

NCTU_TaNoShiI

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```

1 set ts=4
2 set sw=4
3 set et
4 set ai
5 set nu
6
7 map <F9> :w<LF>:!g++ -O2 -g -std=c++11 -o %.out % &&
   echo "----Start----" && ./%.out<LF>
8 imap <F9> <ESC><F9>

```

```

1 #include<bits/stdc++.h>
2 #define mp(a,b) make_pair((a),(b))
3 #define pii pair<int,int>
4 #define pdd pair<double,double>
5 #define pll pair<LL,LL>
6 #define pb(x) push_back(x)
7 #define x first
8 #define y second
9 #define sqr(x) ((x)*(x))
10 #define EPS 1e-6
11 #define mii map<int,int>
12 #define MEM(x) memset(x,0,sizeof(x))
13 #define MEMS(x) memset(x,-1,sizeof(x))
14 #define pi 3.14159265359
15 //#define INF 0x7fffffff
16 #define IOS ios_base::sync_with_stdio(0); cin.tie(0)
17 #define N 300005
18 using namespace std;
19 typedef long long LL;

```

```

1 cat -n "%s" > tmp.print
2 lpr tmp.print

```

2 DataStructure

2.1 PersistentTreap

```

1 const int MEM = 16000004;
2 struct Treap {
3     static Treap nil, mem[MEM], *pmem;
4     Treap *l, *r;

```

```

5   char val;
6   int size;
7   Treap () : l(&nil), r(&nil), size(0) {}
8   Treap (char _val) :
9     l(&nil), r(&nil), val(_val), size(1) {}
10 } Treap::nil, Treap::mem[MEM], *Treap::pmem = Treap
    ::
11 mem;
12 int size(const Treap *t) { return t->size; }
13 void pull(Treap *t) {
14     if (!size(t)) return;
15     t->size = size(t->l) + size(t->r) + 1;
16 }
17 Treap* merge(Treap *a, Treap *b) {
18     if (!size(a)) return b;
19     if (!size(b)) return a;
20     Treap *t;
21     if (rand() % (size(a) + size(b)) < size(a)) {
22         t = new (Treap::pmem++) Treap(*a);
23         t->r = merge(a->r, b);
24     } else {
25         t = new (Treap::pmem++) Treap(*b);
26         t->l = merge(a, b->l);
27     }
28     pull(t);
29     return t;
30 }
31 void split(Treap *t, int k, Treap *a, Treap *b) {
32     if (!size(t)) a = b = &Treap::nil;
33     else if (size(t->l) + 1 <= k) {
34         a = new (Treap::pmem++) Treap(*t);
35         split(t->r, k - size(t->l) - 1, a->r, b);
36         pull(a);
37     } else {
38         b = new (Treap::pmem++) Treap(*t);
39         split(t->l, k, a, b->l);
40         pull(b);
41     }
42 }
43 int nv;
44 Treap *rt[50005];
45 void print(const Treap *t) {
46     if (!size(t)) return;
47     print(t->l);
48     cout << t->val;
49     print(t->r);
50 }
51 int main(int argc, char** argv) {
52     IOS;
53     rt[nv=0] = &Treap::nil;
54     Treap::pmem = Treap::mem;
55     int Q, cmd, p, c, v;
56     string s;
57     cin >> Q;
58     while (Q--) {
59         cin >> cmd;
60         if (cmd == 1) {
61             // insert string s after position p
62             cin >> p >> s;
63             Treap *tl, *tr;
64             split(rt[nv], p, tl, tr);
65             for (int i=0; i<s.size(); i++)
66                 tl = merge(tl, new (Treap::pmem++) Treap
(s[i]));
67             ;
68             rt[++nv] = merge(tl, tr);
69         } else if (cmd == 2) {
70             // remove c characters starting at
position
71             Treap *tl, *tm, *tr;
72             cin >> p >> c;
73             split(rt[nv], p-1, tl, tm);
74             split(tm, c, tm, tr);
75             rt[++nv] = merge(tl, tr);
76         } else if (cmd == 3) {
77             // print c characters starting at
position p, in version v
78             Treap *tl, *tm, *tr;
79             cin >> v >> p >> c;
80             split(rt[v], p-1, tl, tm);
81             split(tm, c, tm, tr);
82             print(tm);

```

```

83         cout << "n";
84     }
85 }
86 return 0;
87 }

```

2.2 Pbds Kth

```

1 #include <bits/extc++.h>
2 using namespace __gnu_pbds;
3 typedef tree<int, null_type, less<int>, rb_tree_tag,
4 tree_order_statistics_node_update> set_t;
5 int main()
6 {
7     // Insert some entries into s.
8     set_t s;
9     s.insert(12); s.insert(505);
10    // The order of the keys should be: 12, 505.
11    assert(*s.find_by_order(0) == 12);
12    assert(*s.find_by_order(3) == 505);
13    // The order of the keys should be: 12, 505.
14    assert(s.order_of_key(12) == 0);
15    assert(s.order_of_key(505) == 1);
16    // Erase an entry.
17    s.erase(12);
18    // The order of the keys should be: 505.
19    assert(*s.find_by_order(0) == 505);
20    // The order of the keys should be: 505.
21    assert(s.order_of_key(505) == 0);
22 }

```

2.3 PbdsHeap

```

1 #include <bits/extc++.h>
2 typedef __gnu_pbds::priority_queue<int> heap_t;
3 heap_t a, b;
4 int main() {
5     a.clear(); b.clear();
6     a.push(1); a.push(3);
7     b.push(2); b.push(4);
8     assert(a.top() == 3);
9     assert(b.top() == 4);
10    // merge two heap
11    a.join(b);
12    assert(a.top() == 4);
13    assert(b.empty());
14    return 0;
15 }

```

2.4 Heavy-LightDecomposition

```

1 #define N
2 void init(); // implement
3 int n, fa[N], belong[N], dep[N], sz[N], que[N];
4 int step, line[N], stPt[N], edPt[N];
5 vector<int> v[N], chain[N];
6 void DFS(int u) {
7     vector<int> &c = chain[belong[u]];
8     for (int i=c.size()-1; i>=0; i--) {
9         int v = c[i];
10        stPt[v] = step;
11        line[step++] = v;
12    }
13    for (int i=0; i<(int)c.size(); i++) {
14        u = c[i];
15        for (vector<int>::iterator it=v[u].begin();
16            it!=v[u].end(); it++) {
17            if (fa[u] == *it || (i && *it == c[i-1]))
18                continue;
19            DFS(*it);
20        }
21        edPt[u] = step-1;
22    }
23 }
24 void build_chain(int st) {
25     int fr, bk;
26     fr=bk=0; que[bk++] = 1; fa[st]=st; dep[st]=0;
27     while (fr < bk) {
28         int u=que[fr++];

```

```

27     for (vector<int>::iterator it=v[u].begin();
    it!=v[u].end();it++){
28         if (*it == fa[u]) continue;
29         que[bk++] = *it;
30         dep[*it] = dep[u]+1;
31         fa[*it] = u;
32     }
33 }
34 for (int i=bk-1,u,pos; i>=0; i--){
35     u = que[i]; sz[u] = 1; pos = -1;
36     for (vector<int>::iterator it=v[u].begin();
    it!=v[u].end();it++){
37         if (*it == fa[u]) continue;
38         sz[u] += sz[*it];
39         if (pos==-1 || sz[*it]>sz[pos]) pos=*it;
40     }
41     if (pos == -1) belong[u] = u;
42     else belong[u] = belong[pos];
43     chain[belong[u]].pb(u);
44 }
45 step = 0;
46 DFS(st);
47 }
48 int getLCA(int u, int v){
49     while (belong[u] != belong[v]){
50         int a = chain[belong[u]].back();
51         int b = chain[belong[v]].back();
52         if (dep[a] > dep[b]) u = fa[a];
53         else v = fa[b];
54     }
55     return sz[u] >= sz[v] ? u : v;
56 }
57 vector<pii> getPathSeg(int u, int v){
58     vector<pii> ret1,ret2;
59     while (belong[u] != belong[v]){
60         int a = chain[belong[u]].back();
61         int b = chain[belong[v]].back();
62         if (dep[a] > dep[b]){
63             ret1.pb(mp(stPt[a],stPt[u]));
64             u = fa[a];
65         } else {
66             ret2.pb(mp(stPt[b],stPt[v]));
67             v = fa[b];
68         }
69     }
70     if (dep[u] > dep[v]) swap(u,v);
71     ret1.pb(mp(stPt[u],stPt[v]));
72     reverse(ret2.begin(), ret2.end());
73     ret1.insert(ret1.end(),ret2.begin(),ret2.end());
74     return ret1;
75 }
76 // Usage
77 void build(){
78     build_chain(1); //change root
79     init();
80 }
81 int get_answer(int u, int v){
82     int ret = -2147483647;
83     vector<pii> vec = getPathSeg(u,v);
84     for (vector<pii>::iterator it =vec.begin();it!=
    vec.end();it++){
85         // check answer with segment [it.F, it.S]
86         return ret;
87 }

```

2.5 KDtree

```

1 struct KDTree {
2     struct Node {
3         int x,y,x1,y1,x2,y2;
4         int id,f;
5         Node *L, *R;
6     }tree[MXN];
7     int n;
8     Node *root;
9     long long dis2(int x1, int y1, int x2, int y2) {
10         long long dx = x1-x2;
11         long long dy = y1-y2;
12         return dx*dx+dy*dy;
13     }
14     static bool cmpx(Node& a, Node& b){ return a.x<b
    .x; }

```

```

15     static bool cmpy(Node& a, Node& b){ return a.y<b
    .y; }
16 void init(vector<pair<int,int>> ip) {
17     n = ip.size();
18     for (int i=0; i<n; i++) {
19         tree[i].id = i;
20         tree[i].x = ip[i].first;
21         tree[i].y = ip[i].second;
22     }
23     root = build_tree(0, n-1, 0);
24 }
25 Node* build_tree(int L, int R, int dep) {
26     if (L>R) return nullptr;
27     int M = (L+R)/2;
28     tree[M].f = dep%2;
29     nth_element(tree+L, tree+M, tree+R+1, tree[M
    ].f ?
30         cmpx : cmpy);
31     tree[M].x1 = tree[M].x2 = tree[M].x;
32     tree[M].y1 = tree[M].y2 = tree[M].y;
33     tree[M].L = build_tree(L, M-1, dep+1);
34     if (tree[M].L) {
35         tree[M].x1 = min(tree[M].x1, tree[M].L->
    x1);
36         tree[M].x2 = max(tree[M].x2, tree[M].L->
    x2);
37         tree[M].y1 = min(tree[M].y1, tree[M].L->
    y1);
38         tree[M].y2 = max(tree[M].y2, tree[M].L->
    y2);
39     }
40     tree[M].R = build_tree(M+1, R, dep+1);
41     if (tree[M].R) {
42         tree[M].x1 = min(tree[M].x1, tree[M].R->
    x1);
43         tree[M].x2 = max(tree[M].x2, tree[M].R->
    x2);
44         tree[M].y1 = min(tree[M].y1, tree[M].R->
    y1);
45         tree[M].y2 = max(tree[M].y2, tree[M].R->
    y2);
46     }
47     return tree+M;
48 }
49 int touch(Node* r, int x, int y, long long d2){
50     long long dis = sqrt(d2)+1;
51     if (x<r->x1-dis || x>r->x2+dis || y<r->y1-
    dis || y>
52         r->y2+dis)
53         return 0;
54     return 1;
55 }
56 void nearest(Node* r, int x, int y, int &mID,
    long
57     long &md2) {
58     if (!r || !touch(r, x, y, md2)) return;
59     long long d2 = dis2(r->x, r->y, x, y);
60     if (d2 < md2 || (d2 == md2 && mID < r->id))
    {
61         mID = r->id;
62         md2 = d2;
63     }
64     // search order depends on split dim
65     if ((r->f == 0 && x < r->x) ||
66         (r->f == 1 && y < r->y)) {
67         nearest(r->L, x, y, mID, md2);
68         nearest(r->R, x, y, mID, md2);
69     } else {
70         nearest(r->R, x, y, mID, md2);
71         nearest(r->L, x, y, mID, md2);
72     }
73 }
74 int query(int x, int y) {
75     int id = 1029384756;
76     long long d2 = 102938475612345678LL;
77     nearest(root, x, y, id, d2);
78     return id;
79 }
80 }tree;

```

2.6 LCT

```

1 const int MXN = 100005;
2 const int MEM = 100005;
3
4 struct Splay {
5     static Splay nil, mem[MEM], *pmem;
6     Splay *ch[2], *f;
7     int val, rev, size;
8     Splay () : val(-1), rev(0), size(0) {
9         f = ch[0] = ch[1] = &nil;
10    }
11    Splay (int _val) : val(_val), rev(0), size(1) {
12        f = ch[0] = ch[1] = &nil;
13    }
14    bool isr() {
15        return f->ch[0] != this && f->ch[1] != this;
16    }
17    int dir() {
18        return f->ch[0] == this ? 0 : 1;
19    }
20    void setCh(Splay *c, int d) {
21        ch[d] = c;
22        if (c != &nil) c->f = this;
23        pull();
24    }
25    void push() {
26        if (rev) {
27            swap(ch[0], ch[1]);
28            if (ch[0] != &nil) ch[0]->rev ^= 1;
29            if (ch[1] != &nil) ch[1]->rev ^= 1;
30            rev=0;
31        }
32    }
33    void pull() {
34        size = ch[0]->size + ch[1]->size + 1;
35        if (ch[0] != &nil) ch[0]->f = this;
36        if (ch[1] != &nil) ch[1]->f = this;
37    }
38 } Splay::nil, Splay::mem[MEM], *Splay::pmem = Splay::mem;
39 Splay *nil = &Splay::nil;
40
41 void rotate(Splay *x) {
42     Splay *p = x->f;
43     int d = x->dir();
44     if (!p->isr()) p->f->setCh(x, p->dir());
45     else x->f = p->f;
46     p->setCh(x->ch[!d], d);
47     x->setCh(p, !d);
48     p->pull(); x->pull();
49 }
50
51 vector<Splay*> splayVec;
52 void splay(Splay *x) {
53     splayVec.clear();
54     for (Splay *q=x;; q=q->f) {
55         splayVec.push_back(q);
56         if (q->isr()) break;
57     }
58     reverse(begin(splayVec), end(splayVec));
59     for (auto it : splayVec) it->push();
60     while (!x->isr()) {
61         if (x->f->isr()) rotate(x);
62         else if (x->dir()==x->f->dir()) rotate(x->f), rotate(x);
63         else rotate(x), rotate(x);
64     }
65 }
66
67 Splay* access(Splay *x) {
68     Splay *q = nil;
69     for (;x!=nil;x=x->f) {
70         splay(x);
71         x->setCh(q, 1);
72         q = x;
73     }
74     return q;
75 }
76 void evert(Splay *x) {
77     access(x);
78     splay(x);
79     x->rev ^= 1;

```

