf{C} \odot = \mathbf{A} \oplus \mathbf{B}$			
	$\mathbf{w} \odot = \mathbf{u} \oplus \mathbf{v}$			
reduce (row)	$\mathbf{w} \odot = \bigoplus_{j} \mathbf{A}(:,j)$			
apply	$\mathbf{C} \odot = F_u(\mathbf{A})$			
	$\mathbf{w} \odot = F_u(\mathbf{u})$			
transpose	$\mathbf{C} \odot = \mathbf{A}^T$			
extract	$\mathbf{C} \odot = \mathbf{A}(\mathbf{i}, \mathbf{j})$			
	$\mathbf{w} \odot = \mathbf{u}(\mathbf{i})$			
assign	$\mathbf{C}(\mathbf{i},\mathbf{j}) \odot = \mathbf{A}$			
	$\mathbf{w}(\mathbf{i}) \odot = \mathbf{u}$			

primitives.png

Here are our operations, which implement those and more:

Name	$\mathbf{U}\mathbf{sage}$
Assigmnent	M = N
Selection	M[A, B, c, d]
Matrix Multiplication	M * N
Convolution	M ~ N
Element-wise Multiplication	M @ N
Element-wise Addition	M + N
Exponentiation/Inverse/Transpose	A^b or A^T
Size	M
Vertical Concatenation	M : N
Reduce Rows	+\$M or *\$M
Semiring Redefinition	<pre><#semiringname> or <_></pre>
Logical Negation	<pre><#semiringname> or <_></pre>
Comparisons	==, !=, >, >=, <, <=
Assignment Variants	*=, .=, @=, +=, ^=, :=

Some of these operators' behaviors are intuitive, but we will explained further the two less intuitive ones:

2.1.6.1 Selection []

The BLAStoff selection operator can be applied to any matrix looks like one of the following three forms:

```
M[A, B, c, d];
M[A, B]
M[A];
```

where A,B are column vectors of non-negative integers $(n\times 1 \text{ matrices})$ and c,d are 1×1 non-negative integer matrices. c,d are optional and have a default value of [1]. B is also optional and its default value is [0]. Abstractly, the way this operator works is by taking the Cartesian product of $A,B,R=A\times B,$ and for each $(j,i)\in R$, we select all the sub-matrices in M with a top-left corner at row j, column i, height of c, and width of d. (BLAStoff is 0-indexed.) This Cartesian makes the select operator a very powerful operator that can do things like change a specific of indices, while also being general enough to allow for simple indexing. Take the following code example:

```
M = Zero(4)
M[[0;2], [0;2]] = 1;
```

This would result in the following matrix:

$$M = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

as in this case $R = \{(0,0), (0,1), (1,0), (1,1)\}$, so for every 1×1 matrix at each point in R, we set the value to 1. Note that the matrix on the right hand side must be of size $c \times d$. That was a relatively complicated use of the select operator, but simple uses still have very easy syntax:

```
M = Zero(2);
M[1, 0] = 1;
N = Zero(3);
N[1, 1, 2, 2] = I(2);
```

This would result in:

$$M = \begin{bmatrix} 0 & 0 \\ 1 & 0 \end{bmatrix}$$

$$N = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

The reason why 0 is the default value of B is to allow for easy column vector access. Example:

```
v = [1;1;1];
v[1] = 2;
u = [1;1;1];
u[[0;2]] = 2;
```

This would result in:

$$v = \begin{bmatrix} 1\\2\\1 \end{bmatrix}$$
$$u = \begin{bmatrix} 2\\1\\1 \end{bmatrix}$$

Now, perhaps it is clear why we included the range generator function. Example:

```
v = Zeroes([5;1]);
v[range(5)] = 1;
```

This would result in:

$$v = \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$$

As you'd expect, trying to access anything out-of-bounds with the selection operator will throw an error.

We have shown the selection operator so far as a way of setting elements in a matrix, but it's also a way of extracting values from a matrix, as we will show below:

```
A = [1,2,3;

4,5,6;

7,8,9];

B = A[0, 0, 2, 2];
```

This would result in:

$$B = \begin{bmatrix} 1 & 2 \\ 4 & 5 \end{bmatrix}$$

Extraction is quite understandable when A and B are 1×1 , as that results in only one matrix, but it is a bit more complicated when they are column vectors. In that case, we concatenate the number of resultant matrices, both vertically and horizontally. I think an example makes this clearer:

```
A = [1,2,3;

4,5,6;

7,8,9];

B = A[[0;2], [0;2], 1, 1];

v = [1;2;3;4];

u = v[[0;2;3]];
```

This would result in:

$$B = \begin{bmatrix} 1 & 3 \\ 7 & 9 \end{bmatrix}$$
$$u = \begin{bmatrix} 1 \\ 3 \\ 4 \end{bmatrix}$$

2.1.6.2 Semiring redefinition <>

You may have noticed that though we have defined a number of operations on matrices, we want a way to control which operations are used on the elements of these matrices beyond standard arithmetic + and \times . We want to be able to use a number of semiring operators, such as those defined in the image above. BLAStoff allows for semiring redefinition in one of the following forms:

So what does this syntax actually do? Ignore the underscore case for now. The other three are commands to switch the command to the one denoted in the brackets. Let's see an example:

```
a = 2.1;
   b = 3;
   c = 0;
   <#arithmetic>;
   a + b; //returns 5.1
   a * b; //returns 6.3
   a * c; //returns 0
   <#logical>;
10
   a + b; //returns 1: plus is now logical or; 0 is the only false value
       and 1 is the default true value
   a * b; //returns 1 as well: times is now logical and
   a * c; //returns 0
14
15
   <#maxmin>;
   b + c; //returns 2.1; plus is now minimum
   a * b; //returns 3; times is now maximum
   a * c; //returns 5.1
```

#arithmetic is the default, so that line was technically redundant, but included for clarity. The example we gave was with 1×1 matrices, but the semiring definitions work on matrices of any size:

```
A = [1,4;

2 6,3];

3 B = [5,2;

4 7,1];

5 C = A+B;
```

This would result in:

$$C = \begin{bmatrix} 1 & 2 \\ 6 & 1 \end{bmatrix}$$

Semiring redefinition generally is reset back to the default arithmetic when you call a function:

```
def add(x, y) {
    return x + y;
}

a = 4;
b = 3;

*#logical>;

a + b; // will return 1
add(a, b); // will return 7
```

But we provide the <_> in order to solve this: calling that command will set the semiring to whatever it was as this function was called (or to arithmetic as a default if you're not in a function):

2.1.6.3 Extensions

We can possibly add support for max-plus or Galois, but that will be a stretch goal. Another, possibly loftier stretch goal, is to allow custom semirings:

```
4, f1, i1>
2 <*, f2, i2>
```

where f_1, f_2 is the name a function defined elsewhere that has exactly 2 arguments, and i_1, i_2 are number literals. This would use $f_1(a, b)$ for a + b and $f_2(a, b)$ for $a \times b$. i_1, i_2 are the new empty sum and product. We will determine if this is easy/feasible/useful/reasonable.

2.1.7 Keywords

BLAStoff reserves the following keywords:

```
I, Zero, range, def, return, if, else, for, while, T
```

2.1.8 Memory

BLAStoff will use pass-by-reference and copy-by-value. Here's an example of how this will works:

```
def f(x){
     x += 1;
}

4     a = 1;

5     f(a);
6     a == 1; //TRUE
7     a == 2; //TRUE
8
```

```
9 b = 1;

10 c = b;

11 c += 1;

12 c == 2; //TRUE

13 b == 2; //FALSE

14 b == 1; //TRUE
```

BLAStoff will be garbage-collected.

2.1.9 Scope

BLAStoff has scope shared between blocks in the same function call, but not in different function calls. Example:

```
1
2  a = 1;
3  {
4     b = 2 + a; // valid
5  }
6  c = b + 1; // valid
7
8  def f(x){
9     return x * (b + c); // compile-time error
10 }
```

2.1.10 Libraries/Importing Functions

There will be a way to make/use a library and import functions, but we have not settled on the syntax nor semantics.

2.1.11 I/O

There will be a way to use input and output, but we also have not settled on the syntax nor semantics.

2.2 Sample Code

2.2.1 Some Standard Library Functions

As we have discussed, we intend to provide a standard library that should have include a good number of the other Linear Algebra operations that aren't primitives. Here are some examples:

2.2.1.1 One

One works exactly like Zero, but has all 1s in the matrix:

```
def One(size){
    A = Zero(size);
    m = size[0];
    A[range(size[0]), range(size[1])] = 1;
    return A;
}
```

2.2.1.2 Horizontal Concatenation

We don't include this as an operator because it is quite easy to write as a function using vertical concatenation and transpose:

```
def horizontalConcat(A, B){
    return (A^T:B^T)^T;
}
```

2.2.1.3 Plus/Times Column Reduce

Column reduction follows similarly:

2.2.1.4 Sum

sum gives you the sum of all the elements in the matrix. There are two simple O(N) implementations (where N is the total number of elements in the matrix), and I'll provide both options as an example:

2.2.1.5 Range From Vector

rangeFromVector takes in a column vector and returns a vector of the indices that have non-zero. For instance:

rangeFromVector(
$$\begin{bmatrix} 0\\1\\1\\0\\1 \end{bmatrix}) = \begin{bmatrix} 1\\2\\4 \end{bmatrix}$$

This will come in handy in the BFS algorithm that we will write:

```
def rangeFromVector(v){
       <#logical>;
       vlogic = v~1;
       <#arithmetic>;
       n = plusColumnReduce(v); // the number of non-zero values
       u = Zero(n, 1);
       j = 0;
       for (i = 0; i < |v|[0]; i += 1) {
           if (v[i]) {
              u[j] = i;
10
              j++;
           }
12
       }
   }
14
```

2.2.2 Graph Algorithms: Breadth First Search

Here we demonstrate how pseudocode from a 2019 presentation by John Gilbert describing BFS in linear algebraic terms [Gil] can be expressed in BLAStoff

```
Input: graph, frontier, levels
2 depth \leftarrow \emptyset
3 while nvals(frontier) > \emptyset:
4 depth \leftarrow depth + 1
5 levels[frontier] \leftarrow depth
6 frontier<\neglevels,replace> \leftarrow graph^T \oplus . \otimes frontier
BFS pseudocode.png
7 where \oplus . \otimes = \bigoplus . \bigotimes (\text{LogicalSemiring})
```

Our corresponding code for BFS looks like the following:

Let's look at how this code works. (Note: the cited slides can be helpful for understanding the linear algebra aspects of the algorithm.). It takes in an $n \times n$ adjacency matrix G and a column vector frontier of height n as well, where each entry is 0 or a true value, to denote whether that vertex is in the starting list. On line 4, we then create levels, a vector of the same size as frontier. This will be our output vector, as it levels[i] will contain the closest distance from vertex i to a vertex in frontiers, or -1 if its unreachable. You'll notice that we initialize levels with 0s as we will decrement on line 17. We then make a new variable maskedGT on line 5, which is just the transpose of G. We do this because we are going to be modifying this matrix, but we don't want to change the original G. We take the transpose because that's what allows for part of the algorithm, which I'll explain in a second, and we don't want to do that on every iteration. We then set a variable depth to 0 on 6. This will keep track of our iterations.

