## Assignment 3 - Shading SIGB Spring 2014

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## **Appendix**

https://github.com/MartinFaartoft/sigb

## Assignment Cube.py

```
Created on March 20, 2014
  @author: Diako Mardanbegi (dima@itu.dk)
  from numpy import *
7 import numpy as np
  from pylab import *
9 from scipy import linalg
  import cv2
11 import cv2.cv as cv
  from SIGBTools import *
13 import math
15 def DrawLines(img, points):
       for i in range(1, len(points[0])):
17
            x1 = points[0, i-1]
            y1 = points[1, i - 1]
            x2 \, = \, points \, [\, 0 \; , \quad i \, ]
19
            y2 = points[1, i]
            cv2.line(img, (int(x1), int(y1)), (int(x2), int(y2)),
21
      (255, 0, 0), 5)
      return img
  def findChessBoardCorners(image):
       pattern size = (9, 6)
      flag = cv2.CALIB CB FAST CHECK + cv2.cv.
      CV CALIB CB NORMALIZE IMAGE
      gray = cv2.cvtColor(image, cv2.COLOR BGR2GRAY)
      return cv2.findChessboardCorners(gray, pattern size, flags=
      flag)
  def update(img):
      image=copy(img)
31
      if Undistorting: #Use previous stored camera matrix and
      distortion coefficient to undistort the image
           ''' <004> Here Undistort the image'''
           image = cv2.undistort(image, cameraMatrix,
35
      distortion Coefficient)
       if (ProcessFrame):
37
           ''' <005> Here Find the Chess pattern in the current
           patternFound, corners = findChessBoardCorners(image)
           if patternFound = True:
```

```
''' <006> Here Define the cameraMatrix P=K[R|t] of
      the current frame ',',
43
                if debug:
                    P = findPFromHomography (corners)
                else:
                    P = createPCurrentFromObjectPose(corners)
                cam2 = Camera(P)
49
                if ShowText:
                     ''', <011> Here show the distance between the
      camera origin and the world origin in the image '''
                    cv2.putText(image, str("frame: " + str(frameNumber
      )), (20,10), cv2.FONT HERSHEY PLAIN,1, (255, 255, 255))#Draw
      the text
                    center = cam2.center()
                    distance = np.linalg.norm(center)
57
                    cv2.putText(image, str("distance: \%02d" \%
       {\tt distance)}\,,\;\; (20\,,\!30)\,, {\tt cv2}\,. {\tt FONT\_HERSHEY\_PLAIN}, 1\,,\;\; (255\,,\;\; 255\,,\;\; 255))
      #Draw the text
59
                ,,, <\!\!008\!\!> Here Draw the world coordinate system in
       the image,,,
                cam2 = Camera(P)
                coordinate_system = getCoordinateSystemChessPlane()
63
                transformed\_coordinate\_system \ =
       projectChessBoardPoints(cam2, coordinate system)
                drawCoordinateSystem (image,
65
      transformed coordinate system)
                if TextureMap:
67
                     ^{,\,,\,,} <012> calculate the normal vectors of the
      cube faces and draw these normal vectors on the center of
      each face ',
                    face\_normals = calculate\_face\_normals()
69
                    draw_face_normals(image, cam2, face_normals)
71
                     ,,, <\!013\!> Here Remove the hidden faces ,,
                    idx = back\_face\_culling(face\_normals, cam2)
73
                    faces to be drawn = np.array(Faces)[idx]
                    textures to be drawn = np.array(FaceTextures)[
75
      idx]
                    face \ corner\_normals = np.array (\, CornerNormals \,) \, [
      idx]
                     ,,, <\!010\!> Here Do he texture mapping and draw
      the texture on the faces of the cube,
                    for i in range(len(faces_to_be_drawn)):
                         face = faces\_to\_be\_drawn[i]
79
                         translate\_to = \begin{bmatrix} 8 & 6 & -1 \end{bmatrix}
                         f = copy(face)
81
```

```
f[0,:] = f[0,:] + translate\_to[0]
                        f[1,:] = f[1,:] + translate_to[1]
83
                        f[2,:] = f[2,:] + translate_to[2]
                        texture = textures_to_be_drawn[i]