```

80     x->push(); x->pull();
81 }
82 void link(Splay *x, Splay *y) {
83     // evert(x);
84     access(x);
85     splay(x);
86     evert(y);
87     x->setCh(y, 1);
88 }
89 void cut(Splay *x, Splay *y) {
90     // evert(x);
91     access(y);
92     splay(y);
93     y->push();
94     y->ch[0] = y->ch[0]->f = nil;
95 }
96
97 int N, Q;
98 Splay *vt[MXN];
99
100 int ask(Splay *x, Splay *y) {
101     access(x);
102     access(y);
103     splay(x);
104     int res = x->f->val;
105     if (res == -1) res=x->val;
106     return res;
107 }
108 int main(int argc, char** argv) {
109     scanf("%d%d", &N, &Q);
110     for (int i=1; i<=N; i++)
111         vt[i] = new (Splay::pmem++) Splay(i);
112     while (Q--) {
113         char cmd[105];
114         int u, v;
115         scanf("%s", cmd);
116         if (cmd[1] == 'i') {
117             scanf("%d%d", &u, &v);
118             link(vt[v], vt[u]);
119         } else if (cmd[0] == 'c') {
120             scanf("%d", &v);
121             cut(vt[1], vt[v]);
122         } else {
123             scanf("%d%d", &u, &v);
124             int res=ask(vt[u], vt[v]);
125             printf("%d\n", res);
126         }
127     }
128     return 0;
129 }
130 }

```

3 Flow

3.1 Minmunwieghtmatchclique

```

1 struct Graph {
2     // Minimum General Weighted Matching (Perfect
3     Match) clique
4     static const int MXN = 105;
5     int n, edge[MXN][MXN];
6     int match[MXN], dis[MXN], onstk[MXN];
7     vector<int> stk;
8     void init(int _n) {
9         n = _n;
10        MEM(edge);
11    }
12    void add_edge(int u, int v, int w) {
13        edge[u][v] = edge[v][u] = w;
14    }
15    bool SPFA(int u){
16        if (onstk[u]) return true;
17        stk.pb(u);
18        onstk[u] = 1;
19        for (int v=0; v<n; v++){
20            if (u != v && match[u] != v && !onstk[v])
21                int m = match[v];
22                if (dis[m] > dis[u] - edge[v][m] +
23                    edge[u][v]){

```

```

22         dis[m] = dis[u] - edge[v][m] +
    edge[u][v];
23         onstk[v] = 1;
24         stk.pb(v);
25         if (SPFA(m)) return true;
26         stk.pop_back();
27         onstk[v] = 0;
28     }
29 }
30 }
31 onstk[u] = 0;
32 stk.pop_back();
33 return false;
34 }
35 int solve() {
36     // find a match
37     for (int i=0; i<n; i+=2){
38         match[i] = i+1;
39         match[i+1] = i;
40     }
41     while (true){
42         int found = 0;
43         MEM(dis); MEM(onstk);
44         for (int i=0; i<n; i++){
45             stk.clear();
46             if (!onstk[i] && SPFA(i)){
47                 found = 1;
48                 while (stk.size()>=2){
49                     int u = stk.back(); stk.
pop_back();
50                     int v = stk.back(); stk.
pop_back();
51                     match[u] = v;
52                     match[v] = u;
53                 }
54             }
55             if (!found) break;
56         }
57     }
58     int ret = 0;
59     for (int i=0; i<n; i++){
60         ret += edge[i][match[i]];
61         ret /= 2;
62     }
63     return ret;
64 }graph;

```

3.2 CostFlow

```

1 struct CostFlow {
2     static const int MXN = 205;
3     static const long long INF = 102938475610293847
LL;
4     struct Edge {
5         int v, r;
6         long long f, c;
7         Edge(int a, int b, int _c, int d):v(a),r(b),f(
_c),c(d){
8         };
9     };
10    int n, s, t, prv[MXN], prvL[MXN], inq[MXN];
11    long long dis[MXN], fl, cost;
12    vector<Edge> E[MXN];
13    void init(int _n, int _s, int _t) {
14        n = _n; s = _s; t = _t;
15        for (int i=0; i<n; i++) E[i].clear();
16        fl = cost = 0;
17    }
18    void add_edge(int u, int v, long long f, long
long c)
19    {
20        E[u].pb(Edge(v, E[v].size(), f, c));
21        E[v].pb(Edge(u, E[u].size()-1, 0, -c));
22    }
23    pll flow() {
24        while (true) {
25            for (int i=0; i<n; i++) {
26                dis[i] = INF;
27                inq[i] = 0;
28            }
29            dis[s] = 0;

```

```

30        queue<int> que;
31        que.push(s);
32        while (!que.empty()) {
33            int u = que.front(); que.pop();
34            inq[u] = 0;
35            for (int i=0; i<E[u].size(); i++) {
36                int v = E[u][i].v;
37                long long w = E[u][i].c;
38                if (E[u][i].f > 0 && dis[v] >
dis[u] + w) {
39                    prv[v] = u; prvL[v] = i;
40                    dis[v] = dis[u] + w;
41                    if (!inq[v]) {
42                        inq[v] = 1;
43                        que.push(v);
44                    }
45                }
46            }
47        }
48        if (dis[t] == INF) break;
49        long long tf = INF;
50        for (int v=t, u, l; v!=s; v=u) {
51            u=prv[v]; l=prvL[v];
52            tf = min(tf, E[u][l].f);
53        }
54        for (int v=t, u, l; v!=s; v=u) {
55            u=prv[v]; l=prvL[v];
56            E[u][l].f -= tf;
57            E[v][E[u][l].r].f += tf;
58        }
59        cost += tf * dis[t];
60        fl += tf;
61    }
62    return {fl, cost};
63 }
64 }flow;

```

3.3 MincutTree

```

1 set<int> temp;
2 int Vis[3005];
3 int cvis[3005];
4 void dfs(int n){
5     Vis[n]=1;
6     for(auto it=v[n].begin(); it!=v[n].end(); it++){
7         if(val[n][*it]>flow[n][*it]&&Vis[*it]){
8             dfs(*it);
9             if(cvis[*it])
10                temp.insert(*it);
11        }
12    }
13 }
14 int n;
15 int dc(set<int> s, int flag){
16     if(s.size()==1)
17         return *s.begin();
18     for(int i=0; i<n; i++){
19         for(auto it=v[i].begin(); it!=v[i].end(); it++){
20             flow[i][*it]=0;
21         }
22         for(auto it=s.begin(); it!=s.end(); it++){
23             cvis[*it]=1;
24         }
25         int res=Flow(*s.begin(), *s.rbegin());
26         MEM(Vis);
27         dfs(*s.begin());
28         temp.insert(*s.begin());
29         for(auto it=s.begin(); it!=s.end(); it++){
30             cvis[*it]=0;
31         }
32         set<int> s1, s2;
33         swap(s1, temp);
34         temp.clear();
35         for(auto it=s1.begin(); it!=s1.end(); it++){
36             s.erase(*it);
37             swap(s2, s);
38             int x=dc(s1, 0);
39             int y=dc(s2, 1);
40             vt[x].pb(mp(y, res));
41             vt[y].pb(mp(x, res));
42             if(flag==0)
43                 return x;

```



```

43 else
44 return y;
45 }

```

3.4 Dinic

```

1 struct Dinic{
2     static const int MXN = 10000;
3     struct Edge{ int v,f,re; Edge(int a,int b,int c)
4         :v(a),f(b),re(c){}};
5     int n,s,t,level[MXN];
6     vector<Edge> E[MXN];
7     void init(int _n, int _s, int _t){
8         n = _n; s = _s; t = _t;
9         for (int i=0; i<=n; i++) E[i].clear();
10    }
11    void add_edge(int u, int v, int f){
12        E[u].pb(Edge(v,f,E[u].size()));
13        E[v].pb(Edge(u,0,E[v].size()-1)); //direct
14    }
15    bool BFS(){
16        MEMS(level);
17        queue<int> que;
18        que.push(s);
19        level[s] = 0;
20        while (!que.empty()){
21            int u = que.front(); que.pop();
22            for (auto it : E[u]){
23                if (it.f > 0 && level[it.v] == -1){
24                    level[it.v] = level[u]+1;
25                    que.push(it.v);
26                }
27            }
28        }
29        return level[t] != -1;
30    }
31    int DFS(int u, int nf){
32        if (u == t) return nf;
33        int res = 0;
34        for (auto &it : E[u]){
35            if (it.f > 0 && level[it.v] == level[u]
36                ]+1){
37                int tf = DFS(it.v, min(nf,it.f));
38                res += tf; nf -= tf; it.f -= tf;
39                E[it.v][it.re].f += tf;
40                if (nf == 0) return res;
41            }
42        }
43        if (!res) level[u] = -1;
44        return res;
45    }
46    int flow(int res=0){
47        while (BFS())
48            res += DFS(s,2147483647);
49    }
50 }

```

3.5 GeneralGraphmatch

```

1 struct GenMatch { // 1-base
2     static const int MAXN = 505;
3     int V;
4     bool el[MAXN][MAXN];
5     int pr[MAXN];
6     bool inq[MAXN],inp[MAXN],inb[MAXN];
7     queue<int> qe;
8     int st,ed;
9     int nb;
10    int bk[MAXN],djs[MAXN];
11    int ans;
12    void init(int _V) {
13        V = _V;
14        MEM(el); MEM(pr);
15        MEM(inq); MEM(inp); MEM(inb);
16        MEM(bk); MEM(djs);
17        ans = 0;
18    }
19    void add_edge(int u, int v) {
20        el[u][v] = el[v][u] = 1;
21    }

```

```

22    int lca(int u,int v) {
23        memset(inp,0,sizeof(inp));
24        while(1) {
25            u = djs[u];
26            inp[u] = true;
27            if(u == st) break;
28            u = bk[pr[u]];
29        }
30        while(1) {
31            v = djs[v];
32            if(inp[v]) return v;
33            v = bk[pr[v]];
34        }
35        return v;
36    }
37    void upd(int u) {
38        int v;
39        while(djs[u] != nb) {
40            v = pr[u];
41            inb[djs[u]] = inb[djs[v]] = true;
42            u = bk[v];
43            if(djs[u] != nb) bk[u] = v;
44        }
45    }
46    void blo(int u,int v) {
47        nb = lca(u,v);
48        memset(inb,0,sizeof(inb));
49        upd(u); upd(v);
50        if(djs[u] != nb) bk[u] = v;
51        if(djs[v] != nb) bk[v] = u;
52        for(int tu = 1; tu <= V; tu++)
53            if(inb[djs[tu]]) {
54                djs[tu] = nb;
55                if(!inq[tu]){
56                    qe.push(tu);
57                    inq[tu] = 1;
58                }
59            }
60    }
61    void flow() {
62        memset(inq,false,sizeof(inq));
63        memset(bk,0,sizeof(bk));
64        for(int i = 1; i <= V; i++)
65            djs[i] = i;
66        while(qe.size()) qe.pop();
67        qe.push(st);
68        inq[st] = 1;
69        ed = 0;
70        while(qe.size()) {
71            int u = qe.front(); qe.pop();
72            for(int v = 1; v <= V; v++)
73                if(el[u][v] && (djs[u] != djs[v]) && (pr
74                    [u] !=
75                    v)) {
76                    if((v == st) || ((pr[v] > 0) && bk[
77                        pr[v]] >
78                        0))
79                        blo(u,v);
80                    else if(bk[v] == 0) {
81                        bk[v] = u;
82                        if(pr[v] > 0) {
83                            if(!inq[pr[v]]) qe.push(pr[v]
84                                ]);
85                        } else {
86                            ed = v;
87                            return;
88                        }
89                    }
90                }
91            }
92        }
93    }
94    void aug() {
95        int u,v,w;
96        u = ed;
97        while(u > 0) {
98            v = bk[u];
99            w = pr[v];
100            pr[v] = u;
101            pr[u] = v;
102            u = w;
103        }
104    }

```

```

101 int solve() {
102     memset(pr,0,sizeof(pr));
103     for(int u = 1; u <= V; u++)
104         if(pr[u] == 0) {
105             st = u;
106             flow();
107             if(ed > 0) {
108                 aug();
109                 ans ++;
110             }
111         }
112     return ans;
113 }
114 }gp;

```

3.6 KM

```

1 typedef pair<long long, long long> pll;
2 struct KM{
3     // Maximum Bipartite Weighted Matching (Perfect Match)
4     static const int MXN = 650;
5     static const int INF = 2147483647; // long long
6     int n, match[MXN], vx[MXN], vy[MXN];
7     int edge[MXN][MXN], lx[MXN], ly[MXN], slack[MXN];
8     // ^^^^ long long
9     void init(int _n){
10         n = _n;
11         for (int i=0; i<n; i++)
12             for (int j=0; j<n; j++)
13                 edge[i][j] = 0;
14     }
15     void add_edge(int x, int y, int w){ // long long
16         edge[x][y] = w;
17     }
18     bool DFS(int x){
19         vx[x] = 1;
20         for (int y=0; y<n; y++){
21             if (vy[y]) continue;
22             if (lx[x]+ly[y] > edge[x][y]){
23                 slack[y] = min(slack[y], lx[x]+ly[y]
24 ]-edge[x][y]);
25             } else {
26                 vy[y] = 1;
27                 if (match[y] == -1 || DFS(match[y])){
28                     match[y] = x;
29                     return true;
30                 }
31             }
32         }
33         return false;
34     }
35     int solve(){
36         fill(match, match+n, -1);
37         fill(lx, lx+n, -INF);
38         fill(ly, ly+n, 0);
39         for (int i=0; i<n; i++)
40             for (int j=0; j<n; j++)
41                 lx[i] = max(lx[i], edge[i][j]);
42         for (int i=0; i<n; i++){
43             fill(slack, slack+n, INF);
44             while (true){
45                 fill(vx, vx+n, 0);
46                 fill(vy, vy+n, 0);
47                 if ( DFS(i) ) break;
48                 int d = INF; // long long
49                 for (int j=0; j<n; j++)
50                     if (!vy[j]) d = min(d, slack[j]);
51                 for (int j=0; j<n; j++){
52                     if (vx[j]) lx[j] -= d;
53                     if (vy[j]) ly[j] += d;
54                     else slack[j] -= d;
55                 }
56             }
57         }
58         int res=0;
59         for (int i=0; i<n; i++)
60             res += edge[match[i]][i];
61         return res;

```

```

62     }
63 }graph;

```

3.7 SWmincut

```

1 struct SW{ // 0(V^3)
2     static const int MXN = 514;
3     int n, vst[MXN], del[MXN];
4     int edge[MXN][MXN], wei[MXN];
5     void init(int _n){
6         n = _n;
7         MEM(edge);
8         MEM(del);
9     }
10    void add_edge(int u, int v, int w){
11        edge[u][v] += w;
12        edge[v][u] += w;
13    }
14    void search(int &s, int &t){
15        MEM(vst); MEM(wei);
16        s = t = -1;
17        while (true){
18            int mx=-1, cur=0;
19            for (int i=0; i<n; i++)
20                if (!del[i] && !vst[i] && mx<wei[i])
21                    cur = i, mx = wei[i];
22            if (mx == -1) break;
23            vst[cur] = 1;
24            s = t;
25            t = cur;
26            for (int i=0; i<n; i++)
27                if (!vst[i] && !del[i]) wei[i] += edge[
28 cur][i];
29        }
30    }
31    int solve(){
32        int res = 2147483647;
33        for (int i=0, x, y; i<n-1; i++){
34            search(x, y);
35            res = min(res, wei[y]);
36            del[y] = 1;
37            for (int j=0; j<n; j++)
38                edge[x][j] = (edge[j][x] += edge[y][j]);
39        }
40        return res;
41    }graph;

```

4 Geometry

4.1 Circleintersection

```

1 using ld = double;
2 vector<pdd> interCircle(pdd o1, double r1, pdd o2,
3 double r2) {
4     ld d2 = (o1 - o2) * (o1 - o2);
5     ld d = sqrt(d2);
6     if (d > r1+r2) return {};
7     pdd u = 0.5*(o1+o2) + ((r2*r2-r1*r1)/(2*d2))*(o1
8 -o2);
9     double A = sqrt((r1+r2+d) * (r1-r2+d) * (r1+r2-d)
10 *(-r1+r2+d));
11     pdd v = A / (2*d2) * pdd(o1.S-o2.S, -o1.F+o2.F);
12     return {u+v, u-v};

```

4.2 Fermat's Point

