

Deep Learning

Session 18

Introduction to Attention

Applied Data Science 2024/2025

Recap: RNNs

 $\hat{\boldsymbol{y}}^{(4)} = P(\boldsymbol{x}^{(5)}|\text{the students opened their})$

laptops

books



BRAGA

output distribution

$$\hat{y} = \text{softmax}(W_2 h^{(t)} + b_2)$$

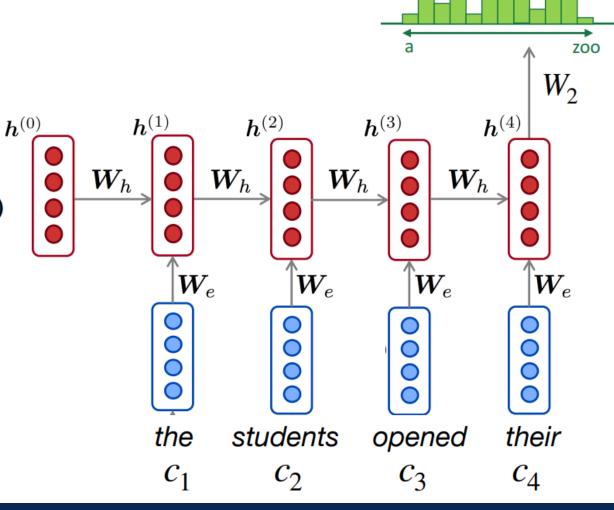
hidden states

$$h^{(t)} = f(W_h h^{(t-1)} + W_e c_t + b_1)$$

h⁽⁰⁾ is initial hidden state!

word embeddings

$$c_1, c_2, c_3, c_4$$



Recap: RNNs



laptops

 $= P(\mathbf{x}^{(5)}|\text{the students opened their})$

books

RNN Advantages:

Can process any length input

Model size doesn't increase for longer input

Computation for step t can (in theory) use information from

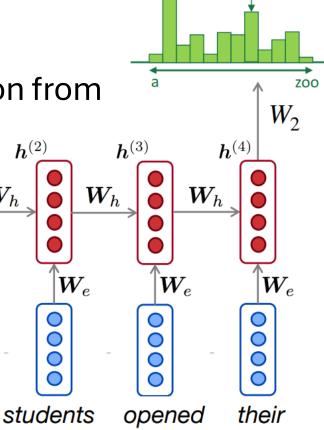
many steps back.

Weights are shared across timesteps

RNN Disadvantages:

Recurrent computation is slow

In practice, difficult to access information from many steps back.



 c_4

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 $oldsymbol{W}_h$

 $oldsymbol{W}_h$

the

 $oldsymbol{W}_e$

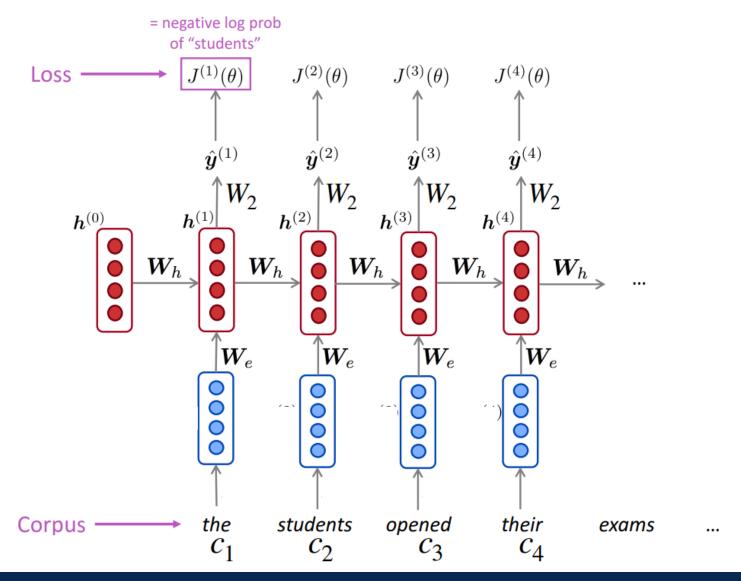


- ullet Get a **big corpus** of text which is a sequence of words $oldsymbol{x}^{(1)}, \dots, oldsymbol{x}^{(T)}$
- Fed it into the RNN. Compute the outpur distribution $\hat{\boldsymbol{y}}^{(t)}$ for **every** step t.
 - i.e. predict the probability distribution of every word given the words so far
- Loss funtion on step t is usualy cross-entropy between the predicted probability distribution $\hat{y}^{(t)}$, and the true next word $y^{(t)} = x^{(t+1)}$:

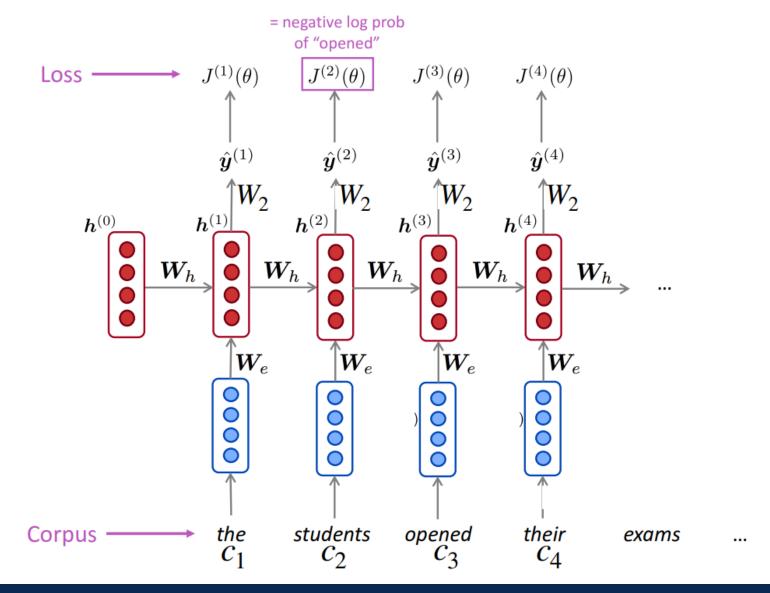
$$J^{(t)}(\theta) = CE(\mathbf{y}^{(t)}, \hat{\mathbf{y}}^{(t)}) = -\sum_{j=1}^{|V|} y_j^{(t)} \log \hat{y}_j^{(t)} \longrightarrow J(\theta) = \frac{1}{T} \sum_{t=1}^{T} J^{(t)}(\theta)$$

