



UNIVERSITY OF RAJSHAHI

DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING

CSE4222 COMPUTER GRAPHICS LAB

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## Lab Report

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# Chapter 1

## Lab Manual

### 1.1 Lab Question

#### 1.1.1 Experiment:

1. Implement the Cohen-Sutherland Line Clipping algorithm
2. Implement the Sutherland-Hodgman Polygon Clipping algorithm
3. Create the Bezier Curve
4. Simulate two-dimensional geometric Translation, Rotation, and Scaling
5. Draw a line with the Bresenham Line Drawing algorithm
6. Draw a circle with the Bresenham Circle Drawing algorithm
7. Draw the Snowflake Pattern with Fractal Geometry

# Chapter 2

## Python Code

### 2.1 Sutherland-Hodgeman Line Clipping

#### 2.1.1 Code:

```
1 import matplotlib.pyplot as plt
2 import matplotlib.patches as patches
3
4 INSIDE=0
5 LEFT=1
6 RIGHT=2
7 BOTTOM=4
8 UP=8
9
10 def compute_outcode(x,y,xmin,ymin,xmax,ymax):
11     code = INSIDE
12     if x<xmin:
13         code|=LEFT
14     elif x>xmax:
15         code|=RIGHT
16     elif y<ymin:
17         code|=BOTTOM
18     elif y>ymax:
19         code|=UP
20     return code
21 def cohen_sutherland_clipping(x1,y1,x2,y2,xmin,ymin,xmax,ymax):
22     outcode1=compute_outcode(x1,y1,xmin,ymin,xmax,ymax)
23     outcode2=compute_outcode(x2,y2,xmin,ymin,xmax,ymax)
24     accepted=False
25     while True:
26         if not(outcode1|outcode2):
27             accepted=True
28             break
29         elif (outcode1&outcode2):
30             break
31         else:
32             outcode_out=outcode1 if outcode1 else outcode2
33             x,y=0,0
34             if outcode_out&UP:
35                 x=x1+(x2-x1)*(ymax-y1)/(y2-y1)
36                 y=ymax
37             elif outcode_out&BOTTOM:
38                 x=x1+(x2-x1)*(ymin-y1)/(y2-y1)
39                 y=ymin
40             elif outcode_out&LEFT:
41                 x=xmin
42                 y=y1+(y2-y1)*(xmin-x1)/(x2-x1)
```

```

43         elif outcode_out & RIGHT:
44             x = xmax
45             y = y1 + (y2 - y1) * (xmax - x1) / (x2 - x1)
46         if outcode_out == outcode1:
47             x1, y1 = x, y
48             outcode1 = compute_outcode(x1, y1, xmin, ymin, xmax, ymax)
49         else:
50             x2, y2 = x, y
51             outcode2 = compute_outcode(x2, y2, xmin, ymin, xmax, ymax)
52     return accepted, x1, y1, x2, y2
53 def visualize(window, lines):
54     fig, ax = plt.subplots(1, len(lines), figsize=(5 * len(lines), 5))
55     if len(lines) == 1:
56         ax = [ax]
57     xmin, ymin, xmax, ymax = window
58     for i, (title, line) in enumerate(lines.items()):
59         x1, y1, x2, y2 = line
60         clip_rect = patches.Rectangle((xmin, ymin), xmax - xmin, ymax - ymin, linewidth
=1.5, edgecolor='red', facecolor='none', linestyle='--')
61         ax[i].add_patch(clip_rect)
62         ax[i].plot([x1, x2], [y1, y2], 'gray', linestyle=':', marker='o', label='
Original Line')
63         accepted, cl_x1, cl_y1, cl_x2, cl_y2 = cohen_sutherland_clipping(x1, y1, x2, y2,
xmin, ymin, xmax, ymax)
64         if accepted:
65             ax[i].plot([cl_x1, cl_x2], [cl_y1, cl_y2], 'blue', marker='o', label="
Clipped LLine")
66             print(f"{title} : Accepted. Clipped to ({cl_x1:.2f},{cl_y1:.2f})-({
cl_x2:.2f},{cl_y2:.2f})")
67         else:
68             print(f"{title} : Rejected")
69         ax[i].set_title(title)
70         ax[i].set_xlim(0, 20)
71         ax[i].set_ylim(0, 20)
72         ax[i].set_aspect('equal', adjustable='box')
73         ax[i].legend()
74         ax[i].grid(True)
75     plt.tight_layout()
76     plt.show()
77
78 if __name__ == "__main__":
79     CLIP_WINDOW = (5, 5, 15, 15)
80
81     test_lines = {
82         "1. Fully Inside": (6, 6, 14, 14),
83         "2. Fully Outside (Reject)": (1, 1, 4, 4),
84         "3. Crossing One Boundary": (1, 10, 10, 10),
85         "4. Crossing Two Boundaries": (4, 18, 16, 2),
86         "5. Diagonal Corner Crossing": (16, 16, 4, 4),
87         "6. Vertical Line": (10, 1, 10, 19),
88     }
89
90     visualize(CLIP_WINDOW, test_lines)

