```
Contents
                                       15
                                             }
                                           }
                                      16
                                      17
                                           cout << dp[l1][l2] << '\n';
                                      18
 1 DP
   1.1 LCS .
                                      19
                                           return 0;
   1.2 LIS O(n^2) . . . . . . . . . . . . . . . . . .
                                      20 }
   1.4 LIS O(n \log n)
                                        1.2 LIS O(n^2)
   #include <bits/stdc++.h>
   2
                                        #define IOS
  ios_base::sync_with_stdio(false);cin.tie(0);cout.tie(0);
                                        using namespace std;
 3 Graph
                                        typedef long long 11;
  3.1 Floyd Warshall . . . . . . . . . . . . . . . . .
   int main(){
   TOS
   3.4 Dijkstra
                                           int arr[100];
   3.5 SecondSP
                                           int n;
   cin >> n;
                                       9
   10
                                           for(int i = 0; i < n; i++) cin >> arr[i];
  11
                                           int dp[100];
                                           for(int i = 0; i < n; i++) dp[i] = 1;
                                           for(int i = 0; i < n; i++){</pre>
 4 RMO
                                      14
                                              for(int j = 0; j < i; j++){
   6
   6
                                      15
                                                if(arr[i] > arr[j])
                                                   dp[i] = max(dp[j] + 1, dp[i]);
                                      16
   }
                                      18
                                     8
 5 Uncategorized
   5.1 快速冪
                                      19
                                           int ans = 1;
                                     8
   20
                                           for(int i = 0; i < n; i++) ans = max(ans, dp[i]);
                                           cout << ans << '\n';
                                      21
                                     9
  23
                                           return 0;
                                      24 }
                                        1.3 LIS O(n \log n)
   class Solution {
 8 Trick
                                        public:
  8.1 求根號和解決 pow 精度問題 . . . . . . .
                                           int lengthOfLIS(vector<int>& nums) {
   vector<int> v;
   int n = nums.size();
  8.4 n!modp.
        for(int i = 0; i < n; i++){</pre>
   8.5 從 1 ...
                                       6
  8.6 二項式係數 Binomial Coefficient (也可以用在 C 幾取幾)....
                                                int p = lower_bound(v.begin(), v.end(),
  nums[i]) - v.begin();
                                                if(p == v.size()) v.push_back(nums[i]);
                                                else v[p] = nums[i];
  Math
                                     10
  10
                                      10
   10
                                              return v.size();
   12
                                           }
                                       13 };
    DP
                                        1.4 LIS O(n \log n)
 1.1 LCS
                                       1 for(int i=0;i<num.size();i++){</pre>
                                           if(lis.empty()||lis.back()<num[i]){</pre>
                                       2
1 | #include <bits/stdc++.h>
                                             lis.push_back(num[i]);
2 #define IOS
                                              dp[i]=lis.size();
    ios_base::sync_with_stdio(false);cin.tie(0);cout.tie(4)
                                           }
3 using namespace std;
                                           else{
4 string s1, s2;
                                             auto iter=lower_bound(all(lis), num[i]);
 int dp[505][505];
                                       8
                                              dp[i]=iter-lis.begin()+1;
6 int main(){
                                       9
                                              *iter=num[i];
    IOS
                                       10
    cin >> s1 >> s2;
8
                                      11
9
    memset(dp, 0, sizeof(dp));
                                        int length=lis.size();
    int l1 = s1.size(), l2 = s2.size();
10
                                        for(int i=num.size()-1;i>=0;i--){
                                      13
    for(int i = 1; i <= 11; i++){</pre>
```

if(dp[i]==length){

length --;

ans.push_back(num[i]);

14

15

16

18 }

}

11

12

13

14

for(int $j = 1; j \le 12; j++){$

- 1]);

if(s1[i - 1] == s2[j - 1]) dp[i][j] =

else dp[i][j] = max(dp[i - 1][j], dp[i][j

dp[i - 1][j - 1] + 1;

2 Prime

2.1 質數篩 CPP

```
1| bitset < MAXN > prime_bool;
2 vector<ll> prime;
3 void find_prime(){
       prime_bool.set();
       for(int i=2;i<MAXN;i++){</pre>
           if(prime_bool[i]){
7
                prime.push_back(i);
8
9
            for(auto j:prime){
                if(j*i>=MAXN)
10
11
                     break;
12
                prime_bool[j*i]=0;
                if(i%j==0)
13
14
                     break;
15
           }
16
       }
17 }
```

2.2 質數篩 PY

```
1 is_prime = n * [1]
2 is_prime[0] = is_prime[1] = 0
3
4 for i in range(2, n):
5     if is_prime[i]:
6         for j in range(2, n):
7         if i * j >= n:
8              break
9         is_prime[i * j] = 0
```

2.3 單一質數

```
bool prime(int n){
    if(n < 2) return false;
    if(n <= 3) return true;

if(!(n % 2) || !(n % 3)) return false;

for(int i = 5; i * i <= n; i += 6)
    if(!(n % i) || !(n % (i + 2))) return false;

return true;

8 }</pre>
```

2.4 egcd CPP

```
int exgcd(int a, int b, int &x, int &y){
   if(b==0){
       x=1, y=0;
       return a;
}
int gcd=exgcd(b, a%b, y, x);
y-=a/b*x;
return gcd;
}
```

2.5 egcd PY

3 Graph

3.1 Floyd Warshall

```
1 int n, rd, 1, r, v;
 2 cin >> n >> rd;
 3 vector<vector<int>> dp(n + 1, vector<int>(n + 1,
       1e9));
  for(int i = 0; i < rd; i++){</pre>
       cin >> 1 >> r >> v;
 5
       dp[1][r] = dp[r][1] = v;
       //每條路皆雙向
 7
 8 }
10
  //以下即 Floyd-Warshall
  for(int k = 1; i <= n; i++){</pre>
11
       for(int i = 1; j <= n; j++){</pre>
12
           for(int j = 1; k <= n; k++){</pre>
13
                dp[i][j] = min(dp[i][k] + dp[k][j],
14
                    dp[i][j]);
                //窮舉所有鬆弛可能
15
           }
16
17
       }
18 }
19 cin >> 1 >> r;
20 cout << dp[1][r];</pre>
```

