

3.

Letter Grade

No. of students (observed distribution)

A

77

B

150

C

210

D

125

F

38

Total = 600

~~Total = 604~~

Assuming it to be ~~in~~ a standard normal distribution

Expected distribution

$$A \rightarrow 7.5\% = 0.075 \times 600 = 45$$

$$B \rightarrow 22.5\% = 0.225 \times 600 = 135$$

$$C \rightarrow 35\% = 0.35 \times 600 = 210$$

$$D \rightarrow 22.5\% = 0.225 \times 600 = 135$$

$$F \rightarrow 7.5\% = 0.075 \times 600 = 45$$

$$\text{Degrees of Freedom} = 5 - 1 = 4$$

Critical value ( $\chi^2$ )

$$\text{For } 5\% \text{ significance} = 9.488$$

$$\text{For } 10\% \text{ significance} = 7.779$$

$$\chi^2 = \sum_i \frac{(O_i - E_i)^2}{E_i}$$

$$= \frac{(77-45)^2}{45} + \frac{(150-135)^2}{135} + \frac{(210-210)^2}{210} + \frac{(125-135)^2}{135} + \frac{(38-45)^2}{45}$$

$$= 26.25$$

$\therefore$  Since,  $\chi^2 = 26.25 > \text{Critical value at } 5\% \text{ significance}$   
also  $\chi^2 > \text{Critical value at } 10\% \text{ significance}$

$\therefore$  The observed distribution is not a normal distribution  
~~in both cases~~ for both significances,

4.

~~Mean(A) =  $\frac{\sum f_i}{N}$~~

$$\text{Mean}(\bar{A}) = \sum_i \frac{f_i}{N} = 4.7146 \text{ cm}$$

$$\text{Mean}(\bar{B}) = \sum_i \frac{f_i}{N} = 4.74 \text{ cm}$$

~~Variance(A) =~~

$$\text{Variance} = \frac{1}{N-1} \sum (f_i - \bar{f})^2$$

$$\text{Variance}(A) = 0.01026 \text{ cm}^2$$

$$\text{Variance}(B) = 0.00567 \text{ cm}^2$$

$$\therefore F = \frac{\text{Variance}(A)}{\text{Variance}(B)} = 1.809$$

$$\therefore t = \frac{\bar{A} - \bar{B}}{\sqrt{\frac{\text{Variance}(A)}{n_A} + \frac{\text{Variance}(B)}{n_B}}} = \frac{-0.0254}{\sqrt{0.00079 + 0.00081}} = -0.635$$

$$\therefore |t| = 0.635$$

$$\therefore F\text{-critical} = 3.999935 \quad , \quad \left[ \because \begin{array}{l} \text{Degree of freedom}(A) = 12 \\ \text{Degree of freedom}(B) = 6 \end{array} \right]$$

$$\therefore t\text{-critical} = 2.1009 \quad \left[ \because \text{Degree of freedom} = (n_A - 1) + (n_B - 1) = 18 \right]$$

$\therefore$  Since, the value of F-test and t-test are less than the critical values, the means and variances are not significantly different.

~~$\therefore$  Both the~~

$\therefore$  Both the shipment of lenses are from same population.