```

## 2.1.2 Output:

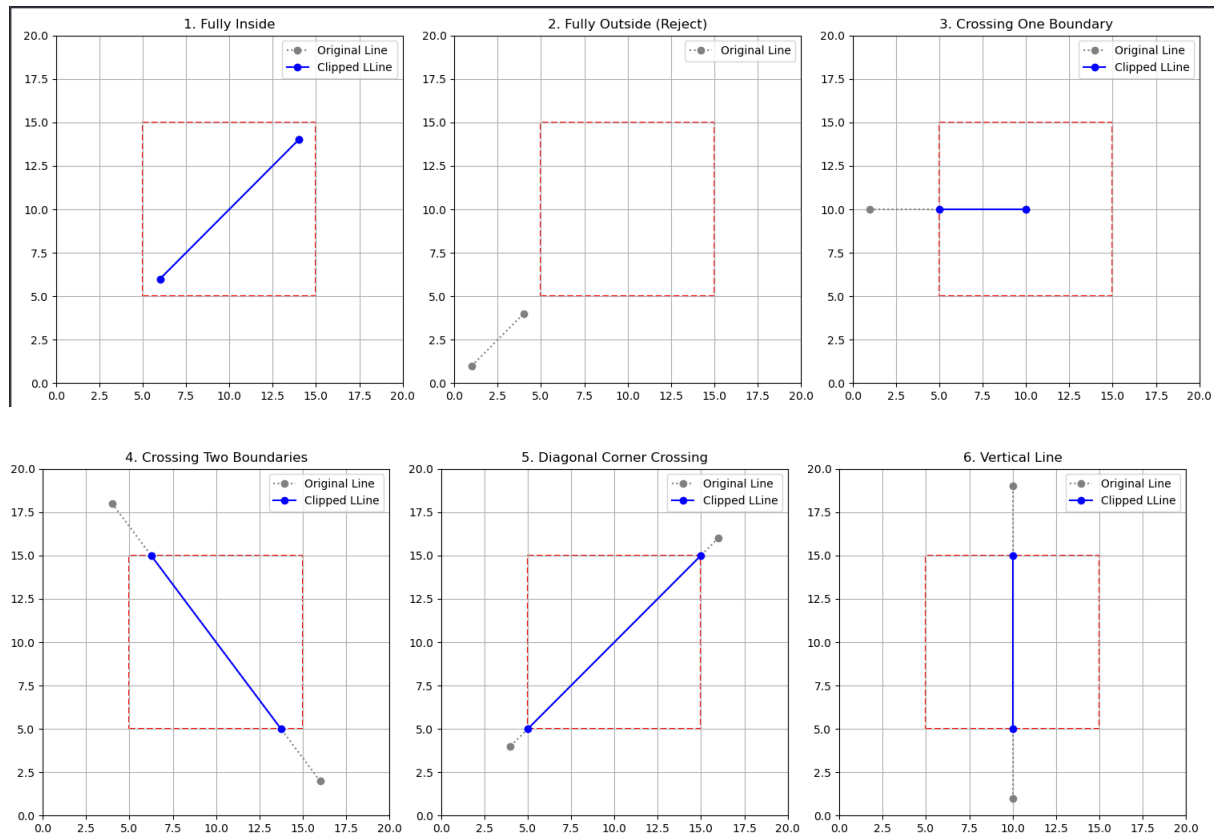


Figure 2.1: Sutherland-Hodgeman Line Clipping

## 2.2 Sutherland-Hodgeman Polygon Clipping

### 2.2.1 Code:

```
1 import matplotlib.pyplot as plt
2 import matplotlib.patches as patches
3
4 LEFT = 0
5 RIGHT = 1
6 BOTTOM = 2
7 TOP = 3
8
9 def is_inside(p, edge, clip_value):
10     x, y = p
11     if edge == LEFT:
12         return x >= clip_value
13     elif edge == RIGHT:
14         return x <= clip_value
15     elif edge == BOTTOM:
16         return y >= clip_value
17     elif edge == TOP:
18         return y <= clip_value
19     return False
20
21 def get_intersection(p1, p2, edge, clip_value):
22     x1, y1 = p1
23     x2, y2 = p2
24     dx = x2 - x1
25     dy = y2 - y1
26
27     if edge == LEFT or edge == RIGHT:
28         if dx == 0:
29             return (clip_value, y1)
30         y = y1 + dy * (clip_value - x1) / dx
31         return (clip_value, y)
32
33     elif edge == BOTTOM or edge == TOP:
34         if dy == 0:
35             return (x1, clip_value)
36         x = x1 + dx * (clip_value - y1) / dy
37         return (x, clip_value)
38
39 def clip_polygon_against_edge(polygon, edge, clip_value):
40     output_polygon = []
41     if not polygon:
42         return output_polygon
43
44     s = polygon[-1]
45
46     for p in polygon:
47         s_inside = is_inside(s, edge, clip_value)
48         p_inside = is_inside(p, edge, clip_value)
49
50         # Case 1: Both points are inside -> Add the second point
51         if s_inside and p_inside:
52             output_polygon.append(p)
53         # Case 2: S is inside, P is outside -> Add intersection only
54         elif s_inside and not p_inside:
55             intersection = get_intersection(s, p, edge, clip_value)
56             output_polygon.append(intersection)
57         # Case 3: S is outside, P is inside -> Add intersection AND the second
point
58         elif not s_inside and p_inside:
```

```

59         intersection = get_intersection(s, p, edge, clip_value)
60         output_polygon.append(intersection)
61         output_polygon.append(p)
62         # Case 4: Both points are outside -> Do nothing
63
64         s = p # Move to the next edge
65     return output_polygon
66
67 def sutherland_hodgman_polygon_clip(polygon, clip_window):
68     x_min, y_min, x_max, y_max = clip_window
69
70     clipped = clip_polygon_against_edge(polygon, LEFT, x_min)
71     clipped = clip_polygon_against_edge(clipped, RIGHT, x_max)
72     clipped = clip_polygon_against_edge(clipped, BOTTOM, y_min)
73     clipped = clip_polygon_against_edge(clipped, TOP, y_max)
74
75     return clipped
76
77 def plot_polygons(polygon, window, clipped):
78     fig, ax = plt.subplots()
79
80     poly_org = patches.Polygon(polygon, closed=True, edgecolor='red', facecolor=
'none', linestyle='--', linewidth=2, label='Original Polygon')
81     ax.add_patch(poly_org)
82
83     x_min, y_min, x_max, y_max = window
84     rect = patches.Rectangle((x_min, y_min), x_max - x_min, y_max - y_min,
85                             linewidth=2, facecolor='none', edgecolor='green',
linestyle=':', label='Clipping Window')
86     ax.add_patch(rect)
87
88     if clipped:
89         poly_clipped = patches.Polygon(clipped, closed=True, edgecolor='blue',
linewidth=2, facecolor='blue', alpha=0.4, label='Clipped Polygon')
90         ax.add_patch(poly_clipped)
91
92     ax.set_title("Sutherland-Hodgman Polygon Clipping")
93     ax.legend()
94     ax.set_aspect('equal', 'box')
95
96     all_points = polygon + [(x_min, y_min), (x_max, y_max)]
97     all_x = [p[0] for p in all_points]
98     all_y = [p[1] for p in all_points]
99     plt.xlim(min(all_x) - 20, max(all_x) + 20)
100    plt.ylim(min(all_y) - 20, max(all_y) + 20)
101
102    plt.grid(True)
103    plt.show()
104
105 if __name__ == "__main__":
106     subject_polygon = [(50, 150), (200, 50), (350, 150), (100, 250), (200,150)]
107     clip_window = (100, 100, 300, 200)
108
109     clipped_polygon = sutherland_hodgman_polygon_clip(subject_polygon,
clip_window)
110
111     print("Original Polygon Vertices:", subject_polygon)
112     print("Clipped Polygon Vertices:", clipped_polygon)
113
114     plot_polygons(subject_polygon, clip_window, clipped_polygon)