3.2 Bellman Ford

```
1 #include <bits/stdc++.h>
2 #define IOS
       ios_base::sync_with_stdio(false);cin.tie(0);cout.tie(0);
  #define INF 0x3f3f3f3f
  using namespace std;
  typedef long long 11;
  struct Edge{
7
   int x, y, t;
8
  };
9
  int dis[1005];
10 int main(){
    IOS
12
    int c;
13
     cin >> c;
14
     while(c--){
15
       vector<Edge> edge;
16
       int n, m;
       cin >> n >> m;
17
18
       for(int i = 0; i <= n; i++) dis[i] = INF;</pre>
19
       dis[0] = 0;
20
       for(int i = 0; i < m; i++){
21
         int x, y, t;
22
         cin >> x >> y >> t;
23
         edge.push_back({x, y, t});
24
25
       for(int i = 0; i < n - 1; i++){
26
         for(int j = 0; j < m; j++){
           if(dis[edge[j].x] + edge[j].t <</pre>
27
                dis[edge[j].y]){
28
              dis[edge[j].y] = dis[edge[j].x] + edge[j].t;
29
           }
         }
30
31
32
       bool judge = true;
       for(auto e : edge){
33
         if(dis[e.x] + e.t < dis[e.y]){
35
           judge = false;
36
           break:
37
         }
38
       }
39
       cout << (judge ? "not possible" : "possible") <<</pre>
40
41
     return 0;
```

```
43 }
                                                                31
                                                                            }
                                                                       }
                                                                32
                                                                        int maxd = -1, cnt = 0;
                                                                33
                                                                       for(int i = 0; i < n; i++){</pre>
                                                                34
  3.3 SPFA
                                                                35
                                                                            if(dis[i] < INF){</pre>
                                                                36
                                                                                if(dis[i] > maxd) maxd = dis[i];
                                                                37
1 #define mem(x) memset(x, 0, sizeof(x))
                                                                38
                                                                            else cnt++:
2 struct road{
                                                                       }
                                                                39
    int r, val;
                                                                       cout << maxd << '\n' << cnt << '\n';
                                                                40
4 };
                                                                41 }
5 int main(){
                                                                42
                                                                   int main(){
    int n, e, 1, r, v;
                                                                43
                                                                       IOS
7
     cin >> n >> e:
                                                                        cin >> n >> m;
                                                                44
8
     vector < int > dp(n + 1, 1e9);
                                                                45
                                                                        for(int i = 0; i < m; i++){</pre>
     vector<road> rd[n + 1];
9
                                                                46
                                                                            int u, v, w;
     for(int i = 0; i < e; i++){
10
                                                                47
                                                                            cin >> u >> v >> w;
11
       cin >> 1 >> r >> v;
                                                                48
                                                                            adj[u].push_back(make_pair(v, w));
       rd[1].push\_back(\{r,\ v\});
12
                                                                49
                                                                            adj[v].push_back(make_pair(u, w));
13
       rd[r].push_back({1, v});
                                                                50
14
                                                                51
                                                                        solve();
15
     cin >> 1 >> r;
                                                                52
16
     dp[1] = 0;
                                                                53
                                                                        return 0;
17
     queue < int > que;
                                                                54 }
18
     que.push(1);
     bool check[n + 1]; mem(check);
19
20
     int cnt[n + 1]; mem(cnt);
                                                                   3.5 SecondSP
21
     while(!que.empty()){
22
       int tmp = que.front(); que.pop();
23
       check[tmp] = 0, cnt[tmp]++;
                                                                 1 #include <bits/stdc++.h>
24
       if(cnt[tmp] >= n) {cout << "neg cycle\n"; break;}</pre>
                                                                 2 #define IOS
       for(auto & i : rd[tmp]){
25
                                                                        ios\_base::sync\_with\_stdio(\textbf{false}); cin.tie(\emptyset); cout.tie(\emptyset);
         if(dp[i.r] > dp[tmp] + i.val){
26
                                                                   #define INF 0x3f3f3f3f
           dp[i.r] = dp[tmp] + i.val;
27
                                                                   using namespace std;
           if(!check[i.r]) check[i.r] = 1, que.push(i.r);
28
29
                                                                 6
                                                                   typedef pair<int, int> pii;
30
       }
                                                                 7
                                                                   typedef long long 11;
31
     }
     for(auto & i : dp) cout << i << ' ';</pre>
32
                                                                   const int MAXN = 1005;
                                                                 9
33
     return 0;
                                                                10
34 }
                                                                   vector<pii> adj[MAXN]; // adj[u] stores pairs {v,
                                                                11
                                                                        weight?
                                                                12
                                                                   int dist[MAXN], sec_dist[MAXN]; // shortest and
                                                                        second shortest distances
  3.4 Dijkstra
                                                                14
                                                                   void dijkstra(int s, int n){
1 #include <iostream>
                                                                15
                                                                        // Min-heap to store {distance, node}
2 #include <algorithm>
                                                                16
                                                                        priority_queue<pii, vector<pii>, greater<pii>> pq;
3 #include <vector>
                                                                17
                                                                        fill(dist, dist + n + 1, INF);
4 #include <queue>
                                                                18
                                                                       fill(sec_dist, sec_dist + n + 1, INF);
5 #define IOS
                                                                19
       ios_base::sync_with_stdio(false);cin.tie(0);cout.tie100
                                                                        dist[s] = 0;
6 #define INF 2147483647
                                                                        pq.push({0, s});
7 using namespace std;
                                                                22
                                                                23
                                                                        while(!pq.empty()){
8 int n, m;
9 vector<pair<int, int>> adj[100005];
                                                                24
                                                                            int d = pq.top().first;
10 bool visited[100005] = {false};
                                                                25
                                                                            int u = pq.top().second;
11 priority_queue < pair < int , int >> pq;
                                                                26
                                                                            pq.pop();
12 int dis[100005], parent[100005];
                                                                27
13 void solve(){ // Dijkstra
                                                                28
                                                                            // If we found a path longer than the second
       dis[0] = 0;
14
                                                                                 shortest, skip it
15
       for(int i = 1; i < n; i++) dis[i] = INF;</pre>
                                                                29
                                                                            if (sec_dist[u] < d) continue;</pre>
       pq.push(make_pair(0, 0));
16
                                                                30
17
       while(!pq.empty()){
                                                                31
                                                                            for (auto &edge : adj[u]){
18
           auto node = pq.top();
                                                                32
                                                                                int v = edge.first;
           pq.pop();
                                                                33
                                                                                int w = edge.second;
19
20
           int v = node.second; // parent
                                                                34
           if(visited[v]) continue;
                                                                                int new_dist = d + w;
21
                                                                35
22
           visited[v] = true;
                                                                36
                                                                                // If this gives a new shortest path to v
23
           for(auto i : adj[v]){
                                                                37
24
                int vertex = i.first, weight = i.second;
                                                                38
                                                                                if(new_dist < dist[v]){</pre>
25
                if(visited[vertex]) continue;
                                                                39
                                                                                     sec_dist[v] = dist[v];
                if(dis[v] + weight < dis[vertex]){</pre>
                                                                                     dist[v] = new_dist;
                                                                40
26
                    dis[vertex] = dis[v] + weight;
                                                                41
                                                                                     pq.push({dist[v], v});
27
28
                    parent[vertex] = v;
                                                                42
                                                                                     pq.push({sec_dist[v], v});
29
                    pq.push(make_pair(-dis[vertex],
                                                                43
```