                        corner_normals = face_corner_normals[i]
                        image = textureFace(image, f, cam2, texture)
                        image = ShadeFace(image, f, corner_normals,
89
      cam2)
               if ProjectPattern:
91
                    ''' <007> Here Test the camera matrix of the
       current view by projecting the pattern points '''
                    cam2 = Camera(P)
93
                   X = projectChessBoardPoints(cam2,
       points_from_chess_board_plane)
95
                    for p in X:
                        C = int(p[0]), int(p[1])
97
                        cv2.circle(image,C, 2,(255,0,255),4)
99
               if WireFrame:
                    ,,, <\!009\!> Here Project the box into the current
       camera image and draw the box edges '''
                    cam2 = Camera(P)
103
                    if (Teapot):
                        teapot = parse_teapot()
105
                        #rotated box = rotateFigure(box, 0, 0, angle
107
        scale, scale, scale)
                        drawObjectScatter(cam2, image, teapot)
                   ## stop
109
                    else:
                        \# figure = box if frameNumber \% 100 < 50 else
111
       pyramid
                        angle = frameNumber * (math.pi / 50.0)
113
                        scale = 2 + math.sin(angle)
                        box1 = transformFigure(box, 0, 0, -angle, 1,
115
       1, 1)
                        box2 = getPyramidPoints([0, 0, -1], 1,
       chessSquare size)
                        box2 = transformFigure(box2, 0, 0, angle, 1,
117
       1, 1)
                        #rotated box = rotateFigure (figure, 0, 0,
       angle, scale, scale, scale)
                        drawFigure(image, cam2, box1)
119
                        drawFigure(image, cam2, box2)
121
       cv2.namedWindow('Web cam')
       cv2.imshow('Web cam', image)
123
       videoWriter.write(image)
       global result
125
```

```
result=copy(image)
127
def drawFigure(image, camera, figure):
       X = figure.T
       ones = np.ones((X.shape[0],1))
131
       X = np.column_stack((X, ones)).T
133
       projected\_figure = camera.project(X)
       DrawLines (image, projected_figure)
135
137 def getImageSequence(capture, fastForward):
        '','Load the video sequence (fileName) and proceeds,
       fastForward number of frames. '''
       global frameNumber
139
141
       for t in range(fastForward):
           isSequenceOK, originalImage = capture.read() # Get the
       first frames
           frameNumber = frameNumber+1
143
       return originalImage, isSequenceOK
145
147 def printUsage():
       print "Q or ESC: Stop"
       print "SPACE: Pause"
149
       print "p: turning the processing on/off "
             'u: undistorting the image'
             'g: project the pattern using the camera matrix (test)
       print
       print 'x: your key!'
153
       print 'the following keys will be used in the next
       assignment;
       print 'i: show info'
       print 't: texture map'
157
       print 's: save frame
159
161
   def run(speed, video):
163
       ''''MAIN Method to load the image sequence and handle user
       inputs,,,
165
       capture = cv2. VideoCapture(video)
167
       resultFile = "recording.avi"
169
171
       image , isSequenceOK = getImageSequence(capture , speed)
173
```

```
imSize = np.shape(image)
175
       global videoWriter
177
       videoWriter = cv2.VideoWriter(resultFile, cv.CV FOURCC('D', '
       I', 'V', '3'), 30.0, (imSize[1], imSize[0]), True) #Make a video
       writer
       if (isSequenceOK):
179
            update (image)
            printUsage()
181
       while (isSequenceOK):
183
            OriginalImage=copy(image)
185
            inputKey = cv2.waitKey(1)
187
189
            if inputKey == 32:# stop by SPACE key
                update (OriginalImage)
                if speed == 0:
191
                    speed \ = \ tempSpeed \ ;
                else:
193
                    tempSpeed = speed
                    speed = 0;
195