```

1 #define F(n) Fi(i,n)
2 #define Fi(i,n) Fl(i,0,n)
3 #define Fl(i,l,n) for(int i=(l);i<(int)(n);++i)
4 #include <bits/stdc++.h>
5 // #include <ext/pb_ds/assoc_container.hpp>
6 // #include <ext/pb_ds/priority_queue.hpp>
7 using namespace std;
8 // using namespace __gnu_pbds;
9 const double pi = acos(-1), eps = 1e-9;
10 const double st = sin(pi/3), ct = cos(pi/3);

```

```

11 struct point {
12     point(double x_ = 0, double y_ = 0): x(x_), y(y_)
13     {}
14     double x, y;
15     inline friend istream& operator>>(istream& is,
16     point& p) {
17         is >> p.x >> p.y;
18         return is;
19     }
20     inline friend ostream& operator<<(ostream& os,
21     const point& p) {
22         os << p.x << ' ' << p.y;
23         return os;
24     }
25 };
26 struct line {
27     line(double a_ = 0, double b_ = 0, double c_ = 0):
28     a(a_), b(b_), c(c_) {}
29     double a, b, c;
30     inline double calc(point p) {
31         return a*p.x+b*p.y;
32     }
33 };
34 inline double calc(double a, double b, point p) {
35     return a*p.x+b*p.y;
36 }
37 inline double dist2(point a, point b) {
38     return (a.x-b.x)*(a.x-b.x)+(a.y-b.y)*(a.y-b.y);
39 }
40 inline point rot(point O, point p) {
41     p.x -= O.x, p.y -= O.y;
42     return point(0.x+p.x*ct-p.y*st, 0.y+p.x*st+p.y*ct);
43 }
44 inline line cln(point a, point b) {
45     return line(a.y-b.y, b.x-a.x, calc(a.y-b.y, b.x-a.
46     x, a));
47 }
48 inline point ntse(line f, line g) {
49     double det = f.a*g.b-g.a*f.b, dx = f.c*g.b-g.c*f.b
50     , dy = f.a*g.c-g.a*f.c;
51     return point(dx/det, dy/det);
52 }
53 inline point fema(point a, point b, point c) {
54     double la = dist2(b, c), lb = dist2(a, c), lc =
55     dist2(a, b);
56     double sa = sqrt(la), sb = sqrt(lb), sc = sqrt(lc)
57     ;
58     if ((lb+lc-la)/(2.0*sb*sc) < -0.5 + eps)
59         return a;
60     if ((la+lc-lb)/(2.0*sa*sc) < -0.5 + eps)
61         return b;
62     if ((la+lb-lc)/(2.0*sa*sb) < -0.5 + eps)
63         return c;
64     point t1 = rot(a, b), t2 = rot(b, a);
65     if (dist2(c, t1) < dist2(c, t2)) swap(t1, t2);
66     point s1 = rot(b, c), s2 = rot(c, b);
67     if (dist2(a, s1) < dist2(a, s2)) swap(s1, s2);
68     return ntse(cln(c, t1), cln(a, s1));
69 }
70 int main() {
71     ios_base::sync_with_stdio(false);
72     cin.tie(NULL);
73     point a, b, c;
74     cin >> a >> b >> c;
75     cout << setprecision(10) << fixed << fema(a, b, c)
76     << '\n';
77 }

```

4.3 Pointoperators

```

1 #define x first
2 #define y second
3 #define cpdd const pdd
4 struct pdd : pair<double, double> {
5     using pair<double, double>::pair;
6     pdd operator + (cpdd &p) const {
7         return {x+p.x, y+p.y};
8     }
9     pdd operator - () const {
10         return {-x, -y};

```

```

11     }
12     pdd operator - (cpdd &p) const {
13         return (*this) + (-p);
14     }
15     pdd operator * (double f) const {
16         return {f*x, f*y};
17     }
18     double operator * (cpdd &p) const {
19         return x*p.x + y*p.y;
20     }
21 };
22 double abs(cpdd &p) { return hypot(p.x, p.y); }
23 double arg(cpdd &p) { return atan2(p.y, p.x); }
24 double cross(cpdd &p, cpdd &q) { return p.x*q.y - p.
25     y*q
26     .x; }
27 double cross(cpdd &p, cpdd &q, cpdd &o) { return
28     cross(
29     p-o, q-o); }
30 pdd operator * (double f, cpdd &p) { return p*f; }
31 //!! Not f*p !!

```

4.4 3DConvexHull

```

1 int flag[MXN][MXN];
2 struct Point{
3     ld x,y,z;
4     Point operator - (const Point &b) const {
5         return (Point){x-b.x,y-b.y,z-b.z};
6     }
7     Point operator * (const ld &b) const {
8         return (Point){x*b,y*b,z*b};
9     }
10     ld len() const { return sqrtl(x*x+y*y+z*z); }
11     ld dot(const Point &a) const {
12         return x*a.x+y*a.y+z*a.z;
13     }
14     Point operator * (const Point &b) const {
15         return (Point){y*b.z-b.y*z,z*b.x-b.z*x,x*b.y
16         -b.x*y
17         };
18 };
19 Point ver(Point a, Point b, Point c) {
20     return (b - a) * (c - a);
21 }
22 vector<Face> convex_hull_3D(const vector<Point> pt)
23 {
24     int n = SZ(pt);
25     REP(i,n) REP(j,n)
26     flag[i][j] = 0;
27     vector<Face> now;
28     now.push_back((Face){0,1,2});
29     now.push_back((Face){2,1,0});
30     int ftop = 0;
31     for (int i=3; i<n; i++){
32         ftop++;
33         vector<Face> next;
34         REP(j, SZ(now)) {
35             Face& f=now[j];
36             ld d=(pt[i]-pt[f.a]).dot(ver(pt[f.a], pt
37             [f.b], pt
38             [f.c]));
39             if (d <= 0) next.push_back(f);
40             int ff = 0;
41             if (d > 0) ff=ftop;
42             else if (d < 0) ff=-ftop;
43             flag[f.a][f.b] = flag[f.b][f.c] = flag[f
44             .c][f.a]
45             = ff;
46         }
47         REP(j, SZ(now)) {
48             Face& f=now[j];
49             if (flag[f.a][f.b] > 0 and flag[f.a][f.b
50             ] != flag
51             [f.b][f.c])
52                 next.push_back((Face){f.a,f.b,i});
53             if (flag[f.b][f.c] > 0 and flag[f.b][f.c
54             ] != flag
55             [f.c][f.a])
56                 next.push_back((Face){f.b,f.c,i});

```



```

52         if (flag[f.c][f.a] > 0 and flag[f.c][f.a]
53             ] != flag
54             [f.a][f.c])
55             next.push_back((Face){f.c, f.a, i});
56         }
57         now=next;
58     }
59     return now;

```

4.5 Halfplaneintersection

```

1 typedef pdd Point;
2 typedef vector<Point> Polygon;
3 typedef pair<Point, Point> Line;
4 #define N 10
5 #define p1 first
6 #define p2 second
7 pdd operator-(const pdd &a, const pdd &b){
8     return mp(a.x-b.x, a.y-b.y);
9 }
10 pdd operator+(const pdd &a, const pdd &b){
11     return mp(a.x+b.x, a.y+b.y);
12 }
13 pdd operator*(const pdd &a, const double &b){
14     return mp(b*a.x, b*a.y);
15 }
16 double cross(Point a, Point b){
17     return a.x * b.y - a.y * b.x;
18 }
19 double cross(Point o, Point a, Point b){
20     return cross(a-o, b-o);
21 }
22 double cross(Line l, Point p){
23     return cross(l.p1, l.p2, p);
24 }
25 double arg(const pdd &a){
26     return atan2(a.y, a.x);
27 }
28 bool parallel(Line l1, Line l2){
29     return cross(l1.p2 - l1.p1, l2.p2 - l2.p1) < 1e
30         -8 && cross(l1.p2 - l1.p1, l2.p2 - l2.p1) > -1e
31         -8;
32 }
33 Point intersection(Line l1, Line l2){
34     Point& a1 = l1.p1, &a2 = l1.p2;
35     Point& b1 = l2.p1, &b2 = l2.p2;
36     Point a = a2 - a1, b = b2 - b1, s = b1 - a1;
37     return a1 + a * (cross(b, s) / cross(b, a));
38 }
39 bool cmp(Line l1, Line l2){
40     return arg(l1.p2 - l1.p1) < arg(l2.p2 - l2.p1);
41 }
42 Polygon halfplane_intersection(vector<Line> hp){
43     sort(hp.begin(), hp.end(), cmp);
44     int L = 0, R = 0;
45     vector<Line> l(N);
46     vector<Point> p(N);
47     l[R] = hp[0];
48     for (int i=1; i<hp.size(); i++){
49         while (L < R && cross(hp[i], p[R-1]) < 0) R--;
50         while (L < R && cross(hp[i], p[L]) < 0) L++;
51         l[++R] = hp[i];
52         if (parallel(l[R-1], hp[i]) &&
53             cross(l[R-1], hp[i].p1) > 0) l[R] = hp[i];
54     }
55     while (L < R && cross(l[L], p[R-1]) < 0) R--;
56     if (R-L <= 1) return Polygon();
57     if (L < R) p[R] = intersection(l[L], l[R]);
58     Polygon ch;
59     for (int i=L; i<=R; i++) ch.push_back(p[i]);
60     ch.resize(unique(ch.begin(), ch.end()) - ch.
61         begin());
62     if (ch.size() > 1 && ch.front() == ch.back())
63         ch.pop_back();

```

```

63     return ch;
64 }
65 double cal(Polygon p){
66     if(p.empty())
67         return 0;
68     p.pb(*p.begin());
69     double ans=0;
70     for(int i=0; i<p.size()-1; i++){
71         ans+=p[i].x*p[i+1].y;
72         ans-=p[i].y*p[i+1].x;
73     }
74     ans/=2;
75     ans=abs(ans);
76     return ans;
77 }

```

4.6 ConvexHull

```

1 sort(p, p+n);
2 pii ans[N];
3 ans[0]=p[0];
4 int k=0;
5 int now=0;
6 for(int yy=0; yy<2; yy++){
7     for(int i=1; i<n; i++){
8         while(now!=k && cross(ans[now].x, p[j].x, ans[now
9             -1].x)<0){
10             now--;
11         }
12         ans[++now]=p[i];
13     }
14     k=now;
15     reverse(p, p+n);

```

4.7 Triangulation

```

1 bool inCircle(pdd a, pdd b, pdd c, pdd d) {
2     b = b - a;
3     c = c - a;
4     d = d - a;
5     if (cross(b, c) < 0) swap(b, c);
6     double m[3][3] = {
7         {b.x, b.y, b*b},
8         {c.x, c.y, c*c},
9         {d.x, d.y, d*d}
10    };
11    double det = m[0][0] * (m[1][1]*m[2][2] - m
12        [1][2]*m
13        [2][1])
14    + m[0][1] * (m[1][2]*m[2][0] - m[1][0]*m
15        [2][2])
16    + m[0][2] * (m[1][0]*m[2][1] - m[1][1]*m
17        [2][0]);
18    return det < 0;
19 }
20 bool intersect(pdd a, pdd b, pdd c, pdd d) {
21     return cross(b, c, a) * cross(b, d, a) < 0 and
22         cross(d, a, c) * cross(d, b, c) < 0;
23 }
24 const double EPS = 1e-12;
25 struct Triangulation {
26     static const int MXN = 1e5+5;
27     int N;
28     vector<int> ord;
29     vector<pdd> pts;
30     set<int> E[MXN];
31     vector<vector<int>> solve(vector<pdd> p) {
32         N = SZ(p);
33         ord.resize(N);
34         for (int i=0; i<N; i++) {
35             E[i].clear();
36             ord[i] = i;
37         }
38         sort(ALL(ord), [&p](int i, int j) {
39             return p[i] < p[j];
40         });
41         pts.resize(N);
42         for (int i=0; i<N; i++) pts[i] = p[ord[i]];
43         go(0, N);
44         vector<vector<int>> res(N);

```

```

44     for (int i=0; i<N; i++) {
45         int o = ord[i];
46         for (auto x: E[i]) {
47             res[o].PB(ord[x]);
48         }
49     }
50     return res;
51 }
52 void add_edge(int u, int v) {
53     E[u].insert(v);
54     E[v].insert(u);
55 }
56 void remove_edge(int u, int v) {
57     E[u].erase(v);
58     E[v].erase(u);
59 }
60 void go(int l, int r) {
61     int n = r - l;
62     if (n <= 3) {
63         for (int i=l; i<r; i++)
64             for (int j=i+1; j<r; j++) add_edge(i, j);
65         return;
66     }
67     int md = (l+r)/2;
68     go(l, md);
69     go(md, r);
70     int il = l, ir = r-1;
71     while (1) {
72         int nx = -1;
73         for (auto i: E[il]) {
74             double cs = cross(pts[il], pts[i],
75 pts[
76         ir]);
77         if (cs > EPS ||
78             (abs(cs) < EPS and abs(pts[i]-pts[
79             ir]) < abs(pts[il]-pts[ir]))) {
80             nx = i;
81             break;
82         }
83     }
84     if (nx != -1) {
85         il = nx;
86         continue;
87     }
88     for (auto i: E[ir]) {
89 pts[
90         double cs = cross(pts[ir], pts[i],
91         il]);
92         if (cs < -EPS ||
93             (abs(cs) < EPS and abs(pts[i]-pts[
94             il]) < abs(pts[ir]-pts[il]))) {
95             nx = i;
96             break;
97         }
98     }
99     if (nx != -1) {
100         ir = nx;
101     } else break;
102 }
103 add_edge(il, ir);
104 while (1) {
105     int nx = -1;
106     bool is2 = false;
107     National Taiwan University
108     AcThPaUNpPUAmCmBkCfEsFmMdNoLr 19
109     for (int i: E[il]) {
110         if (cross(pts[il], pts[i], pts[ir])
111 < -
112             EPS and
113             (nx == -1 or inCircle(pts[il], pts[
114             ir], pts[nx], pts[i]))) nx = i;
115         }
116     for (int i: E[ir]) {
117         if (cross(pts[ir], pts[i], pts[il])
118 >
119             EPS and
120             (nx == -1 or inCircle(pts[il], pts[

```

```

121         int a = il, b = ir;
122         if (is2) swap(a, b);
123         for (auto i: E[a]) {
124             if (intersect(pts[a], pts[i], pts[b
125             ],
126             pts[nx])) {
127             remove_edge(a, i);
128         }
129         if (is2) {
130             add_edge(il, nx);
131             ir = nx;
132         } else {
133             add_edge(ir, nx);
134             il = nx;
135         }
136     }
137 }
138 } tri;

```

4.8 K-closet Pair

