

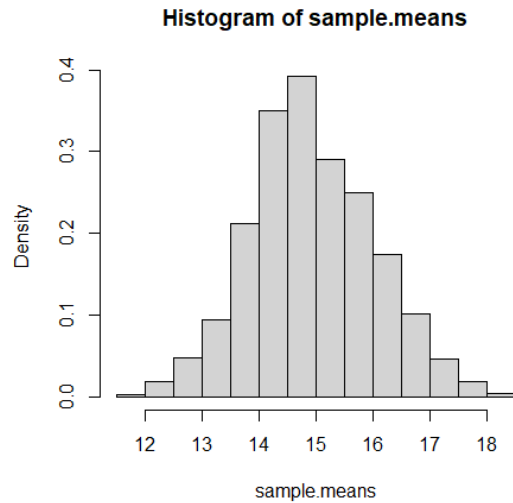
Math 341 Homework 7

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Problem 3

Problem 8



a)

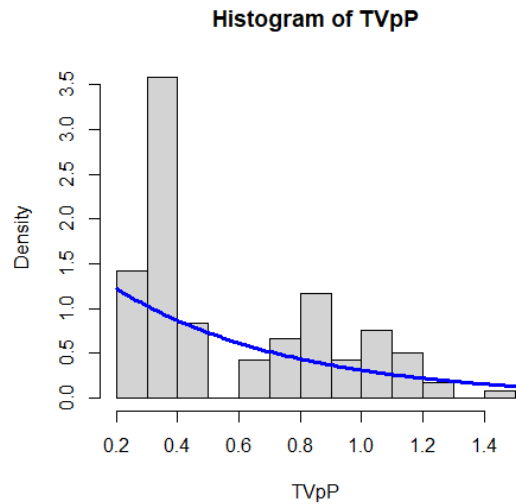
b) Yes, the sample means appear to be normally distributed.

c) For $X \sim \text{Exp}(15)$, it is known that $\mu = 15$ and $\sigma^2 = 225$. By the CLT, this implies that \bar{X} is approximately normally distributed with mean 15 and variance $225/n$, where $n = 200$ in this case. Calculate `mean(sample.means)` and `var(sample.means)` and report if these values are close to the theoretical values given by the CLT.

<code>mean(sample.means)</code>	14.93516
<code>var(sample.means)</code>	1.162514

Problem 9

Hogwarts Legacy Pog



a)

The exponential distribution assumption does not fit the data very well, though it could be argued that in terms of decay, the PDF does seem to exponentially decay, albeit not very smoothly. Given our options from class (exponential, normal, and constant), the best option would indeed be exponential.

b) Use the CLT.

$$\begin{aligned}
 P(0.55 \leq \bar{x} \leq 0.65) &= \\
 &= P\left(\frac{0.55 - \mu}{\sigma/\sqrt{n}} \leq \frac{\bar{x} - \mu}{\sigma/\sqrt{n}} \leq \frac{0.65 - \mu}{\sigma/\sqrt{n}}\right)
 \end{aligned}$$

$$n = 100 \text{ ('Next 100 TVpP')}$$

$$\mu = 0.58 \text{ (Given in R code)}$$

$$\sigma = 0.58$$

$$\begin{aligned}
 X &\sim \text{Exp}(\theta), \theta = 0.58 \\
 (\text{CLT}) &\approx P\left(\frac{0.55 - 0.58}{0.58/\sqrt{100}} \leq Z \leq \frac{0.65 - 0.58}{0.58/\sqrt{100}}\right) \\
 &\approx P(-0.005172414 \leq Z \leq 0.01206897) \\
 &\approx 0.0068782
 \end{aligned}$$

c) The simulated probability is 0.8351 (compared to the actual probability being ≈ 0.0068782).