```



### 2.2.2 Output:

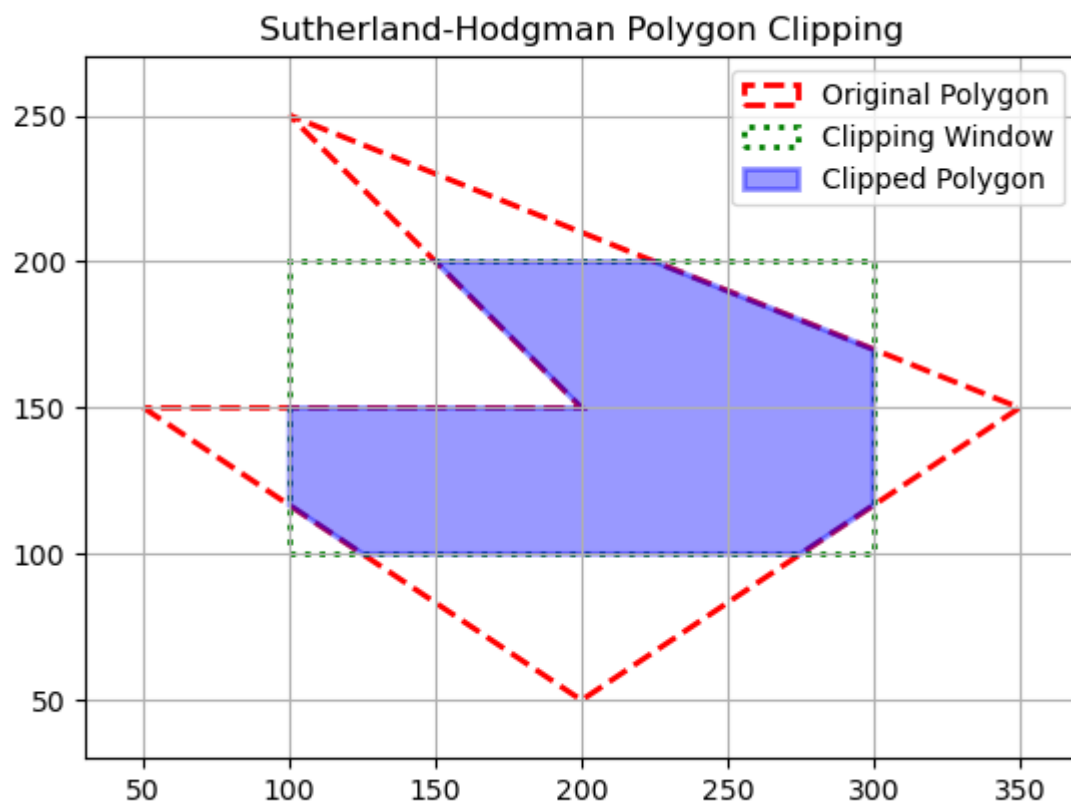


Figure 2.2: Sutherland-Hodgeman Polygon Clipping

## 2.3 Translation

### 2.3.1 Code:

```
1 import matplotlib.pyplot as plt
2 import numpy as np
3
4 def plot_shape(shape, title="", color='blue'):
5     plt.plot(shape[:, 0], shape[:, 1], color=color, marker='o', linestyle='-',
6             label=title)
7
8 def get_traslation_matrix(tx,ty):
9     return np.array([
10         [1,0,tx],
11         [0,1,ty],
12         [0,0,1]
13     ])
14
15 def transformation(shape,matrix):
16     homogeneous_shape=np.hstack([shape,np.ones((shape.shape[0],1))])
17     transformed_shape=(matrix@homogeneous_shape.T).T
18     return transformed_shape[:, :2]
19
20 if __name__=="__main__":
21     house_shape=np.array([
22         [0, 0], [0, 10], [5, 15], [10, 10], [10, 0], [0, 0]
23     ])
24
25     tx,ty=23,30
26     translation_matrix= get_traslation_matrix(tx,ty)
27     translated_house= transformation(house_shape,translation_matrix)
28
29     plt.figure(figsize=(12,8))
30     ax=plt.gca()
31     ax.set_aspect('equal',adjustable='box')
32     plot_shape(house_shape,"Original",'gray')
33     plot_shape(translated_house,f"Translated by [{tx},{ty}]", "purple")
34     plt.title("2D Geometric Transformations")
35     plt.xlabel("X-axis")
36     plt.ylabel("Y-axis")
37     plt.legend()
38     plt.grid(True)
39     plt.show()
```

### 2.3.2 Output:

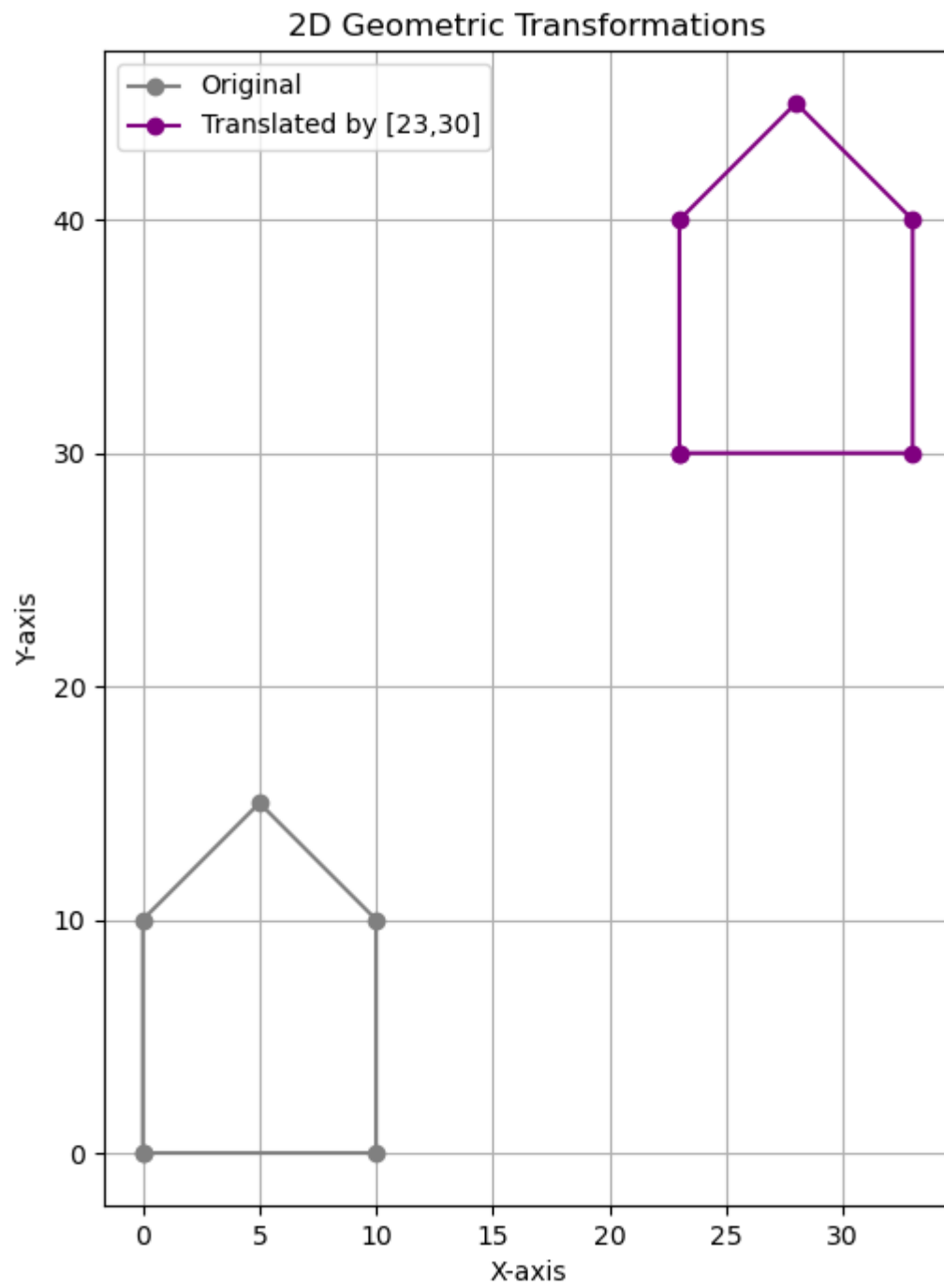


Figure 2.3: Translation

## 2.4 Rotation

### 2.4.1 Code:

```
1 import matplotlib.pyplot as plt
2 import numpy as np
3
4 def plot_shape(shape, title="", color='blue'):
5     plt.plot(shape[:, 0], shape[:, 1], color=color, marker='o', linestyle='-',
6             label=title)
7
8 def get_rotation_matrix(angles):
9     cos_a=np.cos(angles)
10    sin_a=np.sin(angles)
11    return np.array([
12        [cos_a,-sin_a,0],
13        [sin_a,cos_a,0],
14        [0,0,1]
15    ])
16 def transformation(shape,matrix):
17     homogeneous_shape=np.hstack([shape,np.ones((shape.shape[0],1))])
18     transformed_shape=(matrix@homogeneous_shape.T).T
19     return transformed_shape[:, :2]
20
21 if __name__=="__main__":
22     house_shape=np.array([
23         [0, 0], [0, 10], [5, 15], [10, 10], [10, 0], [0, 0]
24     ])
25
26     angles=75
27     rotation_matrix= get_rotation_matrix(angles)
28     rotated_house= transformation(house_shape,rotation_matrix)
29
30     plt.figure(figsize=(12,8))
31     ax=plt.gca()
32     ax.set_aspect('equal',adjustable='box')
33     plot_shape(house_shape,"Original",'gray')
34     plot_shape(rotated_house,f"Rotated by [{angles}]", "purple")
35     plt.title("2D Geometric Transformations")
36     plt.xlabel("X-axis")
37     plt.ylabel("Y-axis")
38     plt.legend()
39     plt.grid(True)
40     plt.show()
```