Average to get the **overall loss!**

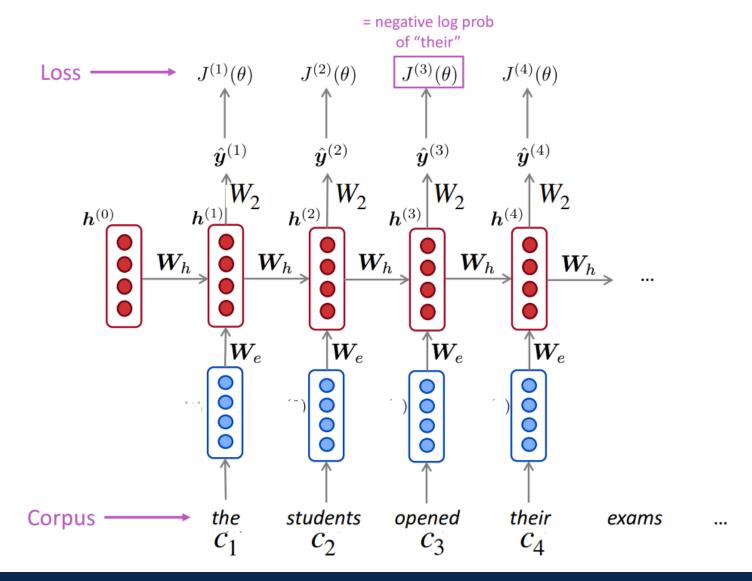




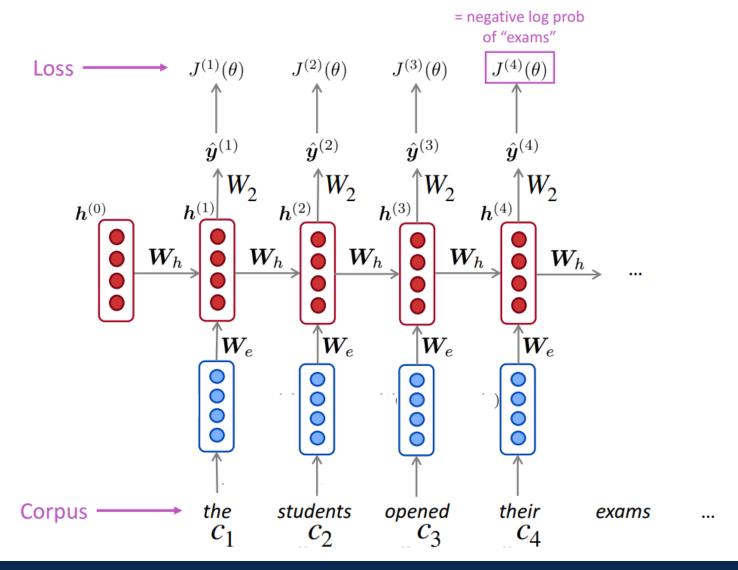




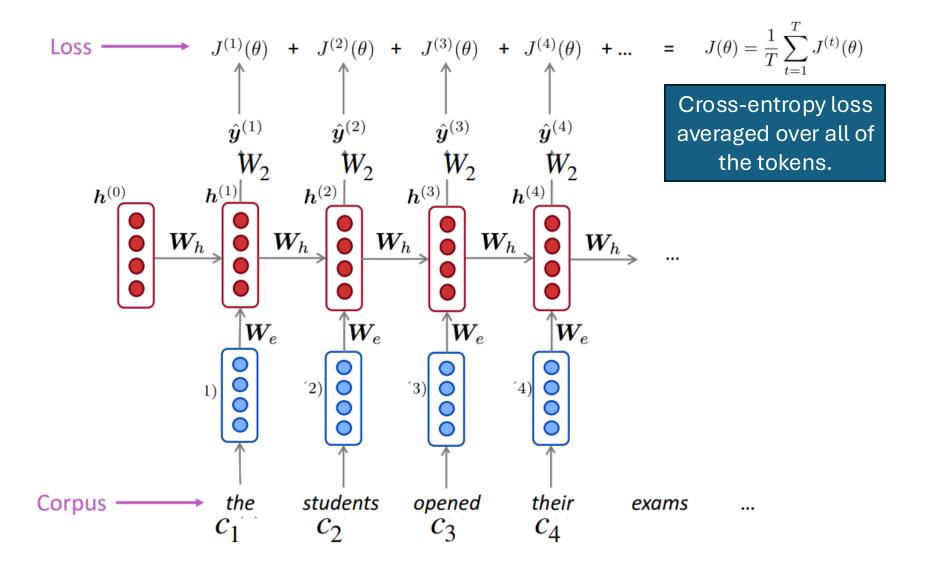




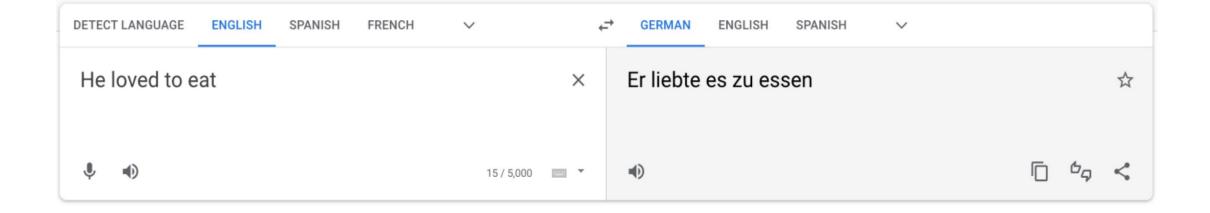




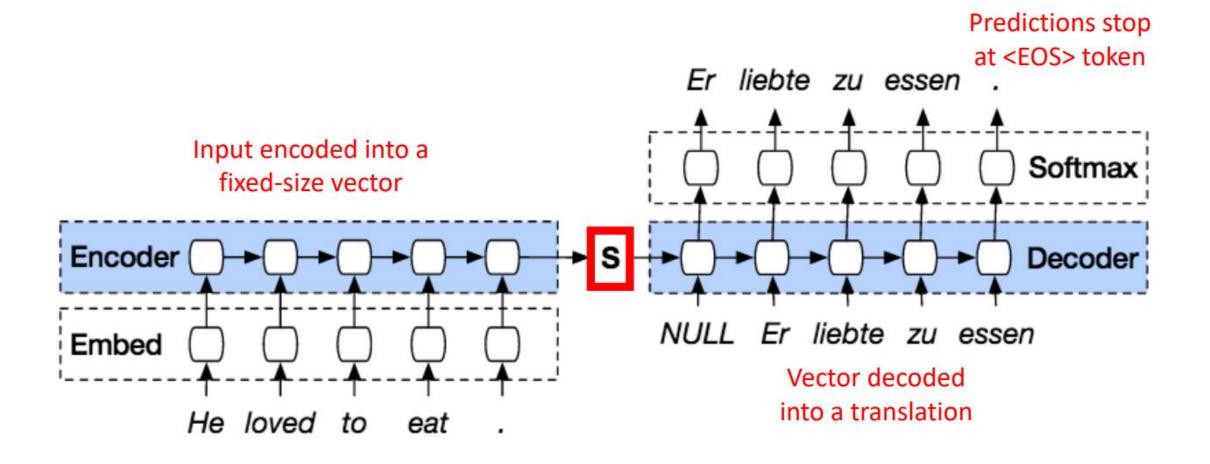




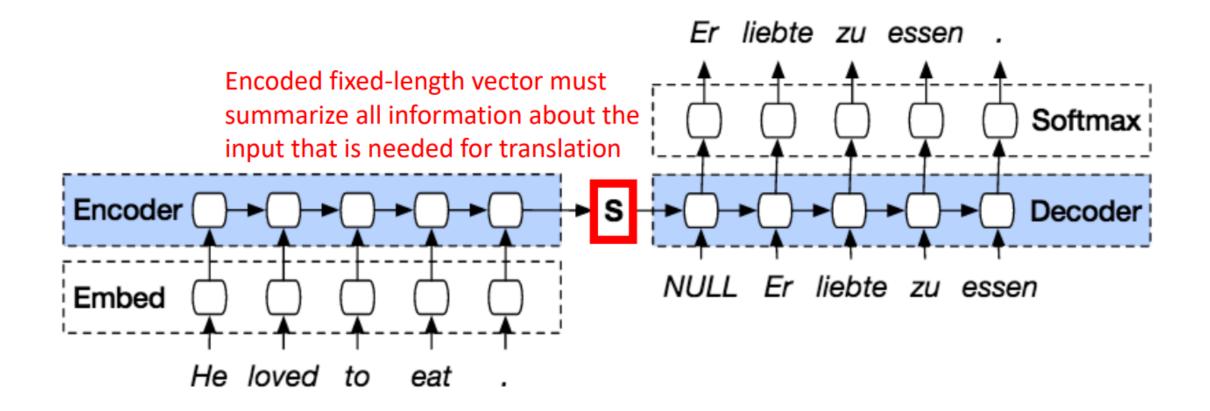