44

vertex));

}

30

// If this gives a new second shortest

path to v

else if(new_dist > dist[v] && new_dist <</pre>

45

31

32

33

34

cin >> u >> v >> w;

sort(adj.begin(), adj.end());

adj.push_back({u, v, w});

// for(int i = 0;i < m;i++) cout << adj[i].w << '

for(int i = 1;i <= n;i++) anc[i] = i;</pre>

if(merge(edge[j].a, edge[j].b)){

for(int j = 0; j < edge.size(); j++){</pre> if(mst[i] == j) continue;

```
sec_dist[v]){
                     sec_dist[v] = new_dist;
                                                                         int cost = 0, n_edge = 0;
46
                                                                  36
                     pq.push({sec_dist[v], v});
                                                                         for(Edge e : adj){
47
                                                                  37
                                                                              if(merge(e.u, e.v)){
48
                                                                  38
49
            }
                                                                  39
                                                                                  cost += e.w;
       }
                                                                  40
                                                                                  n_edge++;
50
51 }
                                                                  41
                                                                              }
                                                                  42
52
                                                                         if(n_edge == n - 1) cout << cost << '\n';</pre>
53
   int main() {
                                                                  43
                                                                         else cout << -1 << '\n';
54
       IOS
                                                                  44
                                                                  45
55
       int t;
56
       cin >> t;
                                                                  46
                                                                         return 0;
                                                                  47 }
       while(t--){
57
58
            int n, m, s, d;
            cin >> n >> m >> s >> d;
59
60
                                                                           SecondMST
61
            // Reset adjacency list
            for(int i = 1; i <= n; i++) adj[i].clear();</pre>
62
                                                                   1 #include <bits/stdc++.h>
63
                                                                     #define IOS
            for(int i = 0; i < m; i++){</pre>
64
                                                                         ios\_base::sync\_with\_stdio(\textbf{false}); cin.tie(\emptyset); cout.tie(\emptyset);
65
                int u, v, w;
                                                                     #define INF 0x3f3f3f3f
66
                cin >> u >> v >> w;
                                                                     using namespace std;
                adj[u].push_back({v, w});
67
                                                                     typedef long long 11;
                adj[v].push_back({u, w}); // If the graph
68
                                                                     int anc[105], sz[105];
                     is undirected
                                                                     struct Edge{
            }
69
                                                                   8
                                                                         int a, b, c;
70
                                                                     };
71
            dijkstra(s, n);
                                                                  9
                                                                     int Find(int a){
                                                                  10
72
                                                                  11
                                                                         return (anc[a] == a ? a : anc[a] = Find(anc[a]));
            if(sec_dist[d] == INF) cout << -1 << '\n'; //</pre>
73
                                                                     }
                                                                  12
                No second shortest path
                                                                     bool merge(int a, int b){
                                                                  13
            else cout << sec_dist[d] << '\n';</pre>
74
                                                                         a = Find(a);
75
                                                                  14
                                                                  15
                                                                         b = Find(b);
76
77
       return 0:
                                                                  16
                                                                         if(a == b) return false;
                                                                         if(sz[a] < sz[b]) swap(a, b);</pre>
                                                                  17
78 }
                                                                  18
                                                                         anc[b] = a;
                                                                  19
                                                                         sz[a] += sz[b];
                                                                  20
                                                                         return true;
                                                                  21 }
   3.6 Kurskal's Algorithm
                                                                  22
                                                                     int main(){
                                                                  23
                                                                         IOS
1 #include <bits/stdc++.h>
                                                                  24
                                                                         int t:
 2 #define IOS
                                                                         cin >> t;
       ios_base::sync_with_stdio(false);cin.tie(0);cout.tie1@
                                                                         while(t--){
3 using namespace std;
                                                                  27
                                                                              int n, m;
4 int parent[10005];
                                                                  28
                                                                              vector < Edge > edge;
5 struct Edge{
                                                                              cin >> n >> m;
                                                                  29
       int u, v, w;
                                                                  30
                                                                              vector<pair<int, int> > vec[105];
       bool operator < (Edge &b){</pre>
7
                                                                              for(int i = 0; i < m; i++){}
                                                                  31
8
           return w < b.w;</pre>
                                                                  32
                                                                                  int a, b, c;
9
                                                                  33
                                                                                  cin >> a >> b >> c;
10 };
                                                                  34
                                                                                  edge.push_back({a, b, c});
11 int query(int a){
                                                                  35
       if(parent[a] == -1) return a;
                                                                  36
                                                                              for(int i = 1; i \le n; i++){
12
13
       return parent[a] = query(parent[a]);
                                                                  37
                                                                                  sz[i] = 0;
14 }
                                                                  38
                                                                                  anc[i] = i;
15 bool merge(int a, int b){
                                                                  39
16
       int r1 = query(a);
                                                                  40
                                                                              sort(edge.begin(), edge.end(), [&](Edge &u,
17
       int r2 = query(b);
                                                                                  Edge &v)\{return u.c < v.c;\}\};
18
       if(r1 == r2) return false;
                                                                  41
                                                                              int cost1 = 0, cnt = 0;
                                                                              vector<int> mst;
19
       if(parent[r1] < parent[r2]) parent[r2] = r1;</pre>
                                                                  42
20
       else parent[r1] = r2;
                                                                  43
                                                                              for(int i = 0; i < edge.size(); i++){</pre>
21
       return true;
                                                                  44
                                                                                  if(merge(edge[i].a, edge[i].b)){
                                                                                       cost1 += edge[i].c;
22 }
                                                                  45
23
   int main(){
                                                                  46
                                                                                       mst.push_back(i);
                                                                                       if(++cnt == n - 1) break;
       IOS
24
                                                                  47
25
       int n, m;
                                                                  48
                                                                                  }
                                                                              }
26
       memset(parent, -1, sizeof(parent));
                                                                  49
27
       cin >> n >> m:
                                                                  50
                                                                              int cost2 = INF;
28
       vector < Edge > adj;
                                                                  51
                                                                              for(int i = 0; i < mst.size(); i++){</pre>
       for(int i = 0; i < m; i++){</pre>
                                                                  52
                                                                                  cnt = 0;
29
                                                                  53
                                                                                  int res = 0;
30
            int u, v, w;
```