### 2.4.2 Output:

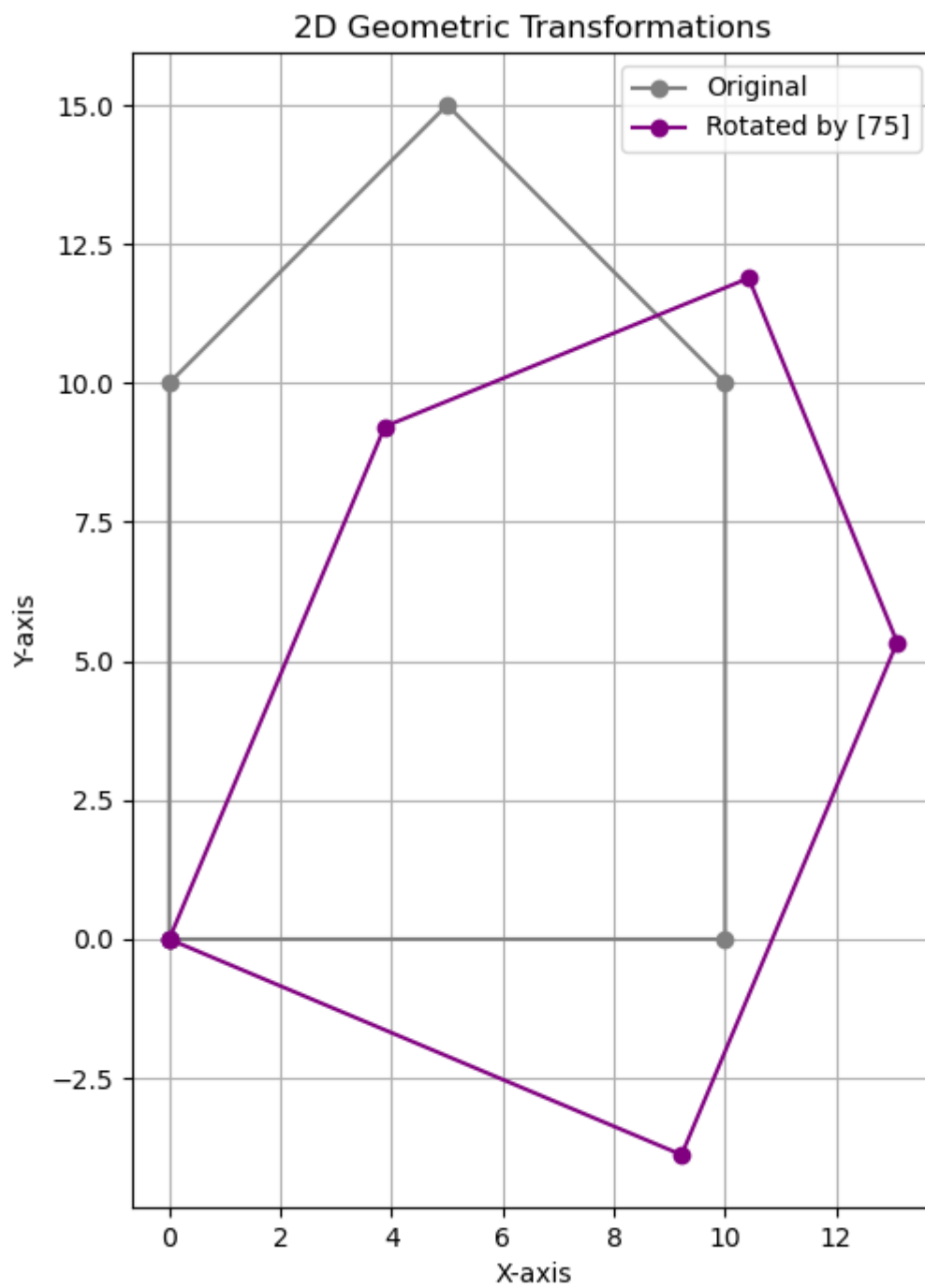


Figure 2.4: Rotation

## 2.5 Scaling

### 2.5.1 Code:

```
1 import matplotlib.pyplot as plt
2 import numpy as np
3
4 def plot_shape(shape, title="", color='blue'):
5     plt.plot(shape[:, 0], shape[:, 1], color=color, marker='o', linestyle='-',
6             label=title)
7
8 def get_scaling_matrix(sx,sy):
9     return np.array([
10         [sx,0,0],
11         [0,sy,0],
12         [0,0,1]
13     ])
14 def transformation(shape,matrix):
15     homogeneous_shape=np.hstack([shape,np.ones((shape.shape[0],1))])
16     transformed_shape=(matrix@homogeneous_shape.T).T
17     return transformed_shape[:, :2]
18
19 if __name__=="__main__":
20     house_shape=np.array([
21         [0, 0], [0, 10], [5, 15], [10, 10], [10, 0], [0, 0]
22     ])
23
24     sx,sy=2,0.5
25     scaling_matrix= get_scaling_matrix(sx,sy)
26     rotated_house= transformation(house_shape,scaling_matrix)
27
28     plt.figure(figsize=(12,8))
29     ax=plt.gca()
30     ax.set_aspect('equal',adjustable='box')
31     plot_shape(house_shape,"Original",'gray')
32     plot_shape(rotated_house,f"Scaled by [{sx},{sy}]", "purple")
33     plt.title("2D Geometric Transformations")
34     plt.xlabel("X-axis")
35     plt.ylabel("Y-axis")
36     plt.legend()
37     plt.grid(True)
38     plt.show()
```