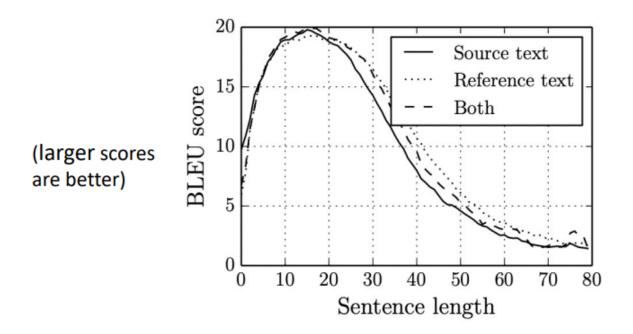


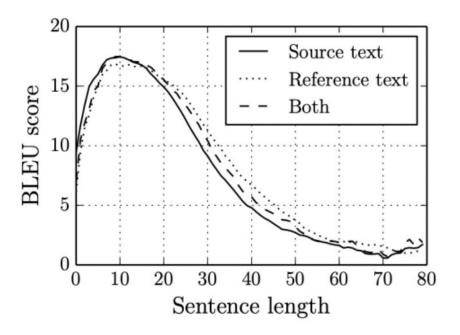






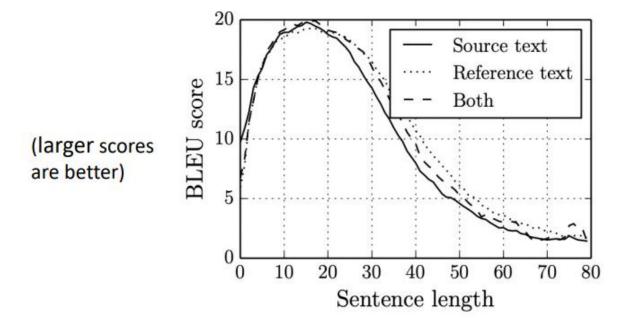


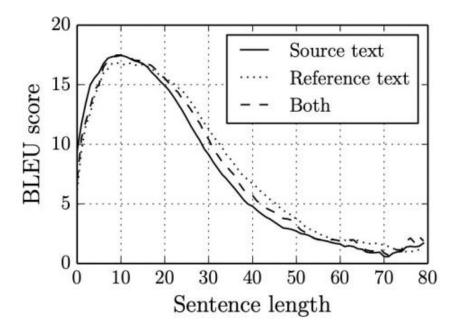




What performance trend is observed for inputs (source) and outputs (reference) as the number of words in each sentence grows?