54

55

56

```
res += edge[j].c;
58
                                                                 3 #define INF 0x3f3f3f3f
                         if(++cnt == n - 1){
59
                                                                   using namespace std;
                             cost2 = min(cost2, res);
                                                                   typedef long long 11;
60
61
                                                                   const int N = 2e5 + 5;
62
                                                                   int n, q;
                    }
63
                                                                   vector<int> vec[N];
               }
                                                                   int p[20][N], in[N], out[N];
64
65
           }
                                                                   bool valid(int a, int b){
                                                                       return (in[a] <= in[b] && out[b] <= out[a]);</pre>
66
                                                                11
           cout << cost1 << ' ' << cost2 << '\n';
67
                                                                12
68
                                                                13
                                                                   void dfs(int cur, int par){
                                                                       static int t = 0;
69
                                                                14
70
       return 0;
                                                                15
                                                                       p[0][cur] = par;
71 | }
                                                                16
                                                                        in[cur] = t++;
                                                                17
                                                                        for(auto e : vec[cur]){
                                                                            dfs(e, cur);
                                                                18
                                                                19
         Prim's Algorithm
                                                                20
                                                                       out[cur] = t++;
                                                                21
1 #include <iostream>
                                                                   int lca(int a, int b){
                                                                22
2 #include <queue>
                                                                        if(valid(a, b)) return a;
                                                                23
3 #include <algorithm>
                                                                24
                                                                        for(int i = 19; i >= 0; i--){
4 #include <cstring>
                                                                25
                                                                            if(!valid(p[i][a], b)) a = p[i][a];
5 #define IOS
                                                                26
       ios_base::sync_with_stdio(false);cin.tie(0);cout.tie1/2
                                                                        return p[0][a];
6 using namespace std;
                                                                28 }
7 int n, m, dis[10005], parent[10005];
                                                                   int main(){
8 | bool visited[10005] = {false};
                                                                30
                                                                       TOS
  vector<pair<int, int> > adj[100005];
                                                                31
                                                                        cin >> n >> q;
10 int main(){
                                                                32
                                                                        for(int i = 2; i \le n; i++){
       IOS
11
                                                                33
                                                                            int e:
       // freopen("input.in", "r", stdin);
12
                                                                            cin >> e;
       cin >> n >> m;
13
                                                                35
                                                                            vec[e].push_back(i);
       memset(dis, 0x3f3f3f3f, sizeof(dis));
14
                                                                36
       memset(parent, -1, sizeof(parent));
15
                                                                37
                                                                       dfs(1, 1);
16
       for(int i = 0; i < m; i++){</pre>
                                                                38
                                                                       for(int i = 1; i < 20; i++){
17
           int u, v, w;
                                                                39
                                                                            for(int j = 1; j \le n; j++){}
18
           cin >> u >> v >> w;
                                                                                p[i][j] = p[i - 1][p[i - 1][j]];
                                                                40
19
           adj[u].push_back({v, w});
                                                                41
20
           adj[v].push_back({u, w});
                                                                42
21
       }
                                                                43
                                                                        while(q--){
       int start = 0;
                                                                            int u, v;
22
                                                                44
                                                                            cin >> u >> v;
23
       dis[start] = 0;
                                                                45
24
       priority_queue < pair < int , int > , vector < pair < int ,</pre>
                                                                            cout << lca(u, v) << '\n';
                                                                46
           int> >, greater<pair<int, int> > pq;
                                                                       }
                                                                47
       pq.push({dis[start], start});
25
                                                                48
       while(!pq.empty()){
26
                                                                49
                                                                        return 0;
27
           pair<int, int> cur = pq.top();
                                                                50 }
28
           pq.pop();
29
           if(visited[cur.second]) continue:
30
           visited[cur.second] = true;
                                                                   3.10 Topological Sort
           for(auto i : adj[cur.second]){
31
                if(visited[i.first]) continue;
32
                                                                 1 #include <bits/stdc++.h>
33
                if(dis[i.first] > i.second){
                                                                   #define IOS
34
                    dis[i.first] = i.second;
                                                                        ios_base::sync_with_stdio(false);cin.tie(0);cout.tie(0);
35
                    parent[i.first] = cur.second;
                                                                   using namespace std;
36
                    pq.push({dis[i.first], i.first});
                                                                   typedef long long 11;
37
           }
                                                                   vector<int> vec[200005];
38
                                                                   int ind[100005];
39
                                                                   int main(){
40
       int cost = 0, err = 0;
                                                                       IOS
41
       for(int i = 0; i < n; i++){</pre>
42
           if(dis[i] < 0x3f3f3f3f) cost += dis[i];</pre>
                                                                 9
                                                                       int n, m;
                                                                10
                                                                        cin >> n >> m;
43
           else err++;
                                                                11
                                                                       memset(ind, 0, sizeof(ind));
44
                                                                        for(int i = 0;i < m;i++){</pre>
       cout << (err ? -1 : cost) << "\n";</pre>
                                                                12
45
46
       // for(int i = 0; i < n; i++) cout << dis[i] << ' ';
                                                                            int a, b;
47
                                                                14
                                                                            cin >> a >> b:
                                                                15
                                                                            ind[b]++;
48
       return 0;
49 }
                                                                16
                                                                            vec[a].push_back(b);
                                                                17
                                                                       }
                                                                        queue<int> q;
                                                                18
                                                                19
                                                                       for(int i = 1; i \le n; i++){
  3.9
         LCA
                                                                20
                                                                            if(ind[i] == 0) q.push(i);
                                                                21
                                                                       }
1 #include <bits/stdc++.h>
                                                                22
                                                                       vector<int> top;
```

23

ios_base::sync_with_stdio(false);cin.tie(0);cout.tie14

while(!q.empty()){

int cur = q.front();