Then we start the while loop, which keeps going as long as there is one non-zero value in *frontier*; that is, we still have vertices we want to look at. We then increment depth on line 9, switching quickly to arithmetic for this one line, as otherwise depth would never go above 1. Using our range-fromvector function defined in the standard library, line 11 essentially sets levels[i]equal to the current depth if frontier[i] is non-zero. That way, all the vertices that we're currently searching for have their distance in levels as the current iteration in our while loop. This will be one more than the level, but we're going to decrement on line 17. The key portion of this code is line 14, which multiplies maskedGT and frontier. Because of the way the adjacency matrix is constructed, this will give us a vector in the same format as frontier, only now with the vertices reachable from the vertices in the original frontier, and we will overwrite frontier with this new frontier. With all that I've explained so far, the algorithm would be give you the correct reachable nodes, but would run over paths to vertices for which we've already found a closer path, so depths would be wrong.

To account for this issue, on lines 12 and 13 we remove all the edges to the nodes in frontier, so that as we continue in BFS, we add a previously visited node. We generate a mask by taking our frontier, transposing it, concatenating

it down N times, and negating it. Here's an example:

$$frontier = \begin{bmatrix} 0\\1\\1\\0\\0\\1 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1 & 1 & 0 & 0 & 1 \end{bmatrix} \\ \begin{bmatrix} 0 & 1 & 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 & 1 & 0 \end{bmatrix}$$

In this map, all the ones denote edges not to items in frontier, and thus edges we can keep. So, if we do element-wise multiplication between this mask matrix and our ongoing, masked, G^T , we will keep removing those edges and ensure we never revisit!