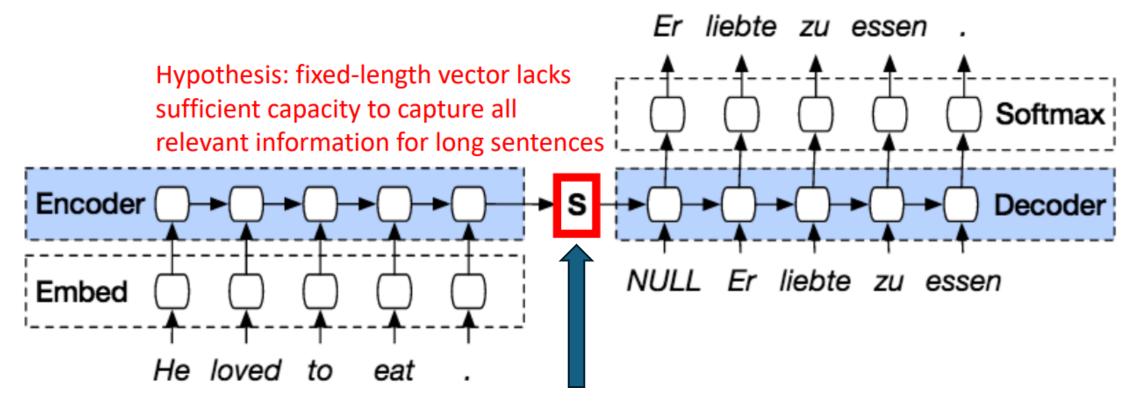




Performance drops for longer sentences!

Problem: Performance Drops as Sentence Length Grows

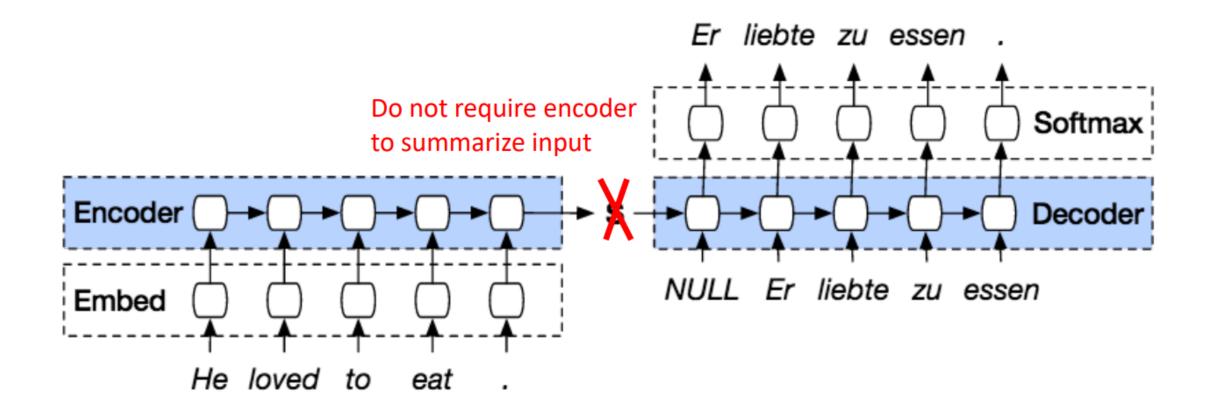




Bottleneck problem!

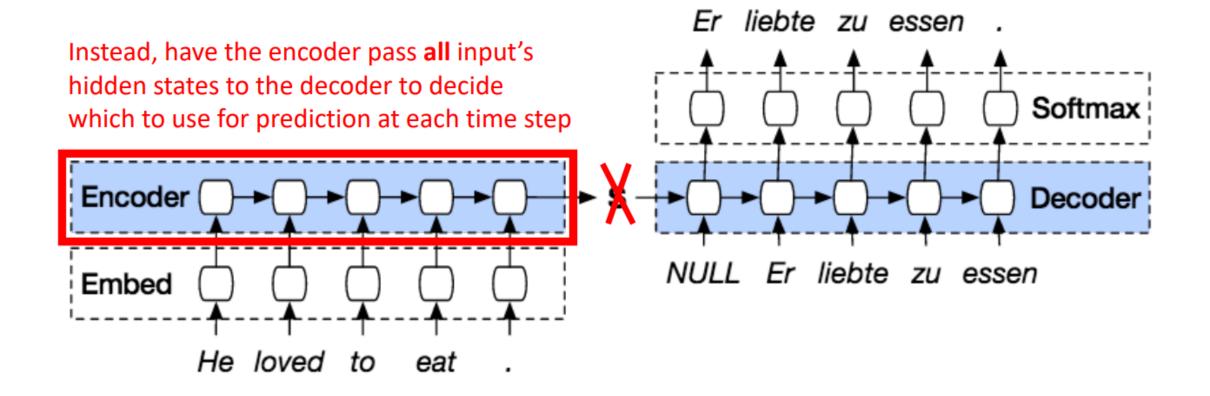
How to preserve Performance for Long Sequences?





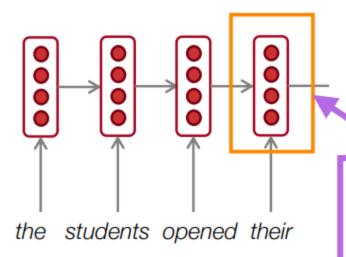
How to preserve Performance for Long Sequences?





Idea: What If We Use Multiple Vectors?

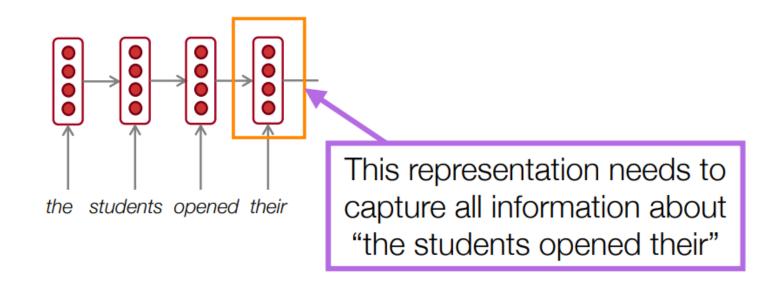




This representation needs to capture all information about "the students opened their"

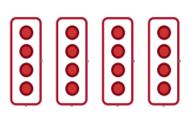
Idea: What If We Use Multiple Vectors?