2 #define IOS

```
25
           q.pop();
                                                             48
                                                                    int mid = (1 + r) >> 1;
           top.push_back(cur);
                                                                   if(qr <= mid) return query(L(x), 1, mid, ql, qr);</pre>
                                                             49
26
27
           for(auto e : vec[cur]){
                                                             50
                                                                    else if(ql > mid) return query(R(x), mid + 1, r,
               ind[e]--;
28
                                                                        ql, qr);
29
               if(ind[e] == 0){
                                                             51
                                                                    else return query(L(x), 1, mid, ql, mid) +
30
                   q.push(e);
                                                                        query(R(x), mid + 1, r, mid + 1, qr);
                                                             52 }
31
32
           }
                                                             53 int main(){
33
                                                             54
                                                                   IOS
34
       if(top.size() == n){
                                                             55
                                                                    init();
           \label{eq:formula} \mbox{for(auto i : top) cout} <<\mbox{ i }<<\mbox{ ' ';}
35
                                                             56
                                                                   cin >> n;
           cout << '\n';
                                                                    build(1, 1, n);
                                                             57
36
37
                                                             58
                                                                    cin >> q;
       else cout << "IMPOSSIBLE" << '\n';</pre>
                                                             59
                                                                    while(q--){
38
39
                                                             60
                                                                        int v, x, y, k;
                                                                        cin >> v;
40
       return 0;
                                                             61
41 }
                                                             62
                                                                        if(v == 1){
                                                             63
                                                                            cin >> x >> y >> k;
                                                                            modify(1, 1, n, x, y, k);
                                                             64
                                                                        }
                                                             65
                                                             66
                                                                        else{
       RMO
                                                             67
                                                                            cin >> x >> y;
                                                             68
                                                                            ll ans = query(1, 1, n, x, y);
                                                             69
                                                                            cout << ans << '\n';
  4.1
         Segment Tree V1
                                                             70
                                                                   }
                                                             71
1 #include <bits/stdc++.h>
                                                             72
2 #define IOS
                                                             73
                                                                    return 0;
       ios_base::sync_with_stdio(false);cin.tie(0);cout.tie(1)}
3 #define L(x) (x << 1)
4 #define R(x) ((x << 1) | 1)
5 using namespace std;
6 typedef long long 11;
                                                               4.2 Segment Tree V2
7 | 11 seg[500005 << 2], lazy[500005 << 2];
8 int n, q;
9 void init(){
                                                             1 struct Node{
      memset(seg, 0, sizeof(seg));
10
                                                                   int left; // 左邊邊界
                                                             2
11
       memset(lazy, 0, sizeof(lazy));
                                                             3
                                                                   int right; //右邊邊界
12 }
13 void build(int x, int 1, int r){
                                                                   int value; //儲存的值
       if(1 == r){
                                                                   int z; //區間修改用,如果沒有區間修改就不需要
14
15
          cin >> seg[x];
                                                             6
                                                               }node[4 * N ];
16
           return;
17
      }
                                                               #define Lson(x) (x << 1) //左子樹
                                                             8
       int mid = (1 + r) >> 1;
18
                                                               #define Rson(x) ((x << 1) +1) //右子樹
                                                             9
19
       build(L(x), 1, mid);
                                                             10
20
       build(R(x), mid + 1, r);
                                                            11
                                                               void question(){
21
       seg[x] = seg[L(x)] + seg[R(x)];
                                                            12
                                                                   for(int i = 1; i <= 10; i++) num[i] = i * 123 % 5;
22 }
                                                                    // num 為題目產生的一段數列
                                                            13
23 void push(int pos, int size){
                                                                    // hash 函數,讓 num 的 i 被隨機打亂
                                                             14
      lazy[L(pos)] += lazy[pos];
24
                                                             15 }
25
       lazy[R(pos)] += lazy[pos];
                                                             16
26
       seg[pos] = seg[pos] + lazy[pos] * size;
                                                             17 void build(int left , int right , int x = 1 ){
       lazy[pos] = 0;
27
                                                                    // left 為題目最大左邊界, right
                                                             18
28 }
                                                                        為題目最大右邊界,圖片最上面的 root
29 void modify(int x, int l, int r, int ql, int qr, int
                                                                        為第一個節點
                                                                    node[x].left = left ; //給 x 節點左右邊界
       if(lazy[x]) push(x, (r - 1) + 1);
30
                                                             19
       // seg[x] = seg[L(x)] + (mid - 1) * lazy[L(x)] +
                                                                    node[x].right = right ;
                                                             20
31
           seg[R(x)] + (r - mid) * lazy[R(x)];
                                                             21
                                                                    if(left == right){
                                                                        //如果左右邊界節點相同,表示這裡是葉節點
       seg[x] += val * (qr - ql + 1);
32
33
       if(q1 <= 1 && qr >= r){
                                                                        node[x].value = num[left]; //把 num 值給
                                                             22
34
           lazy[x] += val;
                                                                            node[x]
35
           return:
                                                                        //這裡的 num 值表示,我們要在 value 要放的值
                                                             23
36
                                                             24
                                                                        return; //向前返回
37
       int mid = (1 + r) >> 1;
                                                                   }
                                                             25
38
       if(qr <= mid) modify(L(x), 1, mid, ql, qr, val);</pre>
                                                                   int mid = (left + right ) / 2 ; //切半,產生二元樹
                                                             26
       else if(ql > mid) modify(R(x), mid + 1, r, ql,
39
                                                             27
           qr, val);
                                                                    //debug
                                                             28
       else{
40
                                                                   //cout << mid << '\n' ;
//cout << x << ' ' << node[x].left << ' ' <<
                                                             29
41
           modify(L(x), 1, mid, ql, mid, val);
                                                             30
42
           modify(R(x), mid + 1, r, mid + 1, qr, val);
                                                                        node[x].right << ' ' << '\n';
43
                                                             31
44 }
                                                                   build(left , mid , Lson(x)) ; //將區間改為 [left,
                                                             32
```

33

mid] 然後帶給左子樹

build(mid + 1 , right , Rson(x)) ; //將區間改為

[mid+1, right] 然後帶給右子樹

45 | 11 query(int x, int 1, int r, int q1, int qr){

if(lazy[x]) push(x, (r - 1) + 1);

(r - 1);