- 3 Project Plan
- 4 Test Plan
- 5 Lessons Learned
- 5.1 Katon
- 5.2 Michael
- 5.3 Jake
- 5.4 Jason
- 6 Appendix

```
(* Top-level of the BLAStoff compiler: scan & parse the input,
      check the resulting AST and generate an SAST from it, generate LLVM
      and dump the module *)
   type action =
     | Ast
     | Semant
     | LLVM_IR
     | Compile
10
11 let () =
     let action = ref Compile in
     let set_action a () = action := a in
     let speclist =
14
       [ "-a", Arg.Unit (set_action Ast), "Print the AST"
       ; "-s", Arg.Unit (set_action Semant), "Print the SAST"
16
       ; "-1", Arg.Unit (set_action LLVM_IR), "Print the generated LLVM IR"
       ; ( "-c"
         , Arg.Unit (set_action Compile)
         , "Check and print the generated LLVM IR (default)" )
20
21
     in
22
     let usage_msg = "usage: ./blastoff.native [-a|-s|-l|-c] [file.blst]" in
23
     let channel = ref stdin in
24
     Arg.parse speclist (fun filename -> channel := open_in filename)
     let lexbuf = Lexing.from_channel !channel in
     let scanner_token_wrapper lb =
       let tok = Scanner.token lb in
       tok
     let ast = Blastoffparser.program scanner_token_wrapper lexbuf in
31
     match !action with
32
     | Ast -> print_string (Ast.string_of_program ast)
33
     | _ ->
34
       let sast =
35
         try Semant.check ast with
         | e ->
           let msg = Printexc.to_string e in
           raise (Failure ("Semantic Checking Error: " ^ msg))
39
40
       (match !action with
41
       | Ast -> ()
42
       | Semant -> print_string (Ast.string_of_program sast)
       | LLVM_IR -> print_string (Llvm.string_of_llmodule
44
            (Codegen.translate sast))
       | Compile ->
45
         let m = Codegen.translate sast in
```

```
Llvm_analysis.assert_valid_module m;
47
         print_string (Llvm.string_of_llmodule m))
48
   ;;
   (* Ocamllex scanner for BLAStoff *)
   { open Blastoffparser
   (* http://caml.inria.fr/pub/docs/manual-ocaml-4.00/manual026.html#toc111
   let keyword_table = Hashtbl.create 97
   let _ = List.iter (fun (kwd, tok) -> Hashtbl.add keyword_table kwd tok)
       [ "while", WHILE;
         "return", RETURN;
9
         "if", IF;
10
         "else", ELSE;
11
         "for", FOR;
12
         "def", FDECL;
         "T", TRANSP]
  }
15
16
   let digit = ['0'-'9']
17
   let arrow = ['-']['>']
   rule token = parse
20
     [' ' '\t' '\r' '\n'] { token lexbuf } (* Whitespace *)
21
   | "/*"
             { comment lexbuf }
                                        (* Comments *)
22
             { single_line_comment lexbuf }
   '-'?digit* as lxm { INTLITERAL(int_of_string lxm) }
   | ['-']?digit*['.']digit* as lxm { FLOATLITERAL(float_of_string lxm) }
             { VLINE }
   | '|'
             { LBRACK }
   | '['
   | ']'
             { RBRACK }
             { LPAREN }
             { RPAREN }
   1 '{'
             { LBRACE }
   1 '}'
             { RBRACE }
     '\''[^'\'']*'\'' as str { STRINGLITERAL(String.sub str 1
        ((String.length str) - 2)) }
   | '@'
             { ELMUL }
34
   "@="
             { ELMULASSIGN }
   | ,~,
             { CONV }
   1 "~="
             { CONVASSIGN }
   1 ':'
             { CONCAT }
   1 ":="
             { CONCATASSIGN }
  | ';'
             { SEMI }
  | ','
             { COMMA }
42 '+'
             { PLUS }
  "+="
             { PLUSASSIGN }
```

```
{ MATMUL }
   | '*'
             { MATMULASSIGN }
   | '='
             { ASSIGN }
             { EDGE }
   arrow
   | ['+']['%'] { PLUSREDUCE }
   | ['*']['%']
                  { MULREDUCE }
             { EQ }
             { NEQ }
   | '<'
             { LT }
   | "<="
             { LEQ }
   | ">"
             { GT }
   | ">="
             { GEQ }
             { RAISE }
             { RAISEASSIGN }
             { NOT }
   | '#'
             { SEMIRING }
   | ['a'-'z' 'A'-'Z' '_']['a'-'z' 'A'-'Z' '0'-'9' '_']* as lxm
     { (*print_endline "find lxm: ";
         print_endline lxm;*)
       try
63
         Hashtbl.find keyword_table lxm
64
       with Not_found ->
65
         ID(lxm)}
   | eof { EOF }
   | _ as char { raise (Failure("illegal character " ^ Char.escaped char)) }
69
   and comment = parse
70
         "*/" { token lexbuf }
71
     | _ { comment lexbuf }
72
   and single_line_comment = parse
     \n' \  token lexbuf }
74
     | _ { single_line_comment lexbuf }
   (* Abstract Syntax Tree and functions for printing it *)
   type op =
     | Add
     | Matmul
     | Elmul
     | Conv
     | Equal
     | Neq
     | Less
10
11
     | Leq
     | Greater
     | Geq
     | Concat
14
     | Exponent
15
```

```
type uop =
    | Neg
     | Transp
     | Plusreduce
     | Mulreduce
     | Size
23
   type lit =
    | IntLit of int
    | FloatLit of float
26
   type expr =
28
     | GraphLit of (int * int) list
     | UnkMatLit of lit list list
30
     | IntMatLit of int list list
     | FloatMatLit of float list list
    | Id of string
     | Binop of expr * op * expr
     | Unop of uop * expr
     | Assign of expr * expr
     | IdAssign of string * expr
37
     | SelectAssign of string * expr list * expr
     | Selection of expr * expr list
     | Call of string * expr list
     | StringLit of string
41
   type stmt =
43
     | Semiring of string
44
     | Block of stmt list
45
     | Expr of expr
     | Return of expr
     | If of expr * stmt * stmt
49
     | While of expr * stmt
50
   type func_decl =
51
     { fname : string
     ; formals : string list
     ; body : stmt list
56
   type program = func_decl list * stmt list
57
58
   (* Pretty-printing functions *)
59
   let string_of_op = function
   | Add -> "+"
   | Matmul -> "*"
63
   | Elmul -> "@"
64
   | Conv -> "~"
65
     | Equal -> "=="
```

```
| Neq -> "!="
67
      | Less -> "<"
68
     | Leq -> "<="
69
      | Greater -> ">"
      | Geq -> ">="
      | Exponent -> "^"
      | Concat -> ":"
74
75
    let string_of_mat lit_to_string m =
      let string_of_row row =
       String.concat "," (List.fold_left (fun acc lit -> lit_to_string lit
78
            :: acc) [] row)
      in
79
      " ["
80
      ^ String.concat ";" (List.fold_left (fun acc row -> string_of_row row
81
          :: acc) [] m)
82
83
   ;;
84
    let string_of_graph g =
85
      let string_of_edge (v1, v2) = string_of_int v1 ^ "->" ^ string_of_int
      "[" ^ String.concat ";" (List.map string_of_edge g) ^ "]"
    ;;
88
    let rec string_of_expr = function
90
     | Id s -> s
91
      | Binop (e1, o, e2) ->
92
        string_of_expr e1 ^ " " ^ string_of_op o ^ " " ^ string_of_expr e2
93
      | Unop (o, e) -> string_of_e_with_uop e o
      | Assign (e1, e2) -> string_of_expr e1 ^ " = " ^ string_of_expr e2
      | IdAssign (s, e) -> s ^ " = " ^ string_of_expr e
96
      | Call (f, el) -> f ^ "(" ^ String.concat ", " (List.map
97
          string_of_expr el) ^ ")"
      | UnkMatLit m ->
98
       string_of_mat
99
         (fun lit ->
           match lit with
           | IntLit ilit -> string_of_int ilit
           | FloatLit flit -> string_of_float flit)
104
      | IntMatLit m -> string_of_mat string_of_int m
      | GraphLit g -> string_of_graph g
      | StringLit s -> "'" ^ s ^ "'"
      | FloatMatLit m -> string_of_mat string_of_float m
      | Selection (e, args) ->
        string_of_expr e ^ "[" ^ String.concat ", " (List.map string_of_expr
            args) ^ "]"
      | SelectAssign (s, args, e) ->
```

```
S
        ^ "F"
        ^ String.concat ", " (List.map string_of_expr args)
115
        ^ H = H
116
        ^ string_of_expr e
117
118
    and string_of_e_with_uop e =
      let str_expr = string_of_expr e in
120
      function
121
      | Neg -> "!" ^ str_expr
      | Size -> "|" ^ str_expr ^ "|"
123
      | Transp -> str_expr ^ "^T"
124
      | Plusreduce -> "+%" ^ str_expr
      | Mulreduce -> "*%" ^ str_expr
126
127
    ;;
128
    let rec string_of_stmt = function
      | Semiring ring -> "#" ^ ring ^ "\n"
130
      | Block stmts -> "{\n" ^ String.concat "" (List.map string_of_stmt
          stmts) ^{"}\n"
      | Expr expr -> string_of_expr expr ^ ";\n"
      | Return expr -> "return " ^ string_of_expr expr ^ ";\n"
      | If (e, s, Block []) -> "if (" ^ string_of_expr e ^ ")\n" ^
          string_of_stmt s
      | If (e, s1, s2) ->
135
        "if (" ^ string_of_expr e ^ ")\n" ^ string_of_stmt s1 ^ "else\n" ^
136
            string_of_stmt s2
      | While (e, s) -> "while (" ^ string_of_expr e ^ ") " ^ string_of_stmt
137
138
    ;;
139
    let string_of_func func =
140
141
      ^ func.fname
142
      ^ "("
143
      ^ String.concat ", " func.formals
144
      ^ "{\n"
146
      ^ String.concat "" (List.map string_of_stmt func.body)
147
      ^ "}\n"
148
149
150
    let string_of_program (funcs, stmts) =
151
      String.concat "" (List.map string_of_func funcs)
152
153
154
      ^ String.concat "" (List.map string_of_stmt stmts)
155
    ;;
```

```
/* Ocamlyacc parser for BLAStoff */
   %{
   open Ast
   %}
   %token SEMI LPAREN RPAREN LBRACE RBRACE LBRACK RBRACK COMMA SEMIRING EDGE
   %token MATMUL ELMUL ASSIGN FDECL RANGEMAT CONV PLUS RAISE PLUSREDUCE
        MULREDUCE
   %token NOT EQ NEQ LT LEQ GT GEQ IMAT ELMAT TRANSP VLINE SEMIRING CONCAT
        ZEROMAT
10 %token RETURN IF ELSE FOR WHILE INT BOOL FLOAT VOID
   %token PLUSASSIGN ELMULASSIGN CONVASSIGN MATMULASSIGN CONCATASSIGN
       RAISEASSIGN
12 %token <int> INTLITERAL
13 %token <float> FLOATLITERAL
14 %token <string> STRINGLITERAL
   %token <string> ID
   %token EOF
   %start program
   %type <Ast.program> program
20
21 %nonassoc NOELSE
22 %nonassoc ELSE
23 %right ASSIGN PLUSASSIGN ELMULASSIGN CONVASSIGN MATMULASSIGN
       CONCATASSIGN RAISEASSIGN
24 %left EQ NEQ
25 %left LT GT LEQ GEQ
26 %right LBRACK RBRACK
   %left PLUS
   %left MATMUL ELMUL
   %left CONCAT CONV
   %left RAISE
   %left EDGE
32 %right PLUSREDUCE MULREDUCE
33 %left TRANSP
34 %right NOT
35 %%
36
  program:
37
   units EOF { (List.rev (fst $1), snd $1) }
38
39
  units:
40
      /* empty */ { ([], []) }
       | units fdecl { ($2 :: fst $1 , snd $1) }
       | units stmt { (fst $1, $2 :: snd $1) }
44
45 fdecl:
```

```
FDECL ID LPAREN formals_opt RPAREN LBRACE stmt_list RBRACE
46
      { fname = $2;
47
          formals = $4;
48
          body = List.rev $7 } }
49
50
   formals_opt:
51
       /* nothing */ { [] }
     | formal_list { $1 }
53
54
   formal_list:
55
                          { [$1] }
       TD
     | formal_list COMMA ID { $3 :: $1 }