### 2.5.2 Output:

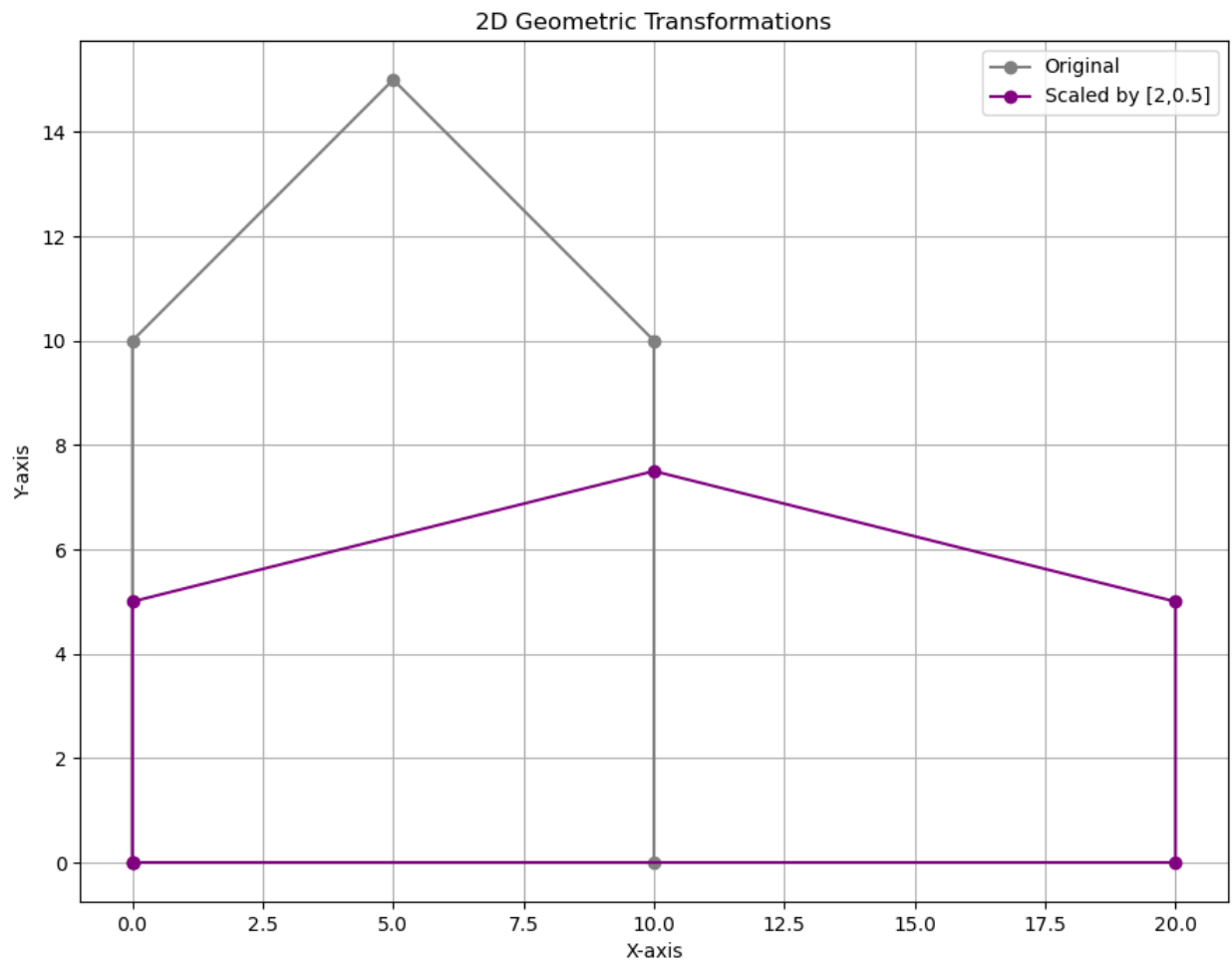


Figure 2.5: Scaling

## 2.6 Translation and Rotation

### 2.6.1 Code:

```
1 import matplotlib.pyplot as plt
2 import numpy as np
3
4 def plot_shape(shape, title="", color='blue'):
5     plt.plot(shape[:, 0], shape[:, 1], color=color, marker='o', linestyle='-',
6             label=title)
7
8 def get_traslation_matrix(tx,ty):
9     return np.array([
10         [1,0,tx],
11         [0,1,ty],
12         [0,0,1]
13     ])
14
15 def get_rotation_matrix(angles):
16     cos_a=np.cos(angles)
17     sin_a=np.sin(angles)
18     return np.array([
19         [cos_a,-sin_a,0],
20         [sin_a,cos_a,0],
21         [0,0,1]
22     ])
23
24 def transformation(shape,matrix):
25     homogeneous_shape=np.hstack([shape,np.ones((shape.shape[0],1))])
26     transformed_shape=(matrix@homogeneous_shape.T).T
27     return transformed_shape[:, :2]
28
29 if __name__=="__main__":
30     house_shape=np.array([
31         [0, 0], [0, 10], [5, 15], [10, 10], [10, 0], [0, 0]
32     ])
33
34     tx,ty=5,10
35     translation_matrix= get_traslation_matrix(tx,ty)
36     translated_house= transformation(house_shape,translation_matrix)
37     angles=-130
38     rotation_matrix= get_rotation_matrix(angles)
39     rotated_house= transformation(translated_house,rotation_matrix)
40
41     plt.figure(figsize=(12,8))
42     ax=plt.gca()
43     ax.set_aspect('equal',adjustable='box')
44     plot_shape(house_shape,"Original",'gray')
45     plot_shape(rotated_house,f"Translated and Rotate the house","purple")
46     plt.title("2D Geometric Transformations")
47     plt.xlabel("X-axis")
48     plt.ylabel("Y-axis")
49     plt.legend()
50     plt.grid(True)
51     plt.show()
```