```

1 #define F(n) Fi(i,n)
2 #define Fi(i,n) Fl(i,0,n)
3 #define Fl(i,l,n) for(int i=(l);i<(int)(n);++i)
4 #include <bits/stdc++.h>
5 // #include <ext/pb_ds/assoc_container.hpp>
6 // #include <ext/pb_ds/priority_queue.hpp>
7 using namespace std;
8 // using namespace __gnu_pbds;
9 typedef long long ll;
10 struct point {
11     point(ll x_ = 0, ll y_ = 0): x(x_), y(y_) {} ll x
12     , y;
13     inline bool operator<(const point &e_) const {
14         return (x != e_.x ? x < e_.x : y < e_.y);
15     }
16     inline friend istream& operator>>(istream &is_,
17     point& e_) {
18         is_ >> e_.x >> e_.y;
19         return is_;
20     }
21     int k;
22     priority_queue<ll> PQ;
23     inline ll dist2(const point &e1, const point &e2) {
24         ll res = (e1.x-e2.x)*(e1.x-e2.x)+(e1.y-e2.y)*(e1.y
25         -e2.y);
26         PQ.push(res);
27         if (PQ.size() > k) {
28             PQ.pop();
29         }
30         return res;
31     }
32 #define N 500005
33 point p[N];
34 queue<point> Q;
35 ll closet_point(int l, int m, int r, ll delta2) {
36     ll xmid = p[m-1].x;
37     while (!Q.empty()) {
38         Q.pop();
39     }
40     for (int i = l, j = m; i < m; ++i) {
41         if ((p[i].x-xmid)*(p[i].x-xmid) >= delta2) {
42             continue;
43         }
44         while (j < r && p[j].y < p[i].y && (p[j].y-p[i].
45         y)*(p[j].y-p[i].y) < delta2) {
46             if ((p[j].x-xmid)*(p[j].x-xmid) < delta2) {
47                 Q.push(p[j]);
48             }
49             ++j;
50         }
51         while (!Q.empty() && Q.front().y < p[i].y && (Q.
52         front().y-p[i].y)*(Q.front().y-p[i].y) > delta2
53         ) {
54             Q.pop();
55         }
56         while (!Q.empty()) {
57             delta2 = min(delta2, dist2(p[i], Q.front()));
58             Q.pop();
59         }

```

```

54     }
55 }
56 return delta2;
57 }
58 ll find_distance(int l, int r) {
59     if (r - l <= 3000) {
60         ll ans = 0x3f3f3f3f3f3f3f3f;
61         for (int i = l; i < r; ++i)
62             for (int j = i+1; j < r; ++j)
63                 ans = min(ans, dist2(p[i], p[j]));
64         return ans;
65     }
66     int m = (l+r)/2;
67     ll delta2 = min(find_distance(l, m), find_distance(m, r));
68     return min(delta2, closet_point(l, m, r, delta2));
69 }
70 int main() {
71     ios_base::sync_with_stdio(false);
72     cin.tie(NULL);
73     int n;
74     cin >> n >> k;
75     F(n) cin >> p[i];
76     sort(p, p+n);
77     find_distance(0, n);
78     cout << PQ.top() << '\n';
79 }

```

4.9 MCC

```

1 struct Mcc{
2     // return pair of center and r^2
3     static const int MAXN = 1000100;
4     int n;
5     pdd p[MAXN], cen;
6     double r2;
7     void init(int _n, pdd _p[]){
8         n = _n;
9         memcpy(p, _p, sizeof(pdd)*n);
10    }
11    double sqr(double a){ return a*a; }
12    double abs2(pdd a){ return a*a; }
13    pdd center(pdd p0, pdd p1, pdd p2) {
14        pdd a = p1-p0;
15        pdd b = p2-p0;
16        double c1=abs2(a)*0.5;
17        double c2=abs2(b)*0.5;
18        double d = a.x*b.y-b.x*a.y;
19        double x = p0.x + (c1 * b.y - c2 * a.y) / d;
20        double y = p0.y + (a.x * c2 - b.x * c1) / d;
21        return pdd(x,y);
22    }
23    pair<pdd,double> solve(){
24        random_shuffle(p,p+n);
25        r2=0;
26        for (int i=0; i<n; i++){
27            if (abs2(cen-p[i]) <= r2) continue;
28            cen = p[i];
29            r2 = 0;
30            for (int j=0; j<i; j++){
31                if (abs2(cen-p[j]) <= r2) continue;
32                cen = 0.5 * (p[i]+p[j]);
33                r2 = abs2(cen-p[j]);
34                for (int k=0; k<j; k++){
35                    if (abs2(cen-p[k]) <= r2)
36                        continue;
37                    cen = center(p[i],p[j],p[k]);
38                    r2 = abs2(cen-p[k]);
39                }
40            }
41            return {cen,r2};
42        }
43    }mcc;

```

4.10 LineIntersection

```

1 pdd interPnt(pdd p1, pdd p2, pdd q1, pdd q2, bool &
2 res)
3 {
4     double f1 = cross(p2, q1, p1);

```

```

4     double f2 = -cross(p2, q2, p1);
5     double f = (f1 + f2);
6     if(fabs(f) < EPS) {
7         res = false;
8         return {};
9     }
10    res = true;
11    return (f2 / f) * q1 + (f1 / f) * q2;
12 }

```

4.11 PointToLine

```

1 double cal(const pii &a,const pii &b,const pii &c){
2     int hi=dot(mp(a.x-b.x,a.y-b.y),mp(c.x-b.x,c.y-b.y))
3     );
4     if(hi<=0){
5         return dis(a,b);
6     }
7     hi=dot(mp(a.x-c.x,a.y-c.y),mp(b.x-c.x,b.y-c.y));
8     if(hi<=0){
9         return dis(c,a);
10    }
11    if(b.x==c.x)
12        return abs(a.x-b.x);
13    if(b.y==c.y)
14        return abs(a.y-b.y);
15    double B=(double)(b.x-c.x)/(b.y-c.y);
16    double C=(double)(b.y*c.x-b.x*c.y)/(b.y-c.y);
17    return abs(-a.x+B*a.y+C)/sqrt(1+sqr(B));

```

5 Graph

5.1 Planar

```

1 //skydog
2 #include <iostream>
3 #include <cstdio>
4 #include <cstdlib>
5 #include <iomanip>
6
7 #include <vector>
8 #include <cstring>
9 #include <string>
10 #include <queue>
11 #include <deque>
12 #include <stack>
13 #include <map>
14 #include <set>
15
16 #include <utility>
17 #include <list>
18
19 #include <cmath>
20 #include <algorithm>
21 #include <cassert>
22 #include <bitset>
23 #include <complex>
24 #include <limits>
25 #include <functional>
26 using namespace std;
27
28 typedef long long ll;
29 typedef pair<int, int> ii;
30 typedef pair<ll, ll> l4;
31
32 #define mp make_pair
33 #define pb push_back
34
35 #define debug(x) cerr << #x << " = " << x << " "
36
37 const int N=400+1;
38
39 struct Planar
40 {
41     int n,m,hash[N],fa[N],deep[N],low[N],ecp[N];
42     vector<int> g[N],son[N];
43     set< pair<int,int> > SDlist[N],proots[N];
44     int nxt[N][2],back[N],rev[N];
45     deque<int> q;

```

```

46 void dfs(int u)
47 {
48     hash[u]=1; q.pb(u);
49     ecp[u]=low[u]=deep[u];
50     int v;
51     for (int i = 0; i < g[u].size(); ++i)
52         if(!hash[v=g[u][i]])
53         {
54             fa[v]=u;
55             deep[v]=deep[u]+1;
56             dfs(v);
57             low[u]=min(low[u],low[v]);
58             SDlist[u].insert(mp(low[v],v));
59         }
60         else ecp[u]=min(ecp[u],deep[v]);
61     low[u]=min(low[u],ecp[u]);
62 }
63
64 int visited[N];
65
66 void addtree(int u,int t1,int v,int t2)
67 {
68     nxt[u][t1]=v; nxt[v][t2]=u;
69 }
70
71 void findnxt(int u,int v,int& u1,int& v1)
72 {
73     u1=nxt[u][v^1];
74     if(nxt[u1][0]==u) v1=0;
75     else v1=1;
76 }
77
78 void walkup(int u,int v)
79 {
80     back[v]=u;
81     int v1=v,v2=v,u1=1,u2=0,z;
82     for (;;)
83     {
84         if(hash[v1]==u || hash[v2]==u) break;
85         hash[v1]=u;hash[v2]=u; z=max(v1,v2);
86         if(z>n)
87         {
88             int p=fa[z-n];
89             if(p!=u)
90             {
91                 roots[p].insert(mp(-low[z-n], z
92 ));
93                 v1=p,v2=p,u1=0,u2=1;
94             }
95             else break;
96         }
97         else
98         {
99             findnxt(v1,u1,v1,u1);
100             findnxt(v2,u2,v2,u2);
101         }
102     }
103
104 int topstack;
105 pair<int,int> stack[N];
106
107 int outer(int u,int v)
108 {
109     return ecp[v]<deep[u] || (SDlist[v].size()
110 && SDlist[v].begin()->first<deep[u]);
111 }
112
113 int inside(int u,int v)
114 {
115     return roots[v].size()>0 || back[v]==u;
116 }
117
118 int active(int u,int v)
119 {
120     return inside(u,v) || outer(u,v);
121 }
122
123 void push(int a,int b)
124 {
125     stack[++topstack]=mp(a,b);

```

```

126
127 void mergestack()
128 {
129     int v1,t1,v2,t2,s,s1;
130     v1=stack[topstack].first;t1=stack[topstack].
131     second;
132     topstack--;
133     v2=stack[topstack].first;t2=stack[topstack].
134     second;
135     topstack--;
136     s=nxt[v1][t1^1];
137     s1=(nxt[s][1]==v1);
138     nxt[s][s1]=v2;
139     nxt[v2][t2]=s;
140
141     SDlist[v2].erase( make_pair(low[v1-n],v1-n)
142 );
143     roots[v2].erase( make_pair(-low[v1-n],v1) )
144 ;
145 }
146
147 void findnxtActive(int u,int t,int& v,int& w1,
148 int S)
149 {
150     findnxt(u,t,v,w1);
151     while(u!=v && !active(S,v))
152         findnxt(v,w1,v,w1);
153 }
154
155 void walkdown(int S,int u)
156 {
157     topstack=0;
158     int t1,v=S,w1,x2,y2,x1,y1,p;
159     for(t1=0;t1<2;++t1)
160     {
161         findnxt(S,t1^1,v,w1);
162         while(v!=S)
163         {
164             if(back[v]==u)
165             {
166                 while(topstack>0) mergestack();
167                 addtree(S,t1,v,w1); back[v]=0;
168             }
169             if(roots[v].size())
170             {
171                 push(v,w1);
172                 p=roots[v].begin()->second;
173                 findnxtActive(p,1,x1,y1,u);
174                 findnxtActive(p,0,x2,y2,u);
175                 if(active(u,x1) && !outer(u,x1))
176                     v=x1,w1=y1;
177                 else if(active(u,x2) && !outer(u
178 ,x2))
179                     v=x2,w1=y2;
180                 else if(inside(u,x1) || back[x1
181 ]==u)
182                     v=x1,w1=y1;
183                 else v=x2,w1=y2;
184                 push(p,v==x2);
185             }
186             else if(v>n || ( ecp[v]>=deep[u] &&
187 !outer(u,v) ))
188                 findnxt(v,w1,v,w1);
189             else if(v<=n && outer(u,v) && !
190 topstack)
191             {
192                 addtree(S,t1,v,w1); break;
193             }
194             else break;
195         }
196     }
197 }
198
199 int work(int u)
200 {
201     int v;
202     for (int i = 0; i < g[u].size(); ++i)
203         if(fa[v=g[u][i]]==u)
204         {
205             son[u].push_back(n+v);
206             roots[n+v].clear();

```

```

199         addtree(n+v,1,v,0);
200         addtree(n+v,0,v,1);
201     }
202     for (int i = 0; i < g[u].size(); ++i)
203         if(deep[v=g[u][i]]>deep[u]+1)
204             walkup(u,v);
205     topstack=0;
206     for (int i = 0; i < son[u].size(); ++i)
207         walkdown(son[u][i], u);
208     for (int i = 0; i < g[u].size(); ++i)
209         if(deep[v=g[u][i]]>deep[u]+1 && back[v])
210             return 0;
211     return 1;
212 }
213 void init(int _n)
214 {
215     n = _n;
216     m = 0;
217     for(int i=1;i<=2*n;++i)
218     {
219         g[i].clear();
220         SDlist[i].clear();
221         son[i].clear();
222         proots[i].clear();
223         nxt[i][0]=nxt[i][1]=0;
224         fa[i]=0;
225         hash[i]=0;low[i]=ecp[i]=deep[i]=back[i]
226     ]=0;
227         q.clear();
228     }
229 void add(int u, int v)
230 {
231     ++m;
232     g[u].pb(v); g[v].pb(u);
233 }
234 bool check_planar()
235 {
236     if(m>3*n-5)
237         return false;
238     // memset(hash,0,sizeof hash);
239     for(int i=1;i<=n;++i)
240         if(!hash[i])
241         {
242             deep[i]=1;
243             dfs(i);
244         }
245     memset(hash,0,sizeof hash);
246     //memset(hash, 0, (2*n+1)*sizeof(hash[0]));
247     // originally only looks at last n element
248     assert(q.size() == n);
249     while (!q.empty())
250     {
251         if (!work(q.back()))
252             return false;
253         q.pop_back();
254     }
255     return true;
256 }
257 } base, _new;
258 vector<ii> edges;
259 int n, m;
260 inline void build(int n, Planar &_new)
261 {
262     _new.init(n);
263     for (auto e : edges)
264         _new.add(e.first, e.second);
265 }
266 void end()
267 {
268     puts("-1");
269     exit(0);
270 }
271 bool vis[N];
272 const int maxp = 5;
273 int path[maxp], tp=0;
274 void dfs(int cur)
275 {
276     vis[cur] = true;
277     path[tp++] = cur;
278     if (tp == maxp)

```

```

279 {
280     auto it = lower_bound(base.g[cur].begin(), base.
281     g[cur].end(), path[0]);
282     if ( it != base.g[cur].end() && *it == path
283     [0])
284     {
285         //a cycle
286         int x = n+1;
287         for (int i = 0; i < 5; ++i) edges.pb(mp(
288         x, path[i]));
289         build(x, _new);
290         if (_new.check_planar())
291         {
292             for (int i = 0; i < maxp; ++i)
293                 printf("%d%c", path[i], i==maxp-1?'\\n':' ');
294             exit(0);
295         }
296         for (int i = 0; i < 5; ++i) edges.
297         pop_back();
298     }
299     else
300     {
301         for (auto e : base.g[cur]) if (!vis[e]) dfs(
302         e);
303     }
304     vis[cur] = false;
305     --tp;
306 }
307 int main()
308 {
309     scanf("%d %d", &n, &m);
310     if (n <= 4)
311     {
312         assert(false);
313         puts("0"); return 0;
314     }
315     for (int i = 0; i < m; ++i)
316     {
317         int u, v; scanf("%d %d", &u, &v);
318         edges.pb(mp(u, v));
319     }
320     build(n, base);
321     if (!base.check_planar()) end();
322     for (int i = 1; i <= n; ++i)
323         sort(base.g[i].begin(), base.g[i].end());
324     for (int i = 1; i <= n; ++i)
325         dfs(i);
326     end();
327 }

```

5.2 MMC

```

1 /* minimum mean cycle 最小平均值環*/
2 const int MXN = 16004;
3 const int MAXE = 1805;
4 const int MAXN = 35;
5 const double inf = 1029384756;
6 const double eps = 1e-6;
7 struct Edge {
8     int v,u;
9     double c;
10 };
11 int n,m,prv[MAXN][MAXN], prve[MAXN][MAXN], vst[MAXN]
12 ];
13 Edge e[MAXE];
14 vector<int> edgeID, cycle, rho;
15 double d[MAXN][MAXN];
16 inline void bellman_ford() {
17     for(int i=0; i<n; i++) d[0][i]=0;
18     for(int i=0; i<n; i++) {
19         fill(d[i+1], d[i+1]+n, inf);
20         for(int j=0; j<m; j++) {
21             int v = e[j].v, u = e[j].u;
22             if(d[i][v]<inf && d[i+1][u]>d[i][v]+e[j
23             ].c) {
24                 d[i+1][u] = d[i][v]+e[j].c;
25                 prv[i+1][u] = v;
26                 prve[i+1][u] = j;
27             }
28         }
29     }
30 }

```