Instead of this, let's try:

the students opened their =



(all 4 hidden states!)

The Solution: Attention



- Attention mechanisms (Bahdanau et al., 2015) allow language models to focus on a particular part of the observed context at each time step.
 - Originally developed for machine translation, and intuitively similar to word alignments between different languages

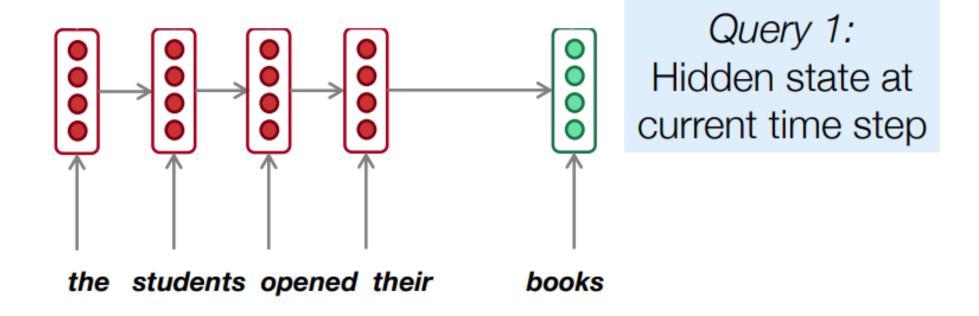
How does attention work?



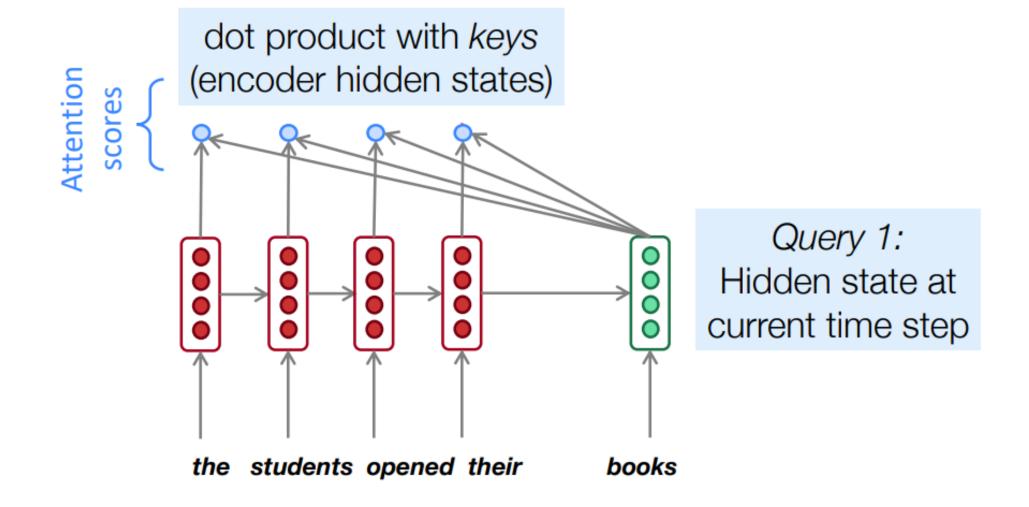
• In general, we have a single query vector and multiple key vectors. We want to score each query-key pair.

In a neural language model, what are the queries and keys?