57
58
   expr_list:
59
      expr
                            { [$1] }
60
     | expr_list COMMA expr { $3 :: $1 }
61
62
   stmt_list:
      /* nothing */ { [] }
     | stmt_list stmt { $2 :: $1 }
65
66
   stmt:
67
       expr SEMI
                                                { Expr $1
68
     | SEMIRING ID SEMI
                                                { Semiring $2
     | RETURN ret_opt SEMI
                                                { Return $2
70
     | LBRACE stmt_list RBRACE
                                                { Block(List.rev $2)
71
     | IF LPAREN expr RPAREN stmt %prec NOELSE { If($3, $5, Block([]))
72
                              }
73
     | IF LPAREN expr RPAREN stmt ELSE stmt
                                               { If($3, $5, $7)
     | WHILE LPAREN expr RPAREN stmt
                                                { While($3, $5)
74
     | FOR LPAREN stmt expr SEMI expr RPAREN stmt { Block([$3; While($4,
          Block([$8; Expr($6)]))])}
76
   ret_opt:
77
         /* nothing */ { UnkMatLit([[]]) }
78
                   { $1 }
     | expr
79
80
81
   lit:
       INTLITERAL { IntLit($1) }
84
     | FLOATLITERAL { FloatLit($1) }
   expr:
                  { UnkMatLit([[$1]]) }
     lit
```

```
| STRINGLITERAL { StringLit($1) }
88
      | ID
                       { Id($1)
89
                                              }
        expr PLUS expr { Binop($1, Add, $3)
90
        ID PLUSASSIGN expr { IdAssign($1, Binop(Id($1), Add, $3)) }
91
        expr MATMUL expr { Binop($1, Matmul, $3) }
        ID MATMULASSIGN expr { IdAssign($1, Binop(Id($1), Matmul, $3)) }
        expr ELMUL expr { Binop($1, Elmul, $3) }
        ID ELMULASSIGN expr { IdAssign($1, Binop(Id($1), Elmul, $3)) }
                   expr { Binop($1, Equal, $3) }
        expr EQ
                   expr { Binop($1, Neq, $3) }
        expr NEQ
                   expr { Binop($1, Less, $3) }
        expr LT
        expr LEQ
                   expr { Binop($1, Leq, $3)
        expr GT
                   expr { Binop($1, Greater, $3) }
                   expr { Binop($1, Geq, $3)
        expr GEQ
        expr CONV expr { Binop($1, Conv, $3) }
      | ID CONVASSIGN expr { IdAssign($1, Binop(Id($1), Conv, $3)) }
        expr CONCAT expr { Binop($1, Concat, $3)}
104
      | ID CONCATASSIGN expr { IdAssign($1, Binop(Id($1), Concat, $3)) }
      | expr RAISE expr { Binop($1, Exponent, $3) }
      | ID RAISEASSIGN expr { IdAssign($1, Binop(Id($1), Exponent, $3)) }
      | expr RAISE TRANSP { Unop(Transp, $1) }
      | NOT expr
                      { Unop(Neg, $2) }
109
      | PLUSREDUCE expr { Unop(Plusreduce, $2) }
      | MULREDUCE expr { Unop(Mulreduce, $2) }
        expr LBRACK expr_list RBRACK { Selection($1, $3)}
        expr ASSIGN expr { Assign($1, $3)
113
      | ID LPAREN args_opt RPAREN { Call($1, $3) }
114
      | LPAREN expr RPAREN { $2
      | VLINE expr VLINE { Unop(Size, $2)
116
      | LBRACK mat_content RBRACK { UnkMatLit($2) }
117
      | LBRACK graph_content RBRACK { GraphLit($2) }
118
119
    mat_content:
120
       mat_row { [$1] }
      | mat_content SEMI mat_row {$3 :: $1}
123
124
    mat_row:
        lit { [$1] }
      | mat_row COMMA lit {$3 :: $1 }
126
      | /* nothing */ {[]}
127
    graph_content:
        edge { [$1] }
130
      | graph_content SEMI edge {$3 :: $1}
133
          INTLITERAL EDGE INTLITERAL { ($1, $3) }
134
135
136
    args_opt:
        /* nothing */ { [] }
137
```

```
| args_list { List.rev $1 }
138
    args_list:
140
                              { [$1] }
141
        expr
      | args_list COMMA expr { $3 :: $1 }
    (* Semantic checking for the BLAStoff compiler *)
    open Ast
    module StringMap = Map.Make (String)
    (* Semantic checking of the AST. Returns an SAST if successful,
       throws an exception if something is wrong.
       Check each global variable, then check each function *)
   let check (funcs, stmts) =
10
      let check_vars loc stmt_lst =
11
       let add_decl lst = function
         | Expr e ->
           (match e with
           | IdAssign(var, _) -> var :: lst
           | Assign(Id var, _) -> var :: lst
           | _ -> lst)
         | _ -> lst
        in
        let decls = List.fold_left add_decl [] stmt_lst in
        let rec check_dups = function
21
         | [] -> ()
         | n1 :: n2 :: _ when n1 = n2 -> raise (Failure ("duplicate " ^ n1
              ^ " in " ^ loc))
         | _ :: tl -> check_dups tl
        check_dups (List.sort compare decls)
      (**** Check functions ****)
      (* Collect function declarations for built-in functions: no bodies *)
     let built_in_decls =
        let add_bind map (name, args) =
         StringMap.add name { fname = name; formals = args; body = [] } map
33
34
       List.fold_left add_bind StringMap.empty Definitions.functions
35
36
      (* Add function name to symbol table *)
      let add_func map fd =
       let built_in_err = "function " ^ fd.fname ^ " may not be defined"
        and dup_err = "duplicate function " ^ fd.fname
        and make_err er = raise (Failure er)
41
        and n = fd.fname (* Name of the function *) in
```

```
match fd with
43
       (* No duplicate functions or redefinitions of built-ins *)
44
       | _ when StringMap.mem n built_in_decls -> make_err built_in_err
       | _ when StringMap.mem n map -> make_err dup_err
       | _ -> StringMap.add n fd map
47
     (* Collect all function names into one symbol table *)
49
     let function_decls = List.fold_left add_func built_in_decls funcs in
50
     let find_func fname =
       try StringMap.find fname function_decls with
52
       | Not_found -> raise (Failure ("Undeclared function " ^ fname))
53
     in
     let is_float = function
       | IntLit _ -> false
56
       | FloatLit _ -> true
57
58
     let contains_float m = List.exists (fun lst -> List.exists is_float
59
         lst) m in
     let get_char_codes s =
       (* Takes string, returns backwards list of character codes *)
61
       let rec exp i l = if i < 0 then l else exp (i - 1) (Char.code s.[i]</pre>
62
            :: 1) in
       exp (String.length s - 1) []
63
     in
     let rec check_expr = function
       | Call (fname, args) as call ->
         let fd = find_func fname in
67
         let num_formals = List.length fd.formals in
68
         if List.length args != num_formals
69
         then
          raise
             (Failure
               ("Expecting "
               ^ string_of_int num_formals
               ^ " arguments in "
               ^ string_of_expr call))
         else Call (fname, List.map check_expr args)
       | StringLit s ->
         let chars = List.rev (get_char_codes s) in
         IntMatLit (List.map (fun c -> [ c ]) chars)
80
       | UnkMatLit m ->
81
         let has_float = contains_float m in
82
         (match has_float with
83
         | true ->
          FloatMatLit
             (List.map
                (fun row ->
                 List.map
                   (function
89
                     | IntLit lit -> float_of_int lit
```

```
| FloatLit lit -> lit)
91
                    row
92
                ) m)
93
          | false ->
           IntMatLit
              (List.map
                (fun row ->
                  List.map
                    (function
                      | IntLit lit -> lit
100
                      | FloatLit _ -> raise (Failure "Expected Integers in
                          Matrix"))
                    row)
                m))
        | Id n \rightarrow Id n
104
        | Binop (e1, op, e2) -> Binop (check_expr e1, op, check_expr e2)
        | Unop (op, e) -> Unop (op, check_expr e)
106
        | FloatMatLit _ -> raise (Failure "Unexpected float matrix in semant
107
            checking")
        | IntMatLit _ -> raise (Failure "Unexpected float matrix in semant
108
            checking")
        | GraphLit g -> GraphLit g
109
        | Selection (e, args) -> Selection (check_expr e, List.map
            check_expr args)
        | IdAssign (n, e) -> IdAssign (n, check_expr e)
        | SelectAssign (n, args, e) -> SelectAssign (n, List.map check_expr
112
            args, check_expr e)
        | Assign (e1, e2) ->
113
          let fix_assign = function
114
            | Id i, e -> check_expr (IdAssign (i, e))
115
            | Selection (Id n, args), e -> check_expr (SelectAssign (n,
                args, e))
            | _ -> raise (Failure "Bad left side of assignment, expected ID
117
                or ID[...]")
          in
118
          fix_assign (e1, e2)
119
120
      in
      let rec check_stmt = function
        | Expr e -> Expr (check_expr e)
        | Semiring ring ->
          (match List.mem_assoc ring Definitions.rings with
124
          | true -> Semiring ring
          | false -> raise (Failure ("Unknown semiring " ^ ring)))
126
        | Block bl -> Block (check_stmt_list bl)
127
        | If (p, b1, b2) -> If (check_expr p, check_stmt b1, check_stmt b2)
129
        | While (p, s) -> While (check_expr p, check_stmt s)
        | Return e -> Return (check_expr e)
130
      and check_stmt_list = function
131
        [ (Return _ as s) ] -> [ check_stmt s ]
        | Return _ :: _ -> raise (Failure "Unreachable statments after
```

```
return")
        | Block sl :: ss -> check_stmt_list (sl @ ss)
134
        | s :: ss -> check_stmt s :: check_stmt_list ss
        | [] -> []
136
137
      in
      let add_return body =
138
       match List.rev body with
        | Return _ :: _ -> body
140
        | _ as 1 -> List.rev (Return (UnkMatLit [ [] ]) :: 1)
141
142
      in
      let check_function func =
143
        let _ = check_vars "body" func.body in
        let checked_body = check_stmt_list (add_return func.body) in
145
        { fname = func.fname; formals = func.formals; body = checked_body }
146
147
      List.map check_function funcs, List.map check_stmt stmts
148
149
    module A = Ast
    open Ast
    open Definitions
    module StringMap = Map.Make (String)
    let translate (functions, statements) =
     let main_fdecl = { fname = "main"; formals = []; body = List.rev
          statements } in
     let function_decls : (L.llvalue * func_decl) StringMap.t =
        let function_decl m fdecl =
         let name = fdecl.fname
         and formal_types = Array.of_list (List.map (fun _ -> matrix_t)
11
              fdecl.formals) in