```

26     }
27 }
28 }
29 double karp_mmc() {
30     // returns inf if no cycle, mmc otherwise
31     double mmc=inf;
32     int st = -1;
33     bellman_ford();
34     for(int i=0; i<n; i++) {
35         double avg=-inf;
36         for(int k=0; k<n; k++) {
37             if(d[n][i]<inf-eps) avg=max(avg,(d[n][i]
38             ]-d[k][i])
39             /(n-k));
40             else avg=max(avg,inf);
41         }
42         if (avg < mmc) tie(mmc, st) = tie(avg, i);
43     }
44     MEM(vst); edgeID.clear(); cycle.clear(); rho.
45     clear();
46     for (int i=n; !vst[st]; st=prv[i--][st]) {
47         vst[st]++;
48         edgeID.pb(prve[i][st]);
49         rho.pb(st);
50     }
51     while (vst[st] != 2) {
52         int v = rho.back(); rho.pop_back();
53         cycle.pb(v);
54         vst[v]++;
55     }
56     reverse(edgeID.begin(),edgeID.end());
57     edgeID.resize(cycle.size());
58     return mmc;
59 }

```

5.3 SomeTheroem

```

1 /*
2  General graph
3  |maximum independent set|+|minimum vertex cover|=|V|
4  |maximum independent edge|+|minimum edge cover|=|V|
5  ||
6  Max_match
7  Bipartite graph
8  |Maximum independent set|=|Minimum edge cover|
9  |Maximum independent edge|=|Minimum vertex cover|
10 |Maximum Independent set|+|Minimum vertex cover|=|V|
11      +              +
12 |Maximum Independent edge|+|Minimum edge cover|=|V|
13      ||              ||
14      |V|              |V|
15 */

```

5.4 Dominator

```

1 struct DominatorTree{
2     static const int MAXN = 200010;
3     int n,s;
4     vector<int> g[MAXN],pred[MAXN];
5     vector<int> cov[MAXN];
6     int dfn[MAXN],nfd[MAXN],ts;
7     int par[MAXN];
8     int sdom[MAXN],idom[MAXN];
9     int mom[MAXN],mn[MAXN];
10
11     inline bool cmp(int u,int v) { return dfn[u] < dfn
12     [v]; }
13
14     int eval(int u) {
15         if(mom[u] == u) return u;
16         int res = eval(mom[u]);
17         if(cmp(sdom[mn[mom[u]]],sdom[mn[u]]))
18             mn[u] = mn[mom[u]];
19         return mom[u] = res;
20     }
21
22     void init(int _n, int _s) {
23         n = _n;
24         s = _s;
25         REP1(i,1,n) {
26             g[i].clear();

```

```

26         pred[i].clear();
27         idom[i] = 0;
28     }
29 }
30 void add_edge(int u, int v) {
31     g[u].push_back(v);
32     pred[v].push_back(u);
33 }
34 void DFS(int u) {
35     ts++;
36     dfn[u] = ts;
37     nfd[ts] = u;
38     for(int v:g[u]) if(dfn[v] == 0) {
39         par[v] = u;
40         DFS(v);
41     }
42 }
43 void build() {
44     ts = 0;
45     REP1(i,1,n) {
46         dfn[i] = nfd[i] = 0;
47         cov[i].clear();
48         mom[i] = mn[i] = sdom[i] = i;
49     }
50     DFS(s);
51     for (int i=ts; i>=2; i--) {
52         int u = nfd[i];
53         if(u == 0) continue;
54         for(int v:pred[u]) if(dfn[v]) {
55             eval(v);
56             if(cmp(sdom[mn[v]],sdom[u])) sdom[u] = sdom[
57             mn[v]];
58             cov[sdom[u]].push_back(u);
59             mom[u] = par[u];
60             for(int w:cov[par[u]]) {
61                 eval(w);
62                 if(cmp(sdom[mn[w]],par[u])) idom[w] = mn[w];
63                 else idom[w] = par[u];
64             }
65             cov[par[u]].clear();
66         }
67         REP1(i,2,ts) {
68             int u = nfd[i];
69             if(u == 0) continue;
70             if(idom[u] != sdom[u]) idom[u] = idom[idom[u]
71             ];
72         }
73     } dom;

```

5.5 DMST

```

1 struct zhu_liu{
2     static const int MAXN=1100,MAXM=1005005;
3     struct node{
4         int u,v;
5         LL w,tag;
6         node *l,*r;
7         node(int u=0,int v=0,LL w=0):u(u),v(v),w(w),tag
8         (0),l(0),r(0){}
9         void down(){
10             w+=tag;
11             if(l)l->tag+=tag;
12             if(r)r->tag+=tag;
13             tag=0;
14         }
15     }mem[MAXN];
16     node *pq[MAXN*2],*E[MAXN*2];
17     int st[MAXN*2],id[MAXN*2],m,from[MAXN*2];
18     void init(int n){
19         for(int i=1;i<=n;++i){
20             pq[i]=E[i]=0;
21             st[i]=id[i]=i;
22             from[i]=0;
23         }m=0;
24     }
25     node *merge(node *a,node *b){//skew heap
26         if(!a||!b)return a?a:b;
27         a->down(),b->down();
28         if(b->w<a->w)return merge(b,a);

```

```

28     if(b->w==a->w&&b->v<a->v)return merge(b,a);//
29     swap(a->l,a->r);
30     a->l=merge(b,a->l);
31     return a;
32 }
33 void add_edge(int u,int v,LL w){
34     if(u!=v)pq[v]=merge(pq[v],&(mem[m++]=node(u,v,w)
35 ));
36 }
37 int find(int x,int *st){
38     return st[x]==x?x:st[x]=find(st[x],st);
39 }
40 LL build(int root,int n){
41     LL ans=0;int N=n,all=n;
42     for(int i=1;i<=N;++i){
43         if(i==root||!pq[i])continue;
44         while(pq[i]){
45             pq[i]->down(),E[i]=pq[i];
46             pq[i]=merge(pq[i]->l,pq[i]->r);
47             if(find(E[i]->u,id)!=find(i,id))break;
48         }
49         if(find(E[i]->u,id)==find(i,id))continue;
50         from[E[i]->v]=E[i]->u;
51         ans+=E[i]->w;
52         if(find(E[i]->u,st)==find(i,st)){
53             if(pq[i])pq[i]->tag-=E[i]->w;
54             pq[++N]=pq[i],id[N]=N;
55             for(int u=find(E[i]->u,id);u!=i;u=find(E[u]
56 )->u,id)){
57                 if(pq[u])pq[u]->tag-=E[u]->w;
58                 id[find(u,id)]=N;
59                 pq[N]=merge(pq[N],pq[u]);
60             }
61             st[N]=find(i,st);
62             id[find(i,id)]=N;
63             }else st[find(i,st)]=find(E[i]->u,st),--all;
64         }
65     }return all==1?ans:-1;//圖不連通就無解
66 }MST;

```

5.6 SCC

```

1 struct Scc{
2     int n, nScc, vst[MXN], bln[MXN];
3     vector<int> E[MXN], rE[MXN], vec;
4     void init(int _n){
5         n = _n;
6         for (int i=0; i<MXN; i++){
7             E[i].clear();
8             rE[i].clear();
9         }
10    }
11    void add_edge(int u, int v){
12        E[u].pb(v);
13        rE[v].pb(u);
14    }
15    void DFS(int u){
16        vst[u]=1;
17        for (auto v : E[u])
18            if (!vst[v]) DFS(v);
19        vec.pb(u);
20    }
21    void rDFS(int u){
22        vst[u] = 1;
23        bln[u] = nScc;
24        for (auto v : rE[u])
25            if (!vst[v]) rDFS(v);
26    }
27    void solve(){
28        nScc = 0;
29        vec.clear();
30        MEM(vst);
31        for (int i=0; i<n; i++)
32            if (!vst[i]) DFS(i);
33        reverse(vec.begin(),vec.end());
34        FZ(vst);
35        for (auto v : vec){
36            if (!vst[v]){
37                rDFS(v);
38                nScc++;

```

```

39     }
40     }
41 }
42 };

```

5.7 GeneralGraphMaximunValueMatch

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 //from vfleaking
4 //自己進行一些進行一些小修改
5 #define INF INT_MAX
6 #define MAXN 400
7 struct edge{
8     int u,v,w;
9     edge(){}
10    edge(int u,int v,int w):u(u),v(v),w(w){}
11 }
12 int n,n_x;
13 edge g[MAXN*2+1][MAXN*2+1];
14 int lab[MAXN*2+1];
15 int match[MAXN*2+1],slack[MAXN*2+1],st[MAXN*2+1],pa[
16     MAXN*2+1];
17 int flower_from[MAXN*2+1][MAXN+1],S[MAXN*2+1],vis[
18     MAXN*2+1];
19 vector<int> flower[MAXN*2+1];
20 queue<int> q;
21 inline int e_delta(const edge &e){ // does not work
22     inside blossoms
23     return lab[e.u]+lab[e.v]-g[e.u][e.v].w*2;
24 }
25 inline void update_slack(int u,int x){
26     if(!slack[x]||e_delta(g[u][x])<e_delta(g[slack[x]
27 ][x]))slack[x]=u;
28 }
29 inline void set_slack(int x){
30     slack[x]=0;
31     for(int u=1;u<=n;++u)
32         if(g[u][x].w>0&&st[u]!=x&&S[st[u]]==0)
33             update_slack(u,x);
34 }
35 void q_push(int x){
36     if(x<=n)q.push(x);
37     else for(size_t i=0;i<flower[x].size();i++)q_push(
38         flower[x][i]);
39 }
40 inline void set_st(int x,int b){
41     st[x]=b;
42     if(x>n)for(size_t i=0;i<flower[x].size();++i)
43         set_st(flower[x][i],b);
44 }
45 inline int get_pr(int b,int xr){
46     int pr=find(flower[b].begin(),flower[b].end(),xr)-
47         flower[b].begin();
48     if(pr%2==1){//檢查他在前一層圖是奇點還是偶點
49         reverse(flower[b].begin()+1,flower[b].end());
50         return (int)flower[b].size()-pr;
51     }else return pr;
52 }
53 inline void set_match(int u,int v){
54     match[u]=g[u][v].v;
55     if(u>n){
56         edge e=g[u][v];
57         int xr=flower_from[u][e.u],pr=get_pr(u,xr);
58         for(int i=0;i<pr;++i)set_match(flower[u][i],
59             flower[u][i^1]);
60         set_match(xr,v);
61         rotate(flower[u].begin(),flower[u].begin()+pr,
62             flower[u].end());
63     }
64 }
65 inline void augment(int u,int v){
66     for(;;){
67         int xnv=st[match[u]];
68         set_match(u,v);
69         if(!xnv)return;
70         set_match(xnv,st[pa[xnv]]);
71         u=st[pa[xnv]],v=xnv;
72     }
73 }
74 inline int get_lca(int u,int v){

```

```

66 static int t=0;
67 for(++t;u!=v;swap(u,v)){
68     if(u==0)continue;
69     if(vis[u]==t)return u;
70     vis[u]=t; //這種方法可以不用清空v陣列
71     u=st[match[u]];
72     if(u)u=st[pa[u]];
73 }
74 return 0;
75 }
76 inline void add_blossom(int u,int lca,int v){
77     int b=n+1;
78     while(b<=n_x&&st[b]==0){
79         if(b>n_x)++n_x;
80         lab[b]=0,S[b]=0;
81         match[b]=match[lca];
82         flower[b].clear();
83         flower[b].push_back(lca);
84         for(int x=u,y; x!=lca; x=st[pa[y]])
85             flower[b].push_back(x),flower[b].push_back(y=st[
86                 match[x]]),q_push(y);
87         reverse(flower[b].begin()+1,flower[b].end());
88         for(int x=v,y; x!=lca; x=st[pa[y]])
89             flower[b].push_back(x),flower[b].push_back(y=st[
90                 match[x]]),q_push(y);
91         set_st(b,b);
92         for(int x=1;x<=n_x;++x)g[b][x].w=g[x][b].w=0;
93         for(int x=1;x<=n;++x)flower_from[b][x]=0;
94         for(size_t i=0;i<flower[b].size();++i){
95             int xs=flower[b][i];
96             for(int x=1;x<=n_x;++x)
97                 if(g[b][x].w==0||e_delta(g[xs][x])<e_delta(g[b][x]))
98                     g[b][x]=g[xs][x],g[x][b]=g[x][xs];
99             for(int x=1;x<=n;++x)
100                 if(flower_from[xs][x])flower_from[b][x]=xs;
101         }
102         set_slack(b);
103 }
104 inline void expand_blossom(int b){ // S[b] == 1
105     for(size_t i=0;i<flower[b].size();++i)
106         set_st(flower[b][i],flower[b][i]);
107     int xr=flower_from[b][g[b][pa[b]].u],pr=get_pr(b,xr);
108     for(int i=0;i<pr;i+=2){
109         int xs=flower[b][i],xns=flower[b][i+1];
110         pa[xs]=g[xns][xs].u;
111         S[xs]=1,S[xns]=0;
112         slack[xs]=0,set_slack(xns);
113         q_push(xns);
114     }
115     S[xr]=1,pa[xr]=pa[b];
116     for(size_t i=pr+1;i<flower[b].size();++i){
117         int xs=flower[b][i];
118         S[xs]=-1,set_slack(xs);
119     }
120     st[b]=0;
121 }
122 inline bool on_found_edge(const edge &e){
123     int u=st[e.u],v=st[e.v];
124     if(S[v]==-1){
125         pa[v]=e.u,S[v]=1;
126         int nu=st[match[v]];
127         slack[v]=slack[nu]=0;
128         S[nu]=0,q_push(nu);
129     }else if(S[v]==0){
130         int lca=get_lca(u,v);
131         if(!lca)return augment(u,v),augment(v,u),true;
132         else add_blossom(u,lca,v);
133     }
134     return false;
135 }
136 inline bool matching(){
137     memset(S+1,-1,sizeof(int)*n_x);
138     memset(slack+1,0,sizeof(int)*n_x);
139     q=queue<int>();
140     for(int x=1;x<=n_x;++x)
141         if(st[x]==x&&!match[x])pa[x]=0,S[x]=0,q_push(x);
142     if(q.empty())return false;
143     for(;;){
144         while(q.size()){
145             int u=q.front();q.pop();