46

47

if(ql <= 1 && qr >= r) return seg[x] + lazy[x] *

```
// 例如我們要查詢 [2, 8],我們只需要查詢 [3,
34
      node[x].value = min(node[Lson(x)].value ,
                                                     90
         node[Rson(x)].value );
                                                               4],不須查詢 [3, 3]、[4, 4],
      //查詢左右子樹哪個數值最小,並讓左右子樹最小值表示此區
                                                           // [3, 4] 已經做到最小值查詢
35
36 }
                                                     92
37
                                                           push_down(x);//有區間修改時才需要寫
                                                     93
38 void modify(int position , int value , int x = 1){
                                                           int mid = (node[x].left + node[x].right ) / 2 ;
                                                     94
                                                               //切半,向下修改
39
      if(node[x].left == position && node[x].right ==
                                                     95
                                                           int ans = INF ; //一開始先假設答案為最大值
         position ){ //找到葉節點
                                                     96
        node[x].value = value ; //修改
40
                                                           if( left <= mid )</pre>
                                                     97
        return ; //傳回
41
                                                               //如果切半後,我們要查詢的區間有在左子樹就向下查詢
42
     }
                                                     98
                                                               ans = min(ans , query(left , right
43
      int mid = (node[x].left + node[x].right ) / 2 ;
                                                                  Lson(x))); //更新答案,比較誰比較小
         //切半,向下修改
                                                           if(mid < right )</pre>
                                                     99
      if(position <= mid )</pre>
44
                                                               //如果切半後,我們要查詢的區間有在右子樹就向下查詢
         //如果要修改的點在左邊,就往左下角追蹤
                                                     100
                                                               ans = min(ans , query(left , right
45
         modify(position , value , Lson(x) );
                                                                  Rson(x))); //更新答案,比較誰比較小
46
      if(mid < position )</pre>
                                                     101
                                                           return ans ; //回傳答案
         //如果要修改的點在右邊,就往右下角追蹤
                                                    102 }
         modify(position , value , Rson(x));
48
      node[x].value = min(node[Lson(x)].value ,
         node[Rson(x)].value );
                                                       4.3 BIT
      //比較左右子樹哪個值比較小,較小值為此節點的 value
49
50
51 }
                                                      1 // BIT
52
                                                       #include <bits/stdc++.h>
53 void push_down(int x, int add){
                                                       #include <ext/pb_ds/assoc_container.hpp>
      //將懶人標記往下推,讓下一層子樹進行區間修改
                                                       #include <ext/pb_ds/tree_policy.hpp>
54
      int lson = Lson(x), rson = Rson(x);
                                                       // #include <ext/pb_ds/detail/standard_policies.hpp>
55
      node[lson].z += add;
                                                       #define IOS
         //給予懶人標記,表示子樹如果要給子樹的子樹區間修改
                                                           ios_base::sync_with_stdio(false);cin.tie(0);cout.tie(0);
      node[rson].z += add;
56
                                                       #define INF 0x3f3f3f3f
         //數值要是多少,左右子樹都需要做
                                                       #define lowbit(x) x&(-x)
57
                                                       using namespace std;
                                                       using namespace __gnu_pbds;
      node[lson].v += add; //更新左右子樹的值
58
      node[rson].v += add;
59
                                                     11
                                                       typedef long long 11;
60 }
                                                       const int N = 2e5 + 5;
                                                     12
61
                                                     13
                                                       11 bit[N], n, q;
62 void update(int a, int b, int cmd, int x = 1){
                                                     14
                                                       11 query(int idx){
63 //a, b 為區間修改的 left and right, cmd 為要增加的數值
                                                     15
                                                           11 \text{ sum} = 0;
                                                           for(int i = idx;i > 0;i -= lowbit(i))
64
      if(a <= node[x].1 && b >= node[x].r){
                                                     16
                                                     17
                                                               sum += bit[i];
65
         //如果節點的 left and right, 跟 a, b
                                                     18
                                                           return sum;
             區間是相等,或更小就,只要在這邊修改 cmd,
                                                     19 }
         //就可以讓 node[x].v
66
                                                       void update(ll val, int idx){
                                                     20
             的值直接變為區間修改後的數值,
                                                           for(int i = idx;i <= n;i += lowbit(i))</pre>
                                                     21
         //之後如果要讓這查詢向子樹進行區間修改,就用
67
                                                               bit[i] += val;
                                                     22
             push down,
                                                       }
                                                     23
         //我們這邊的懶人標記就會告訴左右子樹要修改的值為
68
                                                       int main(){
69
                                                     25
         node[x].v += cmd; //區間修改後的 v
70
                                                           cin >> n >> q;
                                                     26
         node[x].z = cmd; //區間修改是要增加多少數值
                                                           for(int i = 1;i <= n;i++){ // 1-based</pre>
71
                                                     27
                                                               11 in;
72
         return:
                                                     28
                                                               cin >> in;
73
                                                     29
      push_down(x); // 先將之前的區間查詢修改值,往下給子樹以與
                                                               update(in, i);
74
                                                     31
75
      //假如當前的 node[x].z 原本是 3,如果沒有
                                                     32
                                                           while(q--){
         push_down(x),那下面的子樹都沒有被 +3,
                                                               ll o, a, b;
                                                     33
      //導致答案不正確。
76
                                                               cin >> o >> a >> b;
                                                     34
77
                                                     35
                                                               if(o == 1){
      int mid = (node[x].l+node[x].r) / 2;
78
                                                     36
                                                                  ll u = query(a) - query(a - 1);
         //切半,向下修改
                                                     37
                                                                  update(b - u, a);
79
      if(a <= mid) update(a, b, cmd, Lson(x));</pre>
                                                     38
                                                               }
          //如果要修改的點在左邊,就往左下角追蹤
                                                     39
                                                               else{
      if(b > mid) update(a, b, cmd, Rson(x));
80
                                                                  cout << query(b) - query(a - 1) << '\n';</pre>
                                                     40
          //如果要修改的點在右邊,就往右下角追蹤
                                                     41
      node[x].v = node[Lson(x)].v + node[Rson(x)].v;
81
                                                     42
                                                           }
      //比較左右子樹哪個值比較小,較小值為此節點的 value
82
                                                     43
83 }
                                                           return 0;
84 #define INF 0x3f3f3f
                                                     45 }
85
86 int query(int left , int right , int x = 1 ){
87
      if(node[x].left >= left && node[x].right <= right)</pre>
                                                       4.4 Sparse Table
88
         return node[x].Min_Value ;
      //如果我們要查詢的區間比當前節點的區間大,那我們不需再向下查詢直接輸出此答案就好。
89
```