            if (inputKey == 27) or (inputKey == ord('q')):# break
197
       by ECS key
                break
199
            if inputKey == ord('p') or inputKey == ord('P'):
                global ProcessFrame
201
                if ProcessFrame:
                    ProcessFrame = False;
203
                else:
205
                    ProcessFrame = True;
                update (OriginalImage)
207
            if inputKey = ord('u') or inputKey = ord('U'):
209
                global Undistorting
                if Undistorting:
211
                    Undistorting = False;
                else:
213
                    Undistorting = True;
                update (OriginalImage)
215
            if inputKey = ord('w') or inputKey = ord('W'):
                global WireFrame
217
                if WireFrame:
                    WireFrame = False;
                else:
221
                    WireFrame = True;
                update (OriginalImage)
223
            if inputKey == ord('i') or inputKey == ord('I'):
225
```

```
global ShowText
                 if ShowText:
227
                     ShowText = False;
229
                     ShowText = True;
                 update (OriginalImage)
233
            if inputKey = ord('t') or inputKey = ord('T'):
                 global TextureMap
235
                 if TextureMap:
                     TextureMap = False;
237
                 else:
239
                     TextureMap = True;
241
                 update (OriginalImage)
            if inputKey = ord('g') or inputKey = ord('G'):
243
                 global ProjectPattern
                 if ProjectPattern:
245
                     ProjectPattern = False;
247
                 else:
                     ProjectPattern = True;
249
                 update (OriginalImage)
            if inputKey = ord('x') or inputKey = ord('X'):
                 global debug
253
                 if debug:
                     debug = False;
255
                 else:
                     debug = True;
257
                 update (OriginalImage)
259
            if inputKey == ord('l') or inputKey == ord('L'):
                 global Teapot
261
                 Teapot = not Teapot
                 update (OriginalImage)
263
265
            if inputKey = ord('s') or inputKey = ord('S'):
                name='Saved Images/Frame_' + str(frameNumber)+'.png'
267
                 cv2.imwrite(name, result)
269
            if (speed > 0):
                 update (image)
                 image, isSequenceOK = getImageSequence(capture, speed)
   def loadCalibrationData():
        {\color{red} {\bf global}} \ \ {\color{blue} {\bf translation Vectors}}
275
       translation Vectors \ = \ np.\,load\,(\ \verb"numpyData/translation Vectors".
277
        global cameraMatrix
```

```
cameraMatrix = np.load('numpyData/camera matrix.npy')
       global rotatio Vectors
279
       rotatioVectors = np.load('numpyData/rotatioVectors.npy')
281
       global distortionCoefficient
       distortionCoefficient = np.load('numpyData/
       distortion Coefficient.npy')
       {\tt global points\_from\_chess\_board\_plane}
283
       points_from_chess_board_plane = np.load('numpyData/
       obj_points.npy')[0]
       return cameraMatrix, rotatioVectors[0], translationVectors[0]
285
   def calculateP(K, r, t):
       R, _{-} = cv2.Rodrigues(r)
       Rt = np.hstack((R, t))
289
       P = np.dot(K,Rt)
291
       return P
  def displayNumpyPoints(C):
       points = np.load('numpyData/obj_points.npy')
295
       img = cv2.imread('01.png')
297
       x = projectChessBoardPoints(C, points[0])
299
       for p in x:
           C = int(p[0]), int(p[1])
           cv2.circle(img,C, 2,(255,0,255),4)
303
       cv2.imshow('result',img)
       cv2.waitKey(0)
305
  def projectChessBoardPoints(C, X):
       ones = np.ones((X.shape[0],1))
       X = np.column\_stack((X, ones)).T
309
       x = C. project(X)
       x = x.T
311
       return x
   def getCoordinateSystemChessPlane(axis_length = 2.0):
       o = [0., 0., 0.]
315
       x = [axis\_length, 0., 0.]
       y = [0., axis\_length, 0.]