```

```

144         if(S[st[u]]==1)continue;
145         for(int v=1;v<=n_x;++v)
146             if(g[u][v].w>0&&st[u]!=st[v]){
147                 if(e_delta(g[u][v])==0){
148                     if(on_found_edge(g[u][v]))return true;
149                 }else update_slack(u,st[v]);
150             }
151     }
152     int d=INF;
153     for(int b=n+1;b<=n_x;++b)
154         if(st[b]==b&&S[b]==1)d=min(d,lab[b]/2);
155     for(int x=1;x<=n_x;++x)
156         if(st[x]==x&&slack[x]){
157             if(S[x]==-1)d=min(d,e_delta(g[slack[x]][x]));
158             else if(S[x]==0)d=min(d,e_delta(g[slack[x]][
159                 x])/2);
160         }
161     for(int u=1;u<=n;++u){
162         if(S[st[u]]==0){
163             if(lab[u]<=d)return 0;
164             lab[u]-=d;
165         }else if(S[st[u]]==1)lab[u]+=d;
166     }
167     for(int b=n+1;b<=n_x;++b)
168         if(st[b]==b){
169             if(S[st[b]]==0)lab[b]+=d*2;
170             else if(S[st[b]]==1)lab[b]-=d*2;
171         }
172     q=queue<int>();
173     for(int x=1;x<=n_x;++x)
174         if(st[x]==x&&slack[x]&&st[slack[x]]!=x&&
175             e_delta(g[slack[x]][x])==0)
176             if(on_found_edge(g[slack[x]][x]))return true;
177     for(int b=n+1;b<=n_x;++b)
178         if(st[b]==b&&S[b]==1&&lab[b]==0)expand_blossom(b);
179     return false;
180 }
181 inline pair<long long,int> weight_blossom(){
182     memset(match+1,0,sizeof(int)*n);
183     n_x=n;
184     int n_matches=0;
185     long long tot_weight=0;
186     for(int u=0;u<=n;++u)st[u]=u,flower[u].clear();
187     int w_max=0;
188     for(int u=1;u<=n;++u)
189         for(int v=1;v<=n;++v){
190             flower_from[u][v]=(u==v?u:0);
191             w_max=max(w_max,g[u][v].w);
192         }
193     for(int u=1;u<=n;++u)lab[u]=w_max;
194     while(matching())++n_matches;
195     for(int u=1;u<=n;++u)
196         if(match[u]&&match[u]<u)
197             tot_weight+=g[u][match[u]].w;
198     return make_pair(tot_weight,n_matches);
199 }
200 inline void init_weight_graph(){
201     for(int u=1;u<=n;++u)
202         for(int v=1;v<=n;++v)
203             g[u][v]=edge(u,v,0);
204 }
205 int main(){
206     int m;
207     scanf("%d",&n,&m);
208     init_weight_graph();
209     for(int i=0;i<m;++i){
210         int u,v,w;
211         scanf("%d%d%d",&u,&v,&w);
212         g[u][v].w=g[v][u].w=w;
213     }
214     printf("%lld\n",weight_blossom().first);
215     for(int u=1;u<=n;++u)printf("%d ",match[u]);puts("
");
216     return 0;

```

5.8 Stable Marriage

```

1 #define F(n) Fi(i, n)
2 #define Fi(i, n) Fl(i, 0, n)
3 #define Fl(i, l, n) for(int i = l ; i < n ; ++i)
4 #include <bits/stdc++.h>
5 using namespace std;
6 int D, quota[205], weight[205][5];
7 int S, scoretodep[12005][205], score[5];
8 int P, prefer[12005][85], iter[12005];
9 int ans[12005];
10 typedef pair<int, int> PII;
11 map<int, int> samescore[205];
12 typedef priority_queue<PII, vector<PII>, greater<PII>
    >> QQQ;
13 QQQ pri[205];
14 void check(int d) {
15     PII t = pri[d].top();
16     int v;
17     if (pri[d].size() - samescore[d][t.first] + 1 <=
        quota[d]) return;
18     while (pri[d].top().first == t.first) {
19         v = pri[d].top().second;
20         ans[v] = -1;
21         --samescore[d][t.first];
22         pri[d].pop();
23     }
24 }
25 void push(int s, int d) {
26     if (pri[d].size() < quota[d]) {
27         pri[d].push(PII(scoretodep[s][d], s));
28         ans[s] = d;
29         ++samescore[s][scoretodep[s][d]];
30     } else if (scoretodep[s][d] >= pri[d].top().first) {
31         pri[d].push(PII(scoretodep[s][d], s));
32         ans[s] = d;
33         ++samescore[s][scoretodep[s][d]];
34         check(d);
35     }
36 }
37 void f() {
38     int over;
39     while (true) {
40         over = 1;
41         Fi (q, S) {
42             if (ans[q] != -1 || iter[q] >= P) continue;
43             push(q, prefer[q][iter[q]++]);
44             over = 0;
45         }
46         if (over) break;
47     }
48 }
49 main() {
50     ios::sync_with_stdio(false);
51     cin.tie(NULL);
52     int sadmit, stof, dexceed, dfew;
53     while (cin >> D, D) { // Beware of the input
        format or judge may troll us.
54         sadmit = stof = dexceed = dfew = 0;
55         memset(iter, 0, sizeof(iter));
56         memset(ans, 0, sizeof(ans));
57         Fi (q, 205) {
58             pri[q] = QQQ();
59             samescore[q].clear();
60         }
61         cin >> S >> P;
62         Fi (q, D) {
63             cin >> quota[q];
64             Fi (w, 5) cin >> weight[q][w];
65         }
66         Fi (q, S) {
67             Fi (w, 5) cin >> score[w];
68             Fi (w, D) {
69                 scoretodep[q][w] = 0;
70                 F (5) scoretodep[q][w] += weight[w][i] *
                    score[i];
71             }
72         }
73         Fi (q, S) Fi (w, P) {
74             cin >> prefer[q][w];
75             --prefer[q][w];
76         }

```

```

77     f();
78     Fi (q, D) sadmit += pri[q].size();
79     Fi (q, S) if (ans[q] == prefer[q][0]) ++stof;
80     Fi (q, D) if (pri[q].size() > quota[q]) ++
        dexceed;
81     Fi (q, D) if (pri[q].size() < quota[q]) ++dfew;
82     cout << sadmit << ' ' << stof << ' ' << dexceed
        << ' ' << dfew << '\n';
83 }
84 }

```

5.9 BCCvertex

```

1 const int MXN = 16004;
2 struct BccVertex {
3     int n, nScc, step, dfn[MXN], low[MXN];
4     vector<int> E[MXN], sccv[MXN];
5     int top, stk[MXN];
6     void init(int _n) {
7         n = _n;
8         nScc = step = 0;
9         for (int i=0; i<n; i++) E[i].clear();
10    }
11    void add_edge(int u, int v) {
12        E[u].pb(v);
13        E[v].pb(u);
14    }
15    void DFS(int u, int f) {
16        dfn[u] = low[u] = step++;
17        stk[top++] = u;
18        for (auto v:E[u]) {
19            if (v == f) continue;
20            if (dfn[v] == -1) {
21                DFS(v, u);
22                low[u] = min(low[u], low[v]);
23                if (low[v] >= dfn[u]) {
24                    int z;
25                    sccv[nScc].clear();
26                    do {
27                        z = stk[--top];
28                        sccv[nScc].pb(z);
29                    } while (z != v);
30                    sccv[nScc].pb(u);
31                    nScc++;
32                }
33            } else {
34                low[u] = min(low[u], dfn[v]);
35            }
36        }
37    }
38    vector<vector<int>> solve() {
39        vector<vector<int>> res;
40        for (int i=0; i<n; i++) {
41            dfn[i] = low[i] = -1;
42        }
43        for (int i=0; i<n; i++) {
44            if (dfn[i] == -1) {
45                top = 0;
46                DFS(i, i);
47            }
48        }
49        for (int i=0; i<nScc; i++) res.pb(sccv[i]);
50        return res;
51    }
52 }graph;

```

5.10 MaxClique

```

1 class MaxClique {
2 public:
3     static const int MV = 210;
4     int V;
5     int el[MV][MV/30+1];
6     int dp[MV];
7     int ans;
8     int s[MV][MV/30+1];
9     vector<int> sol;
10    void init(int v) {
11        V = v; ans = 0;
12        MEMS(el); MEMS(dp);
13    }

```

```

14  /* Zero Base */
15  void addEdge(int u, int v) {
16      if(u > v) swap(u, v);
17      if(u == v) return;
18      el[u][v/32] |= (1<<(v%32));
19  }
20  bool dfs(int v, int k) {
21      int c = 0, d = 0;
22      for(int i=0; i<(V+31)/32; i++) {
23          s[k][i] = el[v][i];
24          if(k != 1) s[k][i] &= s[k-1][i];
25          c += __builtin_popcount(s[k][i]);
26      }
27      if(c == 0) {
28          if(k > ans) {
29              ans = k;
30              sol.clear();
31              sol.push_back(v);
32              return 1;
33          }
34          return 0;
35      }
36      for(int i=0; i<(V+31)/32; i++) {
37          for(int a = s[k][i]; a ; d++) {
38              if(k + (c-d) <= ans) return 0;
39              int lb = a&(-a), lg = 0;
40              a ^= lb;
41              while(lb!=1) {
42                  lb = (unsigned int)(lb) >> 1;
43                  lg ++;
44              }
45              int u = i*32 + lg;
46              if(k + dp[u] <= ans) return 0;
47              if(dfs(u, k+1)) {
48                  sol.push_back(v);
49                  return 1;
50              }
51          }
52      }
53      return 0;
54  }
55  int solve() {
56      for(int i=V-1; i>=0; i--) {
57          dfs(i, 1);
58          dp[i] = ans;
59      }
60      return ans;
61  }
62 };

```

5.11 BCCedge

```

1  vector<vector<int>> > v;
2  int vis[100005], lwn[100005];
3  vector<int> stk;
4  int f[100005];
5  int bln[100005];
6  int Find(int a){
7      if(bln[a]==a) return a;
8      return bln[a]=Find(bln[a]);
9  }
10 int t;
11 void dfs(int a, int p){
12     stk.pb(a);
13     bln[a]=a;
14     vis[a]=lwn[a]=++t;
15     int cnt=0;
16     for(int i=0; i<v[a].size(); i++){
17         int x=v[a][i];
18         if(x!=p || cnt==1){
19             if(vis[x]==0){
20                 dfs(x, a);
21                 if(lwn[x]>vis[a]){
22                     int fa=Find(x);
23                     f[x]=Find(a);
24                     while(stk.back()!=x){
25                         bln[stk.back()]=fa;
26                         stk.pop_back();
27                     }
28                     bln[stk.back()]=fa;
29                     stk.pop_back();

```

```

30     }
31     lwn[a]=min(lwn[a], lwn[x]);
32     }
33     else{
34         lwn[a]=min(lwn[a], vis[x]);
35     }
36     }
37     else{
38         cnt++;
39     }
40 }
41 }

```

6 JAVA

6.1 Big Integer

```

1  import java.math.*;
2  import java.io.*;
3  import java.util.*;
4  public class Main{
5      public static void main(String []argv){
6          c[0][0]=BigInteger.ONE;
7          for(int i=1; i<3001; i++){
8              c[i][0]=BigInteger.ONE;
9              c[i][i]=BigInteger.ONE;
10             for(int j=1; j<i; j++) c[i][j]=c[i-1][j].
11                 add(c[i-1][j-1]);
12         }
13         Scanner scanner = new Scanner(System.in);
14         int T = scanner.nextInt();
15         BigInteger x;
16         BigInteger ans;
17         while(T-- > 0){
18             ans = BigInteger.ZERO;
19             int n = scanner.nextInt();
20             for(int i=0; i<n; i++){
21                 x = new BigInteger(scanner.next());
22                 if(i%2 == 1) ans=ans.subtract(c[n-1][i].
23                     multiply(x));
24                 else ans=ans.add(c[n-1][i].multiply(
25                     x));
26             }
27             if(n%2 == 0) ans=BigInteger.ZERO.subtract
28                 (ans);
29             System.out.println(ans);
30         }
31     }
32 }

```

6.2 Prime

```

1  import java.math.*;
2  import java.io.*;
3  import java.util.*;
4  public class Main{
5      public static void main(String []argv){
6          Scanner scanner = new Scanner(System.in);
7          int T = scanner.nextInt();
8          for (int cs = 0 ; cs < T ; cs++){
9              if (cs != 0) { System.out.println(""); }
10             int a = scanner.nextInt();
11             int b = scanner.nextInt();
12             for (int i = a ; i <= b ; i++) {
13                 BigInteger x = BigInteger.valueOf(i)
14                     ;
15                 if (x.isProbablePrime(5) == true) {
16                     System.out.println(x);
17                 }
18             }
19         }
20     }

```

7 Other

7.1 Annealing


```

1 double distForAllPoints(double x, double y,
2     vector< pair<int, int> > &D) {
3     double sum = 0;
4     for(int i = D.size()-1; i >= 0; i--) {
5         sum += hypot(D[i].first - x, D[i].second - y);
6     }
7     return sum;
8 }
9 double randDouble() {
10    return (rand() % 32767) / 32767.0;
11 }
12 double annealing(vector< pair<int, int> > &D) {
13     #define S_MUL 0.6f
14     #define S_LEN 1000
15     #define T_CNT 10
16     #define E_CNT 10
17     double step = S_LEN;
18     double x[E_CNT], y[E_CNT], val[E_CNT];
19     double Lx, Ly, Rx, Ry, tx, ty, tcost;
20     Lx = Rx = D[0].first;
21     Ly = Ry = D[0].second;
22     for(int i = 0; i < D.size(); i++) {
23         Lx = min(Lx, (double)D[i].first);
24         Rx = max(Rx, (double)D[i].first);
25         Ly = min(Ly, (double)D[i].second);
26         Ry = max(Ry, (double)D[i].second);
27     }
28     for(int i = 0; i < E_CNT; i++) {
29         x[i] = randDouble() * (Rx - Lx) + Lx;
30         y[i] = randDouble() * (Ry - Ly) + Ly;
31         val[i] = distForAllPoints(x[i], y[i], D);
32     }
33     while(step > 0.1) {
34         for(int i = 0; i < E_CNT; i++) {
35             for(int j = 0; j < T_CNT; j++) {
36                 tx = x[i] + randDouble() * 2 * step - step;
37                 ty = y[i] + randDouble() * 2 * step - step;
38                 tcost = distForAllPoints(tx, ty, D);
39                 if(tcost < val[i]) {
40                     val[i] = tcost, x[i] = tx, y[i] = ty;
41                 }
42             }
43         }
44         step *= S_MUL;
45     }
46     double ret = val[0];
47     for(int i = 0; i < E_CNT; i++) {
48         ret = min(ret, val[i]);
49     }
50     printf("%.0lf\n", ret);
51 }
52 int main() {
53     int testcase, N;
54     scanf("%d", &testcase);
55     while(testcase--) {
56         scanf("%d", &N);
57         vector< pair<int, int> > D;
58         int x, y;
59         for(int i = 0; i < N; i++) {
60             scanf("%d %d", &x, &y);
61             D.push_back(make_pair(x, y));
62         }
63         annealing(D);
64         if(testcase)
65             puts("");
66     }
67     return 0;
68 }

```

7.2 DLX

```

1 struct DLX{
2     int n,m,len;
3     int U[maxnode],D[maxnode],R[maxnode],L[maxnode],
4     Row[maxnode],Col[maxnode];
5     int H[maxn];
6     int S[maxm];
7     int ansd,ans[maxn];
8
9     void init(int _n,int _m){
10        n = _n;m = _m;