1 #include <bits/stdc++.h>

```
2 #define IOS
                                                                5 typedef long long 11;
       ios_base::sync_with_stdio(false);cin.tie(0);cout.tie(0) 11 mod = 1000000007;
3 #define INF 0x3f3f3f3f
                                                                  struct Matrix{
                                                                      11 \text{ mat}[2][2] = \{\{0\}\};
4 using namespace std;
5 typedef long long 11;
                                                                9
                                                                       Matrix operator * (Matrix &inp){
6 const int N = 5e5 + 5;
                                                               10
                                                                           Matrix tmp;
7 int n, m, arr[N], dp[35][N];
                                                                           for(int i = 0; i < 2; i++){
                                                               11
8 void sparse_table(int n){
                                                                12
                                                                               for(int j = 0; j < 2; j++){
       for(int i = 1; i <= 31; i++){
                                                                                    for(int k = 0; k < 2; k++){
9
                                                               13
           for(int j = 0;(j + (1LL << (i - 1))) < n;j++){}
10
                                                                                        tmp.mat[i][j] = ((tmp.mat[i][j] +
11
                dp[i][j] = max(dp[i - 1][j], dp[i - 1][j]
                                                                                             (mat[i][k] % mod) *
                    + (1LL << (i - 1))]);
                                                                                             (inp.mat[k][j] % mod)) % mod)
12
           }
                                                                                             % mod;
      }
                                                                                   }
13
                                                               15
14 }
                                                               16
                                                                               }
                                                                           }
                                                               17
15 int query(int 1, int r){
       int idx = _{-}lg(r - l + 1);
                                                               18
                                                                           return tmp;
16
17
       return max(dp[idx][1], dp[idx][r - (1LL << idx) +</pre>
                                                               19
                                                               20
                                                                  };
18 }
                                                                  Matrix base;
                                                               21
  int main(){
                                                                  Matrix fast_pow(int exp){
19
                                                               22
20
       IOS
                                                               23
                                                                       if(exp == 1) return base;
       cin >> n;
21
                                                               24
                                                                       if(exp % 2 == 0){
22
       for(int i = 0; i < n; i++) cin >> arr[i];
                                                               25
                                                                           Matrix res = fast_pow(exp >> 1);
23
                                                               26
                                                                           return res * res;
       cin >> m;
       for(int i = 0; i < n; i++) dp[0][i] = arr[i];</pre>
24
                                                               27
                                                                      }
       sparse_table(n);
25
                                                               28
                                                                       Matrix res = fast_pow(exp >> 1);
26
       while(m--){
                                                               29
                                                                       return base * res * res;
           int 1, r;
27
                                                               30
                                                                  }
28
           cin >> 1 >> r;
                                                               31
                                                                  int main(){
           if(1 > r) swap(1, r);
                                                                       IOS
                                                               32
29
30
           1--, r--;
                                                               33
                                                                       base.mat[0][0] = 1;
31
           cout << query(1, r) << '\n';
                                                               34
                                                                       base.mat[0][1] = 4;
32
                                                               35
                                                                       base.mat[1][0] = 2;
33
                                                               36
                                                                       base.mat[1][1] = 3;
34
       return 0:
                                                               37
                                                                       Matrix output = fast_pow(10);
35 }
                                                               38
                                                                       for(int i = 0; i < 2; i++){}
                                                                           for(int j = 0; j < 2; j++){
                                                               39
                                                               40
                                                                               cout << output.mat[i][j] << ' ';</pre>
                                                                           }
                                                               41
       Uncategorized
                                                               42
                                                                           cout << '\n';
                                                               43
                                                                      }
                                                               44
         快速冪
  5.1
                                                               45
                                                                       return 0:
                                                               46 }
1 #include <bits/stdc++.h>
2 #define IOS
      ios_base::sync_with_stdio(false);cin.tie(0);cout.tie(0)5.3 快速計算費氏數列
3 using namespace std;
4 typedef long long 11;
                                                                1 #include <bits/stdc++.h>
5 11 mod = 1000000007;
                                                                  #define IOS
6 11 fast_pow(int base, int exp){
                                                                       ios_base::sync_with_stdio(false);cin.tie(0);cout.tie(0);
7
      11 \text{ res} = 1:
                                                                3 #define INF 0x3f3f3f3f
8
       while(exp > 0){
                                                                  using namespace std;
           if(exp & 1) res = res * base % mod;
9
                                                                  typedef long long 11;
10
           base = base * base % mod;
                                                                6
                                                                  11 \mod = 1000000007;
11
           exp >>= 1;
                                                                  struct Matrix{
                                                                7
12
      }
                                                                       11 mat[2][2] = {{0}};
       return res;
13
                                                                9
                                                                       Matrix operator * (Matrix &inp){
14 }
                                                                           Matrix tmp;
                                                               10
15 int main(){
                                                               11
                                                                           for(int i = 0; i < 2; i++){
16
                                                                               for(int j = 0; j < 2; j++){
                                                               12
17
       int base = 3, exp = 15;
                                                               13
                                                                                    for(int k = 0; k < 2; k++){
18
       cout << fast_pow(base, exp) << '\n';</pre>
                                                               14
                                                                                        tmp.mat[i][j] = ((tmp.mat[i][j] +
19
                                                                                             (mat[i][k] % mod) *
20
       return 0;
                                                                                             (inp.mat[k][j] % mod)) % mod)
21 | }
                                                                                             % mod:
                                                                15
                                                                                   }
                                                                               }
                                                               16
                                                               17
                                                                           }
         矩陣快速冪
                                                               18
                                                                           return tmp;
                                                                      }
                                                               19
1 #include <bits/stdc++.h>
                                                               20 };
```

21 Matrix base;

if(n == 1) return base;

 $if(n \% 2 == 0){$

23

24

ios_base::sync_with_stdio(false);cin.tie(0);cout.tie122 Matrix fast_pow(int n){

2 #define IOS

3 #define INF 0x3f3f3f3f

4 using namespace std;

```
25
           Matrix res = fast_pow(n >> 1);
           return res * res;
26
27
       Matrix res = fast_pow(n >> 1);
28
29
       return base * res * res;
30 }
31 int main(){
       IOS
       base.mat[0][0] = 1;
33
       base.mat[0][1] = 1;
34
35
       base.mat[1][0] = 1;
       base.mat[1][1] = 0;
36
37
       Matrix output = fast_pow(20);
       cout << output.mat[0][0] << '\n';</pre>
38
39
       return 0;
40
41 }
```

6 常用小扣

6.1 01 背包問題

```
1 // 01 backpack
2 for(int i=1;i<=n;i++){
3    for(int j=x;j>=w[i];j--){
4         dp[j]=max(dp[j],dp[j-w[i]]+v[i]);
5    }
6 }
```

6.2 Topological

```
1 // 拓鋪
2 int N, M, u, v, deg[MAXN];
                               // deg[i] 紀錄點 i
      被連入邊數
3 vector<int> edge[MAXN];
5 /*----- 1. 計算 indegree -----*/
6 cin >> N >> M;
7 while(M--)
8 {
      cin >> u >> v;
9
10
      edge[u].push_back(v);
11
      ++deg[v];
12 }
14 /*---- 2. 將 indegree 為 0 的點放入 queue 中
      ----*/
15 queue < int > q;
                              // 紀錄待拔點
  for(int i = 0; i < N; ++i)</pre>
      if(deg[i] == 0)
17
          q.push(i);
18
19
20 /*----- 3. 重複拔點,直到 queue 清空 -----*/
21 while(!q.empty())
22 {
      int cur = q.front(); q.pop();
23
      cout << cur << "\n";
24
      for(int i: edge[cur])
25
26
27
          --deg[i];
                                             // 3-1.
              相連點 indgree 減一
28
          if(deg[i] == 0) q.push(i);
                                      // 3-2. 若該點
              indgree 減至 0,則放入 queue 中
      }
29
30 }
```

