

Q02

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## Practical considerations when measuring correlation functions

Previous two weeks: Correlation functions

Experimentally remarkable:

It is possible to make detectors that are sensitive at the single-photon level (Hadfield 2009)

- Photo-multiplication tubes
- Avalanche photo diodes
- Super-conducting nanowire SPD
- Transition-edge sensors

Efficiency up to ~90% (InSb since 2011),  
but typically 10-50%

But: Dark counts, dead time

No (or limited) number resolution (link: efficiency)

So under what conditions can we really measure, e.g., quantum correlation functions of order 2?

$$\frac{\langle a^\dagger a^\dagger a a \rangle}{\langle a^\dagger a \rangle^2} = 1 - \frac{1}{n} \sim \begin{array}{l} \text{probability to simultaneously} \\ \text{have two photons} \end{array}$$

In experiment: split up modes.

$$\frac{D}{D + \eta} = \frac{P_{11}}{P_1 P_2} \quad \begin{array}{l} \text{probabilities per detection} \\ \text{window} \end{array}$$

Good approximation if  $P_x \ll 1$  (avoid saturation)  
 $P_x \gg P_{\text{dark}}$  (negligible dark counts)

Note: A more realistic detection operator (Makhni)

$$\hat{D} = \hat{I} - (1 - P_{\text{det}})(1 - \eta)^n : 1 \text{ minus probability of having neither photon nor dark count}$$

Not also: Normalized correlation functions factor out the loss of photons (conditional measurements, post-selection)

### 13 Quantum Light Sources

Light with properties that cannot be explained by classical theory (exception: shot noise)

Examples (single-mode)

- Fock states ( $g^{(1)} < 1$  non-classical)
- Squeezed states (continuous variables, not treated)

Examples (multi-mode)

- Entangled states (polarization, photon number, energy, orbital angular momentum...)

### 1B.1 Single-photon sources

Requires single emitter. Possibilities:

- single molecule
- single atom
- NV-center or similar
- Quantum dots

Parameters:

- Yield (emitted photons per request)
- Collection efficiency
- Indistinguishability (photon and emitters)

Slides ...

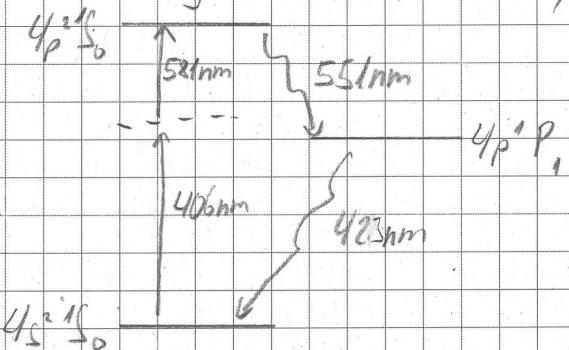
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### 13.2 Photon-Pair sources

It is difficult to entangle two single photons.

⇒ easier to generate an entangled pair

Creating photon pairs by cascade decay (Aspect 1981)

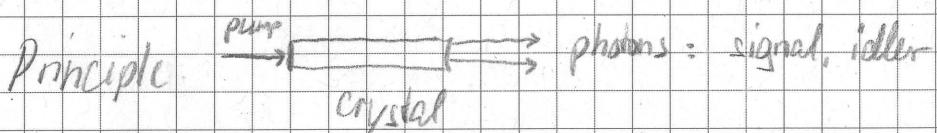


Atom decays back to ground state by emitting two photons.

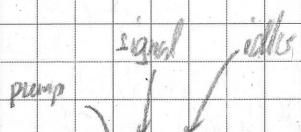
Entangled in polarization!

Calcium atoms

Photon-pair sources based on non-linear materials



Simple model:



$$\text{Interaction Hamiltonian: } \mathcal{H} = \hbar \chi (a b c^\dagger + a^\dagger b c)$$

Hermitian!

Cannot be solved analytically (as far as I know).

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Non-depleted (classical) pump approximation:

Assume pump in coherent state  $|\alpha\rangle$  with  $\alpha \gg 1$

$$\Rightarrow a|\alpha\rangle = \alpha|\alpha\rangle \text{ and } a^{\dagger}|\alpha\rangle \approx \alpha^*|\alpha\rangle$$

$$\Rightarrow H = \hbar\omega (a^{\dagger}b^{\dagger}c + \alpha^*bc)$$

We want to know what happens to modes b and c,  
when they are initially in vacuum.