317
       z = [0., 0., -axis\_length] #positive z is away from camera,
       by default
       return np. array ([o, x, y, z])
319
  def drawObjectScatter(C, img, points):
       points = points.T
       ones = np.ones((points.shape[0],1))
323
       points = np.column_stack((points, ones)).T
       points = C. project (points)
325
       points = points.T
327
       for point in points:
```

```
cv2.circle(img, (int(point[0]), int(point[1])), 3, (0,
329
       255, 0), -1)
   def drawCoordinateSystem(img, coordinate_system):
        o = coordinate system[0]
333
        x = coordinate system[1]
        y = coordinate_system[2]
335
        z = coordinate system[3]
337
        cv2.line(img, (int(o[0]), int(o[1])), (int(x[0]), int(x[1]))
        ,(255, 0, 0), 3)
339
        cv2.line(img, (int(o[0]), int(o[1])), (int(y[0]), int(y[1])),
        (255, 0, 0), 3)
        cv2.line(img, (int(o[0]), int(o[1])), (int(z[0]), int(z[1])),
        (255, 0, 0), 3)
341
        cv2.circle(img, (int(x[0]), int(x[1])), 3, (0, 255, 0), -1)
        cv2.\,circle\,(img\,,\ (int\,(y\,[\,0\,]\,)\,\,,int\,(y\,[\,1\,]\,)\,)\,\,,\ 3\,,\ (0\,,\ 255\,,\ 0)\,\,,\ -1)
343
        cv2.\,circle\,(img\,,\ (int\,(z\,[0])\,,int\,(z\,[1])\,)\,,\ 3\,,\ (0\,,\ 255\,,\ 0)\,,\ -1)
        cv2.\,circle\,(img\,,\ (int\,(o\,[\,0\,]\,)\,\,,int\,(o\,[\,1\,]\,)\,)\,\,,\ 3\,,\ (0\,,\ 0\,,\ 255)\,\,,\ -1)
345
347 def createPCurrentFromObjectPose(corners):
        found, r \text{ vec}, t \text{ vec} = cv2.solvePnP
       points from chess board plane, corners, cameraMatrix,
        distortionCoefficient)
        return calculateP(cameraMatrix, r_vec, t_vec)
   def findPFromHomography(corners_current):
351
        cam1 = C
353
        img = cv2.imread("01.png")
         _, corners_1 = findChessBoardCorners(img)
355
        H, _ = cv2.findHomography(corners_1, corners_current)
357
        cam2 = Camera(np.dot(H, cam1.P))
        A = np. dot(linalg.inv(K), cam2.P[:,:3])
359
        r1 = A[:,0]
361
        r2 = A[:,1]
        r3 = np.cross(r1, r2)
363
        r3 = r3/np.linalg.norm(r3)
365
        A = np.array([r1, r2, r3]).T
        cam2.P[:,:3] = np.dot(K,A)
367
        return cam2.P
   def parse_teapot():
371
        points = []
        with open("teapot.data", "r") as infile:
             lines = infile.read().splitlines()
373
             for line in lines:
                 line = line.split(",")
375
```

```
x = float(line[0]) + 5
377
                y = float(line[1]) + 5
                z = (float(line[2]) * -1) - 5
379
                points.append([x, y, z])
        result = np.array(points).T
       return result * 2
383
385 def transformFigure(figure, theta_x, theta_y, theta_z, scale_x,
       scale_y , scale_z):
       translate\_to = [8, 6, -1]
387
       rotation_matrix_x = np.array([ [1, 0, 0], [0, cos(theta_x),
389
       -\sin(\text{theta } x), [0, \sin(\text{theta } x), \cos(\text{theta } x)]
       rotation_matrix_y = np.array([ [cos(theta_y), 0, sin(theta_y
       )], [0, 1, 0], [-\sin(\text{theta}_y), 0, \cos(\text{theta}_y)]])
391
       rotation_matrix_z = np.array([ [cos(theta_z), -sin(theta_z),
        0, [\sin(\text{theta}_z), \cos(\text{theta}_z), 0], [0, 0, 1]
       rotated_x = []
393
       rotated_y = []
       rotated_z = []
395
       rotation = np.dot(rotation_matrix_x, np.dot(
       rotation matrix y, rotation matrix z))
       for i in range(len(figure[0])):
            p = np.array([figure [0][i], figure [1][i], figure [2][i]])
            p_rot = np.dot(rotation, p)
399
            rotated\_x.append(scale\_x \ * \ p\_rot[0] \ + \ translate\_to[0])
            rotated\_y.append(scale\_y \ * \ p\_rot[1] \ + \ translate\_to[1])
401
            rotated_z.append(scale_z * p_rot[2] + translate_to[2])
403
        result = np.array([rotated_x, rotated_y, rotated_z])
       return result
405
407 def back face culling (face normals, camera):
       \#center = camera.c
409
       box\_center = [8, 6, -1]
