

Search & Sort

Data Structures – Coding Course

Search

Linear search

```
int linearSearch(int arr[], int n, int key) {  
    for (int i = 0; i < n; i++)  
        if (arr[i] == key)  
            return i;  
    return -1;  
}
```

$O(n)$

Jump search

- Sorted structures

```
int jumpSearch(int arr[], int n, int key) {  
    int step = sqrt(n);  
    int prev = 0;  
    // Find the block  
    while (arr[min(step, n) - 1] < key) {  
        prev = step;  
        step += sqrt(n);  
        if (prev >= n)  
            return -1;  
    }  
    // Linear  
    for (int i = prev; i < min(step, n); i++) {  
        if (arr[i] == key)  
            return i;  
    }  
    return -1;  
}
```

$O(\sqrt{n})$

Binary search

- Sorted structures

```
int binarySearch(int arr[], int n, int key) {  
    int low = 0, high = n - 1;  
    while (low <= high) {  
        int mid = (low + high) / 2;  
        if (arr[mid] == key) return mid;  
        else if (arr[mid] < key) low = mid + 1;  
        else high = mid - 1;  
    }  
    return -1;}  
● ● ●
```

O(logn)

Sort

Bubble sort

```
void bubbleSort(int arr[], int n) {  
    for (int i = 0; i < n - 1; i++)  
        for (int j = 0; j < n - i - 1; j++)  
            if (arr[j] > arr[j + 1])  
                swap(arr[j], arr[j + 1]);  
}
```

$O(n^2)$

Selection sort

```
void selectionSort(int arr[], int n) {  
    for (int i = 0; i < n - 1; i++) {  
        int minIndex = i;  
        for (int j = i + 1; j < n; j++)  
            if (arr[j] < arr[minIndex])  
                minIndex = j;  
        swap(arr[i], arr[minIndex]);  
    }  
}
```

$O(n^2)$

Merge sort

- Usually recursively
- Devide & conquer

```
void merge(int arr[], int l, int m, int r) {  
    int n1 = m - l + 1, n2 = r - m;  
    int L[100], R[100];  
    for (int i = 0; i < n1; i++) L[i] = arr[l  
+ i];  
    for (int j = 0; j < n2; j++) R[j] = arr[m  
+ 1 + j];  
    int i = 0, j = 0, k = l;  
    while (i < n1 && j < n2)  
        arr[k++] = (L[i] <= R[j]) ? L[i++] :  
R[j++];  
    while (i < n1) arr[k++] = L[i++];  
    while (j < n2) arr[k++] = R[j++];}  
void mergeSort(int arr[], int l, int r) {  
    if (l < r) {  
        int m = (l + r) / 2;  
        mergeSort(arr, l, m);  
        mergeSort(arr, m + 1, r);  
        merge(arr, l, m, r);  
    }  
}
```

$O(n \log n)$

2	8	5	3	9	4	1	7
---	---	---	---	---	---	---	---

2	8	5	3
---	---	---	---

9	4	1	7
---	---	---	---

2	8

5	3

9	4

1	7

2

8

5

3

9

4

1

7

2

8

5

3

9

4

1

7

2 8

3 5

4 9

1 7

2 3 5 8

1 4 7 9

1 2 3 4 5 7 8 9

Quick sort

```
int partition(int arr[], int low, int high) {  
    int pivot = arr[high], i = low - 1;  
    for (int j = low; j < high; j++) {  
        if (arr[j] < pivot) {  
            i++;  
            swap(arr[i], arr[j]);  
        }  
    }  
    swap(arr[i + 1], arr[high]);  
    return i + 1;  
}  
  
void quickSort(int arr[], int low, int high) {  
    if (low < high) {  
        int pi = partition(arr, low, high);  
        quickSort(arr, low, pi - 1);  
        quickSort(arr, pi + 1, high);  
    }  
}
```

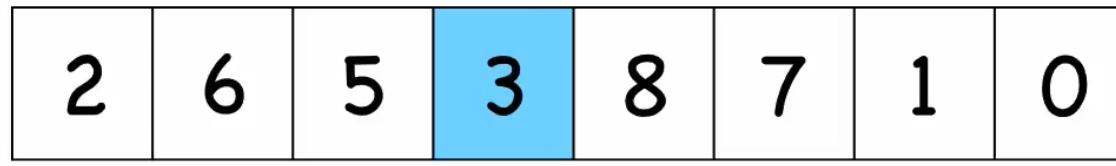
$O(n \log n)$

quick sort = pivot

1. Correct position in final, sorted array
2. Items to the left are smaller
3. Items to the right are larger

2	6	5	3	8	7	1	0
---	---	---	---	---	---	---	---

pivot



1. itemFromLeft that is larger than pivot
2. itemFromRight that is smaller than pivot