         let ftype = L.function_type matrix_t formal_types in
         StringMap.add name (L.define_function name ftype blastoff_module,
13
              fdecl) m
        in
14
        let decls = List.fold_left function_decl StringMap.empty functions in
       StringMap.add
         main_fdecl.fname
          ( L.define_function
             main_fdecl.fname
19
             (L.function_type i32_t (Array.of_list []))
20
             blastoff_module
21
          , main_fdecl )
22
23
         decls
24
      in
     let build_function_body fdecl is_main =
26
        let func, _ =
          try StringMap.find fdecl.fname function_decls with
          | Not_found -> raise (Failure ("Unknown function, " ^ fdecl.fname))
```

```
in
29
       let builder = L.builder_at_end context (L.entry_block func) in
30
       let local_vars =
31
         let add_formal m n p =
           L.set_value_name n p;
           let local = L.build_alloca matrix_t n builder in
           ignore (L.build_store p local builder);
           StringMap.add n local m
         in
         let add_local m n =
           if StringMap.mem n m
           then m
           else (
41
             let local_var = L.build_alloca matrix_t n builder in
42
             StringMap.add n local_var m)
43
         in
44
         let formals =
45
          List.fold_left2
            add_formal
             StringMap.empty
             fdecl.formals
49
             (Array.to_list (L.params func))
50
51
         let rec add_assignment lst = function
           | Expr e ->
             (match e with
             | IdAssign (id, _) -> id :: lst
             | _ -> lst)
56
           | Block stmts -> List.fold_left add_assignment lst stmts
57
           | If (_, s1, s2) -> add_assignment (add_assignment lst s1) s2
           | While (_, s) -> add_assignment lst s
           | _ -> lst
61
         let locals = List.fold_left add_assignment [] fdecl.body in
62
         List.fold_left add_local formals locals
63
64
       let lookup n =
         try StringMap.find n local_vars with
         | Not_found -> raise (Failure ("Undeclared variable " ^ n))
68
       let add_terminal builder instr =
69
         match L.block_terminator (L.insertion_block builder) with
70
         | Some _ -> ()
71
         | None -> ignore (instr builder)
72
       in
       let build_graph_matrix builder m =
         let max3 a b c =
75
           if a >= b && a >= c then a else if b >= c && b >= a then b else c
76
         let dim = 1 + List.fold_left (fun acc elem -> max3 acc (fst elem)
```

```
(snd elem)) 0 m in
          let mat =
79
            L.build_call
80
              matrix_create_f
81
              [| L.const_int i32_t dim; L.const_int i32_t dim |]
              "matrix_create"
              builder
84
          in
85
          List.iter
86
            (fun elem ->
              ignore
                (L.build_call
                   {\tt matrix\_setelem\_f}
90
                   [| mat
91
                    ; L.const_int i32_t 1 \,
92
                    ; L.const_int i32_t (fst elem)
93
                    ; L.const_int i32_t (snd elem)
94
                   1]
                   "matrix_setelem"
                   builder))
97
            m;
98
          mat
99
        in
100
        let build_matrix typ builder m =
          let mat =
102
            L.build_call
103
              matrix_create_f
              [| L.const_int i32_t (List.length m)
               ; L.const_int i32_t (List.length (List.hd m))
106
              1]
107
              "matrix_create"
108
109
              builder
          in
          List.iteri
111
            (fun i row ->
              (List.iteri (fun j elem ->
113
                   ignore
114
                     (L.build_call
115
                        matrix_setelem_f
116
                        [| mat
117
                         ; typ elem
118
                         ; L.const_int i32_t i
119
                         ; L.const_int i32_t j
120
                        1]
121
122
                        "matrix_setelem"
123
                        builder)))
124
                (List.rev row))
            (List.rev m);
          mat
126
        in
127
```

```
let rec fill_select_args builder args =
128
          let zero =
            L.build_call
130
             matrix_create_f
131
              [| L.const_int i32_t 1; L.const_int i32_t 1 |]
              "matrix_create"
133
              builder
134
          in
          let base =
136
            L.build_call
              matrix_create_f
              [| L.const_int i32_t 1; L.const_int i32_t 1 |]
139
              "matrix_create"
140
              builder
141
          in
142
          let one =
143
            ignore
144
              (L.build_call
145
                matrix_setelem_f
146
                 [| base; L.const_int i32_t 1; L.const_int i32_t 0;
147
                     L.const_int i32_t 0 |]
                "matrix_setelem"
148
                builder);
149
            base
          in
          match args with
152
          | [ _; _; _; _ ] as 1 -> 1
          | [ _; _; _ ] as 1 -> fill_select_args builder (one :: 1)
154
          | [ _; _ ] as 1 -> fill_select_args builder (one :: 1)
          | [ _ ] as 1 -> fill_select_args builder (zero :: 1)
156
          | _ -> raise (Failure "Too many/few arguments to selection")
157
        in
        let rec build_expr builder e =
159
          match e with
160
          | IntMatLit m -> build_matrix (fun el -> L.const_int i32_t el)
161
              builder m
          | GraphLit m -> build_graph_matrix builder m
          | FloatMatLit m -> build_matrix (fun el -> L.const_float float_t
              el) builder m
          | IdAssign (v, e) ->
164
            let comp_e = build_expr builder e in
165
            (match v with
166
            | s -> ignore (L.build_store comp_e (lookup s) builder));
167
168
            comp_e
          | Call (fname, exprs) ->
170
            (match fname with
            | "print" ->
171
              (match exprs with
              | [ e ] ->
173
                 build_call "matrix_print" [| build_expr builder e |] builder
174
```

```
| _ -> raise (Failure "Invalid list of expressions passed to
                  print"))
            | "toString" ->
              (match exprs with
177
              | [ e ] ->
178
                build_call
179
                  "matrix_tostring"
180
                  [| build_expr builder e |]
181
                 builder
182
              | _ -> raise (Failure "Invalid list of expressions passed to
183
                  toString"))
            | "I" ->
              (match exprs with
185
              | [e] ->
186
               build_call
187
                  "matrix_create_identity"
188
                  [| build_expr builder e |]
189
                 builder
190
              | _ -> raise (Failure "Invalid list of expressions passed to
191
                  I"))
            | "Zero" ->
              (match exprs with
193
              | [ e ] ->
194
                build_call "matrix_create_zero" [| build_expr builder e |]
                    builder
              | _ -> raise (Failure "Invalid list of expressions passed to
196
                  Zero"))
            | "range" ->
197
              (match exprs with
198
              | [ e ] ->
199
                build_call "matrix_create_range" [| build_expr builder e |]
                    builder
              | _ -> raise (Failure "Invalid list of expressions passed to
201
                  range"))
            | "__ring_push" ->
202
              (match exprs with
203
              | [] -> L.build_call ring_push_f [||] "__ring_push" builder
204
              | _ -> raise (Failure "Invalid list of expressions passed to
                  __ring_push"))
            | "__ring_pop" ->
206
              (match exprs with
207
              | [] -> L.build_call ring_pop_f [||] "__ring_pop" builder
208
              | _ -> raise (Failure "Invalid list of expressions passed to
209
                  __ring_pop"))
            | f ->
210
211
              let fdef, fdecl =
                try StringMap.find f function_decls with
212
                | Not_found ->
213
                 raise (Failure ("Undeclared function, " ^ f ^ ", found in
214
                      code generation"))
```

```
215
             let args = List.map (build_expr builder) (List.rev exprs) in
             L.build_call fdef (Array.of_list args) (fdecl.fname
217
                  "_result") builder)
          | Binop (e1, op, e2) ->
           let e1' = build_expr builder e1
219
           and e2' = build_expr builder e2 in
            (match op with
221
            | A.Matmul -> build_call "matrix_mul" [| e1'; e2' |] builder
            | A.Exponent -> L.build_call matrix_exp_f [| e1'; e2' |]
                "matrix_mul" builder
            | A.Conv -> build_call "matrix_conv" [| e1'; e2' |] builder
            | A.Elmul -> build_call "matrix_elmul" [| e1'; e2' |] builder
225
           | A.Add -> build_call "matrix_eladd" [| e1'; e2' |] builder
           | A.Concat -> build_call "matrix_concat" [| e1'; e2' |] builder
           | A.Equal -> build_call "matrix_eq" [| e1'; e2' |] builder
228
           | A.Neq -> build_call "matrix_neq" [| e1'; e2' |] builder
           | A.Leq -> build_call "matrix_leq" [| e1'; e2' |] builder
           | A.Less -> build_call "matrix_less" [| e1'; e2' |] builder
231
           | A.Geq -> build_call "matrix_geq" [| e1'; e2' |] builder
232
            | A.Greater ->
233
             build_call "matrix_greater" [| e1'; e2' |] builder)
234
          | UnkMatLit _ -> raise (Failure "Type of matrix is unknown")
          | Assign _ -> raise (Failure "Assign in codegen")
           StringLit _ -> raise (Failure "StringLit in codegen")
          | Unop (op, e) ->
238
           let e' = build_expr builder e in
           (match op with
240
           | A.Size -> build_call "matrix_size" [| e' |] builder
241
           | A.Transp -> build_call "matrix_transpose" [| e' |] builder
           | A.Plusreduce ->
             build_call
               "matrix_reduce"
               [| e'; L.const_int i32_t 0 |]
246
               builder
            | A.Mulreduce ->
             build_call
249
               "matrix_reduce"
               [| e'; L.const_int i32_t 1 |]
251
               builder
            | A.Neg -> build_call "matrix_negate" [| e' |] builder)
253