### 2.6.2 Output:

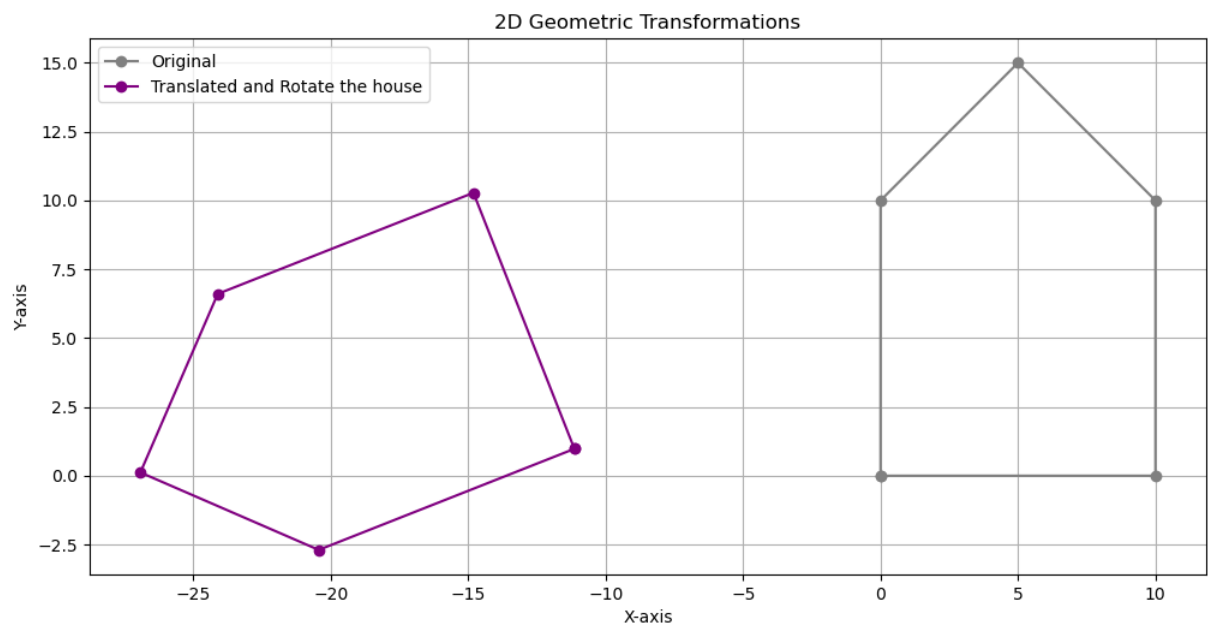


Figure 2.6: Translation and Rotation

## 2.7 Scaling and Rotation

### 2.7.1 Code:

```
1 import matplotlib.pyplot as plt
2 import numpy as np
3
4 def plot_shape(shape, title="", color='blue'):
5     plt.plot(shape[:, 0], shape[:, 1], color=color, marker='o', linestyle='-',
6             label=title)
7
8 def get_scaling_matrix(sx,sy):
9     return np.array([
10         [sx,0,0],
11         [0,sy,0],
12         [0,0,1]
13     ])
14 def get_rotation_matrix(angles):
15     cos_a=np.cos(angles)
16     sin_a=np.sin(angles)
17     return np.array([
18         [cos_a,-sin_a,0],
19         [sin_a,cos_a,0],
20         [0,0,1]
21     ])
22
23
24 def transformation(shape,matrix):
25     homogeneous_shape=np.hstack([shape,np.ones((shape.shape[0],1))])
26     transformed_shape=(matrix@homogeneous_shape.T).T
27     return transformed_shape[:, :2]
28
29 if __name__=="__main__":
30     house_shape=np.array([
31         [0, 0], [0, 10], [5, 15], [10, 10], [10, 0], [0, 0]
32     ])
33
34     sx,sy=2,0.5
35     scaling_matrix= get_scaling_matrix(sx,sy)
36     scaled_house= transformation(house_shape,scaling_matrix)
37     angles=75
38     rotation_matrix= get_rotation_matrix(angles)
39     scaled_rot_house= transformation(scaled_house,rotation_matrix)
40
41     plt.figure(figsize=(12,8))
42     ax=plt.gca()
43     ax.set_aspect('equal',adjustable='box')
44     plot_shape(house_shape,"Original",'gray')
45     plot_shape(scaled_rot_house,f"Scaled and Rotated","purple")
46     plt.title("2D Geometric Transformations")
47     plt.xlabel("X-axis")
48     plt.ylabel("Y-axis")
49     plt.legend()
50     plt.grid(True)
51     plt.show()
```