       camera_center = camera.center()
       camera_x = camera_center[0,0]
411
       camera\_y = camera\_center[1,0]
       camera_z = camera_center[2,0]
413
       camera_center = np.array([camera_x, camera_y, camera_z])
415
       view_vector = box_center - camera_center
417
       view_vector = view_vector / np.linalg.norm(view_vector)
419
       angles = [np.dot(view\_vector, face) for face in face\_normals]
       angles = np.array(angles)
421
       idx = angles \le 0
423
       #print angles
```

```
return idx
425
   def textureFace (image, face, currentCam, texturePath):
       \#translate to = \begin{bmatrix} 8, 6, -1 \end{bmatrix}
       \#f = copy(face)
       texture = cv2.imread(texturePath)
       m, n, d = texture.shape
431
       mask = zeros((m,n)) + 255
       face\_corners = np.array([[0.,0.],[float(n),0.],[float(n),
433
       float (m) ], [0., float (m)]])
       \#f[0,:] = f[0,:] + translate to[0]
435
       \#f[1,:] = f[1,:] + translate_to[1]
       \#f[2,:] = f[2,:] + translate_to[2]
437
       X \, = \, \, face \, .T
439
       ones = np.ones((X.shape[0],1))
441
       X = np.column\_stack((X, ones)).T
       projected\_face \, = \, currentCam \, . \, project \, (X) \, . T
       projected_face = projected_face[:,:-1]
443
       I = copy(image)
445
       H, = cv2.findHomography(face corners, projected face)
447
       h, w, d = image.shape
449
       warped texture = cv2.warpPerspective(texture, H,(w, h))
       warped mask = cv2.warpPerspective(mask, H,(w, h))
       idx = warped_mask != 0
       image[idx] = warped\_texture[idx]
453
       return image
455
457 def ShadeFace(image, points, faceCorner Normals, camera):
        global shadeRes
       shadeRes=10
459
       videoHeight, videoWidth, vd = array(image).shape
461
       #.....
       points_Proj=camera.project(toHomogenious(points))
       points_Proj1 = np.array([[int(points_Proj[0,0]),int(
463
       points_Proj[1,0])],[int(points_Proj[0,1]),int(points_Proj
       [1\,,1])\,]\,,[\,\mathrm{int}\,(\,\mathrm{points}\,\_\,\mathrm{Proj}\,[0\,,2])\,\,,\mathrm{int}\,(\,\mathrm{points}\,\_\,\mathrm{Proj}\,[1\,,2])\,]\,,[\,\mathrm{int}\,(\,
       points_Proj[0,3]), int(points_Proj[1,3])])
       square = np.array([[0, 0], [shadeRes-1, 0], [shadeRes-1, 0]])
       shadeRes - 1, [0, shadeRes - 1])
465
       H = estimateHomography(square, points_Proj1)
       Mr0, Mg0, Mb0=CalculateShadeMatrix(image, shadeRes, points,
       faceCorner_Normals, camera)
       \# HINT
469
       # type(Mr0): <type 'numpy.ndarray'>
       # Mr0.shape: (shadeRes, shadeRes)
471
       #.........
```

```
Mr = cv2.warpPerspective(Mr0, H, (videoWidth, videoHeight),
473
       flags=cv2.INTER LINEAR)
       Mg = cv2.warpPerspective(Mg0, H, (videoWidth, videoHeight),
       flags=cv2.INTER LINEAR)
       Mb = cv2.warpPerspective(Mb0, H, (videoWidth, videoHeight),
       flags = cv2.INTER\_LINEAR)
       image=cv2.cvtColor(image, cv2.COLOR\_BGR2RGB)
       [r,g,b]=cv2.split(image)
479
       whiteMask = np.copy(r)
       whiteMask [:,:] = [0]
481
       points Proj2 = []
       points Proj 2. append ([int (points Proj [0,0]), int (points Proj
483
       [1,0])
       points_Proj2.append([int(points_Proj[0,1]),int(points_Proj
       [1,1])])
       points Proj 2. append ([int(points Proj [0,2]), int(points Proj
485
       [1,2])])
       points\_Proj2.append([int(points\_Proj[0\,,3]),int(points\_Proj
       [1,3])])
       cv2.fillConvexPoly(whiteMask, array(points Proj2)
487
       ,(255,255,255))
       r[nonzero(whiteMask>0)] = map(lambda x: max(min(x,255),0),r[
       nonzero(whiteMask>0)] *Mr[nonzero(whiteMask>0)])
       g[nonzero(whiteMask>0)]=map(lambda x: max(min(x,255),0),g[
       nonzero(whiteMask>0)]*Mg[nonzero(whiteMask>0)])
       b[nonzero(whiteMask>0)]=map(lambda x: max(min(x,255),0),b[
491
       \verb"nonzero" (\verb"whiteMask">0) ]*Mb[\verb"nonzero" (\verb"whiteMask">0) ])
       #......