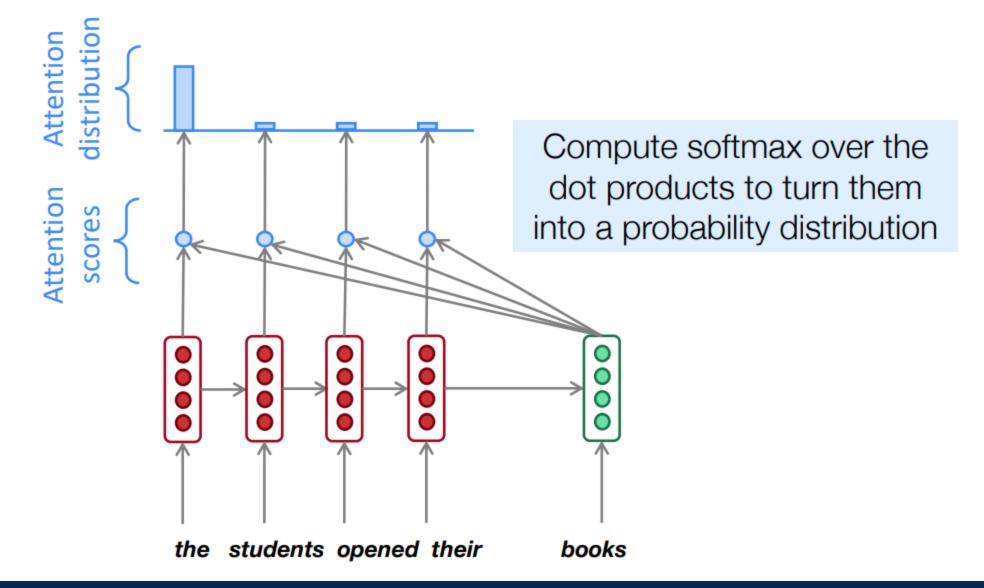




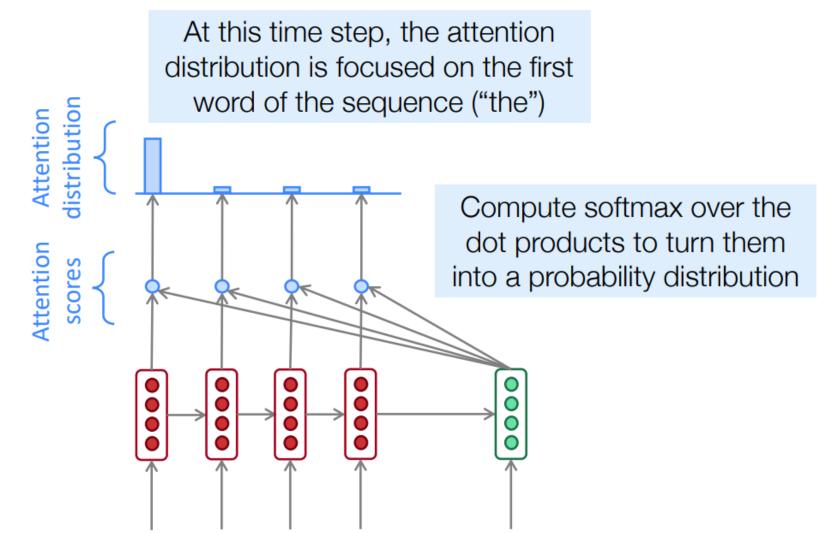












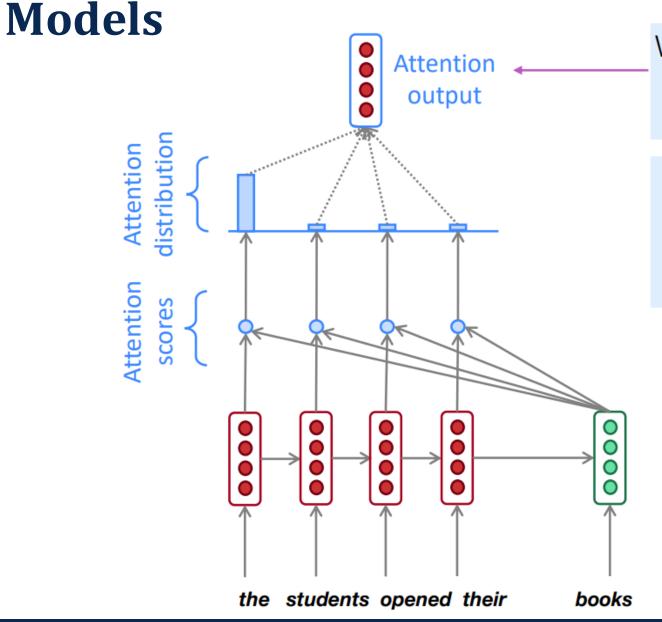
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books

students opened their



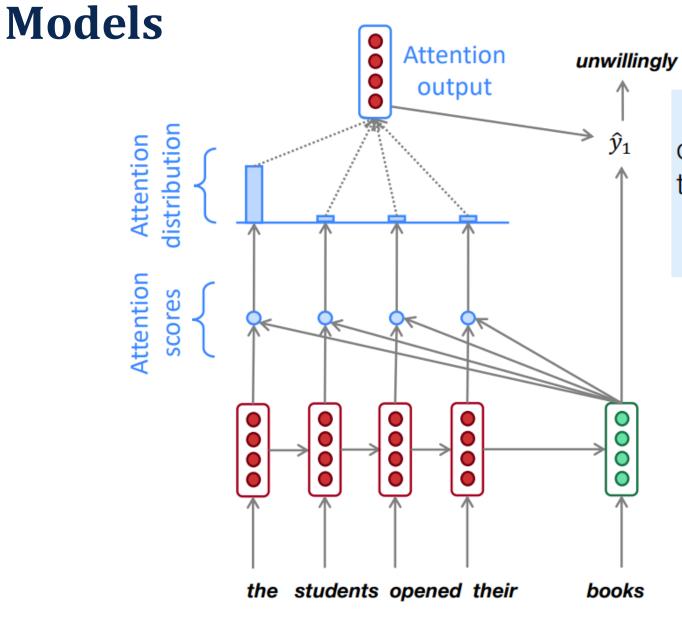
BRAGA



We use the attention distribution to compute a weighted average of the hidden states.

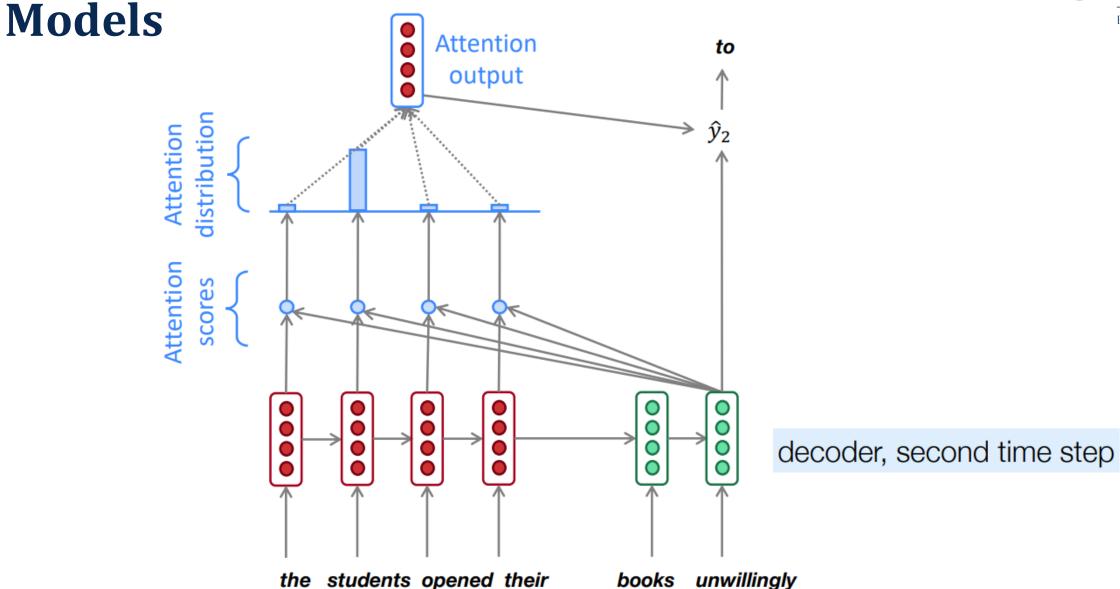
Intuitively, the resulting attention output contains information from hidden states that received high attention scores