          | Id v -> L.build_load (lookup v) v builder
254
255
          | Selection (e, args) ->
           let partialargs' = List.map (build_expr builder) args in
256
           let filledargs' = fill_select_args builder partialargs' in
           let revfilledargs' = List.rev filledargs' in
           let e' = build_expr builder e in
           let args' = e' :: revfilledargs' in
260
           L.build_call matrix_extract_f (Array.of_list args')
261
                "matrix_extract" builder
```

```
| SelectAssign (v, args, e) ->
262
           let partialargs' = List.map (build_expr builder) args in
263
           let filledargs' = fill_select_args builder partialargs' in
264
           let revfilledargs' = List.rev filledargs' in
265
           let e' = build_expr builder e in
           let v' = L.build_load (lookup v) v builder in
           let args' = v' :: e' :: revfilledargs' in
268
           build_call "matrix_insert" (Array.of_list args') builder
269
        in
        let rec build_stmt builder = function
          | Block sl -> List.fold_left build_stmt builder sl
          | Semiring ring ->
           ignore
274
              (L.build_call
                ring_change_f
                [| L.const_int i32_t (List.assoc ring Definitions.rings) |]
277
                "ring_change"
278
                builder);
279
           builder
          | Expr e ->
281
           ignore (build_expr builder e);
282
           builder
          | Return e ->
           ignore (build_expr builder (Call ("__ring_pop", [])));
           ignore (L.build_ret (build_expr builder e) builder);
           builder
          | If (pred, thn, els) ->
           let pred_expr = build_expr builder pred in
289
           let mat_truthiness =
290
             L.build_call matrix_truthy_f [| pred_expr |] "matrix_truthy"
291
                  builder
           in
           let bool_val =
293
             L.build_icmp L.Icmp.Eq mat_truthiness (L.const_int i32_t 1)
294
                  "i1_t" builder
           in
295
           let merge_bb = L.append_block context "merge_if" func in
           let build_br_merge = L.build_br merge_bb in
           let then_bb = L.append_block context "then" func in
           add_terminal (build_stmt (L.builder_at_end context then_bb) thn)
                build_br_merge;
           let else_bb = L.append_block context "else" func in
300
           add_terminal (build_stmt (L.builder_at_end context else_bb) els)
301
                build_br_merge;
           ignore (L.build_cond_br bool_val then_bb else_bb builder);
303
           L.builder_at_end context merge_bb
          | While (pred, body) ->
304
           let pred_bb = L.append_block context "while" func in
305
           let pred_builder = L.builder_at_end context pred_bb in
306
           let pred_expr = build_expr pred_builder pred in
307
```

```
let mat_truthiness =
308
             L.build_call matrix_truthy_f [| pred_expr |] "matrix_truthy"
309
                  pred_builder
310
            in
            let bool_val =
311
             L.build_icmp L.Icmp.Eq mat_truthiness (L.const_int i32_t 1)
312
                  "i1_t" pred_builder
313
            ignore (L.build_br pred_bb builder) (* builds branch to while
314
                from entry point *);
            let body_bb = L.append_block context "while_body" func in
            let body_builder = build_stmt (L.builder_at_end context body_bb)
316
                body in
            add_terminal body_builder (L.build_br pred_bb);
317
            let merge_bb = L.append_block context "merge" func in
318
            ignore (L.build_cond_br bool_val body_bb merge_bb pred_builder);
319
            L.builder_at_end context merge_bb
320
        in
321
        let body = Expr (Call ("__ring_push", [])) :: fdecl.body in
322
        let builder = build_stmt builder (Block body) in
        add_terminal
324
          builder
325
          (L.build_ret (L.const_int (if is_main then i32_t else matrix_t) 0))
326
      build_function_body main_fdecl true;
      List.iter2 build_function_body functions (List.map (fun _ -> false)
          functions);
      blastoff_module
330
331
    ;;
    module L = Llvm
    let context = L.global_context ()
    let llmem = L.MemoryBuffer.of_file "graphblas.bc"
    let llm = Llvm_bitreader.parse_bitcode context llmem
    let blastoff_module = L.create_module context "BLAStoff"
    let rings = [ "_", 0; "arithmetic", 1; "logical", 2; "maxmin", 3 ]
    let functions =
10
      [ "I", [ "n" ]
      ; "Zero", [ "d" ]
11
      ; "range", [ "n" ]
      ; "print", [ "e" ]
13
       "toString", [ "e" ]
      ]
16
    ;;
17
    type built_in =
      { name : string
```

```
; ret : L.lltype
20
     ; args : L.lltype list
21
   let i32_t = L.i32_type context
   let float_t = L.double_type context
26
   let matrix_t =
27
     L.pointer_type
       (match L.type_by_name llm "struct.matrix" with
       | None -> raise (Failure "matrix type implementation not found")
       | Some t -> t)
31
32
33
   let built_in_defs : built_in list =
34
     [ { name = "matrix_create"; ret = matrix_t; args = [ matrix_t ] }
     ; { name = "matrix_create_identity"; ret = matrix_t; args = [ matrix_t
         ] }
     ; { name = "matrix_create_zero"; ret = matrix_t; args = [ matrix_t ] }
     ; { name = "matrix_create_range"; ret = matrix_t; args = [ matrix_t ] }
     ; { name = "matrix_print"; ret = matrix_t; args = [ matrix_t ] }
     ; { name = "matrix_tostring"; ret = matrix_t; args = [ matrix_t ] }
     ; { name = "change_ring"; ret = i32_t; args = [ i32_t ] }
     ; { name = "matrix_setelem"; ret = i32_t; args = [ matrix_t; i32_t;
         i32_t; i32_t ] }
     ; { name = "matrix_mul"; ret = matrix_t; args = [ matrix_t; matrix_t ]
     ; { name = "matrix_conv"; ret = matrix_t; args = [ matrix_t; matrix_t
44
         ] }
     ; { name = "matrix_elmul"; ret = matrix_t; args = [ matrix_t; matrix_t
45
         1 }
     ; { name = "matrix_eladd"; ret = matrix_t; args = [ matrix_t; matrix_t
         ] }
     ; { name = "matrix_extract"
       ; ret = matrix_t
48
       ; args = [ matrix_t; matrix_t; matrix_t; matrix_t; matrix_t ]
49
50
     ; { name = "matrix_insert"
51
       ; ret = matrix_t
       ; args = [ matrix_t; matrix_t; matrix_t; matrix_t; matrix_t;
           matrix_t ]
54
     ;{name = "matrix_eq"; ret = matrix_t; args = [ matrix_t; matrix_t ]}
     ;{name = "matrix_neq"; ret = matrix_t; args = [ matrix_t; matrix_t ]}
     ;{name = "matrix_leq"; ret = matrix_t; args = [ matrix_t; matrix_t ]}
     ;{name = "matrix_less"; ret = matrix_t; args = [ matrix_t; matrix_t ]}
     ;{name = "matrix_geq"; ret = matrix_t; args = [ matrix_t; matrix_t ]}
59
     ;{name = "matrix_greater"; ret = matrix_t; args = [ matrix_t; matrix_t
60
         ]}
     ;{name = "matrix_concat"; ret = matrix_t; args = [ matrix_t; matrix_t
```

```
]}
     ;{ name = "matrix_bool"; ret = i32_t; args = [ matrix_t ] }
62
     ;{ name = "matrix_negate"; ret = matrix_t; args = [ matrix_t ] }
63
     ;{ name = "matrix_reduce"; ret = matrix_t; args = [ matrix_t ; i32_t] }
64
     ;{ name = "matrix_insert"; ret = matrix_t; args = [ matrix_t;
         matrix_t; matrix_t; matrix_t; matrix_t; matrix_t] }
     ;{ name = "matrix_reduce"; ret = matrix_t; args = [ matrix_t ; i32_t] }
66
     ;{ name = "matrix_size"; ret = matrix_t; args = [ matrix_t ] }
     ;{ name = "matrix_transpose"; ret = matrix_t; args = [ matrix_t ] }
     ;{ name = "matrix_truthy"; ret = matrix_t; args = [ matrix_t ] }
     ٦
71
   ;;
72
   let matrix_truthy_t = L.function_type i32_t [| matrix_t |]
   let matrix_truthy_f = L.declare_function "matrix_truthy" matrix_truthy_t
       blastoff_module
   let matrix_exp_t = L.function_type matrix_t [| matrix_t; matrix_t |]
   let matrix_exp_f = L.declare_function "matrix_exp" matrix_exp_t
       blastoff_module
   let create_fun_type fdef = L.function_type fdef.ret (Array.of_list
80
       fdef.args)
   let declare_fun fname ftype = L.declare_function fname ftype
       blastoff_module
   let built_ins = List.map (fun fdef -> fdef.name, declare_fun fdef.name
        (create_fun_type fdef)) built_in_defs
   let build_call fname args builder = L.build_call (List.assoc fname
83
       built_ins) args fname builder
   let matrix_create_t = L.function_type matrix_t [| i32_t; i32_t |]
   let matrix_create_f = L.declare_function "matrix_create" matrix_create_t
       blastoff_module
   let matrix_identity_t = L.function_type matrix_t [| matrix_t |]
   let matrix_identity_f =
     L.declare_function "matrix_create_identity" matrix_identity_t
         blastoff_module
   let ring_push_t = L.function_type i32_t [||]
   let ring_push_f = L.declare_function "ring_push" ring_push_t
       blastoff_module
92 let ring_pop_t = L.function_type i32_t [||]
93 let ring_pop_f = L.declare_function "ring_pop" ring_pop_t blastoff_module
   let ring_change_t = L.function_type i32_t [| i32_t |]
   let ring_change_f = L.declare_function "ring_change" ring_change_t
       blastoff_module
   let matrix_setelem_t = L.function_type i32_t [| matrix_t; i32_t; i32_t;
       i32_t |]
   let matrix_setelem_f =
     L.declare_function "matrix_setelem" matrix_setelem_t blastoff_module
```

```
L.function_type matrix_t [| matrix_t; matrix_t; matrix_t; matrix_t;
100
          matrix_t |]
   let matrix_extract_f =
101
      L.declare\_function \ "matrix\_extract" \ matrix\_extract\_t \ blastoff\_module
 #include <stdlib.h>
 #include <stdio.h>
    #include <errno.h>
    #include <GraphBLAS.h>
    struct matrix {
        GrB_Matrix mat;
static void die(const char *msg)
11 {
12
        if (errno)
13
           perror(msg);
        else
14
           fprintf(stderr, "%s\n", msg);
15
        exit(1);
16
    }
17
    #define GrB_die(msg, object)
19
20
        const char *GrB_msg;
21
       GrB_error(&GrB_msg, object);
22
        \label{eq:continuity} fprintf(stderr, "%s\n", GrB_msg); \ \ \\
23
        die(msg);
24
    } while (0)
    static int GrB_ok(GrB_Info info)
28
        if (info == GrB_SUCCESS || info == GrB_NO_VALUE) {
29
           return 1;
30
       } else {
31
            fprintf(stderr, "GrB_ok saw error code: %d\n", info);
            return 0;
33
34
        }
    }
35
36
   void GrB_print(GrB_Matrix mat)
37
38
    {
        if (!GrB_ok(GxB_Matrix_fprint(mat, NULL, GxB_COMPLETE_VERBOSE,
            stdout)))
            die("GxB_Matrix_fprint");
40
    }
41
42
```

