

# Different LP Problems

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## 1 Wikipedia

Problem:

$$\operatorname{argmax}_{x \in \mathbb{R}^n} \{c^t x \mid Ax \leq b, x \geq 0\}$$

Phase I:

$$\operatorname{argmin}_{z \in \mathbb{R}^m} \left\{ \sum_{i=1}^m z_i \mid Ax + z = b, x \geq 0, z \geq 0 \right\}$$

in standard form

$$\operatorname{argmax}_{z \in \mathbb{R}^m} \{ \sum_{i=1}^m z_i \mid Ax + z = b, x \geq 0, z \geq 0 \}$$

## 2 Grötschel

Problem:

$$\operatorname{argmax}_{x \in \mathbb{R}^n} \{c^t x \mid Ax \leq b\}$$

p111-p

Lineares Program in Standardform [p112]:

$$\operatorname{argmax}_{x \in \mathbb{R}^n} \{c^t x \mid Ax = b, x \geq 0\}$$

mit

1.  $m < n$
2.  $A \in \mathbb{R}^{m,n}$
3.  $\operatorname{rang}(A) = m$
4.  $P(A, b) \neq \emptyset$

Phase I:

$$\begin{array}{rcl} \max \mathbf{1}^t A x & & \\ (A, I) \begin{pmatrix} x \\ z \end{pmatrix} & = & b \\ x & \geq & 0 \\ z & \geq & 0 \end{array}$$