6.3 常用

```
1 while(getline(ss,str,'m'))//以m分割
2 cout << str << endl;
3 int a,b; char c;
4 while(ss>>a>c>>b)//處理像是-2/9+9/7
5 cout<<a<" "<<c<<" "<<b<<endl;
6 //輸出 -2 / 9 endl 9 / 7
```

7 Basic

7.1 GCD

```
1 int gcd(int a, int b){
2     if(b == 0) return a;
3     else return gcd(b, a % b);
4 }
```

7.2 LCM

```
1 int lcm(int a, int b){
2    return a * b / gcd(a, b);
3 }
```

7.3 Leap Year

```
1 bool isLeap(int n){
2    if(n % 100 == 0)
3        if(n % 400 == 0) return true;
4        else return false;
5    if(n % 4 == 0) return true;
6    else return false;
7 }
```

8 Trick

8.1 求根號和解決 pow 精度問題

```
1  // when the number is too large, use powl instead of
    pow
2  // will provide you more accuracy.
3  powl(a,b)
4  (int)round(p,(1.0/n)) //nth root of p
```

8.2 查找和二分搜

8.3 $a^b mod p$

```
1  // a^b mod p
2
3  long powmod(long base, long exp , long modulus){
4  base %= modulus;
5  long result = 1;
6  while(exp > 0){
7   if(exp & 1) result = (result * base) %
6       modulus;
8  base = (base * base) % modulus;
9  exp >> 1;
```

```
10
11
       return result;
12 }
  8.4 n!modp
1 // n! mod p
2
3
   int factmod(int n, int p){
       long long res = 1;
4
       while(n > 1){
           res = (res % powmod(p-1 , n/p , p)) %p;
6
7
           for(int i=2;i<=n%p;i++)</pre>
8
               res = (res * i) % p;
           n /= p;
9
10
11 | }
```

8.5 從 1 n 選 M 個數字

```
1 // n >=m choose m number from 1 ~ n
2
  void combination(int n, int m){
       if (n<m) return;</pre>
3
5
       int a[50] = {0};
6
       int k = 0;
7
       for(int i=1;i<=m;i++) a[i] = i;</pre>
8
9
       while(1){
10
            for(int i=1;i<=m;i++)</pre>
                cout << a[i] << " ";
11
12
            cout << endl;</pre>
13
14
            k = m;
            while((k>0) && (n-a[k] == m-k)) k --;
15
            if(k == 0) break;
16
17
            a[k] ++;
            for(int i=k+1;i<=m;i++){</pre>
18
19
                a[i] = a[i-1] + 1;
20
            }
21
       }
22 }
```

8.6 二項式係數 Binomial Coefficient (也可以用在 C 幾取幾)

```
1 #define MAXN 100 // largest n or m
2 long binomial_coefficient(n, m) // compute n choose m
3 int n, m;{
      int i, j;
      long bc[MAXN][MAXN];
      for(i = 0;i <= n;i++) bc[i][0] = 1;
7
      for(j = 0; j \le n; j++) bc[j][j] = 1;
8
      for(i = 1;i <= n;i++)
9
          for(j = 1; j < i; j++)
10
               bc[i][j] = bc[i - 1][j - 1] + bc[i -
11
      reutrn bc[n][m];
12 }
```

8.7 LICS

```
int a[100] = {0};
int b[100] = {0};
int f[100] = {0};
int n = 0, m = 0;
int main(void){
   cin >> n;
   for(int i = 1; i <= n; i++) cin >> a[i];
```

```
cin >> m;
       for(int i = 1; i <= m; i++) cin >> b[i];
9
       for(int i = 1; i <= n; i++){</pre>
10
           int k = 0;
11
12
            for(int j = 1; j \le m; j++){
                if(a[i] > b[j] && f[j] > k) k = f[j];
13
                else if(a[i] == b[j] && k + 1 > f[j])
14
                     f[j] = k + 1;
           }
15
       }
16
17 }
```

8.8 m-ary to 10-ary

```
1 string num = "0123456789ABCDE";
  int mToTen(string n, int m){
      int multi = 1;
4
5
      int result = 0;
6
7
       for(int i = n.size() - 1;i >= 0;i--){
8
           result += num.find(n[i]) * multi;
           multi *= m;
9
10
11
       return result;
12 }
```

9 Math

9.1 ModInverse

```
1 // 求 a 在模 m 下的模反元素, m 必須是質數
2 ll modInverse(ll a, ll m) {
3     ll res = 1, exp = m - 2;
4     while (exp > 0) {
5         if (exp % 2 == 1) res = (res * a) % m;
6         a = (a * a) % m;
7         exp /= 2;
8     }
9     return res;
10 }
```

9.2 CRT

```
1 | 11 extendedGCD(11 a, 11 b, 11 &x, 11 &y){
       if(b == 0){
           x = 1, y = 0;
4
           return a;
6
      ll x1, y1;
      11 g = extendedGCD(b, a % b, x1, y1);
8
       x = y1;
       y = x1 - (a / b) * y1;
9
10
11 }
12
13 | 11 chineseRemainder(vector<11> &n, vector<11> &a){
       11 \text{ prod} = 1;
14
15
       for(ll num : n) prod *= num; // Calculate the
           product of all moduli
16
       11 \text{ result = 0};
17
18
       for(int i = 0; i < n.size(); i++){</pre>
           11 p = prod / n[i]; // Product divided by
19
               current modulus
           11 x, y;
20
21
           extendedGCD(p, n[i], x, y); // Solve p * x
                1 (mod n[i])
22
           result = (result + a[i] * x * p) % prod; //
                Add current term to result
```

9.3 LinearCongruence

```
1 | 11 solveLinearCongruence(11 a, 11 b, 11 m){
      11 x, y;
2
      11 g = extendedGCD(a, m, x, y); // Solve a * x +
3
         m * y = gcd(a, m)
      if (b % g != 0) return -1; // No solution if
4
          gcd(a, m) does not divide b
5
6
      x = (x * (b / g)) % m;
      if (x < 0) x += m; // Ensure the result is
         positive
8
      return x;
9 }
```