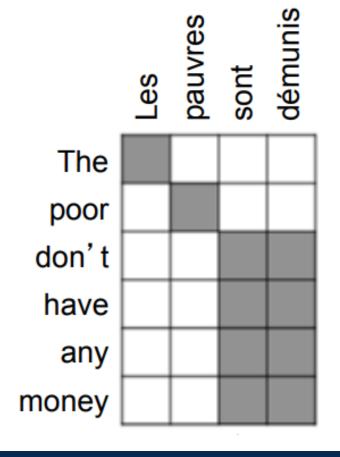
Concatenate (or otherwise compose) the attention output with the current hidden state, then pass through a softmax layer to predict the next word







- Attention solves the bottleneck problem
 - Attention allows decoder to look directly at source; bypass bottleneck
- Attention helps with vanishing gradient problem
 - Provides shortcut to faraway states
- Attention provides some interpretability
 - By inspecting attention distribution, we can see what the decoder was focusing on
 - We get an alignment for free!
 - This is cool because we never explicitly trained an alignment system
 - The network just learned alignment by itself



Many Variants of Attention



Original formulation:

$$a(\mathbf{q}, \mathbf{k}) = w_2^T \tanh(W_1[\mathbf{q}; \mathbf{k}])$$

• Bilinear product:

$$a(\mathbf{q}, \mathbf{k}) = \mathbf{q}^T W \mathbf{k}$$

Luong et al., 2015

• Dot product:

$$a(\mathbf{q}, \mathbf{k}) = \mathbf{q}^T \mathbf{k}$$

Luong et al., 2015

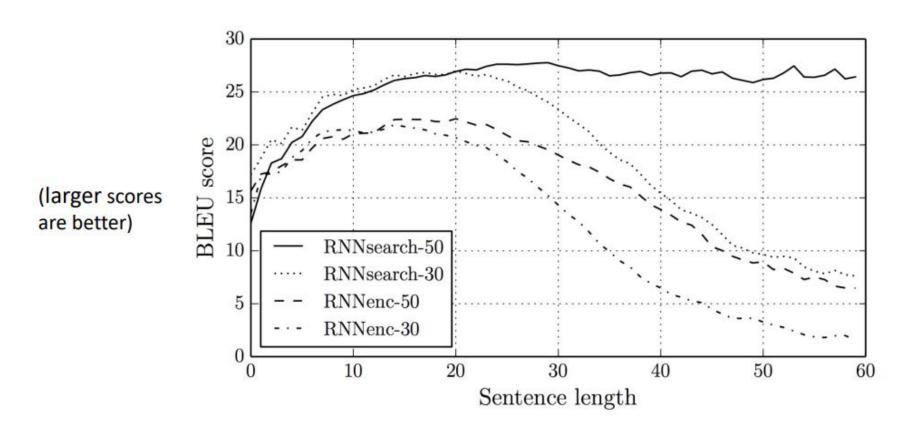
Scaled dot product:

$$a(\mathbf{q}, \mathbf{k}) = \frac{\mathbf{q}^T \mathbf{k}}{\sqrt{|\mathbf{k}|}}$$

Vaswani et al., 2017

Analysis of Attention Models

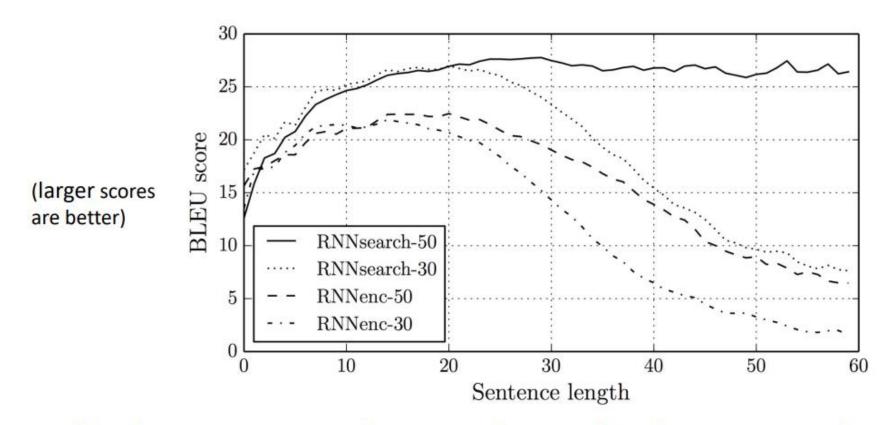




What performance trend is observed as the number of words in the input sentence grows?

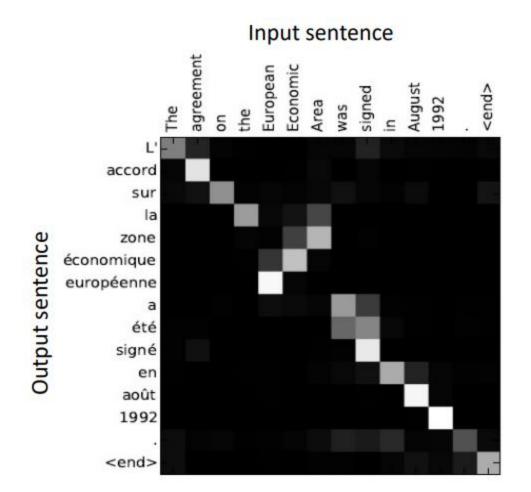
Analysis of Attention Models



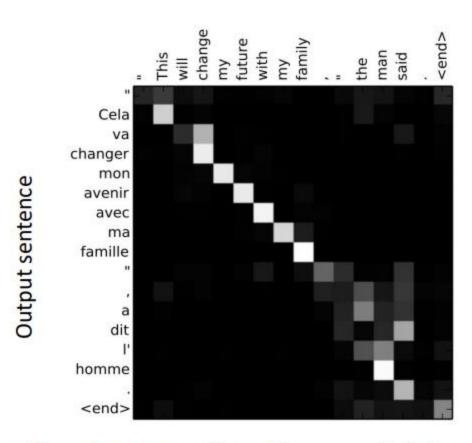


Performance no longer drops for longer sentences!