       image=cv2.merge((r,g,b))
493
       image=cv2.cvtColor(image, cv2.COLOR RGB2BGR)
       return image
495
497 def CalculateShadeMatrix(image, shadeRes, points,
       faceCorner_Normals , camera):
       #given:
       #Ambient light IA=[IaR, IaG, IaB]
499
       cc = camera.center()
501
       camera_position = np.array([cc[0,0], cc[1,0], cc[2,0]])
       light\_source = np.array([cc[0,0], cc[1,0], cc[2,0]])
503
505
       IA = np.matrix([5.0, 5.0, 5.0]).T
       #Point light IA=[IpR, IpG, IpB]
       IP = np.matrix([5.0, 5.0, 5.0]).T
509
       #Light Source Attenuation
       fatt = 1
511
       #Material properties: e.g., Ka=[kaR; kaG; kaB]
       ka=np.matrix([0.2, 0.2, 0.2]).T
513
       kd= np.matrix([0.3, 0.3, 0.3]).T
```

```
ks=np.matrix([0.7, 0.7, 0.7]).T
515
       alpha = 100
517
       \#ambient: I ambient(x) = I a * k a(x)
       r = np.zeros((shadeRes, shadeRes))
       g = np.zeros((shadeRes, shadeRes))
       b = np.zeros((shadeRes, shadeRes))
521
       #Ambient
       r_{ambient} = r + IA[0] * ka[0]
       g_{ambient} = g + IA[1] * ka[1]
       b_{ambient} = b + IA[2] * ka[2]
527
       #Diffuse
529
       point = points.T[0]
531
       \#point = points[0,0]
       point_normal = np.mean(faceCorner_Normals, axis=1)
533
       point \ normal = point\_normal \ / \ np.linalg.norm(point\_normal)
       i_diffuse = diffuse(point, point_normal, light_source) * kd
537
       [0]
       i_spectral = speculate(point, point_normal, light_source,
       camera_position, alpha)
       r\_final = r\_ambient + i\_diffuse + i\_spectral #+ r\_specular +
541
       r_diffused
       g\_final = g\_ambient + i\_diffuse + i\_spectral
       b_final = b_ambient + i_diffuse + i_spectral
543
       return (r_final, g_final, b_final)
545
   def diffuse(point, point_normal, light_source):
       # Regn vector ud fra Light source til point
549
       light_vector = light_source - point
551
       # Calculate distance from point to light
       r = np.linalg.norm(light vector)
       # Normaliser vector
       light direction = light vector / r
557
       \#a,b,c = (0.1,0.1,0.1)
       \#i_l = 1 / float(a * r ** 2 + b * r + c)
561
       i \quad l \,\,=\,\, 1
563
       i\_diffuse = i\_l * max(np.dot(light\_direction, point\_normal)
565
```

```
, 0)
567
       return i diffuse
569
   def speculate(point, point_normal, light_source, camera_position
       , alpha):
       #find 1
571
       incident_vector = point - light_source
       incident_vector = incident_vector/np.linalg.norm(
573
       incident_vector)
       #find r
575
       reflection vector = 2*np.dot(point normal, incident vector)*
       point normal - incident vector
       reflection vector = reflection vector/np.linalg.norm(
       reflection_vector)
       view\_vector = camera\_position - point
       view_vector = view_vector/np.linalg.norm(view_vector)
579
       i s = 1
581
       i spectral = i s*np.dot(view vector, reflection vector)**
583
       alpha
       return i_spectral
585
   def calculate_face_normals():
       return np.array([GetFaceNormal(face) for face in Faces])
       #top normal = GetFaceNormal(TopFace)
589
       #print "top", top normal
       #return np.array([top normal])
   def draw face normals (image, camera, normals):
       cube center = [8, 6, -1]
595
       size = 2
       #find pairs of points (cube_center -> cube_center + normal)
597
       #project and draw
       for normal in normals:
599
           p1 = cube\_center + normal * size
           p2 = p1 + normal * 4
601
           #print p1, p2
           fig = np.array([p1, p2])
603