```

```

10        for(int i = 0; i <= m; i++){
11            S[i] = 0;
12            U[i] = D[i] = i;
13            L[i] = i-1;
14            R[i] = i+1;
15        }
16        R[m] = 0,L[0] = m;
17        len = m;
18        for(int i = 1; i <= n; i++){
19            H[i] = -1;
20        }
21
22        void link(int r,int c){
23            ++S[Col[++len]=c];
24            Row[len] = r;
25            D[len] = D[c];
26            U[D[c]] = len;
27            U[len] = c;
28            D[c] = len;
29            if(H[r] < 0)
30                H[r] = L[len] = R[len] = len;
31            else{
32                R[len] = R[H[r]];
33                L[R[H[r]]] = len;
34                L[len] = H[r];
35                R[H[r]] = len;
36            }
37        }
38
39        void del(int c){
40            L[R[c]] = L[c];
41            R[L[c]] = R[c];
42            for(int i = D[c]; i != c; i = D[i]){
43                for(int j = R[i]; j != i; j = R[j]){
44                    U[D[j]] = U[j];
45                    D[U[j]] = D[j];
46                    --S[Col[j]];
47                }
48            }
49        }
50
51        void resume(int c){
52            for(int i = U[c]; i != c; i = U[i]){
53                for(int j = L[i]; j != i; j = L[j]){
54                    ++S[Col[U[D[j]]=D[U[j]]=j]];
55                }
56            }
57            L[R[c]] = R[L[c]] = c;
58        }
59
60        void dance(int d){
61            //剪枝
62            if(ansd != -1 && ansd <= d)
63                return;
64            if(R[0] == 0){
65                if(ansd == -1)
66                    ansd = d;
67                else if(d < ansd)
68                    ansd = d;
69                return;
70            }
71            int c = R[0];
72            for(int i = R[0]; i != 0; i = R[i]){
73                if(S[i] < S[c])
74                    c = i;
75            }
76            del(c);
77            for(int i = D[c]; i != c; i = D[i]){
78                ans[d] = Row[i];
79                for(int j = R[i]; j != i; j = R[j])
80                    del(Col[j]);
81                dance(d+1);
82                for(int j = L[i]; j != i; j = L[j])
83                    resume(Col[j]);
84            }
85            resume(c);
86        }
87    };

```

7.3 MahattanMST

```

1 #include<bits/stdc++.h>
2 #define REP(i,n) for(int i=0;i<n;i++)
3 using namespace std;
4 typedef long long LL;
5 const int N=200100;
6 int n,m;
7 struct PT {int x,y,z,w,id;}p[N];
8 inline int dis(const PT &a,const PT &b){return abs(a
    .xb.x)+abs(a.y-b.y);}
9 inline bool cpx(const PT &a,const PT &b){return a.x
    !=b.
10 x? a.x>b.x:a.y>b.y;}
11 inline bool cpz(const PT &a,const PT &b){return a.z<
    b.z
12 ;}
13 struct E{int a,b,c;}e[8*N];
14 bool operator<(const E&a,const E&b){return a.c<b.c;}
15 struct Node{
16     int L,R,key;
17 }node[4*N];
18 int s[N];
19 int F(int x){return s[x]==x?s[x]=F(s[x]);}
20 void U(int a,int b){s[F(b)]=F(a);}
21 void init(int id,int L,int R) {
22     node[id]=(Node){L,R,-1};
23     if(L==R)return
24     ;
25     init(id*2,L,(L+R)/2);
26     init(id*2+1,(L+R)/2+1,R);
27 }
28 void ins(int id,int x) {
29     if(node[id].key==-1 || p[node[id].key].w>p[x].w)
30     node[
31     id].key=x;
32     if(node[id].L==node[id].R)return
33     ;
34     if(p[x].z<=(node[id].L+node[id].R)/2)ins(id*2,x)
35     ;
36     else ins(id*2+1,x);
37 }
38 int Q(int id,int L,int R){
39     if(R<node[id].L || L>node[id].R)return -1;
40     if(L<=node[id].L && node[id].R<=R)return node[id]
41     .key ;
42     int a=Q(id*2,L,R),b=Q(id*2+1,L,R);
43     if(b==-1 || (a!=-1 && p[a].w<p[b].w)) return a;
44     else return b;
45 }
46 void calc() {
47     REP(i,n) {
48         p[i].z=p[i].y-p[i].x;
49         p[i].w=p[i].x+p[i].y;
50     }
51     sort(p,p+n,cpz);
52     int cnt=0,j,k;
53     for
54     (int i=0;i<n;i=j){
55         for(j=i+1;p[j].z==p[i].z && j<n;j++);
56         for(k=i,cnt++;k<j;k++)p[k].z=cnt;
57     }
58     init(1,1,cnt);
59     sort(p,p+n,cpx);
60     REP(i,n) {
61         j=Q(1,p[i].z,cnt);
62         if(j!=-1)e[m++]=(E){p[i].id,p[j].id,dis(p[i]
63         ],p[j])
64         };
65         ins(1,i);
66     }
67 }
68 LL MST() {
69     LL r=0;
70     sort(e,e+m);
71     REP(i,m) {
72         if(F(e[i].a)==F(e[i].b))continue;
73         U(e[i].a,e[i].b);
74         r+=e[i].c;
75     }
76     return r;
77 }
78 int main(){
79     int ts;

```

```

76     scanf("%d", &ts);
77     while (ts--) {
78         m = 0;
79         scanf("%d",&n);
80         REP(i,n) {scanf("%d%d",&p[i].x,&p[i].y);p[i]
81         ].id=s[i]=i;}
82         calc();
83         REP(i,n)p[i].y= -p[i].y;
84         calc();
85         REP(i,n)swap(p[i].x,p[i].y);
86         calc();
87         REP(i,n)p[i].x=-p[i].x;
88         calc();
89         printf("%lld\n",MST()*2);
90     }
91     return 0;

```

7.4 MoOnTree

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 #define IOS ios_base::sync_with_stdio(0); cin.tie(0)
4 ;
5 #define SZ(x) ((int)((x).size()))
6 const int MX = 500005;
7 const int SQ = 1400;
8 const int LOG = 17;
9 struct BIT {
10     int bit[MX];
11     int lb(int x) { return x & -x; }
12     void add(int p, int v) {
13         p++;
14         for (int i=p; i<MX; i+=lb(i)) bit[i] += v;
15     }
16     int qry() {
17         int v = 0;
18         for (int i=1<<LOG; i>0; i>=1) {
19             if ((v|i) < MX and bit[v|i]==i) v |= i;
20         }
21         return v;
22     }
23 }bit;
24 struct Query {
25     int l,r,qid;
26 }qry[MX];
27 struct Edge {
28     int v,x;
29 };
30 int N,Q,timestamp[MX],ans[MX];
31 int in[MX],cnt[MX];
32 vector<Edge> E[MX];
33 vector<Edge> seq;
34 void DFS(int u, int f) {
35     timestamp[u] = SZ(seq);
36     for (auto it:E[u]) {
37         if (it.v == f) continue;
38         seq.push_back(it);
39         DFS(it.v,u);
40         seq.push_back(it);
41     }
42 }
43 void poke(int id) {
44     int v = seq[id].v;
45     int x = seq[id].x;
46     in[v] ^= 1;
47     cnt[x] += in[v] ? 1 : -1;
48     if (in[v] and cnt[x] == 1) bit.add(x, 1);
49     if (!in[v] and cnt[x] == 0) bit.add(x, -1);
50 }
51 int main() {
52     IOS;
53     cin >> N >> Q;
54     for (int i=0; i<N-1; i++) {
55         int u,v,x;
56         cin >> u >> v >> x;
57         x = min(x,N);
58         E[u].push_back({v,x});
59         E[v].push_back({u,x});
60     }
61     DFS(1,1);

```

```

61 for (int i=1; i<=Q; i++) {
62     int u,v;
63     cin >> u >> v;
64     int l = timestamp[u], r = timestamp[v];
65     if (l > r) swap(l,r);
66     r--;
67     qry[i] = {l,r,i};
68 }
69 sort(qry+1,qry+1+Q, [](Query a, Query b) {
70     return make_pair(a.l/SQ,a.r) < make_pair(b.l
71     /SQ,b
72     .r);
73 });
74 int curL = 1, curR = 0;
75 for (int i=1; i<=Q; i++) {
76     int ql=qry[i].l,qv=qry[i].r;
77     while (curL > ql) poke(--curL);
78     while (curR < qv) poke(++curR);
79     while (curL < ql) poke(curL++);
80     while (curR > qv) poke(curR--);
81     ans[qry[i].qid] = bit.qry();
82 }
83 for (int i=1; i<=Q; i++) cout << ans[i] << "\n";
84 return 0;
85 }

```

7.5 Det

```

1 LL det(LL a[][20],int n)
2 {
3     LL ret=1;
4     for(int i=1;i<n;i++)
5     {
6         for(int j=i+1;j<n;j++)
7             while(a[j][i])
8             {
9                 LL t=a[i][i]/a[j][i];
10                for(int k=i;k<n;k++)
11                    a[i][k]=a[i][k]-a[j][k]*t;
12                for(int k=i;k<n;k++)
13                    swap(a[i][k],a[j][k]);
14                ret=-ret;
15            }
16        if(a[i][i]==0)return 0;
17        ret=ret*a[i][i];
18    }
19    return ret;
20 }
21 }

```

8 String

8.1 AC

```

1 struct Node{
2     Node *index[30];
3     Node *fail;
4     int word;
5     int num;
6     Node(){
7         for(int i=0;i<30;i++)
8             index[i]=NULL;
9         fail=NULL;
10        word=0;
11        num=-1;
12    }
13 }*root=new Node();
14 void add(char c[]){
15     Node *n=root;
16     for(int i=0;c[i]!='\0';i++){
17         if(!n->index[c[i]-'a'])
18             n->index[c[i]-'a']=new Node();
19         n=n->index[c[i]-'a'];
20     }
21     n->word=1;
22     n->num++;
23 }
24 void ac(){
25     queue<Node*> q;

```

```

27 q.push(root);
28 root->fail=NULL;
29 while(!q.empty()){
30     Node *n=q.front();
31     q.pop();
32     for(int i=0;i<30;i++){
33         if(n->index[i]){
34             q.push(n->index[i]);
35             Node* p=n->fail;
36             while(p!=NULL&&!p->index[i])
37                 p=p->fail;
38             if(p)
39                 n->index[i]->fail=p->index[i];
40             else
41                 n->index[i]->fail=root;
42         }
43     }
44 }
45 }
46 void search(char c[]){
47     Node *n=root;
48     for(int i=0;c[i]!='\0';i++){
49         while(!n->index[c[i]-'a']&&n!=root){
50             n=n->fail;
51         }
52         if(n->index[c[i]-'a'])
53             n=n->index[c[i]-'a'];
54         Node *p=n;
55         while(p){
56             if(p->num!=-1)
57                 ans[p->num]++;
58             p=p->fail;
59         }
60     }
61 }
62 }
63 }
64 }
65 void del(Node *n=root){
66     for(int i=0;i<30;i++)
67         if(n->index[i])
68             del(n->index[i]);
69     free(n);
70 }

```

8.2 SuffixAutomata

```

1 // BZOJ 3998
2 const int MAX_N = 500000 + 10;
3 struct Node {
4     static Node mem[MAX_N<<1] , *pmem;
5     Node *ch[26] , *fail;
6     int mx , val;
7     ll dp;
8     int tag , deg;
9     Node():mx(0),fail(0),dp(0),val(0),tag(0),deg(0){
10         MS(ch , 0);
11     }
12 }
13 Node::mem[MAX_N<<1] , *Node::pmem = Node::mem , *
14     root
15     , *last;
16 int T , N;
17 char s[MAX_N];
18 inline void init() {
19     last = root = new (Node::pmem++)Node();
20 }
21 inline int idx(char c) {
22     return c - 'a';
23 }
24 inline void insert(char c) {
25     c = idx(c);
26     Node *p = last;
27     Node *np = new (Node::pmem++)Node();
28     np->mx = p->mx + 1;
29     np->val = 1;
30     while(p && !p->ch[c]) {
31         p->ch[c] = np;
32         np->deg++;
33         p = p->fail;
34     }

```

```

34     if(!p) np->fail = root;
35     else
36     {
37         Node *q = p->ch[c];
38         if(q->mx == p->mx + 1) np->fail = q;
39         else
40         {
41             Node *nq = new (Node::pmem++)Node();
42             nq->mx = p->mx + 1;
43             nq->val = 0;
44             memcpy(nq->ch, q->ch, sizeof(q->ch));
45             REP(i, 26) {
46                 if(nq->ch[i]) nq->ch[i]->deg++;
47             }
48             nq->fail = q->fail;
49             q->fail = np->fail = nq;
50             while(p && p->ch[c] == q) {
51                 p->ch[c] = nq;
52                 q->deg--;
53                 nq->deg++;
54                 p = p->fail;
55             }
56         }
57     }
58     last = np;
59 }
60 inline void bfs() {
61     static Node* que[MAX_N<<1];
62     int l = 0, r = 0;
63     que[r++] = root;
64     root->tag = 2;
65     vector<Node*> vec;
66     while(l < r) {
67         Node *u = que[l++];
68         REP(i, 26) {
69             if(u->ch[i]) {
70                 if(--u->ch[i]->deg == 0 && u->ch[i]
71 ]->
72                 tag != 1) {
73                     u->ch[i]->tag = 1;
74                     que[r++] = u->ch[i];
75                     vec.PB(u->ch[i]);
76                 }
77             }
78         }
79     }
80     for(int i = SZ(vec) - 1; i >= 0; i--) {
81         Node *u = vec[i];
82         if(T) {
83             if(u->fail) u->fail->val += u->val;
84         }
85         else u->val = 1;
86     }
87     root->val = 0;
88     for(int i = SZ(vec) - 1; i >= 0; i--) {
89         Node *u = vec[i];
90         u->dp = u->val;
91         REP(j, 26) {
92             if(u->ch[j]) u->dp += u->ch[j]->dp;
93         }
94     }
95     REP(i, 26) {
96         if(root->ch[i]) root->dp += root->ch[i]->dp;
97     }
98 inline void solve(int k) {
99     Node *p = root;
100     if(k > p->dp || k <= 0) {
101         puts("-1");
102         return;
103     }
104     while(k > 0) {
105         int flag = 0;
106         REP(i, 26) {
107             if(!p->ch[i]) continue;
108             if(k <= p->ch[i]->dp) {
109                 putchar('a' + i);
110                 k -= p->ch[i]->val;
111                 p = p->ch[i];
112                 flag = 1;
113                 break;
114             }

```

```

115         }
116         else k -= p->ch[i]->dp;
117     }
118     if(!flag) break;
119 }
120 }
121 int main() {
122     scanf("%s", s);
123     int n = strlen(s);
124     N = n;
125     init();
126     REP(i, n) insert(s[i]);
127     int K;
128     scanf("%d%d", &T, &K);
129     bfs();
130     solve(K);
131     return 0;
132 }

```

8.3 Palindromic Tree

```

1 #include<bits/stdc++.h>
2 #include<unistd.h>
3 using namespace std;
4 #define F first
5 #define S second
6 #define MP make_pair
7 #define PB push_back
8 #define IOS ios_base::sync_with_stdio(0); cin.tie(0)
9 #define SZ(x) ((int)((x).size()))
10 #define ALL(x) begin(x),end(x)
11 #define REP(i,x) for (int i=0; i<(x); i++)
12 #define REP1(i,a,b) for (int i=(a); i<=(b); i++)
13
14 struct palindromic_tree{
15     struct node{
16         int next[26],fail,len;
17         int cnt,num,st,ed;
18         node(int l=0):fail(0),len(l),cnt(0),num(0){
19             for(int i=0;i<26;++i)next[i]=0;
20         }
21     };
22     vector<node> state;
23     vector<char> s;
24     int last,n;
25
26     void init(){
27         state.clear();
28         s.clear();
29         last=1;
30         n=0;
31         state.push_back(0);
32         state.push_back(-1);
33         state[0].fail=1;
34         s.push_back(-1);
35     }
36     int get_fail(int x){
37         while(s[n-state[x].len-1]!=s[n])x=state[x].fail;
38         return x;
39     }
40     void add(int c){
41         s.push_back(c-'a');
42         ++n;
43         int cur=get_fail(last);
44         if(!state[cur].next[c]){
45             int now=state.size();
46             state.push_back(state[cur].len+2);
47             state[now].fail=state[get_fail(state[cur].fail
48 )].next[c];
49             state[cur].next[c]=now;
50             state[now].num=state[state[now].fail].num+1;
51         }
52         last=state[cur].next[c];
53         ++state[last].cnt;
54     }
55     int size(){
56         return state.size()-2;
57     }
58 }pt;

```