### 2.7.2 Output:

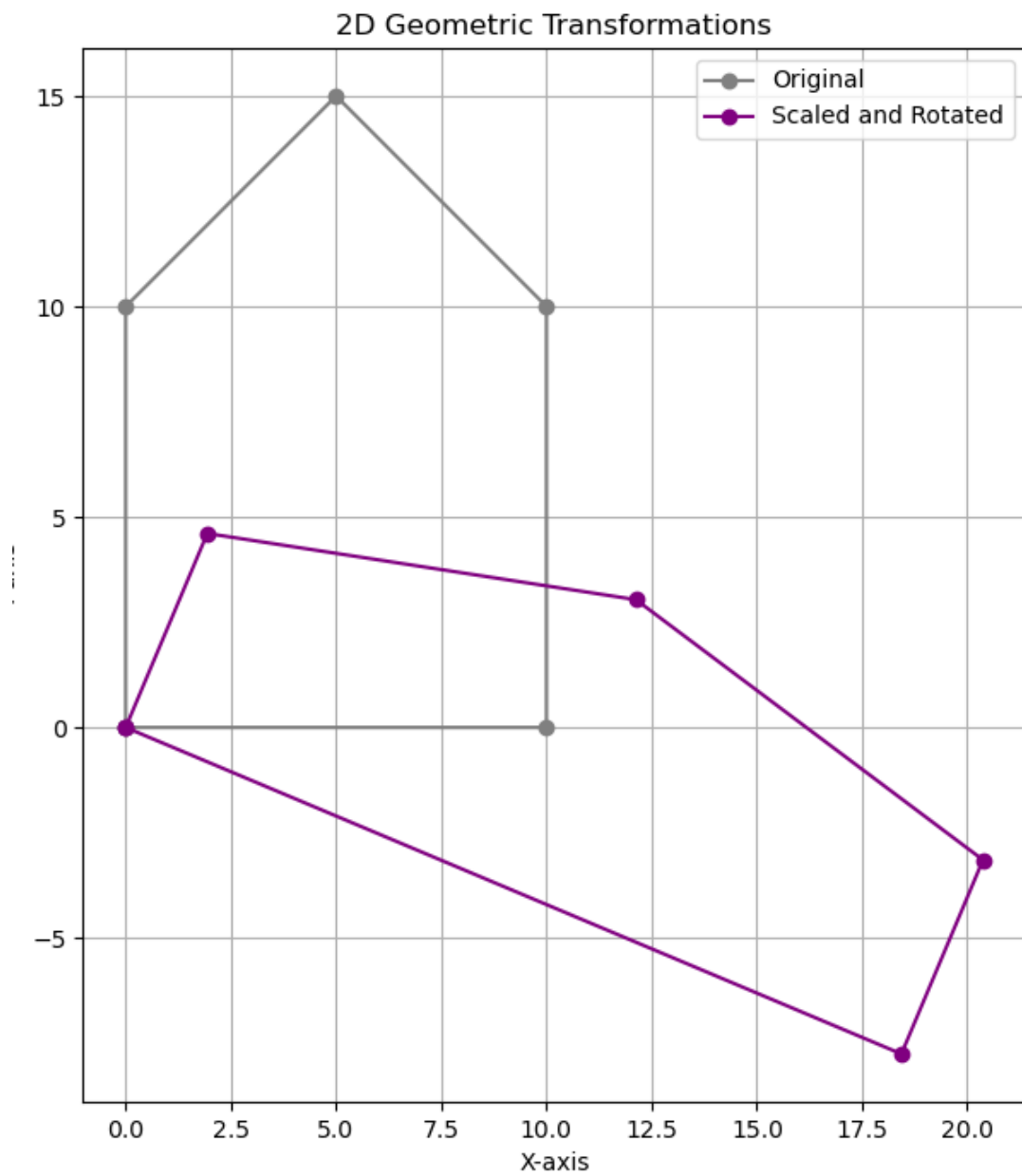


Figure 2.7: Scaling and Rotation

## 2.8 Beizer Curve

### 2.8.1 Code:

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3 from scipy.special import comb
4
5 def Beizer_curve(control_points,n_points=100):
6     n=len(control_points)-1
7     if n<1:
8         raise ValueError("At least two points required.")
9     control_points=np.array(control_points,dtype=float)
10    t=np.linspace(0,1,n_points)
11    curve=np.zeros((n_points,2))
12    for i in range(n+1):
13        bernstain_polygon=comb(n,i)*(t**i)*((1-t)**(n-i))
14        curve+=np.outer(bernstain_polygon,control_points[i])
15    return curve
16 def plot_curve_with_control_points(curve,control_points,title="Beizer Curve"):
17     control_points=np.array(control_points)
18     plt.figure(figsize=(10,8))
19     plt.plot(curve[:,0],curve[:,1],"b-",lw=2,label="Beizer Curve")
20     plt.plot(control_points[:,0],control_points[:,1],'ro--',label="Control
    Polygon")
21     plt.plot(control_points[:,0],control_points[:,1],'go',markersize=10,label='
    Control Points')
22     for i,(x,y) in enumerate(control_points):
23         plt.text(x+5,y,f'P{i}',fontsize=14,verticalalignment='bottom')
24     plt.title(title,fontsize=16)
25     plt.xlabel('X')
26     plt.ylabel('Y')
27     plt.legend()
28     plt.grid(True)
29     plt.axis('equal')
30     plt.show()
31 if __name__=="__main__":
32     quadratic_control_points = [
33         (50, 250),
34         (150, -250),
35         (200, 250),
36         (250, -250),
37         (300, 250),
38         (350, -250)
39     ]
40     quadratic_curve=Beizer_curve(quadratic_control_points)
41     plot_curve_with_control_points(quadratic_curve,quadratic_control_points,
    title="Quadratic Beizer Curve")
```

### 2.8.2 Output:

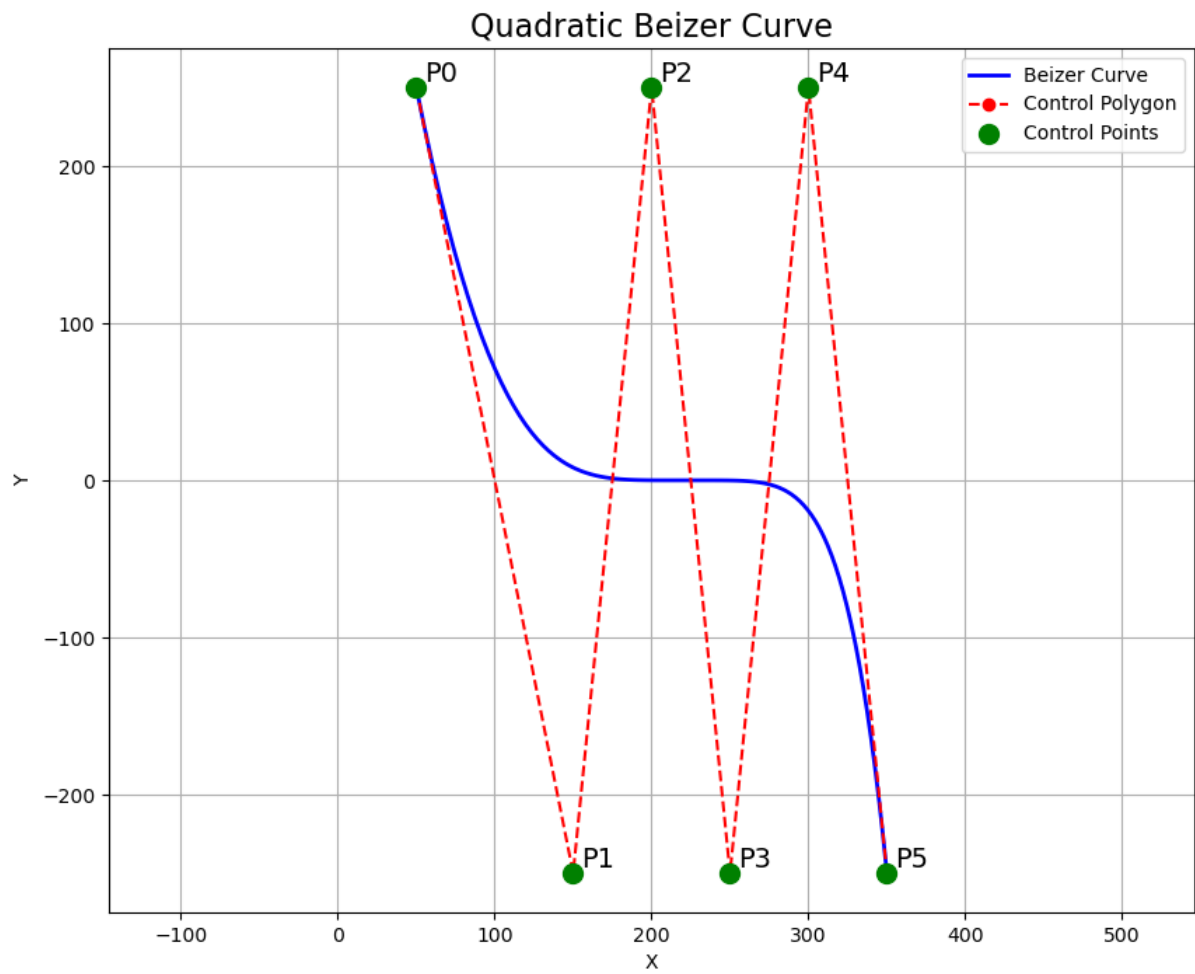


Figure 2.8: Beizer Curve

## 2.9 Bresenham Line Drawing

### 2.9.1 Code:

```
1
2 # bresenham.py
3 from PIL import Image
4
5 def bresenham(x0, y0, x1, y1):
6     """Return list of (x,y) integer points on the line from (x0,y0) to (x1,y1).
7     """
8     points = []
9     dx = abs(x1 - x0)
10    dy = abs(y1 - y0)
11    sx = 1 if x0 < x1 else -1
12    sy = 1 if y0 < y1 else -1
13
14    err = dx - dy
15    x, y = x0, y0
16
17    while True:
18        points.append((x, y))
19        if x == x1 and y == y1:
20            break
21        e2 = 2 * err
22        if e2 > -dy:
23            err -= dy
24            x += sx
25        if e2 < dx:
26            err += dx
27            y += sy
28    return points
29
30 if __name__ == "__main__":
31     # Demo: draw a few lines and save as PNG
32     W, H = 200, 200
33     img = Image.new("RGB", (W, H), "white")
34     px = img.load()
35
36     lines = [
37         (10, 190, 190, 10), # other diagonal
38     ]
39
40     for (x0, y0, x1, y1) in lines:
41         for x, y in bresenham(x0, y0, x1, y1):
42             if 0 <= x < W and 0 <= y < H:
43                 px[x, y] = (0, 0, 0) # black pixel
44
45     img.save("bresenham_demo.png")
46     print("Saved bresenham_demo.png")
```

### 2.9.2 Output:

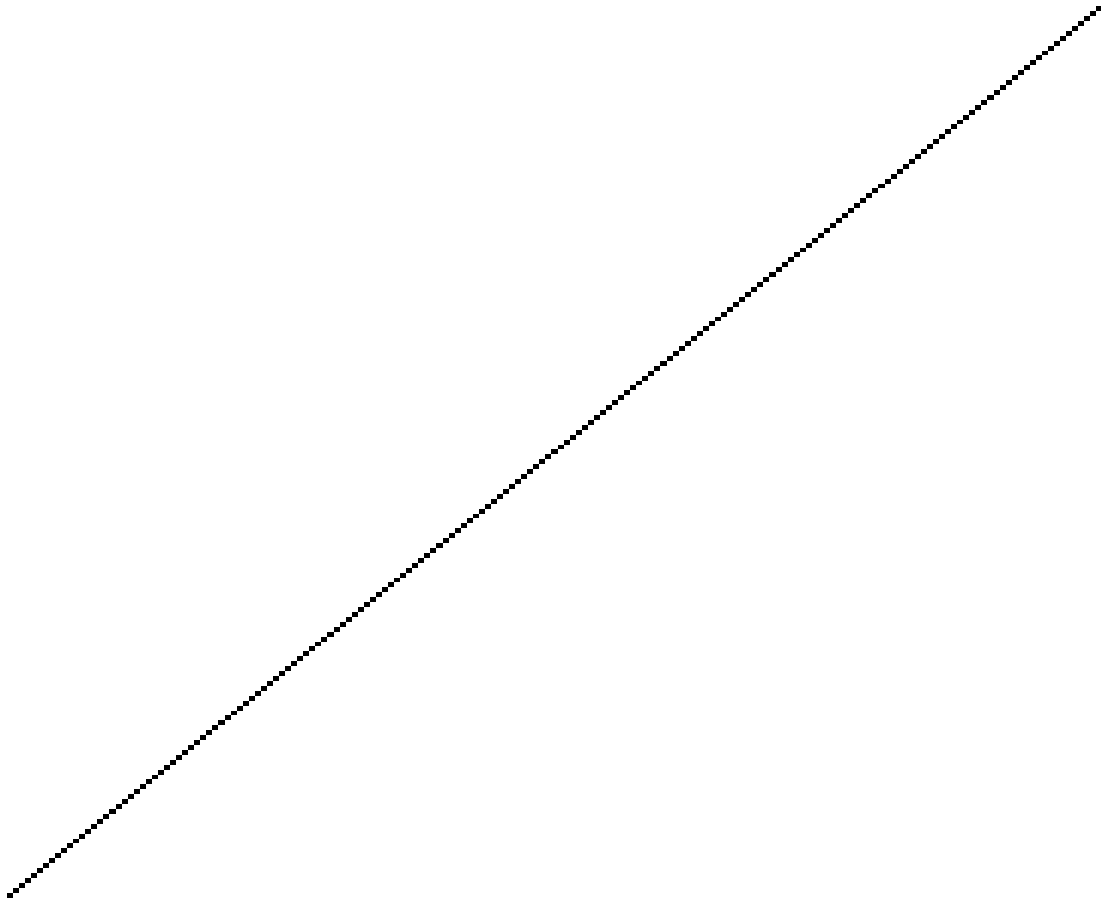


Figure 2.9: Bresenham Line Drawing

## 2.10 Bresenham Circle Drawing

### 2.10.1 Code:

```
1 import matplotlib.pyplot as plt
2
3 def plot_circle_points(xc,yc,x,y,points):
4     points.extend([
5         (xc + x, yc + y),
6         (xc - x, yc + y),
7         (xc + x, yc - y),
8         (xc - x, yc - y),
9         (xc + y, yc + x),
10        (xc - y, yc + x),
11        (xc + y, yc - x),
12        (xc - y, yc - x)
13    ])
14
15 def Bresenham_circle(xc,yc,r):
16     x=0
17     y=r
18     d=3-2*r
19     points=[]
20     while x<=y:
21         plot_circle_points(xc,yc,x,y,points)
22         if d<0:
23             d=d+4*x+6
24         else:
25             d=d+4*(x-y)+10
26             y=y-1
27             x+=1
28     return points
29 if __name__=="__main__":
30     xc,yc,r=-10,34,50
31     circle_points=Bresenham_circle(xc,yc,r)
32     x_vals,y_vals=zip(*circle_points)
33     plt.figure(figsize=(6,6))
34     plt.scatter(x_vals, y_vals, color='blue', s=10)
35     plt.gca().set_aspect('equal', adjustable='box')
36     plt.grid(True)
37     plt.show()
```



### 2.10.2 Output:

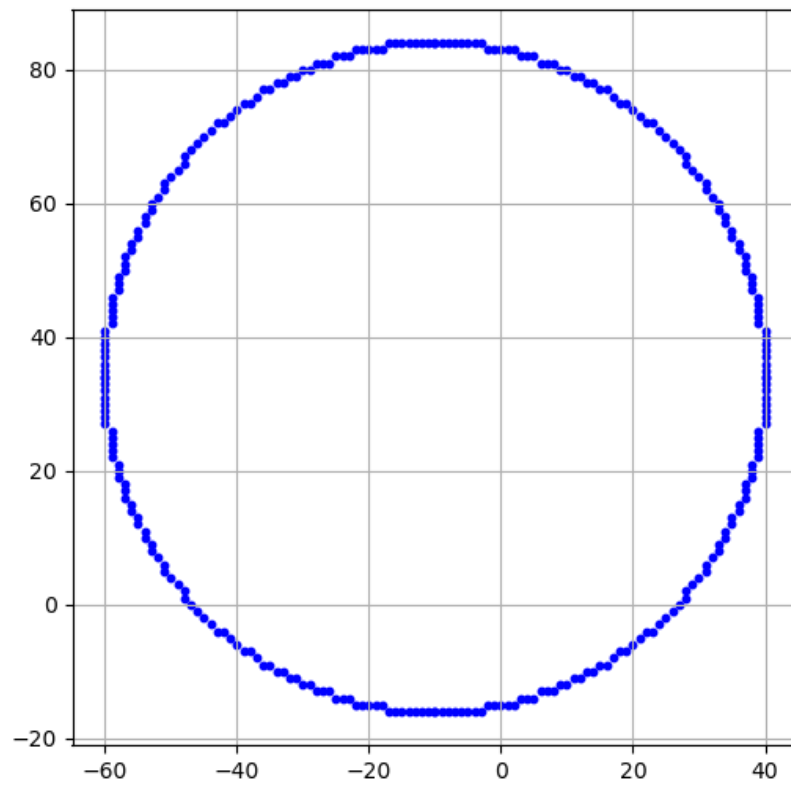


Figure 2.10: Bresenham Circle Drawing

## 2.11 Snowflake Pattern with Fractal Geometry

### 2.11.1 Code:

```
1 import matplotlib.pyplot as plt
2 import numpy as np
3
4 def koch_snowflake(order, scale=10):
5
6     def initial_triangle(scale):
7         # Equilateral triangle vertices (upward triangle)
8         p1 = np.array([0, 0])
9         p2 = np.array([scale, 0])
10        p3 = np.array([scale/2, scale*np.sqrt(3)/2])
11        return np.array([p1, p2, p3, p1])
12
13    def koch_iteration(points):
14        new_points = []
15        for i in range(len(points)-1):
16            p1 = points[i]
17            p2 = points[i+1]
18            delta = (p2 - p1) / 3.0
19            pa = p1 + delta
20            pb = p1 + 2*delta
21
22            angle = -np.pi / 3
23            peak = pa + np.array([
24                delta[0]*np.cos(angle) - delta[1]*np.sin(angle),
25                delta[0]*np.sin(angle) + delta[1]*np.cos(angle)
26            ])
27
28            new_points.extend([p1, pa, peak, pb])
29        new_points.append(points[-1])
30        return np.array(new_points)
31
32    points = initial_triangle(scale)
33    for _ in range(order):
34        points = koch_iteration(points)
35    return points
36
37
38 # Plot Koch snowflake iterations
39 orders = [0, 1, 2, 3, 4, 5]
40 fig, axes = plt.subplots(1, len(orders), figsize=(15, 3))
41
42 for ax, order in zip(axes, orders):
43     points = koch_snowflake(order)
44     ax.plot(points[:, 0], points[:, 1], color="blue")
45     ax.set_aspect('equal')
46     ax.axis("off")
47     ax.set_title(f"Order {order}")
48
49 plt.show()
```

### 2.11.2 Output:

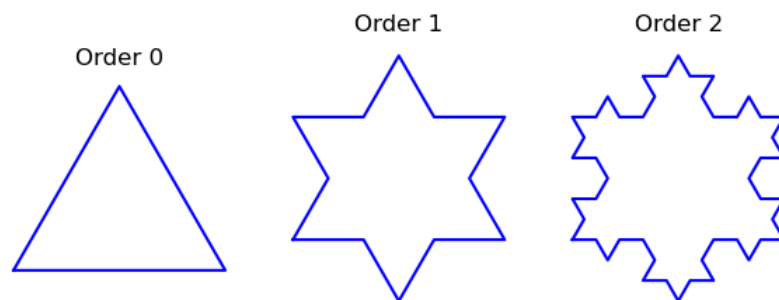


Figure 2.11: Koch Snowflake Pattern

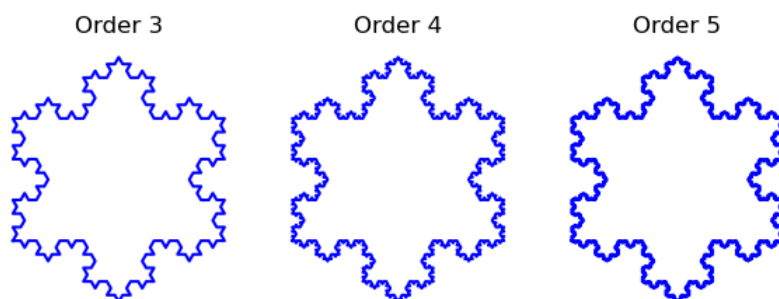


Figure 2.12: Koch Snowflake Pattern