let matrix_extract_t =

```
void GrB_size(GrB_Matrix mat, GrB_Index *nrows, GrB_Index *ncols)
   {
44
       if (nrows && !GrB_ok(GrB_Matrix_nrows(nrows, mat)))
45
           GrB_die("GrB_Matrix_nrows", mat);
46
47
       if (ncols && !GrB_ok(GrB_Matrix_ncols(ncols, mat)))
           GrB_die("GrB_Matrix_ncols", mat);
49
   }
50
   int32_t GrB_scalar(GrB_Matrix mat)
52
53
       GrB_Index nrows, ncols;
54
       int32_t elem;
55
56
       GrB_size(mat, &nrows, &ncols);
       if (nrows != 1 || ncols != 1)
58
           die("GrB_scalar mat dims bad");
59
       if (!GrB_ok(GrB_Matrix_extractElement(&elem, mat, 0, 0)))
           GrB_die("GrB_Matrix_extractElement", mat);
62
63
       return elem;
64
   }
65
   /* automatically called before main() */
67
    __attribute__((constructor))
   static void matrix_lib_init(void) {
69
       if (!GrB_ok(GrB_init(GrB_NONBLOCKING)))
70
           die("GrB_init");
71
   }
72
73
   /* automatically called after main() */
   __attribute__((destructor))
   void matrix_lib_finalize(void)
   {
       if (!GrB_ok(GrB_finalize()))
           die("GrB_finalize");
79
   }
80
81
   /* BELOW: Functions used externally */
82
83
   // begin ring_* functions //
84
85
   // stack of rings, implemented as intrusive linked list
   struct ring {
       GrB_Semiring ring;
       struct ring *prev;
89
   };
90
91
   struct ring *curr_ring = NULL;
```

```
93
    void ring_push()
94
    {
95
        struct ring *r = malloc(sizeof(*r));
96
        r->ring = GrB_PLUS_TIMES_SEMIRING_INT32;
97
        r->prev = curr_ring;
        curr_ring = r;
99
100
    void ring_pop()
103
        struct ring *prev;
104
105
        if (!curr_ring)
106
            die("ring_change: curr_ring is NULL");
108
        prev = curr_ring->prev;
109
        free(curr_ring);
        curr_ring = prev;
111
112
113
    void ring_change(int which)
114
    {
115
        if (!curr_ring)
116
            die("ring_change: curr_ring is NULL");
117
118
        if (which == 0) {
119
            if (!curr_ring->prev)
120
                die("ring_change to #_ but curr_ring->prev is NULL");
121
            curr_ring->ring = curr_ring->prev->ring;
122
        } else if (which == 1) {
            curr_ring->ring = GrB_PLUS_TIMES_SEMIRING_INT32;
        } else if (which == 2) {
            curr_ring->ring = GrB_LAND_LOR_SEMIRING_BOOL;
126
        } else if (which == 3) {
            curr_ring->ring = GrB_MAX_MIN_SEMIRING_INT32;
128
        } else {
129
            die("ring_change: unknown semiring");
130
131
132
    // end ring_* functions //
134
135
    // begin matrix_* functions //
136
137
138
    int matrix_getelem(struct matrix *A, int row, int col)
139
    {
        int32_t elem = 0;
140
141
        if (!GrB_ok(GrB_Matrix_extractElement(&elem, A->mat, row, col)))
142
```

```
GrB_die("GrB_Matrix_extractElement", A->mat);
143
144
        return elem;
145
    }
146
147
    void matrix_setelem(struct matrix *A, int val, int row, int col)
148
149
        // O is the implicit value; storing it explicitly would waste space
150
        int32_t unused;
        if (val == 0 &&
               GrB_Matrix_extractElement(&unused, A->mat, row, col) ==
                    GrB_NO_VALUE)
            return;
154
        if (!GrB_ok(GrB_Matrix_setElement(A->mat, val, row, col)))
156
            GrB_die("GrB_Matrix_setElement", A->mat);
    }
158
159
160
    struct matrix *matrix_create(int nrows, int ncols)
161
162
        struct matrix *A;
163
        if (!(A = malloc(sizeof *A)))
164
            die("malloc failed");
        if (!GrB_ok(GrB_Matrix_new(&A->mat, GrB_INT32, nrows, ncols)))
167
            GrB_die("GrB_Matrix_new", A->mat);
168
169
        return A;
    }
171
172
    struct matrix *matrix_create_zero(struct matrix *dims)
173
174
        GrB_Index dim_nrows, dim_ncols, nrows, ncols;
175
176
        GrB_size(dims->mat, &dim_nrows, &dim_ncols);
        if ((dim_nrows != 1 && dim_nrows != 2) || dim_ncols != 1)
            die("matrix_create_zero invalid dims arg");
180
        nrows = matrix_getelem(dims, 0, 0);
181
        ncols = dim_nrows == 2 ? matrix_getelem(dims, 1, 0) : nrows;
182
183
        return matrix_create(nrows, ncols);
184
    }
185
186
187
    struct matrix *matrix_create_identity(struct matrix *N_scalar)
188
        struct matrix *A;
189
        GrB_Index i, n;
190
191
```

```
n = GrB_scalar(N_scalar->mat);
192
        A = matrix_create(n, n);
193
        for (i = 0; i < n; i++)</pre>
194
            matrix_setelem(A, 1, i, i);
195
        return A;
197
    }
198
199
    struct matrix *matrix_create_range(struct matrix *range)
200
201
        struct matrix *A;
202
        int32_t lo, hi;
203
        GrB_Index i, range_nrows, range_ncols;
204
205
        GrB_size(range->mat, &range_nrows, &range_ncols);
206
        if (range_nrows == 1 && range_ncols == 1) {
207
            lo = 0;
208
            hi = matrix_getelem(range, 0, 0);
        } else if (range_nrows == 2 && range_ncols == 1) {
210
            lo = matrix_getelem(range, 0, 0);
211
            hi = matrix_getelem(range, 1, 0);
212
        } else {
213
            die("matrix_create_range invalid range arg");
214
        if (lo > hi)
217
            return matrix_create(0, 1);
218
219
        A = matrix_create(hi - lo, 1);
220
        i = 0;
221
        while (lo < hi)</pre>
            matrix_setelem(A, lo++, i++, 0);
224
        return A;
225
    }
226
227
    struct matrix *matrix_print(struct matrix *A)
228
229
        GrB_Index nrows, ncols, i;
230
        int elem;
231
232
        GrB_size(A->mat, &nrows, &ncols);
233
        if (ncols != 1)
234
            die("Tried to print string with more than 1 col");
235
237
        for (i = 0; i < nrows && (elem = matrix_getelem(A, i, 0)) != 0; i++)</pre>
238
            putchar(elem);
239
        struct matrix *R = matrix_create(0, 0);
240
        return R;
241
```

```
242 }
243
    struct matrix *matrix_tostring(struct matrix *A)
244
245
        struct matrix *B;
246
247
        GrB_Index nrows, ncols, i, j, k;
        char buf[1000], *b;
248
249
        GrB_size(A->mat, &nrows, &ncols);
        B = matrix_create(nrows * (ncols + 1) * 20, 1);
251
        if (nrows == 0 || ncols == 0)
            return B;
254
255
        k = 0;
256
        for (i = 0; i < nrows; i++) {</pre>
257
            for (j = 0; j < ncols; j++) {</pre>
258
                snprintf(buf, sizeof(buf), "%d ", matrix_getelem(A, i, j));
259
                for (b = buf; *b; b++)
260
                    matrix_setelem(B, *b, k++, 0);
261
            }
262
            matrix_setelem(B, '\n', k++, 0);
263
        }
264
        matrix_setelem(B, 0, k, 0);
        return B;
267
268
269
270
    struct matrix *matrix_mul(struct matrix *A, struct matrix *B)
271
272
273
        struct matrix *C;
        GrB_Info info;
274
        GrB_Index nrows, ncols, eq1, eq2;
275
276
        GrB_size(A->mat, &nrows, &eq1);
277
        GrB_size(B->mat, &eq2, &ncols);
        if (eq1 != eq2)
            die("matrix_mul bad dimensions");
280
281
        C = matrix_create(nrows, ncols);
282
283
        info = GrB_mxm(C->mat,
284
                       GrB_NULL,
285
                       GrB_NULL,
287
                       curr_ring->ring,
                       A->mat,
288
                       B->mat,
289
                       GrB_NULL);
290
291
```

```
if (!GrB_ok(info))
292
            GrB_die("GrB_mxm", A->mat);
293
294
        return C;
295
    }
297
    struct matrix *matrix_exp(struct matrix *A, struct matrix *N_scalar)
298
299
        struct matrix *B;
300
        int n;
301
        GrB_Index i, nrows, ncols;
303
        GrB_size(A->mat, &nrows, &ncols);
304
        if (nrows != ncols)
305
            die("matrix_exp mat not square");
306
307
        n = GrB_scalar(N_scalar->mat);
308
        if (n < 1)
            die("matrix_exp needs positive exponent");
310
311
312
        for (i = 0; i < n - 1; i++) {</pre>
313
            B = matrix_mul(A, B);
314
315
316
        return B;
317
318
319
    struct matrix *matrix_elmul(struct matrix *A, struct matrix *B)
320
321
        struct matrix *C;
322
323
        GrB_Info info;
        GrB_Index A_nrows, A_ncols, B_nrows, B_ncols;
324
325
        GrB_size(A->mat, &A_nrows, &A_ncols);
326
        GrB_size(B->mat, &B_nrows, &B_ncols);
327
328
        if (A_nrows != B_nrows || A_ncols != B_ncols)
            die("matrix_elmul bad dimensions");
330
331
        C = matrix_create(A_nrows, A_ncols);
332
333
        info = GrB_Matrix_eWiseMult_Semiring(C->mat,
334
                                            GrB_NULL,
335
                                            GrB_NULL,
337
                                             curr_ring->ring,
338
                                            A->mat,
339
                                            B->mat,
                                            GrB_NULL);
340
341
```

```
if (!GrB_ok(info))
342
            GrB_die("GrB_Matrix_eWiseMult_Semiring", A->mat);
343
344
        return C;
345
    }
346
347
    struct matrix *matrix_eladd(struct matrix *A, struct matrix *B)
348
349
        struct matrix *C;
350
        GrB_Info info;
351
        GrB_Index A_nrows, A_ncols, B_nrows, B_ncols;
        GrB_size(A->mat, &A_nrows, &A_ncols);
354
        GrB_size(B->mat, &B_nrows, &B_ncols);
355
356
        if (A_nrows != B_nrows || A_ncols != B_ncols)
357
            die("matrix_eladd bad dimensions");
358
359
        C = matrix_create(A_nrows, A_ncols);
361
        info = GrB_Matrix_eWiseAdd_Semiring(C->mat,
362
                                          GrB_NULL,
363
                                          GrB_NULL,
364
                                           curr_ring->ring,
                                           A->mat,
                                          B->mat,
367
                                          GrB_NULL);
368
369
        if (!GrB_ok(info))
370
            GrB_die("GrB_Matrix_eWiseAdd_Semiring", A->mat);
371
372
        return C;
374
    }
375
    struct matrix *matrix_extract(struct matrix *M, struct matrix *A, struct
376
         matrix *B, struct matrix *C, struct matrix *D)
    {
377
        struct matrix *R;
        GrB_Index A_nrows, A_ncols, B_nrows, B_ncols, C_nrows, C_ncols,
379
             D_nrows, D_ncols;
        int i, j, v, w;
380
381
        // verify that A, B, C, D are all integer matrices??
382
383
        //veryify that A, B are column vectors and that C, D are 1x1
        GrB_size(A->mat, &A_nrows, &A_ncols);
386
        GrB_size(B->mat, &B_nrows, &B_ncols);
387
        GrB_size(C->mat, &C_nrows, &C_ncols);
388
        GrB_size(D->mat, &D_nrows, &D_ncols);
389
```

```
390
        if (A_ncols != 1 || B_ncols != 1 || C_nrows != 1 || C_ncols != 1 ||
391
            D_nrows != 1 || D_ncols != 1)
            die("matrix_extract bad dimensions");
392
        int cval = matrix_getelem(C, 0, 0);
394
        int dval = matrix_getelem(D, 0, 0);
395
        R = matrix_create(A_nrows*cval, B_nrows*dval);
396
397
        //(A[i], B[j]) is top-left corner in form (cols, rows)
398
        //(A[i]+v, B[j]+w) is what we iterate through
        //(i*cval+v, j*dval+w) is where we store
        for (i = 0; i < A_nrows; i++){</pre>
401
          for (j = 0; j < B_nrows; j++){</pre>
402
            int Ai = matrix_getelem(A, i, 0);
403
            int Bj = matrix_getelem(B, j, 0);
404
            for (v = 0; v < cval; v++){</pre>
405
              for (w = 0; w < dval; w++){}
406
