## Math 341 Homework 8

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## Problem 7

## Problem 13

(a) Binomial Distribution with n=100 and p=0.05 (success being a CI does not contain the mean  $\mu$ ).

(b)

$$\begin{split} P(3 \leq X < 8) \\ &= P(X \leq 7) - P(X < 3) \\ &= P(X \leq 7) - P(X \leq 2) \\ &\approx 0.872039 - 0.1182629 \\ &\approx 0.7537765 \end{split}$$

(c)

$$Poisson \sim Bionmial$$
  
 $Y \sim Poisson(np)$   
 $\sim Poisson(5)$ 

$$\begin{split} P(3 \le Y < 8) &= P(Y \le 7) - P(Y < 3) \\ &= P(Y \le 7) - P(Y \le 2) \\ &\approx 0.866628 - 0.124652 \\ &\approx 0.7419763 \end{split}$$

(d) The poisson's approximation is a good approximation for the binomial distribution when n is large and p is small, and the two probabilities reflect this.