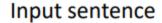


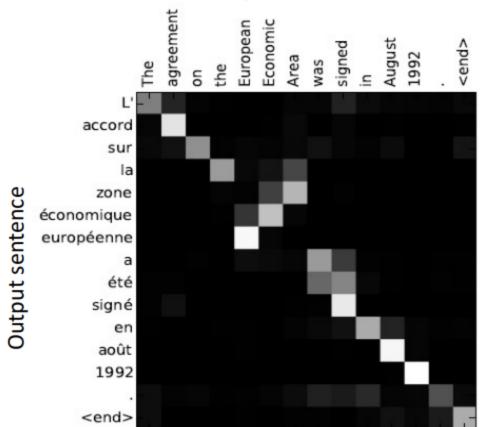
Input sentence



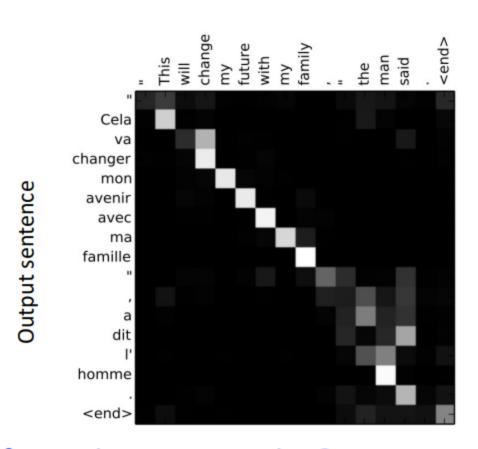
Values are 0 to 1, with whiter pixels indicating larger attention weights





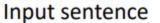


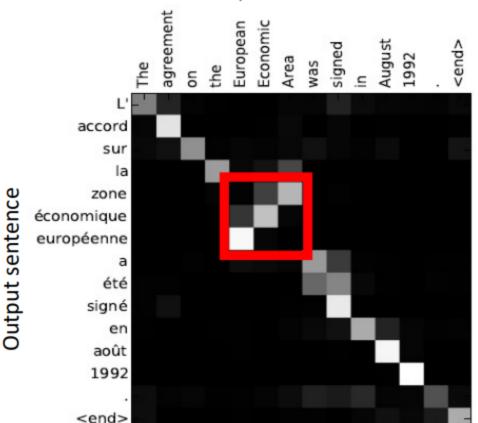
Input sentence



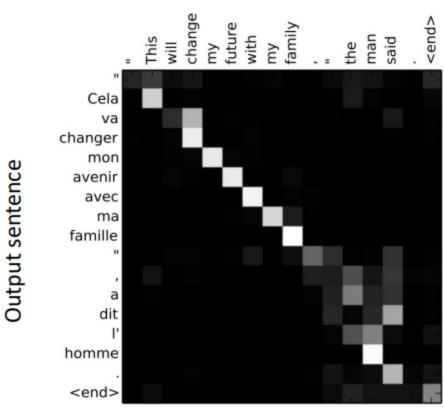
What insights can we glean from these examples?





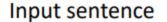


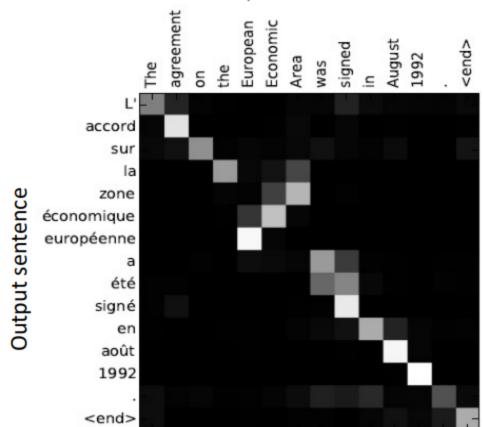
Input sentence



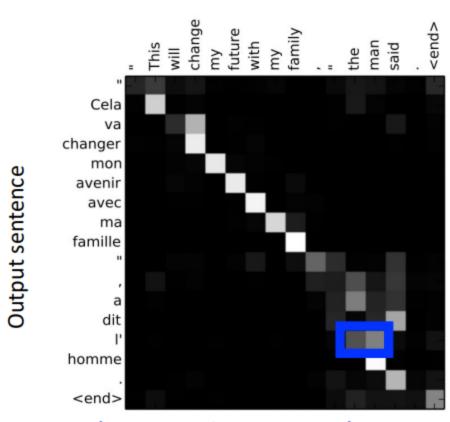
While a linear alignment between input and output sentences is common, there are exceptions (e.g., order of adjectives and nouns can differ)





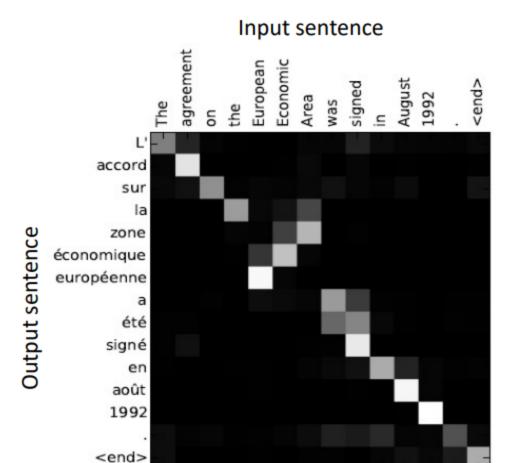


Input sentence

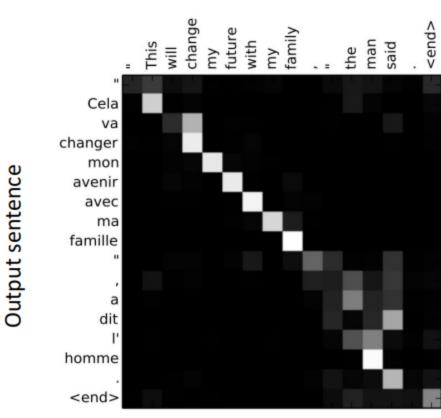


Output words are often informed by more than one input word; e.g., "man" indicates translation of "the" to I' instead of le, la, or les





Input sentence



It naturally handles different input and output lengths (e.g., 1 extra output word for both examples)

Exercises



• Let's implement a attention mechanisms with PyTorch.

• Follow the instructions on the notebook: "seq2seq_translation_exercises.ipynb".