```

59 int main() {
60     string s;
61     cin >> s;
62     pt.init();
63     for (int i=0; i<SZ(s); i++) {
64         int prvsz = pt.size();
65         pt.add(s[i]);
66         if (prvsz != pt.size()) {
67             int r = i;
68             int l = r - pt.state[pt.last].len + 1;
69             cout << "Find pal @ [" << l << " " << r << "]"
70             : " << s.substr(l,r-l+1) << endl;
71         }
72     }
73     return 0;
74 }

```

8.4 MinLexicographicalRotate

```

1 string mcp(string s){
2     int n = s.length();
3     s += s;
4     int i=0, j=1;
5     while (i<n && j<n){
6         int k = 0;
7         while (k < n && s[i+k] == s[j+k]) k++;
8         if (s[i+k] <= s[j+k]) j += k+1;
9         else i += k+1;
10        if (i == j) j++;
11    }
12    int ans = i < n ? i : j;
13    return s.substr(ans, n);
14 }

```

8.5 ZvaluePalindromes

```

1 inline void manacher(char *s,int len,int *z){
2     int l=0,r=0;
3     for(int i=1;i<len;++i){
4         z[i]=r>i?min(z[2*l-i],r-i):1;
5         while(s[i+z[i]]==s[i-z[i]])++z[i];
6         if(z[i]+i>r)r=z[i]+i,l=i;
7     }
8 }

```

8.6 SuffixArray

```

1 int ss[N];
2 int heigh[N];
3 int sa[N];
4 int rank[N];
5 int length;
6 int val[30];
7 int c[N]; // counting sort array
8 int temp[2][N];
9 void suffix_array()
10 {
11     int A = 250;
12     int* rank = temp[0];
13     int* new_rank = temp[1];
14     for (int i=0; i<A; ++i) c[i] = 0;
15     for (int i=0; i<length; ++i) c[rank[i] = ss[i]]++;
16     for (int i=1; i<A; ++i) c[i] += c[i-1];
17     for (int i=length-1; i>=0; --i) sa[--c[ss[i]]] = i;
18     for (int n=1; n<length; n*=2)
19     {
20         for (int i=0; i<A; ++i) c[i] = 0;
21         for (int i=0; i<length; ++i) c[rank[i]]++;
22         for (int i=1; i<A; ++i) c[i] += c[i-1];
23         int* sa2 = new_rank;
24         int r = 0;
25         for (int i=length-n; i<length; ++i)
26             sa2[r++] = i;
27         for (int i=0; i<length; ++i)
28             if (sa[i] >= n)
29                 sa2[r++] = sa[i] - n;
30         for (int i=length-1; i>=0; --i)

```

```

31         sa[--c[rank[sa2[i]]]] = sa2[i];
32         new_rank[sa[0]] = r = 0;
33         for (int i=1; i<length; ++i)
34         {
35             if (!(rank[sa[i-1]] == rank[sa[i]] &&
36                 sa[i-1]+n < length && // stable
37                 rank[sa[i-1]+n] == rank[sa[i]+n]))
38                 r++;
39             new_rank[sa[i]] = r;
40         }
41         swap(rank, new_rank);
42         if (r == length-1) break;
43         A = r + 1;
44     }
45 }
46 void lcp_array()
47 {
48     for (int i=0; i<length; ++i)
49         rank[sa[i]] = i;
50
51     for (int i=0, lcp=0, h=0; i<length; i++)
52         if (rank[i] == 0)
53             heigh[0] = 0;
54         else
55         {
56             int j = sa[rank[i]-1];
57             if (lcp > 0) lcp=--val[ss[i-1]-'a'],h--;
58             while (ss[i+h] == ss[j+h]) lcp+=val[ss[i
59             +h]-'a'],h++;
60             heigh[rank[i]] = lcp;
61         }
62 }

```

8.7 Zvalue

```

1 inline void z_alg1(char *s,int len,int *z){
2     int l=0,r=0;
3     z[0]=len;
4     for(int i=1;i<len;++i){
5         z[i]=r>i?min(r-i+1,z[l]-r-i+1):0;
6         while(i+z[i]<len&&s[z[i]]==s[i+z[i]])++z[i];
7         if(i+z[i]-1>r)r=i+z[i]-1,l=i;
8     }
9 }

```

9 Math

9.1 MillerRabin

```

1 // 4759123141 2, 7, 61
2 //2^64 2, 325, 9375, 28178, 450775, 9780504,
   1795265022
3 bool Isprime(LL n)
4 {
5     if (n == 2) return true;
6     if (n < 2 || n % 2 == 0) return false;
7     LL u = n - 1, t = 0;
8     while (u % 2 == 0) {u >>= 1; t++;}
9     LL sprp[7] = {2, 325, 9375, 28178, 450775,
10     9780504, 1795265022};
11     for (int k=0; k<7; ++k)
12     {
13         LL a = sprp[k] % n;
14         if (a == 0 || a == 1 || a == n-1) continue;
15         long long x = f_pow(a, u, n);
16         if (x == 1 || x == n-1) continue;
17         for (int i = 0; i < t-1; i++)
18         {
19             x = f_pow(x, 2, n);
20             if (x == 1) return false;
21             if (x == n-1) break;
22         }
23         if (x == n-1) continue;
24         return false;
25     }
26     return true;
27 }

```


9.2 Simplex

```

1 const int maxn = 111;
2 const int maxm = 111;
3 const double eps = 1E-10;
4
5 double a[maxn][maxm], b[maxn], c[maxm], d[maxn][maxm];
6 double x[maxm];
7 int ix[maxn + maxm]; // !!! array all indexed from 0
8 // max{cx} subject to {Ax<=b, x>=0}
9 // n: constraints, m: vars !!!
10 // x[] is the optimal solution vector
11 //
12 // usage :
13 // value = simplex(a, b, c, N, M);
14 double simplex(double a[maxn][maxm], double b[maxn],
15               double c[maxm], int n, int m) {
16     ++m;
17     int r = n, s = m - 1;
18     memset(d, 0, sizeof(d));
19     for (int i = 0; i < n + m; ++i) ix[i] = i;
20     for (int i = 0; i < n; ++i) {
21         for (int j = 0; j < m - 1; ++j)
22             d[i][j] = -a[i][j];
23         d[i][m - 1] = 1;
24         d[i][m] = b[i];
25         if (d[r][m] > d[i][m]) r = i;
26     }
27     for (int j = 0; j < m - 1; ++j) d[n][j] = c[j];
28     d[n + 1][m - 1] = -1;
29     for (double dd; ) {
30         if (r < n) {
31             int t = ix[s];
32             ix[s] = ix[r + m]; ix[r + m] = t;
33             d[r][s] = 1.0 / d[r][s];
34             for (int j = 0; j <= m; ++j)
35                 if (j != s) d[r][j] *= -d[r][s];
36             for (int i = 0; i <= n + 1; ++i)
37                 if (i != r) {
38                     for (int j = 0; j <= m; ++j)
39                         if (j != s)
40                             d[i][j] += d[r][j] * d[i][s];
41                 }
42             r = -1; s = -1;
43             for (int j = 0; j < m; ++j)
44                 if (s < 0 || ix[s] > ix[j]) {
45                     if (d[n + 1][j] > eps || (d[n + 1][j] > -eps && d[n][j] > eps)) s = j;
46                 }
47             if (s < 0) break;
48             for (int i = 0; i < n; ++i) if (d[i][s] < -eps) {
49                 if (r < 0 || (dd = d[r][m] / d[r][s] - d[i][m] / d[i][s]) < -eps || (dd < eps && ix[r + m] > ix[i + m])) r = i;
50             }
51             if (r < 0) return -1; // not bounded
52         }
53         if (d[n + 1][m] < -eps) return -1; // not executable
54         double ans = 0;
55         for (int i = 0; i < m; i++) x[i] = 0;
56         for (int i = m; i < n + m; ++i) { // the missing
57             enumerated x[i] = 0
58             if (ix[i] < m - 1)
59                 {
60                     ans += d[i - m][m] * c[ix[i]];
61                     x[ix[i]] = d[i - m][m];
62                 }
63         }
64         return ans;
65     }
66 }

```

9.3 Theorem

```

1 /*
2 Lucas's Theorem:
3 For non-negative integer n,m and prime P,

```

```

4 C(m,n) mod P = C(m/P,n/P) * C(m%P,n%P) mod P
5 -----
6 Pick's Theorem
7 A = i + b/2 - 1
8 */

```

9.4 Prime

```

1 /*
2 * 12721
3 * 13331
4 * 14341
5 * 75577
6 * 123457
7 * 222557
8 * 556679
9 * 999983
10 * 1097774749
11 * 1076767633
12 * 100102021
13 * 999997771
14 * 1001010013
15 * 1000512343
16 * 987654361
17 * 999991231
18 * 999888733
19 * 98789101
20 * 987777733
21 * 999991921
22 * 1010101333
23 * 1010102101
24 * 1000000000039
25 * 100000000000037
26 * 2305843009213693951
27 * 4611686018427387847
28 * 9223372036854775783
29 * 18446744073709551557
30 */

```

9.5 FFT

```

1 #define N 524288
2 #define pi acos(-1)
3 typedef complex<double> C;
4 int n,m,i,t,g[N];
5 C a[N],b[N];
6 void FFTinit(){
7     for (i=1;i<N;i++) g[i]=g[i>>1]>>1|((i&1)<<18);
8 }
9 void FFT(C *a,int f)
10 {
11     int i,j,k,p;
12     for (i=0;i<N;i++)
13         if (g[i]>i) swap(a[i],a[g[i]]);
14     for (i=1;i<N;i<=<=1)
15     {
16         C e(cos(pi/i),f*sin(pi/i));
17         for (j=0;j<N;j+=i<<1)
18         {
19             C w(1,0);for (k=0;k<i;k++,w*=e)
20             {
21                 C x=a[j+k],y=w*a[j+k+i];
22                 a[j+k]=x+y;a[j+k+i]=x-y;
23             }
24         }
25     }
26 }
27 int res[400005];
28 int main()
29 {
30     FFTinit();
31     FFT(a,1);
32     FFT(b,1);
33     for(i=0;i<N;i++) a[i]=a[i]*b[i];
34     FFT(a,-1);
35     for (i=0;i<n+m;i++)
36         (int)a[i].real()/N+0.5)
37 }

```

9.6 Crt Solve2

```

1 ll a[10],n[10],k,k2;
2 int cs;
3 vector<PLL> v[100];
4 int srt(PLL a,PLL b){
5     return a.Y>b.Y;
6 }
7 PLL extgcd(ll a,ll b){
8     if(b==0) return mp(1,0);
9     ll p;
10    PLL q;
11    p = a/b;
12    q = extgcd(b,a%b);
13    return mp(q.Y,q.X-q.Y*p);
14 }
15 ll crt (){
16     ll i,alln,mf,ans,mi,ci;
17     PII f;
18     alln = 1;
19     ans = 0;
20     for(i=0;i<k;i++) alln *= n[i];
21     for(i=0;i<k;i++){
22         mi = alln/n[i];
23         mf = extgcd(mi,n[i]).X; // m[i]*mf % n[i] =
24         1
25         ci = mi*(mf % n[i]); // m[i] * (mf % n[i])
26         ans= (ans + (a[i]*ci))%alln + alln)%alln;
27     }
28     return (ans==0?alln:ans);
29 }
30 int chg(){
31     ll f,mi,xa,xm,c;
32     REP(i,k){
33         f = n[i];
34         REP1(j,2,f+1){
35             c = 0;
36             mi = 1;
37             while(f%j == 0){
38                 f/=j;
39                 c++;
40                 mi*=j;
41             }
42             if(c)v[j].pb(mp(a[i]%mi,mi));
43         }
44         k = 0;
45         REP(i,100){
46             if(LE(v[i])){
47                 sort(ALL(v[i]),srt);
48                 REP(j,LE(v[i])){
49                     xa = v[i][j].X;
50                     xm = v[i][j].Y;
51                     if(v[i][0].X % xm != xa % xm)
52                         return 0;
53                 }
54                 a[k] = v[i][0].X;
55                 n[k] = v[i][0].Y;
56                 k++;
57             }
58         }
59         return 1;
60 }

```

9.7 FWT

```

1 void FWT(int *x,int inv) {
2     for(int i=1;i<lim;i<=1){
3         for(int j=0;j<lim;++j)/* or */
4             if(j&i)
5                 x[j]= inv ? x[j]-x[j^i] : x[j]+x[j^i];
6     }
7     for(int j=0;j<lim;j+=(i<<1))/* and */
8         for(int k=0;k<i;++k)
9             x[j+k]=inv ? x[j+k]-x[j+k+i] : x[j+k]
10            ]+x[j+k+i];
11     for(int j=0;j<lim;j+=(i<<1))/* xor */
12         for(int k=0;k<i;++k) {
13             int y=x[j+k],z=x[j+k+i];
14             x[j+k]=inv ? (y+z)/2 : y+z;
15             x[j+k+i]=inv ? (y-z)/2 : y-z;
16         }
17 }

```

```

15     }
16 }

```

9.8 Extgcd

```

1 typedef pair<int, int> pii;
2 pii gcd(int a, int b){
3     if(b == 0) return mp(1, 0);
4     else{
5         int p = a / b;
6         pii q = gcd(b, a % b);
7         return make_pair(q.y, q.x - q.y * p);
8     }
9 }

```

9.9 Pollard'sRho

```

1 // does not work when n is prime
2 inline LL f(LL x, LL mod) {
3     return (x * x % mod + 1) % mod;
4 }
5 inline LL pollard_rho(LL n) {
6     if(!(n&1)) return 2;
7     while(true) {
8         LL y = 2, x = rand() % (n - 1) + 1, res = 1;
9         for(int sz = 2; res == 1; sz *= 2) {
10             for(int i = 0; i < sz && res <= 1; i++) {
11                 x = f(x, n);
12                 res = __gcd(abs(x - y), n);
13             }
14             y = x;
15         }
16         if (res != 0 && res != n) return res;
17     }
18 }

```

10 monge

$$i \leq i' < j \leq j'$$

$$m(i, j) + m(i', j') \leq m(i', j) + m(i, j')$$

$$k(i, j - 1) \leq k(i, j) \leq k(i + 1, j)$$

11 四心

$$\frac{sa \cdot A + sb \cdot B + sc \cdot C}{sa + sb + sc}$$

外心 $\sin 2A : \sin 2B : \sin 2C$

內心 $\sin A : \sin B : \sin C$

垂心 $\tan A : \tan B : \tan C$

重心 $1 : 1 : 1$

12 Runge-Kutta

$$y_{n+1} = y_n + \frac{h}{6}(k_1 + 2k_2 + 2k_3 + k_4)$$

$$k_1 = f(t_n, y_n)$$

$$k_2 = f(t_n + \frac{h}{2}, y_n + \frac{h}{2}k_1)$$

$$k_3 = f(t_n + \frac{h}{2}, y_n + \frac{h}{2}k_2)$$

$$k_4 = f(t_n + h, y_n + hk_3)$$

13 Householder Matrix

$$I - 2 \frac{vv^T}{v^T v}$$