           drawFigure (image, camera, fig.T)
   def getPyramidPoints(center, size, chessSquare_size):
       points = []
607
       tl = [center[0] - size, center[1] - size, center[2]]
609
       bl = [center[0] - size, center[1] + size, center[2]]
       br = [center[0] + size, center[1] + size, center[2]]
611
       tr = [center[0] + size, center[1] - size, center[2]]
       top = [center[0], center[1], center[2] - size * 2]
613
```

```
615
       \#bottom
        points.append(tl)
617
        points.append(bl)
        points.append(br)
        points.append(tr)
619
        points.append(tl)
621
       #top
       points.append(top)
623
625
       #diagonals
       points.append(bl)
        points.append(br)
627
        points.append(top)
629
        points.append(tr)
        points=dot(points, chessSquare_size)
        return array (points).T
631
633
                           -MAIN BODY
       , , ,
637
639
             -variables-
641 global cameraMatrix
   global distortionCoefficient
643 global homographyPoints
   global calibrationPoints
645 global calibrationCamera
   global chessSquare_size
647
   {\tt ProcessFrame}\!\!=\!\!{\tt True}
^{649} Undistorting=False
   WireFrame = False
   ShowText=True
   TextureMap=True
   ProjectPattern=False
   debug=False
   Teapot = True
   tempSpeed=1
   frameNumber=0
   chessSquare\_size{=}2
661
           ---defining the figures --
```

```
box = getCubePoints([0, 0, 1], 1, chessSquare\_size)
   pyramid = getPyramidPoints([0, 0, 1], 1, chessSquare size)
667
_{669} i = array([[0,0,0,0],[1,1,1,1],[2,2,2,2]]) # indices for
      the first dim
   j = array([[0,3,2,1],[0,3,2,1],[0,3,2,1]]) \# indices for
      the second dim
_{671} TopFace = box[i,j]
673
   i = array([[0,0,0,0],[1,1,1,1],[2,2,2,2]]) \# indices for
      the first dim
i = array([[3,8,7,2],[3,8,7,2],[3,8,7,2]]) # indices for
       the second dim
   RightFace = box[i,j]
677
679 i = array([[0,0,0,0],[1,1,1,1],[2,2,2,2]]) # indices for
       the first dim
   j = array([[5,0,1,6],[5,0,1,6],[5,0,1,6]]) # indices for
       the second dim
681 LeftFace = box[i,j]
683 i = array([[0,0,0,0],[1,1,1,1],[2,2,2,2]]) # indices for
       the first dim
   j = array([ [5,8,3,0], [5,8,3,0] , [5,8,3,0] ]) \# indices for
      the second dim
685 UpFace = box[i,j]
687
   i = array([ \ [0\,,0\,,0\,,0]\,,[1\,,1\,,1\,,1] \ ,[2\,,2\,,2\,,2] \ ]) \ \# indices for
      the first dim
689 j = array([[1,2,7,6], [1,2,7,6], [1,2,7,6]]) # indices for
      the second dim
   DownFace = box[i,j]
691
695
697
   ,,, < 000> Here Call the calibrateCamera from the SIGBTools to
       calibrate the camera and saving the data'''
   Faces = [RightFace, LeftFace, UpFace, DownFace, TopFace]
701 FaceTextures = ['Images/Right.jpg', 'Images/Left.jpg', 'Images/
      Up.jpg', 'Images/Down.jpg', 'Images/Top.jpg']
703 t, r, l, u, d = CalculateFaceCornerNormals(TopFace, RightFace,
      LeftFace, UpFace, DownFace)
   CornerNormals = [r, l, u, d, t]
```

```
\#calibrateCamera(5, (9,6), 2.0, 0)
_{707} ''' <\!\!001\!\!> Here Load the numpy data files saved by the
       cameraCalibrate2 ',',
   K, r, t = loadCalibrationData()
^{709} ''' <\!\!002\!\!> Here Define the camera matrix of the first view image
       (01.png) recorded by the cameraCalibrate2','
711 P = calculateP(K, r, t)
   C = Camera(P)
713
   ''' <\!\!003\!\!> Here Load the first view image (01.png) and find the
       chess pattern and store the 4 corners of the pattern needed
       for homography estimation,,,
715 #displayNumpyPoints(C)
    ,,, <\!003a\!> Find homography H_cs^1 ,,,
719
\#run(1, 0)
721 run(1, "sequence.mov")
```