                 matrix_setelem(R, matrix_getelem(M, Ai+v, Bj+w), i*cval+v,
407
                      j*dval+w);
              }
408
            }
409
          }
410
        }
411
        return R;
413
414
415
    struct matrix *matrix_insert(struct matrix *M, struct matrix *N, struct
416
         matrix *A, struct matrix *B, struct matrix *C, struct matrix *D)
417
        //Syntax is like M[A,B,C,D] = N;
418
        GrB_Index A_nrows, A_ncols, B_nrows, B_ncols, C_nrows, C_ncols,
419
            D_nrows, D_ncols, N_nrows, N_ncols;
        int i, j, v, w;
420
421
        // verify that A, B, C, D are all integer matrices??
422
        //veryify that A, B are column vectors and that C, D are 1x1
424
425
        GrB_size(A->mat, &A_nrows, &A_ncols);
426
        GrB_size(B->mat, &B_nrows, &B_ncols);
427
        GrB_size(C->mat, &C_nrows, &C_ncols);
428
        GrB_size(D->mat, &D_nrows, &D_ncols);
429
        GrB_size(N->mat, &N_nrows, &N_ncols);
430
431
        if (A_ncols != 1 || B_ncols != 1 || C_ncols != 1 || C_nrows != 1 ||
432
            D_nrows != 1 || D_ncols != 1)
            die("matrix_extract bad dimensions");
433
434
```

```
int cval = matrix_getelem(C, 0, 0);
435
        int dval = matrix_getelem(D, 0, 0);
436
437
        if ((N_nrows != cval) | (N_ncols != dval))
438
            die("matrix_extract size mismatch");
440
        for (i = 0; i < A_nrows; i++){</pre>
441
          for (j = 0; j < B_nrows; j++){</pre>
442
            int Ai = matrix_getelem(A, i, 0);
443
            int Bj = matrix_getelem(B, j, 0);
444
            for (v = 0; v < cval; v++){</pre>
              for (w = 0; w < dval; w++){</pre>
446
                  matrix_setelem(M, matrix_getelem(N, v, w), Ai+v, Bj+w);
447
448
            }
449
          }
450
        }
451
452
453
        return N;
    }
454
455
    struct matrix *matrix_size(struct matrix *A)
456
457
        struct matrix *S;
458
        GrB_Index nrows, ncols;
459
        GrB_size(A->mat, &nrows, &ncols);
460
461
        S = matrix_create(2,1);
462
463
        matrix_setelem(S, nrows, 0, 0);
464
        matrix_setelem(S, ncols, 1, 0);
        return S;
467
    }
468
469
    struct matrix *matrix_reduce(struct matrix *A, int mult_flag)
470
471
472
        struct matrix *R;
        GrB_Index nrows;
473
        GrB_size(A->mat, &nrows, NULL);
474
475
        GrB_Vector v;
476
        GrB_Vector_new(&v, GrB_INT32, nrows) ;
477
478
479
        GrB_Monoid op;
480
        if(mult_flag){
481
          GrB_BinaryOp mult;
482
          GxB_Semiring_multiply(&mult, curr_ring->ring);
483
          // TODO: Find a better way of doing mutliplicative identity
484
```

```
GrB_Monoid_new_INT32(&op, mult, 0);
485
        } else {
486
          GxB_Semiring_add(&op, curr_ring->ring);
487
488
        GrB_Matrix_reduce_Monoid(v, GrB_NULL, GrB_NULL, op, A->mat,
490
             GrB_NULL);
491
        R = matrix_create(nrows,1);
492
        GrB_Col_assign(R->mat, GrB_NULL, GrB_NULL, v, GrB_ALL, nrows, 0,
493
             GrB_NULL);
494
        return R;
495
496
497
    struct matrix *matrix_transpose(struct matrix *A)
498
499
        struct matrix *T;
500
501
        GrB_Index nrows, ncols;
        GrB_size(A->mat, &nrows, &ncols);
502
503
        T = matrix_create(ncols, nrows);
504
        GrB_transpose(T->mat, GrB_NULL, GrB_NULL, A->mat, GrB_NULL);
505
        return T;
507
    }
508
509
    struct matrix *matrix_negate(struct matrix *A)
510
511
        struct matrix *R;
512
        GrB_Index nrows, ncols;
513
514
        int i,j;
515
        GrB_size(A->mat, &nrows, &ncols);
516
        R = matrix_create(nrows, ncols);
517
518
        for (i = 0; i < nrows; i++) {</pre>
519
            for (j = 0; j < ncols; j++) {</pre>
              matrix\_setelem(R, matrix\_getelem(A, i, j) == 0, i, j);
521
        }
524
        return R;
525
    }
526
527
528
    struct matrix *matrix_conv(struct matrix *A, struct matrix *B)
529
530
        struct matrix *C;
        struct matrix *E;
531
        struct matrix *f;
532
```

```
struct matrix *g;
        struct matrix *h;
534
        GrB_Index A_nrows, A_ncols, B_nrows, B_ncols, C_nrows, C_ncols;
536
        int i, j;
        GrB_size(A->mat, &A_nrows, &A_ncols);
        GrB_size(B->mat, &B_nrows, &B_ncols);
540
        if (A_nrows < B_nrows || A_ncols < B_ncols)</pre>
541
            die("matrix_conv bad dimensions");
542
        // lots of memory leaked here!
        GrB_Index *row_indices, *col_indices;
        if (!(row_indices = malloc(B_nrows * sizeof(int)))) die("malloc
            failed");
        if (!(col_indices = malloc(B_ncols * sizeof(int)))) die("malloc
548
            failed");
        C_nrows = A_nrows - B_nrows + 1;
        C_ncols = A_ncols - B_ncols + 1;
551
        C = matrix_create(C_nrows, C_ncols);
        E = matrix_create(B_nrows, B_ncols);
553
        f = matrix_create(B_nrows, 1);
        g = matrix_create(1, B_nrows);
        h = matrix_create(1, 1);
        for (i = 0; i < C_nrows; i++) {</pre>
            for (j = 0; j < C_ncols; j++) {</pre>
              int k;
560
              for (k = 0; k < B_nrows; k++) row_indices[k] = i+k;</pre>
              for (k = 0; k < B_ncols; k++) col_indices[k] = j+k;</pre>
              GrB_extract(E->mat, GrB_NULL, GrB_NULL, A->mat, row_indices,
                  B_nrows, col_indices, B_ncols, GrB_NULL);
              E = matrix_elmul(E, B);
564
              f = matrix_reduce(E, 0);
565
              g = matrix_transpose(f);
              h = matrix_reduce(g, 0);
              matrix_setelem(C, matrix_getelem(h, 0, 0), i, j);
568
        }
571
        return C;
572
    }
573
574
575
    struct matrix *matrix_concat(struct matrix *A, struct matrix *B)
576
        struct matrix *C;
        GrB_Info info;
578
        GrB_Index A_nrows, A_ncols, B_nrows, B_ncols;
579
```

```
int i;
580
581
        GrB_size(A->mat, &A_nrows, &A_ncols);
582
        GrB_size(B->mat, &B_nrows, &B_ncols);
583
        if (A_ncols != B_ncols)
            die("matrix_concat bad dimensions");
586
587
        GrB_Index *A_row_indices, *B_row_indices, *col_indices;
588
        if (!(A_row_indices = malloc(A_nrows * sizeof(int)))) die("malloc
589
             failed");
        if (!(B_row_indices = malloc(B_nrows * sizeof(int)))) die("malloc
             failed");
        if (!(col_indices = malloc(A_ncols * sizeof(int)))) die("malloc
591
             failed");
        for (i = 0; i < A_nrows; i++) A_row_indices[i] = i;</pre>
593
        for (i = A_nrows; i < A_nrows + B_nrows; i++) B_row_indices[i -</pre>
594
             A_nrows] = i;
        for (i = 0; i < A_ncols; i++) col_indices[i] = i;</pre>
595
596
        C = matrix_create(A_nrows + B_nrows, A_ncols);
597
        info = GrB_assign(C->mat,
                          GrB_NULL,
                          GrB_NULL,
601
                          A->mat,
602
                          A_row_indices,
603
                          A_nrows,
604
                          GrB_ALL,
605
                          A_ncols,
606
                          GrB_NULL);
608
        info = GrB_assign(C->mat,
609
                          GrB_NULL,
610
                          GrB_NULL,
611
                          B->mat,
612
                          B_row_indices,
613
                          B_nrows,
614
                          GrB_ALL,
615
                          B_ncols,
616
                          GrB_NULL);
617
618
        if (!GrB_ok(info))
619
620
            GrB_die("GrB_Matrix_eWiseAdd_Semiring", A->mat);
621
622
        return C;
    }
623
624
    // Comparison operators
625
```

```
626
    struct matrix *matrix_elcompare(struct matrix *A, struct matrix *B, int
627
         op_index)
628
        struct matrix *C;
629
        int i, j;
630
        int a, b, comp_val;
631
632
        GrB_Index nrows, ncols, nrowsB, ncolsB;
633
        GrB_size(A->mat, &nrows, &ncols);
634
        GrB_size(B->mat, &nrowsB, &ncolsB);
637
        printf("dims of A: %d %d\n", (int) nrows, (int) ncols);
638
        matrix_print(matrix_tostring(A));
639
        printf("dims of B: %d %d\n", (int) nrowsB, (int) ncolsB);
640
        matrix_print(matrix_tostring(B));
641
642
        C = matrix_create(1, 1);
644
645
        if (nrows != nrowsB || ncols != ncolsB)
646
            die("Can't compare two matrices that are different dimensions");
        for (i = 0; i < nrows; i++) {</pre>
            for (j = 0; j < ncols; j++) {</pre>
                a = matrix_getelem(A, i, j);
651
                b = matrix_getelem(B, i, j);
652
                switch (op_index) {
653
                    case 0: comp_val = a == b; break;
654
                    case 1: comp_val = a != b; break;
655
                    case 2: comp_val = a <= b; break;</pre>
                    case 3: comp_val = a < b; break;</pre>
657
                    case 4: comp_val = a >= b; break;
658
                   case 5: comp_val = a > b; break;
659
                   default: die("Unknown comparison operator");
660
                }
661
                if (!comp_val) return C;
            }
663
        }
664
        matrix_setelem(C, 1, 0, 0);
665
        return C;
666
    }
667
668
    struct matrix *matrix_eq(struct matrix *A, struct matrix *B) { return
         matrix_elcompare(A, B, 0); }
    struct matrix *matrix_neq(struct matrix *A, struct matrix *B) { return
670
         matrix_elcompare(A, B, 1); }
    struct matrix *matrix_leq(struct matrix *A, struct matrix *B) { return
         matrix_elcompare(A, B, 2); }
```

```
struct matrix *matrix_less(struct matrix *A, struct matrix *B) { return
         matrix_elcompare(A, B, 3); }
    struct matrix *matrix_geq(struct matrix *A, struct matrix *B) { return
673
         matrix_elcompare(A, B, 4); }
    struct matrix *matrix_greater(struct matrix *A, struct matrix *B) {
         return matrix_elcompare(A, B, 5); }
675
    // "The truth value of an expr is equivalent to expr > 0" (Jake, 2021)
676
    int matrix_truthy(struct matrix *A)
678
        struct matrix *C;
679
        struct matrix *B;
680
        GrB_Index nrows, ncols;
681
        GrB_size(A->mat, &nrows, &ncols);
682
683
        B = matrix_create(nrows, ncols);
684
        C = matrix_greater(A, B);
685
686
        return matrix_getelem(C, 0, 0) > 0;
    }
688
689
    // end matrix_* functions //
690
691
    #ifdef RUN_TEST
    int main(int argc, char **argv){
693
        struct matrix *A, *B, *C;
694
695
        ring_push();
696
697
        A = matrix_create(2, 2);
698
        B = matrix_create(2, 2);
        // B = matrix_create(1, 1);
        matrix_setelem(A, 2, 0, 0);
701
        matrix_setelem(A, 2, 0, 1);
702
        matrix_setelem(A, 2, 1, 0);
703
        matrix_setelem(A, 2, 1, 1);
704
        matrix_setelem(B, 2, 0, 0);
705
        matrix_setelem(B, 2, 0, 1);
        matrix_setelem(B, 2, 1, 0);
707
        matrix_setelem(B, 2, 1, 1);
708
        matrix_print(matrix_tostring(A));
709
        matrix_print(matrix_tostring(B));
710
711
        C = matrix_mul(A, B);
712
713
        matrix_print(matrix_tostring(C));
714 }
715
    #endif
```

References

- [KG11] Jeremy Kepner and John Gilbert. Graph Theory in the Language of Linear Algebra. Society for Industrial and Applied Mathematics, 2011. ISBN: 978-0-89871-990-1. URL: https://www.google.com/books/edition/Graph_Algorithms_in_the_Language_of_Line/BnezR_ 6PnxMC.
- [Gil] John Gilbert. GraphBLAS: Graph Algorithms in the Language of Linear Algebra. URL: https://sites.cs.ucsb.edu/~gilbert/talks/Gilbert-27Jun2019.pdf.