2	6	5	0	8	7	1	3
---	---	---	---	---	---	---	---

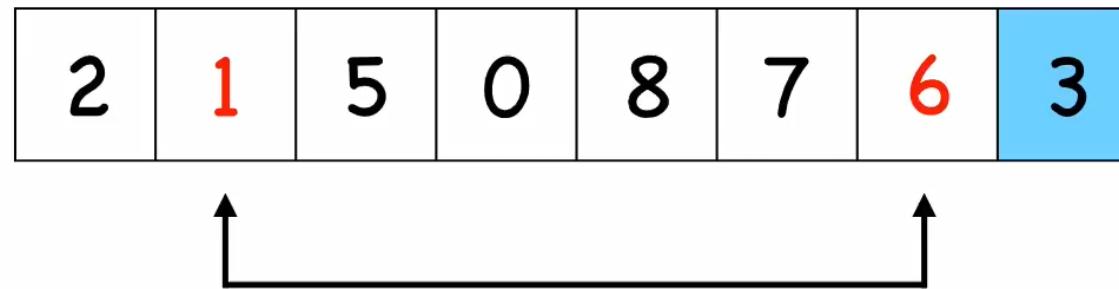


itemFromLeft



itemFromRight

1. itemFromLeft that is larger than pivot
2. itemFromRight that is smaller than pivot



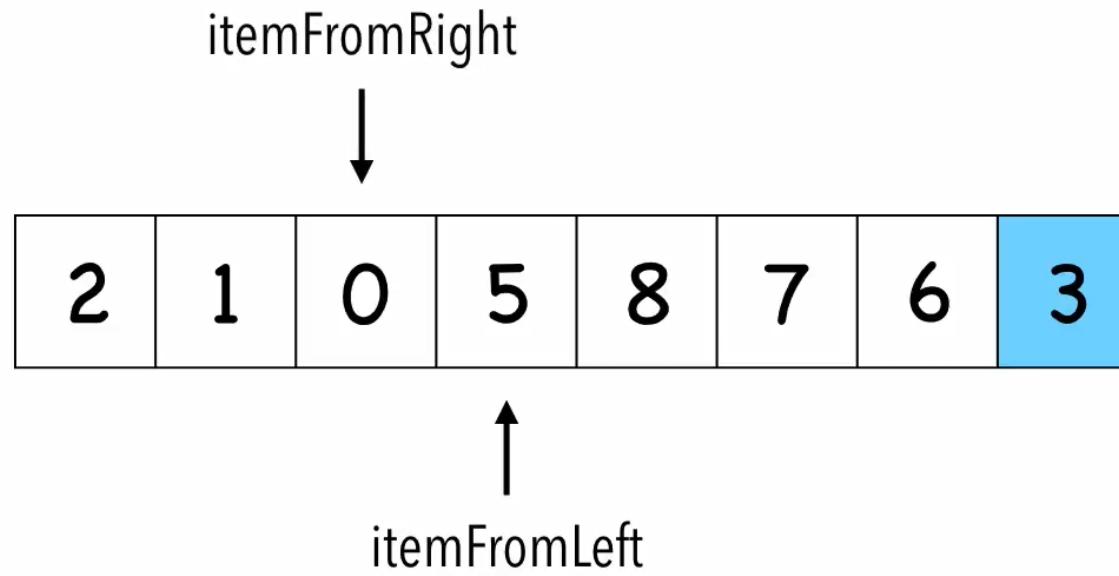
itemFromRight



2	1	5	0	8	7	6	3
---	---	---	---	---	---	---	---



itemFromLeft



Stop when index of itemFromLeft > index of itemFromRight

itemFromRight



2	1	0	5	8	7	6	3
---	---	---	---	---	---	---	---



itemFromLeft

Swap itemFromLeft and pivot

1. Correct position in final, sorted array
2. Items to the left are smaller
3. Items to the right are larger

2	1	0	3	8	7	6	5
---	---	---	---	---	---	---	---

8	7	6	5
---	---	---	---

pivot

2	1	0	3	6	5	7	8
---	---	---	---	---	---	---	---

How to choose the pivot?

median-of-three

2	6	5	3	8	7	1	0	4
---	---	---	---	---	---	---	---	---

2	6	5	3	4	7	1	0	8
---	---	---	---	---	---	---	---	---

pivot

C++ Search built-in methods

Method	Function	How it works	Time Complexity
std::find()	find(begin, end, key)	Linear search	$O(n)$
std::binary_search()	binary_search(begin, end, key)	Binary search	$O(\log n)$

C++ Sort built-in methods

Method	Function	How it works	Time Complexity
<code>std::sort()</code>	<code>sort(begin, end)</code>	Mix	$O(n \log n)$